lab08_backup

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Background

The goal of this mini-project is for you to explore a complete analysis using the unsupervised learning techniques covered in class. You'll extend what you've learned by combining PCA as a preprocessing step to clustering using data that consist of measurements of cell nuclei of human breast masses. This expands on our RNA-Seq analysis from last day.

The mini project explores unsupervised learning techniques covered in class. interpreting principal component analysis (PCA) to reduce the dimensional of the data while retaining variance, and applying hierarchical clustering with different linkage methods. It also includes an optional section on K-means clustering for comparison. The ultimate goal is to combine PCA and clustering to better separate benign and malignant cell samples evaluating the results using metrics like sensitivity and specificity and finally demonstrating how to predict he classification of new samples using the developed PCA model.

Data Import

Our data comes from the University of Wisconsin Medical Center. Omit the ID column from the dataset.

```
# Save your input data file into your Project directory
fna.data <- "WisconsinCancer.csv"

# Complete the following code to input the data and store as wisc.df
wisc.df <- read.csv(fna.data, row.names=1)
head(wisc.df)</pre>
```

	diagnosis	radius mean	texture mean	perimeter_mean	area mea	n
842302	M	-	10.38	122.80	1001.	
842517	М	20.57	17.77	132.90	1326.	0
84300903	М	19.69	21.25	130.00	1203.	
84348301	М	11.42	20.38	77.58	386.	1
84358402	М	20.29	14.34	135.10	1297.	0
843786	М	12.45	15.70	82.57	477.	1
	smoothness	s_mean compa	ctness_mean co	ncavity_mean c	oncave.po	ints_mean
842302	0	.11840	0.27760	0.3001		0.14710
842517	0	.08474	0.07864	0.0869		0.07017
84300903	0	.10960	0.15990	0.1974		0.12790
84348301	0	.14250	0.28390	0.2414		0.10520
84358402	0	.10030	0.13280	0.1980		0.10430
843786	0	.12780	0.17000	0.1578		0.08089
	symmetry_r	mean fractal	_dimension_mea	n radius_se te	xture_se]	perimeter_se
842302	0.3	2419	0.0787	1 1.0950	0.9053	8.589
842517	0.3	1812	0.0566	7 0.5435	0.7339	3.398
84300903	0.2	2069	0.0599	9 0.7456	0.7869	4.585
84348301	0.2	2597	0.0974	4 0.4956	1.1560	3.445
84358402	0.3	1809	0.0588	3 0.7572	0.7813	5.438
843786	0.2	2087	0.0761	3 0.3345	0.8902	2.217
	area_se s	moothness_se	compactness_s	e concavity_se	concave.	points_se
842302	153.40	0.006399	0.0490	4 0.05373		0.01587
842517	74.08	0.005225	0.0130	8 0.01860		0.01340
84300903	94.03	0.006150	0.0400	6 0.03832		0.02058
84348301	27.23	0.009110	0.0745	8 0.05661		0.01867
84358402	94.44	0.011490	0.0246	1 0.05688		0.01885
843786	27.19	0.007510	0.0334	5 0.03672		0.01137
	symmetry_s	se fractal_d	imension_se ra	dius_worst tex	ture_wors	t

842302	0.03003	0.0	006193	25.38	8	17.33
842517	0.01389	0.0	003532	24.99	9	23.41
84300903	0.02250	0.0	004571	23.5	7	25.53
84348301	0.05963	0.0	009208	14.9	1	26.50
84358402	0.01756	0.0	005115	22.5	4	16.67
843786	0.02165	0.0	005082	15.4	7	23.75
	${\tt perimeter_worst}$	${\tt area_worst}$	smoothness	s_worst	compactne	ss_worst
842302	184.60	2019.0		0.1622		0.6656
842517	158.80	1956.0		0.1238		0.1866
84300903	152.50	1709.0		0.1444		0.4245
84348301	98.87	567.7		0.2098		0.8663
84358402	152.20	1575.0		0.1374		0.2050
843786	103.40	741.6		0.1791		0.5249
	${\tt concavity_worst}$	concave.po	ints_worst	symmetry	y_worst	
842302	0.7119		0.2654		0.4601	
842517	0.2416		0.1860		0.2750	
84300903	0.4504		0.2430		0.3613	
84348301	0.6869		0.2575		0.6638	
84358402	0.4000		0.1625		0.2364	
843786	0.5355		0.1741		0.3985	
	<pre>fractal_dimension</pre>	on_worst				
842302		0.11890				
842517		0.08902				
84300903		0.08758				
84348301		0.17300				
84358402		0.07678				
843786		0.12440				

Q. How many patient/samples are in this dataset? nrow()

nrow(wisc.df)

[1] 569

Q. How many of the observations have a malignant diagnosis? table()

```
#summarizes the quantity of diagnosis by malignant or benign
table(wisc.df$diagnosis)
```

B M 357 212

```
#sums the number of malignant diagnosis
sum(wisc.df$diagnosis == "M")
```

[1] 212

Q. How many variables/features in the data are suffixed with _mean?

```
#column names
colnames(wisc.df)
```

```
[1] "diagnosis"
                                "radius_mean"
 [3] "texture_mean"
                                "perimeter_mean"
 [5] "area_mean"
                                "smoothness_mean"
 [7] "compactness_mean"
                                "concavity_mean"
 [9] "concave.points_mean"
                                "symmetry_mean"
[11] "fractal_dimension_mean"
                                "radius_se"
[13] "texture_se"
                                "perimeter_se"
[15] "area_se"
                                "smoothness_se"
[17] "compactness_se"
                                "concavity_se"
[19] "concave.points_se"
                                "symmetry_se"
[21] "fractal_dimension_se"
                                "radius_worst"
[23] "texture_worst"
                                "perimeter_worst"
                                "smoothness_worst"
[25] "area_worst"
[27] "compactness_worst"
                                "concavity_worst"
[29] "concave.points_worst"
                                "symmetry_worst"
[31] "fractal_dimension_worst"
```

```
#dimensions
dim(wisc.df)
```

[1] 569 31

```
#grep gives index of which columns contain mean
length(grep("mean",colnames(wisc.df)))
```

[1] 10

Cleaning the Data

There is a diangosis column that is the clincian conensus that I want to exclude from any further analysis. We will come back later and comapre our results to this, so omit the Diagnosis column.

```
# We can use -1 here to remove the first column
wisc.data <- wisc.df[,-1]
head(wisc.data)</pre>
```

	radius_mean	texture_mean	n perimet	er_mean	area_mean	smoothr	ness_mean
842302	17.99	10.38	3	122.80	1001.0		0.11840
842517	20.57	17.77	7	132.90	1326.0		0.08474
84300903	19.69	21.25	5	130.00	1203.0		0.10960
84348301	11.42	20.38	3	77.58	386.1		0.14250
84358402	20.29	14.34	1	135.10	1297.0		0.10030
843786	12.45	15.70)	82.57	477.1		0.12780
	compactness	_mean concavi	ity_mean	concave.	points_me	an symme	etry_mean
842302	0.2	27760	0.3001		0.147	10	0.2419
842517	0.0	7864	0.0869		0.070	17	0.1812
84300903	0.1	15990	0.1974		0.127	90	0.2069
84348301	0.2	28390	0.2414		0.105	20	0.2597
84358402	0.1	13280	0.1980		0.104	30	0.1809
843786	0.1	17000	0.1578		0.080	89	0.2087
	fractal_dime	ension_mean 1	radius_se	texture	e_se perim	eter_se	area_se
842302		0.07871	1.0950	0.9	9053	8.589	153.40
842517		0.05667	0.5435	0.7	7339	3.398	74.08
84300903		0.05999	0.7456	0.7	7869	4.585	94.03
84348301		0.09744	0.4956	1.1	1560	3.445	27.23
84358402		0.05883	0.7572	0.7	7813	5.438	94.44
843786		0.07613	0.3345	0.8	3902	2.217	27.19
		se compactnes		cavity_s	se concave	_	
842302	0.00639	99 0.0)4904	0.0537	73	0.015	587
842517	0.00522	25 0.0	01308	0.0186	60	0.013	340
84300903	0.00615	50 0.0	04006	0.0383	32	0.020	058
84348301	0.00911	10 0.0	7458	0.0566	31	0.018	367
84358402	0.01149	90 0.0	02461	0.0568	38	0.018	385
843786	0.00751		3345	0.0367		0.011	
	• • •	fractal_dime	_	_	worst tex	ture_wor	rst
842302	0.03003		0.006193		25.38	17.	. 33
842517	0.01389		0.003532		24.99	23	.41

84300903	0.02250	0.0	04571	23.5	57	25.53
84348301	0.05963	0.0	09208	14.9	91	26.50
84358402	0.01756	0.0	05115	22.5	54	16.67
843786	0.02165	0.0	05082	15.4	17	23.75
	perimeter_worst	area_worst	smoothness	s_worst	compactne	ss_worst
842302	184.60	2019.0		0.1622		0.6656
842517	158.80	1956.0		0.1238		0.1866
84300903	152.50	1709.0		0.1444		0.4245
84348301	98.87	567.7		0.2098		0.8663
84358402	152.20	1575.0		0.1374		0.2050
843786	103.40	741.6		0.1791		0.5249
	concavity_worst	concave.poi	.nts_worst	symmetr	ry_worst	
842302	0.7119		0.2654		0.4601	
842517	0.2416		0.1860		0.2750	
84300903	0.4504		0.2430		0.3613	
84348301	0.6869		0.2575		0.6638	
84358402	0.4000		0.1625		0.2364	
843786	0.5355		0.1741		0.3985	
	fractal_dimension	on_worst				
842302		0.11890				
842517		0.08902				
84300903		0.08758				
84348301		0.17300				
84358402		0.07678				
843786		0.12440				

```
diagnosis <- as.factor(wisc.df$diagnosis)</pre>
```

head(diagnosis)

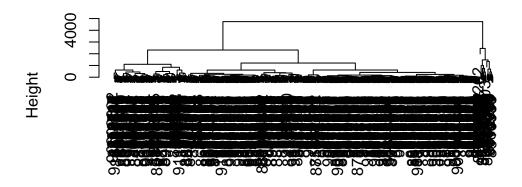
[1] M M M M M M M Levels: B M

Clustering

Let's try hclust()

```
hc <- hclust(dist(wisc.data))
plot(hc)</pre>
```

Cluster Dendrogram



dist(wisc.data) hclust (*, "complete")

We can extract clusters from this rather poor dendrogram/tree with the cutree()

```
grps <- cutree(hc, k = 2)</pre>
```

How many individuals in each cluster

table(grps)

grps 1 2 549 20

We can generate a cross-table that compares our cluster ${\tt grps}$ vector

```
#tells
table(diagnosis, grps)
```

```
grps
diagnosis 1 2
B 357 0
M 192 20
```

Principal Component Analysis (PCA)

The Importance of scaling

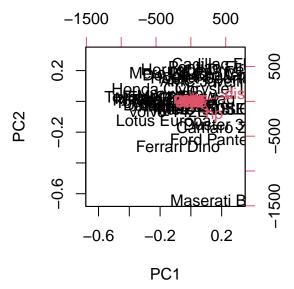
The main function for PCA in base R is prcomp() it has a default input parameter of scale = FALSE.

```
#prcomp()
head(mtcars)
```

	mpg	cyl	disp	hp	drat	wt	qsec	vs	\mathtt{am}	gear	carb
Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4
Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4
Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1	4	1
Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	3	1
Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	0	0	3	2
Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1

We could do a PCA of this data as is and it could be misleading...

```
pc <- prcomp(mtcars)
biplot(pc)</pre>
```



Lets look at the mean values of each column and their standard deviation

colMeans(mtcars)

```
drat
                  cyl
                            disp
                                          hp
                                                                           qsec
                                                                 wt
      mpg
20.090625
            6.187500 230.721875 146.687500
                                               3.596563
                                                                     17.848750
                                                           3.217250
       vs
                            gear
                   am
                                        carb
 0.437500
            0.406250
                        3.687500
                                    2.812500
```

apply(mtcars, 2, sd)

```
cyl
                               disp
                                             hp
                                                        drat
                                                                       wt
      mpg
6.0269481
            1.7859216 123.9386938
                                     68.5628685
                                                   0.5346787
                                                                0.9784574
     qsec
                    ٧s
                                           gear
                                                        carb
                                                   1.6152000
1.7869432
            0.5040161
                         0.4989909
                                      0.7378041
```

We can "scale" this data data before PCA to get a much better representation and analysis of all the columns.

mtscale <- scale(mtcars)</pre>

round(colMeans(mtscale))

```
mpg cyl disp hp drat wt qsec vs am gear carb 0 0 0 0 0 0 0 0 0 0 0
```

apply(mtscale, 2, sd)

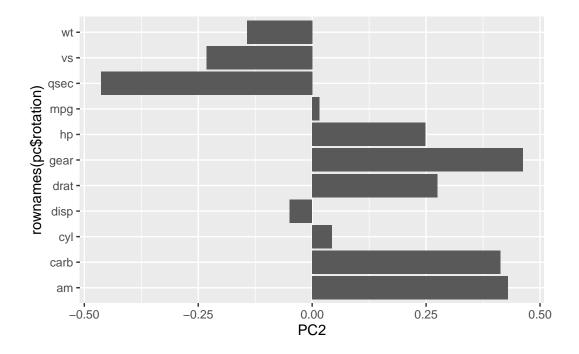
```
        mpg
        cyl
        disp
        hp
        drat
        wt
        qsec
        vs
        am
        gear
        carb

        1
        1
        1
        1
        1
        1
        1
        1
        1
        1
        1
        1
```

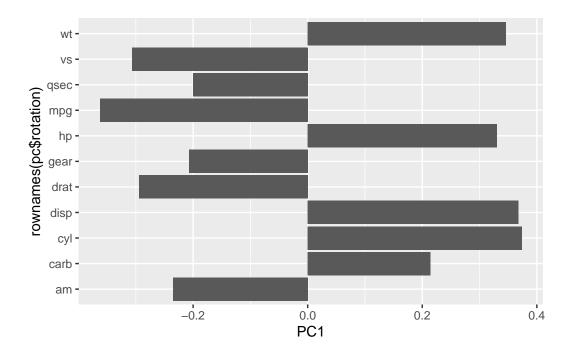
pc.scale <- prcomp(mtscale)</pre>

We can look at the two main results figures from PCA - the "PC plot" aka (score plot, ordienation plot, or PC1 vs PC2 plot). The "loadings plot" how the original variables contribute to the new PCs

```
ggplot(pc.scale$rotation) +
    aes(PC2, rownames(pc$rotation)) +
    geom_col()
```

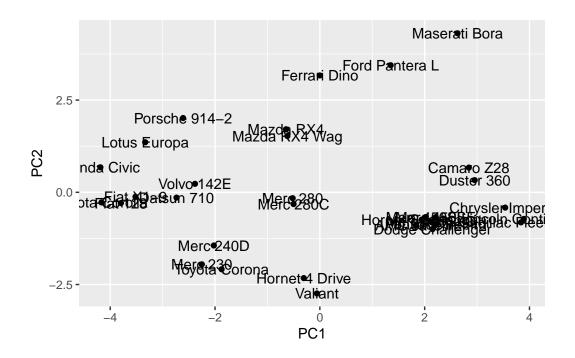


```
ggplot(pc.scale$rotation) +
  aes(PC1, rownames(pc$rotation)) +
  geom_col()
```



PC plot of scaled PCA results

```
ggplot(pc.scale$x) +
  aes(PC1, PC2, label = rownames(pc.scale$x)) +
  geom_point() +
  geom_text()
```



Key point: In general we will set scale = TRUE when we do PCA. This is not the default but porably should be...

Scaling the Wisconsin data

We can check the SD and mean of the different columns in wisc.data to see if we need to scale - hint: we do!

```
wisc.pr <- prcomp(wisc.data, scale = TRUE)</pre>
```

To see how well PCA is doing here in terms of capturing the variance(spread) in the data we can use the sumarry() function

```
summary(wisc.pr)
```

Importance of components:

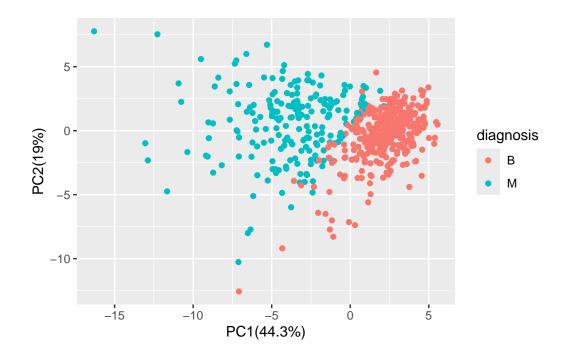
```
PC1
                                  PC2
                                          PC3
                                                  PC4
                                                           PC5
                                                                   PC6
                                                                           PC7
Standard deviation
                       3.6444 2.3857 1.67867 1.40735 1.28403 1.09880 0.82172
Proportion of Variance 0.4427 0.1897 0.09393 0.06602 0.05496 0.04025 0.02251
Cumulative Proportion
                       0.4427 0.6324 0.72636 0.79239 0.84734 0.88759 0.91010
                           PC8
                                   PC9
                                          PC10
                                                 PC11
                                                          PC12
                                                                  PC13
                                                                          PC14
```

```
Standard deviation
                       0.69037 0.6457 0.59219 0.5421 0.51104 0.49128 0.39624
Proportion of Variance 0.01589 0.0139 0.01169 0.0098 0.00871 0.00805 0.00523
Cumulative Proportion 0.92598 0.9399 0.95157 0.9614 0.97007 0.97812 0.98335
                          PC15
                                  PC16
                                          PC17
                                                  PC18
                                                          PC19
                                                                  PC20
                                                                         PC21
Standard deviation
                       0.30681 0.28260 0.24372 0.22939 0.22244 0.17652 0.1731
Proportion of Variance 0.00314 0.00266 0.00198 0.00175 0.00165 0.00104 0.0010
Cumulative Proportion 0.98649 0.98915 0.99113 0.99288 0.99453 0.99557 0.9966
                                         PC24
                          PC22
                                  PC23
                                                 PC25
                                                         PC26
                                                                 PC27
                                                                         PC28
Standard deviation
                       0.16565 0.15602 0.1344 0.12442 0.09043 0.08307 0.03987
Proportion of Variance 0.00091 0.00081 0.0006 0.00052 0.00027 0.00023 0.00005
Cumulative Proportion 0.99749 0.99830 0.9989 0.99942 0.99969 0.99992 0.99997
                          PC29
                                  PC30
Standard deviation
                       0.02736 0.01153
Proportion of Variance 0.00002 0.00000
Cumulative Proportion 1.00000 1.00000
```

Wisconsin PCA plots

Let's make the main PC1 vs PC2

```
ggplot(wisc.pr$x) +
  aes(PC1, PC2, col = diagnosis) +
  geom_point() +
  xlab("PC1(44.3%)") +
  ylab("PC2(19%)")
```



Q. From your results, what proportion of the original variance is captured by the first principal components (PC1)?

0.4427

Q. How many principal components (PCs) are required to describe at least 70% of the original variance in the data?

at least 3 PCs

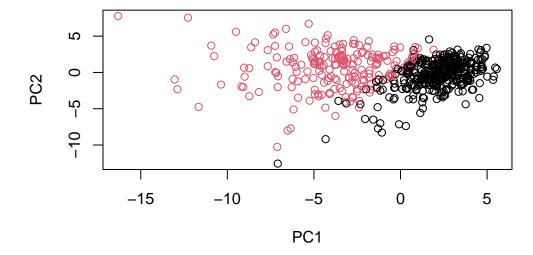
Q. How many principal components (PCs) are required to describe at least 90% of the original variance in the data?

at least 4 PCs

Q. What stands out to you about this plot? Is it easy or difficult to understand? Why?

The biplot of mtcars is not easy to understand, it is very messy compact and diffucult to understand the relationship of anything.

Q. Generate a similar plot for principal components 1 and 3. What do you notice about these plots?



The plots appear to be the same spread but flipped, 1 and 2 are slightly higher on the axis vs 1 and 3 are lower on the axis. The spread/variance however remains the same, the main difference being if you flipped PC1 and PC2 downwards you would have the same result as PC1 and PC3.

Q. For the first principal component, what is the component of the loading vector (i.e. wisc.pr\$rotation[,1]) for the feature concave.points_mean?

wisc.pr\$rotation[,1]

radius_mean	texture_mean	perimeter_mean
-0.21890244	-0.10372458	-0.22753729
area_mean	${\tt smoothness_mean}$	compactness_mean
-0.22099499	-0.14258969	-0.23928535
concavity_mean	concave.points_mean	symmetry_mean
-0.25840048	-0.26085376	-0.13816696
fractal_dimension_mean	radius_se	texture_se
-0.06436335	-0.20597878	-0.01742803

smoothness_se	area_se	perimeter_se
-0.01453145	-0.20286964	-0.21132592
concave.points_se	concavity_se	compactness_se
-0.18341740	-0.15358979	-0.17039345
radius_worst -0.22799663	fractal_dimension_se	symmetry_se -0.04249842
area_worst	perimeter_worst	texture_worst
-0.22487053	-0.23663968	-0.10446933
concavity_worst	compactness_worst	smoothness_worst
-0.22876753	-0.21009588	-0.12795256
fractal_dimension_worst -0.13178394	symmetry_worst -0.12290456	concave.points_worst -0.25088597

concave.points_mean it is -0.26085376

Q. What is the minimum number of principal components required to explain 80% of the variance of the data?

In this instance it is a minimum of 5 PCs

Combining methods

Clustering on PCA results

We can take our PCA results and use them as a basis set for other analysis such as clustering

```
wisc.pr.hclust <- hclust(dist(wisc.pr$x[,1:2]), method = "ward.D2")
plot(wisc.pr.hclust)</pre>
```

Cluster Dendrogram



dist(wisc.pr\$x[, 1:2]) hclust (*, "ward.D2")

We can "cut" this tree to yield our clusters(groups):

```
pc.grps <- cutree(wisc.pr.hclust, k = 2)
table(pc.grps)</pre>
```

pc.grps
 1 2
195 374

Q. Can you find a better cluster vs diagnoses match by cutting into a different number of clusters between 2 and 10?

no, creating more clusters creates a mess of a diagram and table.

How do my cluster grps compare to the expert diagnosis

table(diagnosis, pc.grps)

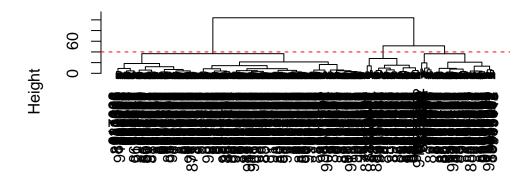
table(diagnosis, grps)

```
grps
diagnosis 1 2
B 357 0
M 192 20
```

Q. Using the plot() and abline() functions, what is the height at which the clustering model has 4 clusters?

```
plot(wisc.pr.hclust)
abline( h = 40, col="red", lty=2)
```

Cluster Dendrogram



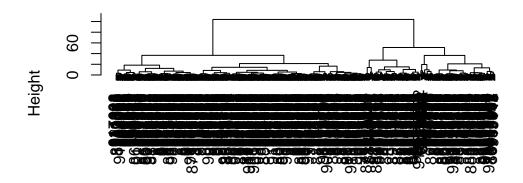
dist(wisc.pr\$x[, 1:2]) hclust (*, "ward.D2")

Q. Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

ward.D2 method gives me my favorite results, this is because the overall diagram is much easier to look at and therefor undersand. The clusters are simplified to be minimal and allow for easier visualization of clustering. The other methods produced very complicated chain/branching diagrams making it more difficult to understand the clusters and the relationships.

```
hc2 <- hclust(dist(wisc.pr$x[,1:2]), method = "ward.D2")
plot(hc2)</pre>
```

Cluster Dendrogram



dist(wisc.pr\$x[, 1:2]) hclust (*, "ward.D2")

How well does k-means separate the two diagnoses? How does it compare to your hclust results?

kmeans is less effective than helust results. comparing the kmeans clusters to diagnosis had 356 benign and 82 malignant in 1 and 1 benign, 130 malignant in 2. However the helust options identified 18 people as B in group 1 and 338 in group 2 whereas malignant diagnosis were 177 in group 1 and 35 in group 2.

```
wisc.km <- kmeans(wisc.data, centers = 2)
table(wisc.km$cluster, diagnosis)</pre>
```

diagnosis B M 1 356 82 2 1 130

Q. How well does the newly created model with four clusters separate out the two diagnoses?

```
clust4 <- cutree(wisc.pr.hclust, k = 4)
table(clust4)</pre>
```

```
clust4
1 2 3 4
112 83 250 124
```

creating four clusters to separate the diagnosis is not recommended. It splits only two diagnosis intwo four different groups of which we are not aware are malignant or benign. It also makes understanding the table results more confusing.

Q. How well do the k-means and hierarchical clustering models you created in previous sections (i.e. before PCA) do in terms of separating the diagnoses? Again, use the table() function to compare the output of each model (wisc.km\$cluster and wisc.hclust.clusters) with the vector containing the actual diagnoses.

They did really badly, we do much better after PCA - the new PCA variables (what we call a basis set) give us much better separation of M and B

Prediction

We can use our PCA model for the analysis of the new "unseen" data. In this case from U. Michigan.

```
#url <- "new_samples.csv"
url <- "https://tinyurl.com/new-samples-CSV"
new <- read.csv(url)
npc <- predict(wisc.pr, newdata=new)
npc</pre>
```

```
PC1
                                PC3
                                           PC4
                                                     PC5
                                                                PC6
                                                                           PC7
                     PC2
     2.576616 -3.135913
                         1.3990492 -0.7631950 2.781648 -0.8150185 -0.3959098
[2,] -4.754928 -3.009033 -0.1660946 -0.6052952 -1.140698 -1.2189945
                                                                     0.8193031
           PC8
                      PC9
                                PC10
                                          PC11
                                                    PC12
                                                              PC13
                                                                       PC14
[1,] -0.2307350 0.1029569 -0.9272861 0.3411457 0.375921 0.1610764 1.187882
[2,] -0.3307423 0.5281896 -0.4855301 0.7173233 -1.185917 0.5893856 0.303029
         PC15
                    PC16
                                 PC17
                                             PC18
                                                         PC19
                                                                    PC20
[1,] 0.3216974 -0.1743616 -0.07875393 -0.11207028 -0.08802955 -0.2495216
[2,] 0.1299153 0.1448061 -0.40509706 0.06565549 0.25591230 -0.4289500
           PC21
                      PC22
                                 PC23
                                            PC24
                                                        PC25
                                                                     PC26
[1,] 0.1228233 0.09358453 0.08347651 0.1223396 0.02124121 0.078884581
```

- [2,] -0.1224776 0.01732146 0.06316631 -0.2338618 -0.20755948 -0.009833238 PC27 PC28 PC29 PC30
- [1,] 0.220199544 -0.02946023 -0.015620933 0.005269029
- [2,] -0.001134152 0.09638361 0.002795349 -0.019015820

Q18. Which of these new patients should we prioritize for follow up based on your results?

We should prioritize all the patients that are under the malignant category of groups 1 and 2.