

ساختمان داده ها

ساخت درخت دودویی از روی پیمایش ها

Binary Tree Construction from Iterations

مدرس: غیاثی شیرازی

دانشگاه فردوسی مشهد

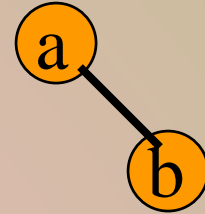
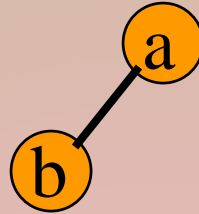
# Binary Tree Construction

- Suppose that the elements in a binary tree are distinct.
- Can you construct the binary tree from which a given traversal sequence came?
- When a traversal sequence has more than one element, the binary tree is not uniquely defined.
- Therefore, the tree from which the sequence was obtained cannot be reconstructed uniquely.

# Some Examples

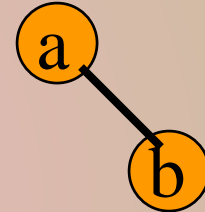
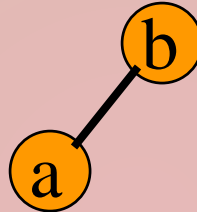
preorder

= ab



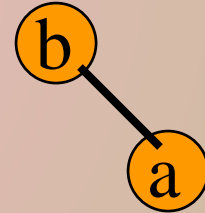
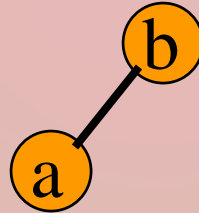
inorder

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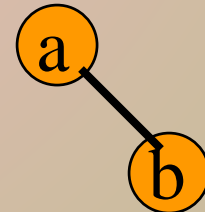
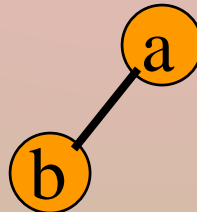
postorder

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level order

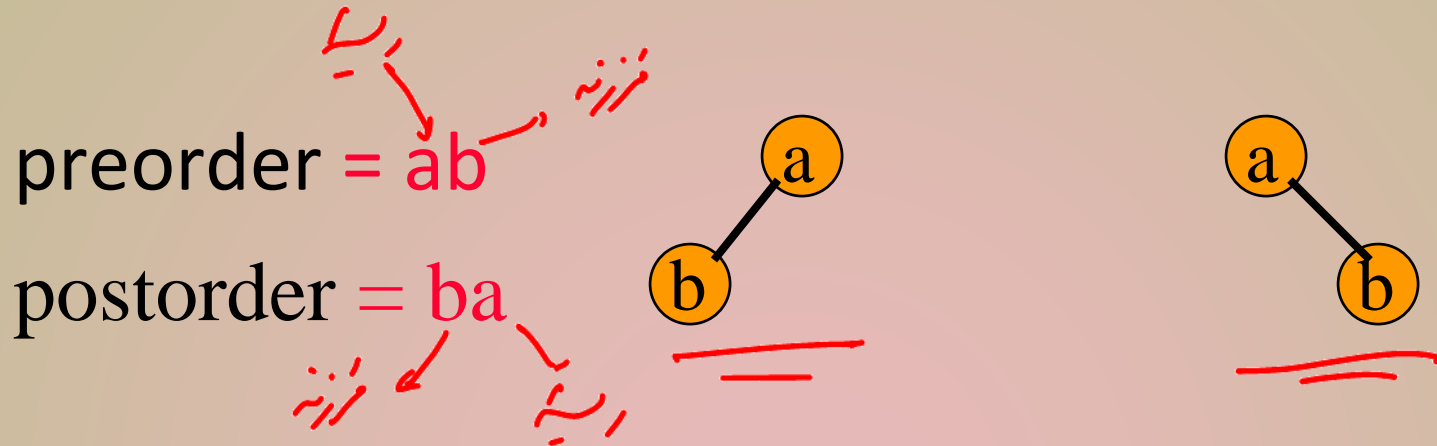
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# Binary Tree Construction

- Can you construct the binary tree, given two traversal sequences?
- Depends on which two sequences are given.

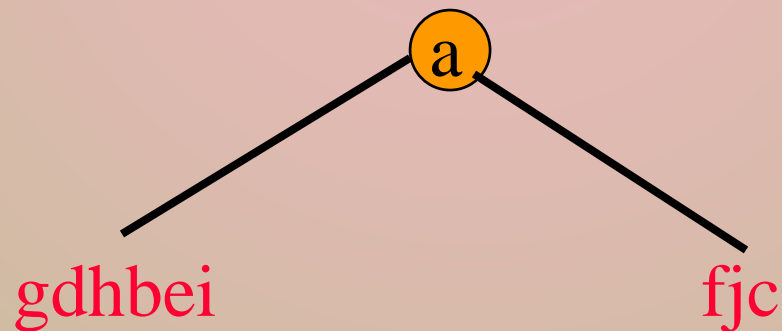
# Preorder And Postorder



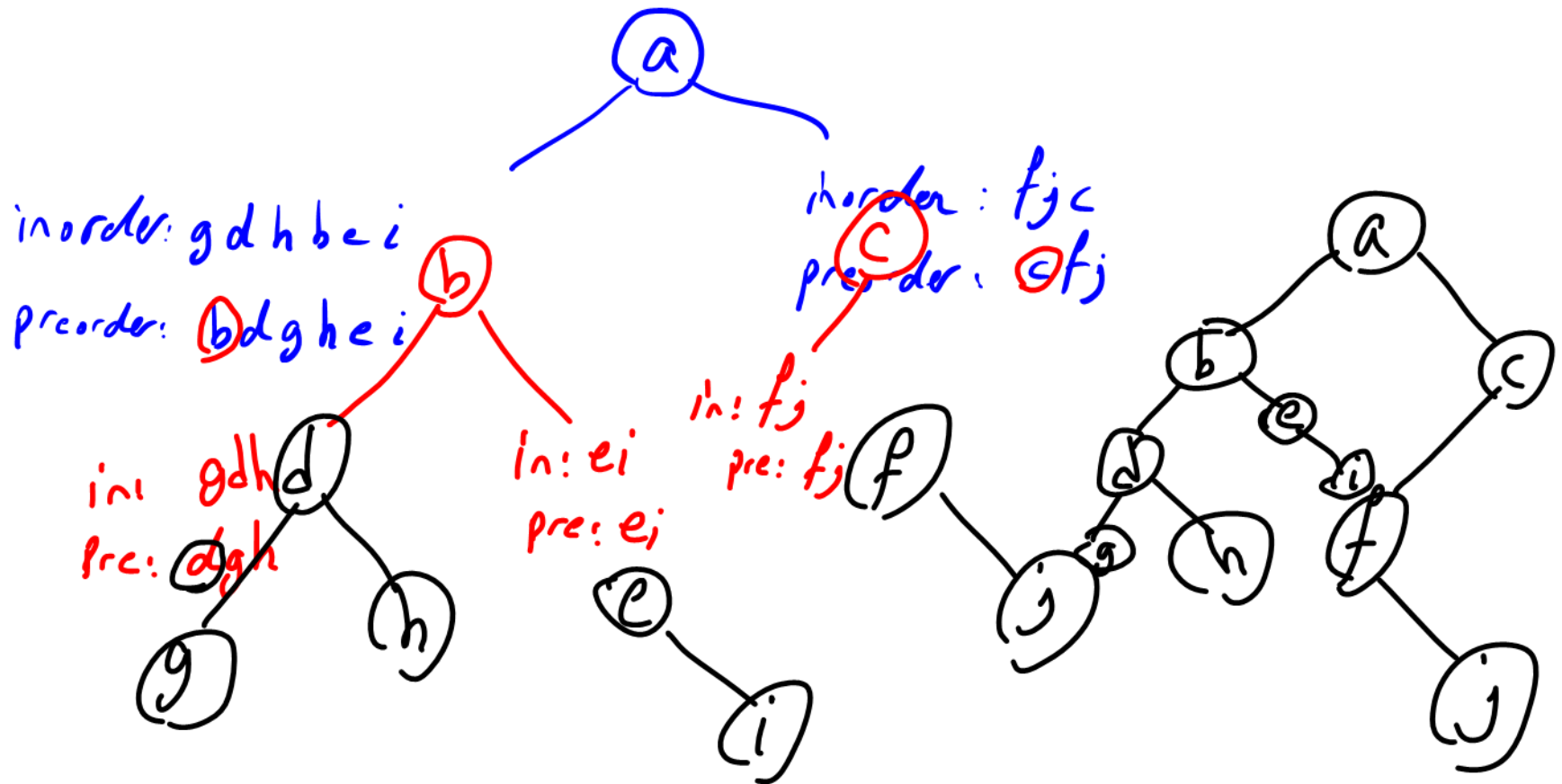
- Preorder and postorder do not uniquely define a binary tree.
- Nor do preorder and level order (same example).
- Nor do postorder and level order (same example).

# Inorder And Preorder

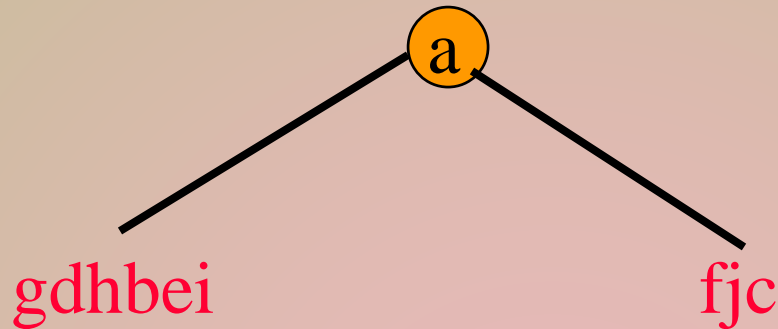
- inorder = g d h b e i a f j c
- preorder = a b d g h e i c f j
- Scan the preorder left to right using the inorder to separate left and right subtrees.
- a is the root of the tree; gdhbei are in the left subtree; fjc are in the right subtree.



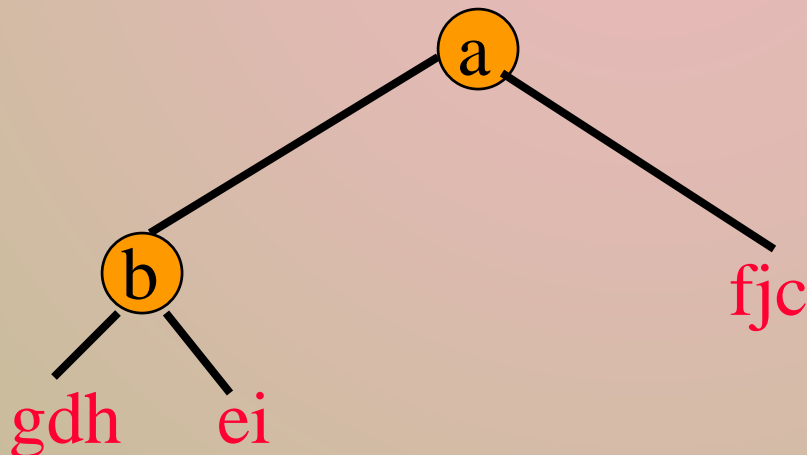
- inorder = g d h b e i a f j c
- preorder = a b d g h e i c f j



# Inorder And Preorder

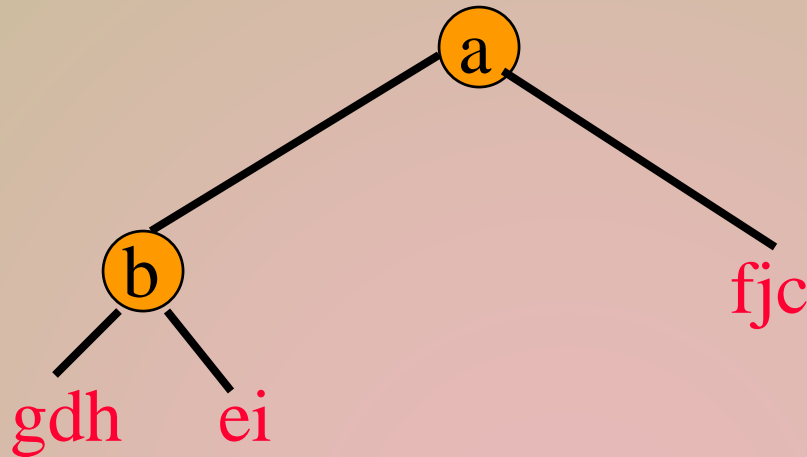


- preorder = a b d g h e i c f j
- b is the next root; gdh are in the left subtree; ei are in the right subtree.

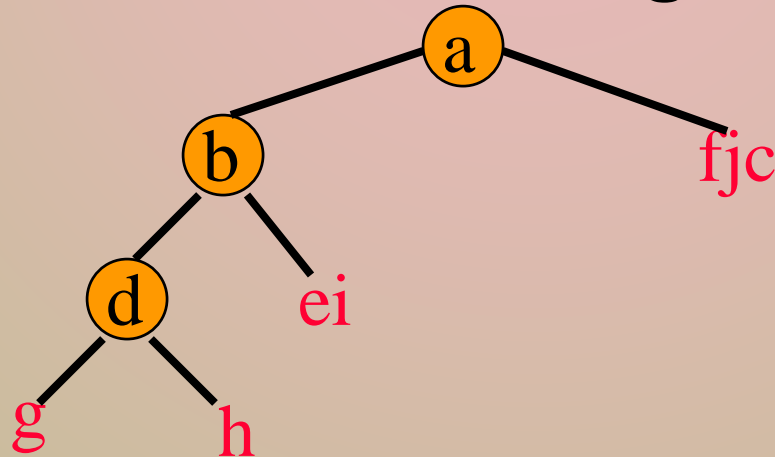




# Inorder And Preorder



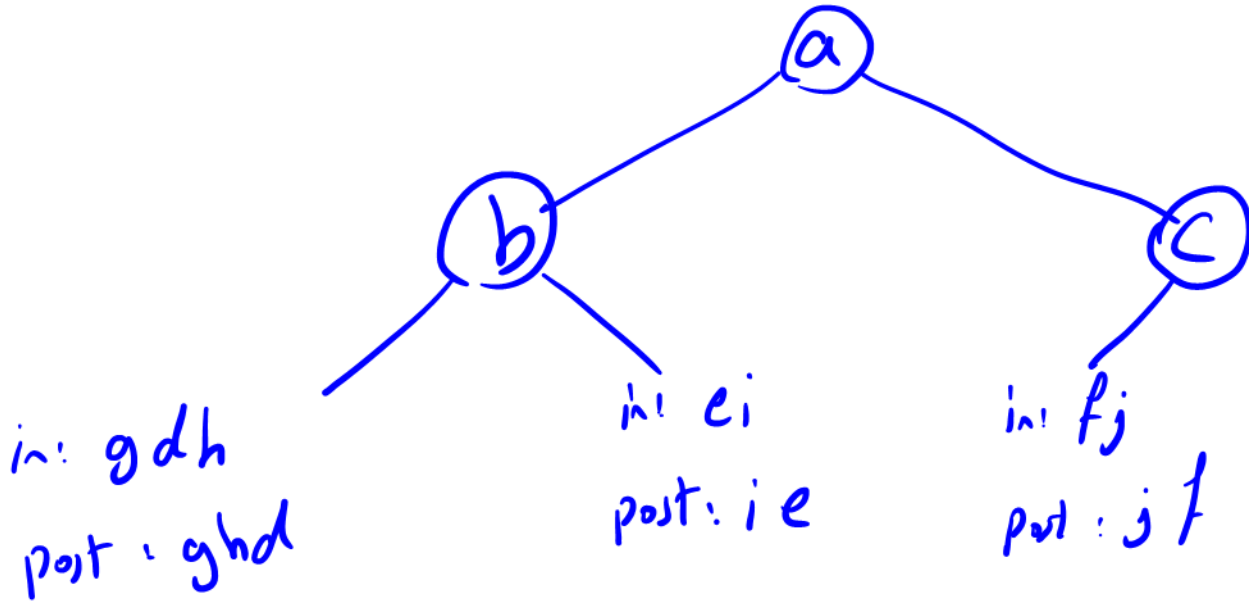
- preorder = a b d g h e i c f j
- d is the next root; g is in the left subtree; h is in the right subtree.



# Inorder And Postorder

- Scan postorder from right to left using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- postorder = g h d i e b j f c a
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.

inorder = g d h b e i a f j c  
postorder = g h d i e b j f c a



# Inorder And Level Order

- Scan level order from left to right using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- level order = a b c d e f g h i j
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.

- inorder = g d h b e i a f j c
- level order = a b c d e f g h i j

