

# BUILDING BLOCKS

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Generic function and overloading sets. Basic concepts.

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# Raising a number to a power

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov
- Let's start with the first one.
- `unsigned nth_power(unsigned x, unsigned n); // returns  $x^n$`
- How to write the body of this function?

# Getting the algorithm right

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
unsigned nth_power(unsigned x, unsigned n) {  
    unsigned acc = 1;  
    if ((x < 2) || (n == 1)) return x;  
    while (n > 0) {  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        x *= x; n /= 2;  
    }  
    return acc;  
}
```

# Figuring out possible generalizations

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
unsigned nth_power(unsigned x, unsigned n) {  
    unsigned acc = 1;  
    if ((x < 2) || (n == 1)) return x;  
    while (n > 0) {  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        x *= x; n /= 2;  
    }  
    return acc;  
}
```

# Naive generalization

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
template <typename T> T nth_power(T x, unsigned n) {  
    T acc = 1;  
    if ((x < 2) || (n == 1)) return x;  
    while (n > 0) {  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        x *= x; n /= 2;  
    }  
    return acc;  
}
```

# Naive generalization issues

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
template <typename T> T nth_power(T x, unsigned n) {  
    T acc = 1;  
    if ((x < 2) || (n == 1)) return x;  
    while (n > 0) {  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        x *= x; n /= 2;  
    }  
    return acc;  
}
```

# Less naive generalization

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
template <typename T> T nth_power(T x, unsigned n) {  
    T acc = id<T>();  
    if ((x == acc) || (n == 1)) return x;  
    while (n > 0) {  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        x *= x; n /= 2;  
    }  
    return acc;  
}
```

# Introducing traits

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
template <typename T, typename Trait = default_id_trait<T>>
T nth_power(T x, unsigned n) {
    T acc = Trait::id();
    if ((x == acc) || (n == 1)) return x;
    while (n > 0) {
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }
        x *= x; n /= 2;
    }
    return acc;
}
```



# Separating the clean part

- "The first step is to get the algorithm right. The second step is to figure out which sorts of things (types) it works for" – Alex Stepanov

```
template <typename T> T nth_power(T x, T acc, unsigned n) {  
    while (n > 0)  
        if ((n & 0x1) == 0x1) { acc *= x; n -= 1; }  
        else { x *= x; n /= 2; }  
    return acc;  
}
```

```
unsigned nth_power(unsigned x, unsigned n) {  
    if (x < 2u || n == 1u) return x;  
    return nth_power<unsigned>(x, 1u, n);  
}
```

# Building blocks

- The building block of generic programming is an overload set.

```
template <typename T> T nth_power(T x, T acc, unsigned n);
```

```
unsigned nth_power(unsigned x, unsigned n);
```

```
double nth_power(double x, unsigned n);
```

- We will encounter this repeatedly: classes are designed with sets of overloaded constructors, operators, methods, etc.

# Back to Strings

- What if we try to write `operator==` для `basic_string`?
- One simple solution

```
template<typename CharT, typename Traits, typename Alloc>
bool operator==(const basic_string<CharT, Traits, Alloc>& lhs,
                const basic_string<CharT, Traits, Alloc>& rhs) {
    return lhs.compare(rhs) == 0;
}
```

- What's wrong with it?

# Back to Strings

- What if we try to write `operator==` для `basic_string`?
- One simple solution

```
template<typename CharT, typename Traits, typename Alloc>
bool operator==(const basic_string<CharT, Traits, Alloc>& lhs,
                const basic_string<CharT, Traits, Alloc>& rhs) {
    return lhs.compare(rhs) == 0;
}
```

- It is inefficient. Think about `("hello" == str)`, an extra copy is clearly created here.
- We would prefer to overload it as a regular function.

# A Better Comparison Approach

- The adopted solution (including in libstdc++) uses overloads.

```
template<typename CharT, typename Traits, typename Alloc>
bool operator==(const basic_string<CharT, Traits, Alloc>& lhs,
                const basic_string<CharT, Traits, Alloc>& rhs) {
    return lhs.compare(rhs) == 0;
}
```

```
template<typename CharT, typename Traits, typename Alloc>
bool operator==(const CharT* lhs, const basic_string<CharT, Traits, Alloc>& rhs) {
    return rhs.compare(lhs) == 0;
}
```

```
template<typename CharT, typename Traits, typename Alloc>
bool operator==(const basic_string<CharT, Traits, Alloc>& lhs, const CharT* rhs) {
    return lhs.compare(rhs) == 0;
}
```

# Discussion

- Are there any general principles for designing an overload set?

# Examples of Good Design

- Different but related types.

```
void Foo(const char* s);  
void Foo(std::string s) { Foo(s.c_str()); }
```

- Different number of parameters.

```
auto s1 = twine("Hello", name).str();  
auto s2 = twine("Hello", name, " ", surname).str();
```

- Optimizations.

```
void vector<T>::push_back(const T&);  
void vector<T>::push_back(T&&);
```

# Winter's Rules

- A person should not be forced to mentally perform overload resolution.
- A single comment can describe the entire set.
- **Each element in the overload set does roughly the same thing.**
- Below is an example of very poor design.

```
// For an integer argument n, returns the smallest coprime  
number greater than 1. For a string argument (a comma-  
separated list of coprimes), deduces and returns the smallest  
possible n that could have generated that list
```

```
int least_coprime(int n);  
int least_coprime(const std::string& x);
```



# Overload Set: Transform

- Is this a good overload set?

```
template <class InputIt, class OutputIt, class UnaryOp>  
OutputIt transform(InputIt first1, InputIt last1,  
                  OutputIt d_first, UnaryOp unary_op);
```

```
template <class ExecutionPolicy,  
          class ForwardIt1, class ForwardIt2, class UnaryOp>  
ForwardIt2 transform(ExecutionPolicy&& policy,  
                    ForwardIt1 first1, ForwardIt1 last1,  
                    ForwardIt2 d_first, UnaryOp unary_op);
```

```
template <class InputIt1, class InputIt2, class OutputIt, class BinaryOp >  
OutputIt transform(InputIt1 first1, InputIt1 last1, InputIt2 first2,  
                  OutputIt d_first, BinaryOp binary_op);
```

# Overload Set: String Constructors

- Is this a good overload set?

```
basic_string();  
basic_string(size_type count, CharT ch);  
basic_string(const basic_string& other, size_type pos);  
basic_string(const basic_string& other, size_type pos, size_type count);  
basic_string(basic_string&& other, size_type pos, size_type count);  
basic_string(const CharT* s, size_type count);  
basic_string(const CharT* s);  
template <class InputIt> basic_string(InputIt first, InputIt last);  
basic_string(const basic_string& other);  
basic_string(basic_string&& other);  
basic_string(std::initializer_list<CharT> ilist);  
template <class StringViewLike> explicit basic_string(const StringViewLike& t);  
template <class StringViewLike> explicit basic_string(const StringViewLike& t,  
                                                         size_type pos, size_type count);
```

# We Must Be Nice

- We must somehow encode the requirements for the interface of generic functions.

```
template <typename T, typename U>  
bool check_eq(T lhs, U rhs) { return (lhs == rhs); }
```

- The simplest way to document this is with a requires constraint.

```
template <typename T, typename U>  
requires is_equality_comparable<T, U>::value  
bool check_eq (T lhs, U rhs) { return (lhs == rhs); }
```

- Now, instead of an error inside the function, we simply exclude it from the overload set.

# Combining Constraints

- Constraints are easy to combine

```
template <typename Iter>  
    requires(is_forward_iterator<Iter>::value &&  
             is_totally_ordered<typename Iter::value_type>::value)  
Iter my_min_element(Iter first, Iter last) {
```

- Here, both requirements must be met.
- Furthermore, different error messages are shown depending on what went wrong.

note: 'is\_forward\_iterator::value' evaluated to false

note: 'is\_totally\_ordered<typename Iter::value\_type, void>::value' evaluated to false

# Overloading by Constraints

- You can overload based on constraints.

```
struct Foo {  
    template <typename Int>  
        requires std::is_integral<Int>::value  
    Foo (Int x) { std::cout << "Creating int-like object\n"; }  
  
    template <typename Float>  
        requires std::is_floating_point<Float>::value  
    Foo (Float x) { std::cout << "Creating float-like object\n" }  
};
```

- If both failed, what to expect?

# Improving Diagnostics

- If no overload is suitable, the failed constraints from each are displayed.

```
struct S{};
```

```
Foo fs(S{});
```

- The error messages will be clear and informative.

```
note:   constraints not satisfied
```

```
note: 'std::is_integral::value' evaluated to false
```

```
note:   constraints not satisfied
```

```
note: 'std::is_floating_point::value' evaluated to false
```

# Complete coverage

- We can use explicit constraints to discriminate between functions.

```
template <typename T> requires (sizeof(T) > 4)
void foo(T x) { do smth with x }
```

```
template <typename T> requires (sizeof(T) <= 4)
void foo(T x) { do smth else with x }
```

- The special status of constraints makes them part of overload resolution.

[over.dcl] two function declarations of the same name refer to the same function if they are in the same scope and have equivalent parameter declarations and equivalent trailing requires-clauses, if any.

# Sometimes This Goes Too Far

- Expressions inside requires don't even require CT evaluation.

```
constexpr bool C() { return true; }  
  
template<typename T> struct A {  
    int f() requires (C()) { return 1; }  
  
    // this is not a redeclaration  
    int f() requires true { return 2; }  
};
```

- This means the analysis of requires clauses happens very early.



# Limitations of Simple Constraints

- Alas, simple type traits are not ordered by how restrictive they are.

```
template <typename It>
struct is_input_iterator: std::is_base_of<
    std::input_iterator_tag,
    typename std::iterator_traits<It>::iterator_category>{};
```

```
template <typename It>
struct is_random_iterator: std::is_base_of<
    std::random_access_iterator_tag,
    typename std::iterator_traits<It>::iterator_category>{};
```

- These are just two different templates. And this leads to problems.

# Limitations of Simple Constraints

- Alas, simple type traits are not ordered by how restrictive they are.

```
template <typename Iter>
    requires is_input_iterator<Iter>::value
int my_distance(Iter first, Iter last) {
    int n = 0;
    while (first != last) { ++first; ++n; }
    return n;
}
```

```
template <typename Iter>
    requires is_random_iterator<Iter>::value
int my_distance(Iter first, Iter last) { return last - first; }
```

- In practice, this would cause ambiguity for `std::vector::iterator`.

# Complex Constraints

- Let's return to a simple example.

```
template <typename T, typename U> bool  
    requires is_equality_comparable<T, U>::value  
check_eq(T &&lhs, U &&rhs) { return (lhs == rhs); }
```

- The same can be written using a requires-expression.

```
template <typename T, typename U> bool  
    requires requires(T t, U u) { t == u; }  
check_eq(T &&lhs, U &&rhs) { return (lhs == rhs); }
```

- Yes, the requires-requires might look confusing. But recall noexcept-clause and noexcept-expression.

# Even Better Diagnostics

```
template <typename T, typename U> bool  
    requires requires(T t, U u) { t == u; }  
check_eq(T &&lhs, U &&rhs) { return (lhs == rhs); }
```

- The expression

```
check_eq(std::string{"1"}, 1);
```

- Yields

note: because 't == u' would be invalid

- This not only states the constraint name, but also the specific ill-formed expression within it.

# The Key Difference of Complex Constraints

- Simple constraints are evaluated at compile time.

```
template <typename T> constexpr int somepred() { return 14; }
```

```
template <typename T>  
    requires(somepred<T>() == 42)  
bool foo(T&& lhs, U&& rhs);
```

- Complex constraints check **the validity of an expression**.

```
template <typename T>  
    requires requires(T t) { somepred<T>() == 42; }  
bool bar(T&& lhs, U&& rhs);
```

# Syntax of Complex Constraints

- Think of a complex constraint as a compile-time function returning true or false.

```
requires(T t, U u) {  
    u + v; // true если u + v синтаксически возможно [simple]  
    typename T::inner; // true если T::inner есть [type]  
}
```

- Think of each requirement inside it as a conjunct.
- Simple requirements and type requirements are basic variants of complex constraints.
- There are two more: compound and nested.

# Concepts: convertible\_to

- To define constraint systems, C++20 introduced the special keyword concept.

```
template<class From, class To>  
concept convertible_to = std::is_convertible_v<From, To> &&  
    requires {  
        static_cast<To>(std::declval<From>());  
    };
```

- Think of a concept as an abbreviation for a requires-expression.
- And of course, many useful concepts are already in your standard library.

# You can check a concept

- Any concept works as a compile-time predicate.
- But it doesn't need to be **called**. A concept is already a value.

```
struct S {};  
static_assert(std::move_constructible<S>); // ok  
bool a = std::convertible_to<int, double>; // true  
bool b = std::convertible_to<int, S>; // false
```



# Compound Requirements

- Compound requirements check type compatibility with expressions.

```
requires requires(T x) { { *x } -> typename T::inner; }
```

- A compound requirement can use concepts.

```
requires requires(T x) {  
    { *x } -> std::convertible_to<typename T::inner>; // concept  
}
```

- There is also a special noexcept syntax.

```
requires requires(T t) {  
    { ++t } noexcept;  
}
```

# Nested constraints

- Inside the requires-expression it can be repeated. This is nested requirement.

```
requires(T t) {  
    requires sizeof(T) == 4; // calculated [nested]  
    requires somepred<T>() == 42; // consteval predicate [nested]  
    requires noexcept(++t); // noexcept expression [nested]  
}
```

- Task: simplify this nested requires-clause.

```
template <typename T> int foo(T)  
requires requires(T t) { requires noexcept(++t); } {  
    return 42;  
}
```

# Constraints on Concepts

- Recursive concepts are not allowed.

```
template<bool b, bool ... bs>  
concept AllTrueRec = b &&  
    ((sizeof...(bs) == 0) ? true : AllTrueRec<bs...>); // ERROR
```

- Concepts cannot be directly constrained by other predicates.

```
template <typename T>  
concept Inner = requires { typename T::inner; };  
  
template <typename T> requires Inner<T>  
concept InOuter = requires { typename T::outer; }; // ERROR
```

# Constraints on Concepts

- Concepts cannot be directly constrained by other predicates.

```
template <typename T>
concept Inner = requires { typename T::inner; };

template <typename T> requires Inner<T>
concept InOuter = requires { typename T::outer; }; // ERROR
```

- This can be somewhat mitigated by conjunction.

```
template <typename T>
concept InOuter = Inner<T> &&
    requires { typename T::outer; }; // OK
```

# Syntax for Using Concepts

- Basic syntax.

```
template <typename T> requires std::integral<T> void foo(T);
```

- Template parameter or local variable.

```
template <std::integral T> void bar(T t);
```

```
void buz(std::integral auto t); // still function template
```

```
std::integral auto x = buz(1);
```

- You can restrict a class template as well.

```
template <typename D> requires std::is_class_v<D>  
class Foo { /* */ };
```

# Funny abbreviations

- Constraint for multiple arguments.

```
template <typename T>  
requires std::same_as<T, int>  
struct S {};
```

- Abbreviation syntax

```
template <std::same_as<int> T>  
struct S {};
```

# Concepts on member functions

- You can constraint member functions.

```
template <typename D> struct Foo {  
    bool empty() requires ranges::forward_range<D>;  
};
```

- We will see how is it used in ranges library.

```
template <typename T> struct Foo {  
    T val;  
    bool empty() requires requires { val.empty(); } {  
        return val.empty();  
    }  
};
```

- As shown above you can also use class members.

# Concept on ctor or class?

- You can constraint only ctors without constraining type.

```
template <typename T> requires requires(T x) { x.foo(); }  
struct Foo {  
    T t;  
    Foo() requires std::default_initializable<T> : t() {}  
    Foo(Foo &f) requires std::copyable<T> : t(f.t) {}  
};
```

- You can have both: generic constraint on type and specific constraints on ctors.



# Concept partial order

```
template <typename T> concept Ord = requires(T a, T b) { a < b; };
template <typename T> concept Inc = requires(T a) { ++a; };
template <typename T> concept Int = std::is_same_v<T, int>;

template <typename T> requires Ord<T> || Inc<T> || Int<T>
int foo(T x) { return 2; }

template <typename T> requires Ord<T>
int foo(T x) { return 22; }

int foo(int x) { return 42; }

double y;

foo(y); // -> ?
```

# Discussion

- How does partial specialization work?
- How does the compiler understand that `Ord` is more specialized than `(Ord || Void)`?

# Conjuncts and Disjuncts

- Every concept consists of atomic constraints joined by logical operations (with the usual short-circuiting rules for them).

```
template<typename T>  
concept Strange = (sizeof(T) == 4) ||  
    (requires() {{T::value} -> convertible_to<bool>} &&  
    T::value == true);
```

```
template<typename T> requires Strange<T>  
void f(T);
```

```
f(1); // ok (lazy rules)
```

# Subsumes

"A constraint  $P$  subsumes a constraint  $Q$  if and only if:

for every disjunctive clause  $P_i$  in the disjunctive normal form of  $P$

$P_i$  subsumes every conjunctive clause  $Q_j$  in the conjunctive normal form of  $Q$ "

[temp.constr.order]

```
template <typename T>  
concept Q1 = Q<T> || sizeof(T) == 4; // How do you think?
```

```
template <typename T>  
concept P = Q<T> && R<T>; // P subsumes Q and R
```

# Atomic constraints

- An atomic constraint  $A$  subsumes another atomic constraint  $B$  if and only if  $A$  and  $B$  are identical [temp.constr.order]

```
template <typename T> constexpr bool Atomic = true;
```

```
template <typename T> concept C = Atomic<T>;
```

```
template <typename T> concept D = Atomic<T*> && true;
```

- Here compiler cannot determine between  $D$  and  $C$ , this is ill-formed
- Of course in the ideal world we would prefer this:

**A constraint  $P$  subsumes a constraint  $Q$  if and only if  $Q$  implies  $P$ .**

# Identical not similar

```
template<typename T>
concept Foo = (sizeof(T) > 4) && std::is_integral_v<T>;

template<typename T>
concept Bar = std::is_integral_v<T>;

template <Foo T> int f(T x) { return x + 1; }

template <Bar T> int f(T x) { return x + 1; }

int main() {
    return f(1ull); // FAIL
}
```

# Subsuming not automatic

```
template<typename T> concept Foo = requires(T x) { x.foo(); };
template<typename T> concept Bar = requires(T x) { x.bar(); };

template<typename T> concept FooBar = requires(T x) {
    x.foo(); x.bar();
};

template <Foo T> int f(T x) { return x.foo(); }
template <FooBar T> int f(T x) { return x.foo() + 1; }

struct SBar { /* have both foo() and bar() */ }

f(SBar{}); // FAIL
```

# Subsuming not automatic

```
template<typename T> concept Foo = requires(T x) { x.foo(); };  
template<typename T> concept Bar = requires(T x) { x.bar(); };  
template<typename T> concept FooBar = Foo<T> && Bar<T>;
```

```
template <Foo T> int f(T x) { return x.foo(); }  
template <FooBar T> int f(T x) { return x.foo() + 1; }  
struct SBar { /* have both foo() and bar() */ }  
f(SBar{}); // OK
```



# Subsumes

- Now we can order constraints on subsuming.

```
template <typename I>
concept InputIterator = Iterator<I> &&
    requires { typename iterator_category_t<I>; } &&
    DerivedFrom<iterator_category_t<I>, input_iterator_tag>;

template <typename I>
concept ForwardIterator = InputIterator<I> &&
    Incrementable<I> && Sentinel<I, I> &&
    DerivedFrom<iterator_category_t<I>, forward_iterator_tag>;
```

- And so on, down to the random access iterator.

# Now overloading works

```
template <InputIterator Iter>
int my_distance(Iter first, Iter last) {
    int n = 0;
    while (first != last) { ++first; ++n; }
    return n;
}
```

```
template <RandomAccessIterator Iter>
int my_distance(Iter first, Iter last) {
    return last - first;
}
```

- Because InputIterator is less general (it is a subcondition of RandomAccessIterator), there is no ambiguity here.

# Sutton's Counterexample

- Lets suppose we have this implementation of copy

```
template <InputIterator In, OutputIterator<value_type_t<In>> Out>
Out copy(In first, In last, Out out) {
    // direct loop
}
```

```
template <ContIterator In, ContIterator Out>
    requires MemCopyable<In, Out>
Out copy(In first, In last, Out out) {
    // memcpy
}
```

- Here subsume relationships are hard and we can run into unexpected issues for some types.

# Sutton's Counterexample

- Sutton advises not to rely too heavily on subsumption.

```
template <InputIterator In, OutputIterator<value_type_t<In>> Out>
Out copy(In first, In last, Out out) {
    if constexpr(MemCopyable<In, Out>) {
        // реализация через memcopy
    } else {
        // реализация явным циклом
    }
}
```

- After all, how often do we introduce new iterator categories?

# The Concepts We Dreamed Of

- In the early articles about concepts, they were much more interesting.

```
concept EqualityComparable<typename T> {  
    requires constraint Equal<T>; // syntactic  
    requires axiom Equivalence_relation<Equal<T>, T>; // semantic  
  
    // if x == y then for any Predicate p, p(x) == p(y)  
    template <Predicate P> axiom Equality(T x, T y, P p) {  
        x == y => p(x) == p(y);  
    }  
  
    // inequality is the negation of equality  
    axiom Inequality(T x, T y) { (x != y) == !(x == y); }  
};
```

# Homework assignment

- [HW3.1][1] Design realistic overload set for generic function `nth_power` using constraints. Account for integers, floating point and matrices.
- [HW3.2][1] Try to explain what is going wrong here

```
template <typename... Ts> concept Addable =  
    requires(Ts... p) { (... + p); requires sizeof...(Ts) > 1; };  
  
template <Addable... Ts> auto sum_all(Ts... p) {  
    return (... + p);  
}  
  
sum_all(1, 2); // FAIL
```

# Bibliography, part 1

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