# Homework 6

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November 30, 2018

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#### 1 Chapter 18

#### 1.1 Problem 1.1

Code for this problem can be found here.

Figure 1 shows the field and obstacles integrated. From this I can take the partial derivatives of each and obtain the best gradient at every point in the field.

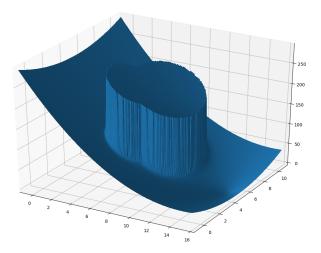


Figure 1: Potential Field with Obstacles

There was a **lot** of testing because I incorrectly entered an obstacle formula into a partial derivative calculator. After finally getting it working I had to tweak  $\gamma$  until it was able to make it through gradient decent.  $\gamma$  is sometimes called  $\alpha$  or *step size*. Once I got it to descend to the goal I had to optimize it (of course). First I tried different static  $\gamma$  values with varrying degrees of success. The real breakthrough came with Figure 2, where I applied the following:

$$\gamma = \frac{1}{(x_0 - x_{goal})^2 + (y_0 - y_{goal})^2}$$

I realized that as the distance to goal decreased it would generate exceedingly large  $\gamma$  values. This was resolved with stepping the function:

$$\begin{cases} \frac{\eta}{(x_0 - x_{goal})^2 + (y_0 - y_{goal})^2} & D > \eta\\ \gamma * 0.9 & 0.01 < D < \eta\\ 0 & D <= 0.01 \end{cases}$$

Where  $\eta=1$ , but I played around with that variable as well. Using this combination for  $\gamma$  I was able to converge in a very reasonable 174 steps. Figure 3 shows the start and end points in green, the path in blue, and the obstacles in red.

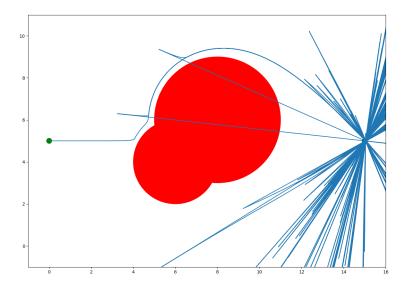


Figure 2: Explosion

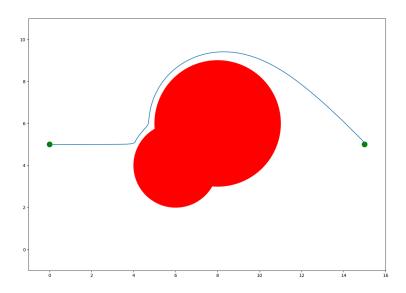


Figure 3: Proper Path Planned