

Homework 4

MacMillan, Kyle

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1 Problem 5.2

The meat and potatoes of this problem is in bump and gps callbacks, the rest is filler but can be found [here](#). The environment used is shown in Figure 1.

```
def bumpCallback(self, msg):
    hit_obj = False
    for i in range(len(msg.data)):
        hit = unpack('b', msg.data[i])[0]
        if hit != 0:
            hit_obj = True

    if hit_obj:
        # Turn right
        self.bumps += 1
        self.setVel(0.0, 2.0)
    else:
        self.bumps = 0
        self.setVel(2.0, 2.0)

def gpsCallback(self, msg):
    # we need to move to goal if we are not bumping a wall
    if self.bumps == 0:
        # Wraps deals with the robot if it spins around somehow
        wraps = np.abs(int(msg.theta / (2 * np.pi)))
        theta = np.fabs(msg.theta) - (wraps * 2 * np.pi)
        beta = np.arctan2(self.goal[1] -
                          msg.y, self.goal[0] -
                          msg.x)

        k = 0.25
        alpha = beta - theta
        w1 = 2.0 + k * alpha
        w2 = 2.0 - k * alpha
        self.setVel(w1, w2)
```

Figure 1: Problem 5.2 Stuck Robot

2 Problem 9

2.1 Problem 9.1

Figure 2 shows the required plot. The robot location is:

$$x = 803.84497$$

$$y = 485.52026$$

$$z = 517.26977$$

With an error of $E = 2720.65$

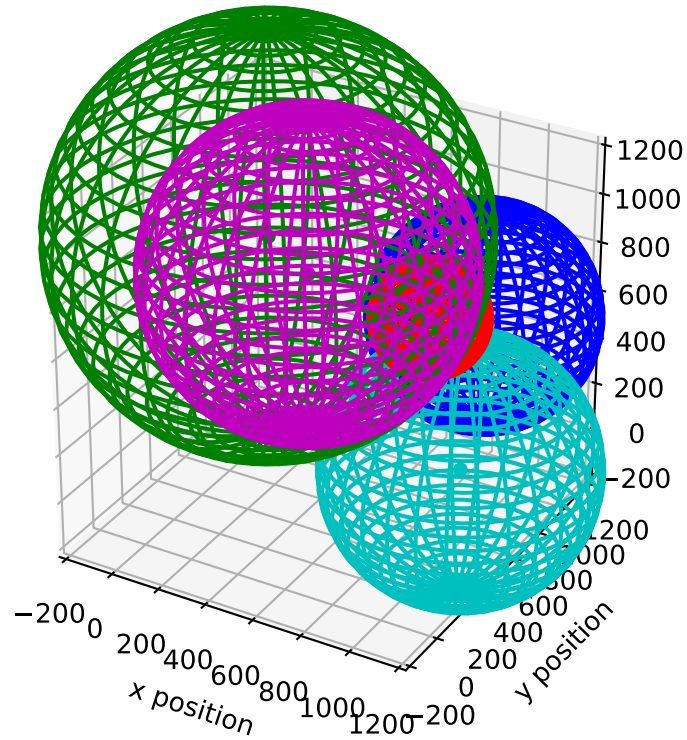


Figure 2: Problem 9.1

2.2 Problem 9.2

$$\lambda = c * 10MHz$$

$$\lambda = 30 \text{ meters}$$

Assuming phase shift $\theta = 10$ we can plug that into our formula to get

$$D' = L + \frac{\theta}{2\pi} \lambda$$

Therefore $D = \frac{D'}{2} = 0.83333333 + 15k$ where k denotes an integer interval. We make the assumption that L is

arbitrarily small compared to the distance travel and is therefore set to 0. If the system has noise we will have to identify a range for $\frac{D'}{2}$, in this case it's 0.825 to $0.841666667 + 15k$. In order to differentiate between 20 and 250 meters we would need a second system at a λ multiple that doesn't overlap before a distance of 250 meters.

3 Problem 10

3.1 Problem 10.1

$$\begin{aligned} f &= 0.8cm \\ b &= 30cm \\ a &= \tan^{-1}\left(\frac{z}{b-x}\right) \\ u &= \frac{fx}{z} \end{aligned}$$

Given the above formulas we can say a is in the range of: $45 < a < 90$ and for u : $3 < u < 45$.

3.2 Problem 10.2

$$\begin{aligned} e &= 10\% \\ v_1 &= 0.2cm \\ v_2 &= 0.3cm \\ z &= \frac{fb}{v_1+v_2} \end{aligned}$$

Given the above formulas we can say that $f * b = 0.7 * 10 = 7$ but the range of z is dependent on $v_1 + v_2$, or:

$$\frac{7}{0.18+0.27} \leq z \leq \frac{7}{0.22+0.33}$$

With zero error we would expect $z = 14$, on the low end we expect $z = 12.72$ and on the upper end we expect $z = 15.56$, leaving an error of 3.7037%.