

# 20251021 mini colloquium

Kosuke Nakamura

**Passive Superconducting Circulator on a Chip**

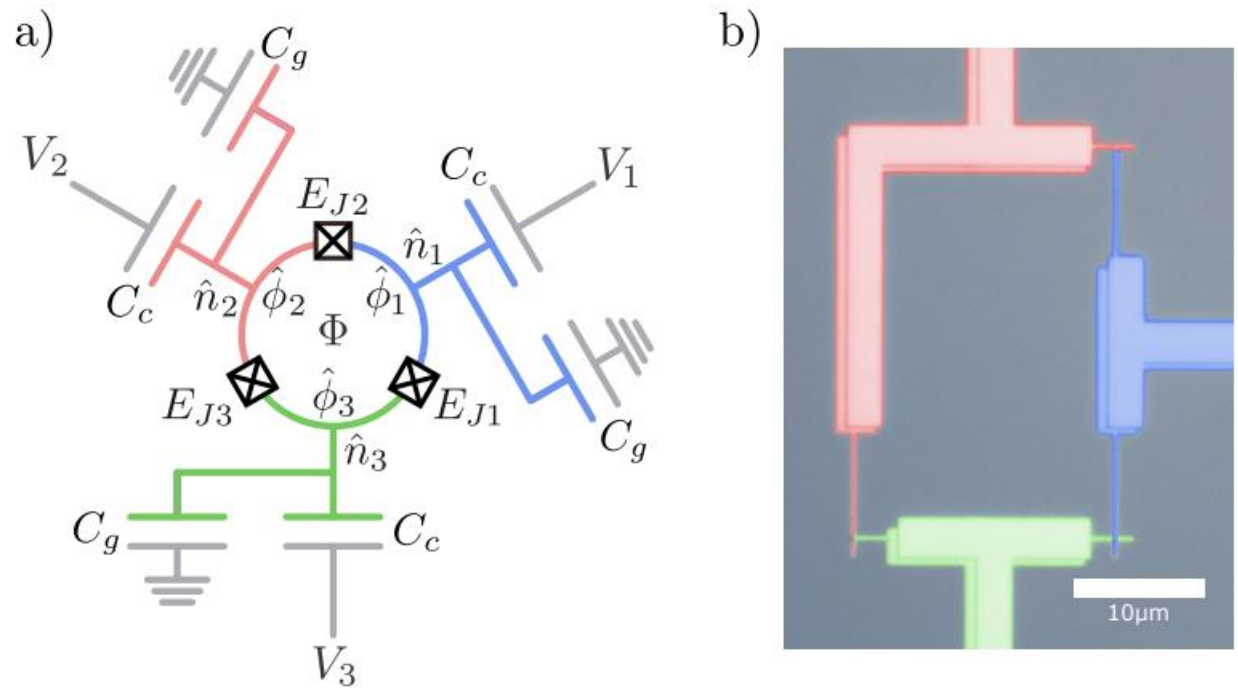
# Background and Purpose

- Microwave circulator utilizing ferrite components
  - A strong magnetic field
  - Too large to be integrated
  - External drive

→ passive, on-chip circulator without using ferrite

# Devise design

- DC bias voltage  $V_i$
- An external flux  $\Phi$



- Hamiltonian

$$\hat{H} = (2e)^2 (\hat{\mathbf{n}} - \mathbf{n}_g) \mathbb{C}^{-1} (\hat{\mathbf{n}} - \mathbf{n}_g) - \sum_{i=1}^3 E_{Ji} \cos(\widehat{\phi_i} - \widehat{\phi_{i+1}} - \frac{1}{3} \phi)$$

# Theoretical model

- Hamiltonian

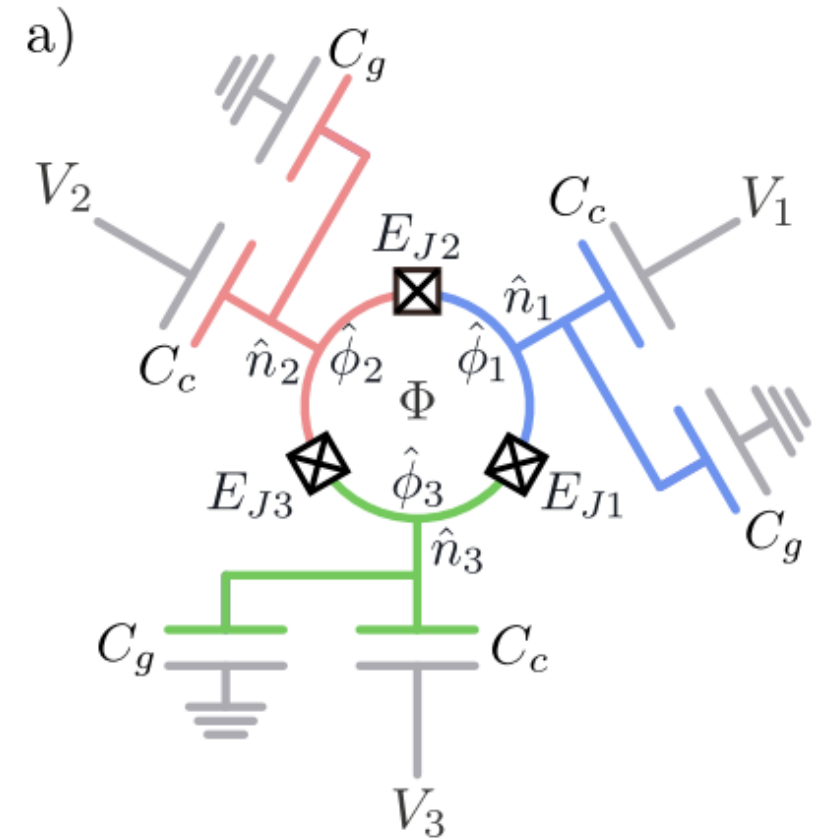
$$\hat{H} = (2e)^2 (\hat{\mathbf{n}} - \mathbf{n}_g) \mathbb{C}^{-1} (\hat{\mathbf{n}} - \mathbf{n}_g) - \sum_{i=1}^3 E_{Ji} \cos(\hat{\phi}_i - \hat{\phi}_{i+1} - \frac{1}{3} \phi)$$

$\hat{n}$ : the charge operator

$n_g$ : the bias charge

$\hat{\phi}_i$ : the superconductive phase

$$\phi = \frac{2\pi\Phi}{\Phi_0}$$



# Theoretical model

- The scattering matrix  $S_{ij}$

$$S_{ij} = \delta_{ij} - \sum_{k=1,2,\dots} \frac{\Gamma \langle k | \hat{n}_j | 0 \rangle \langle 0 | \hat{n}_i | k \rangle}{i\Delta\omega_k + \Gamma_k/2},$$

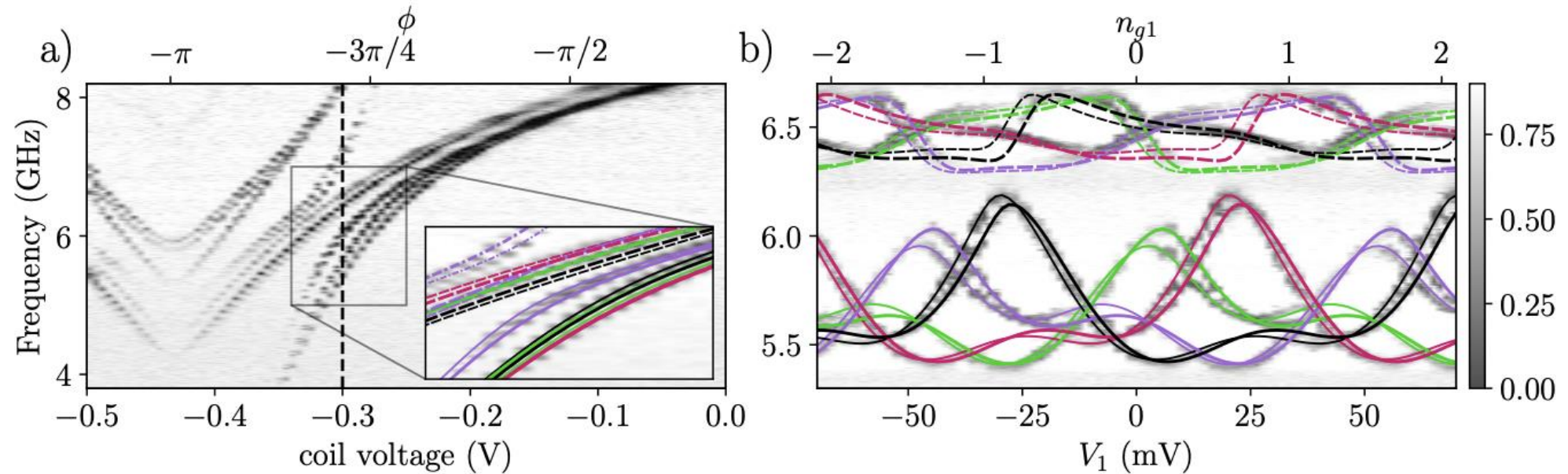
$|k\rangle$ : excited states

$\Delta\omega_k$ : the detuning of the excited eigenenergy

$\Gamma$ : the coupling strength

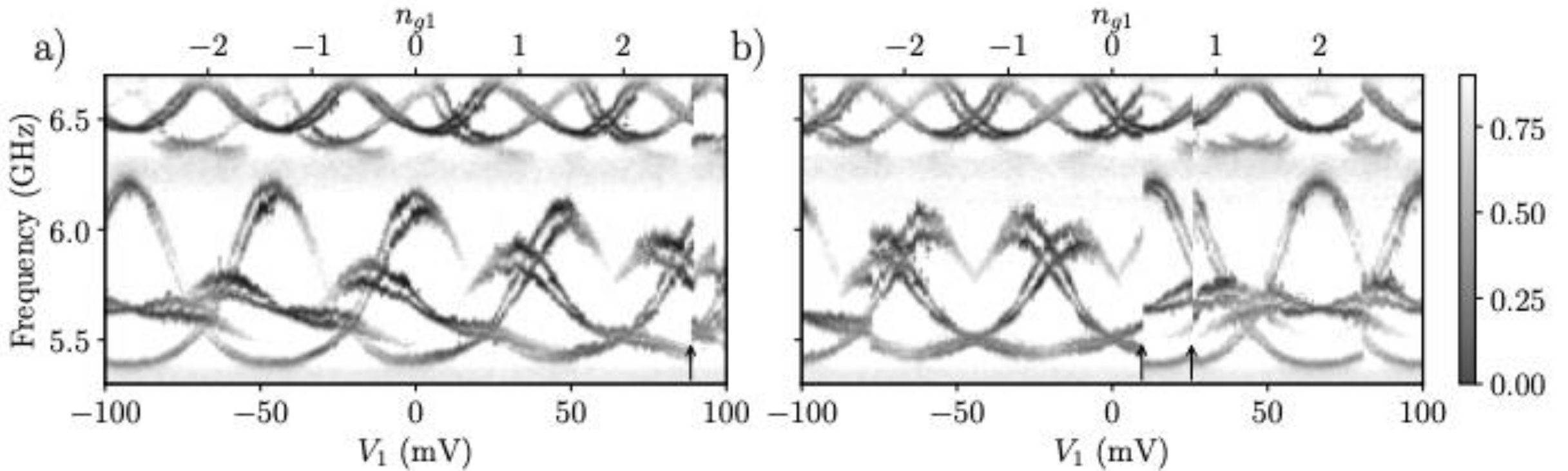
$\Gamma_k$ : the decay rate

# Simulations and result (fig.2)



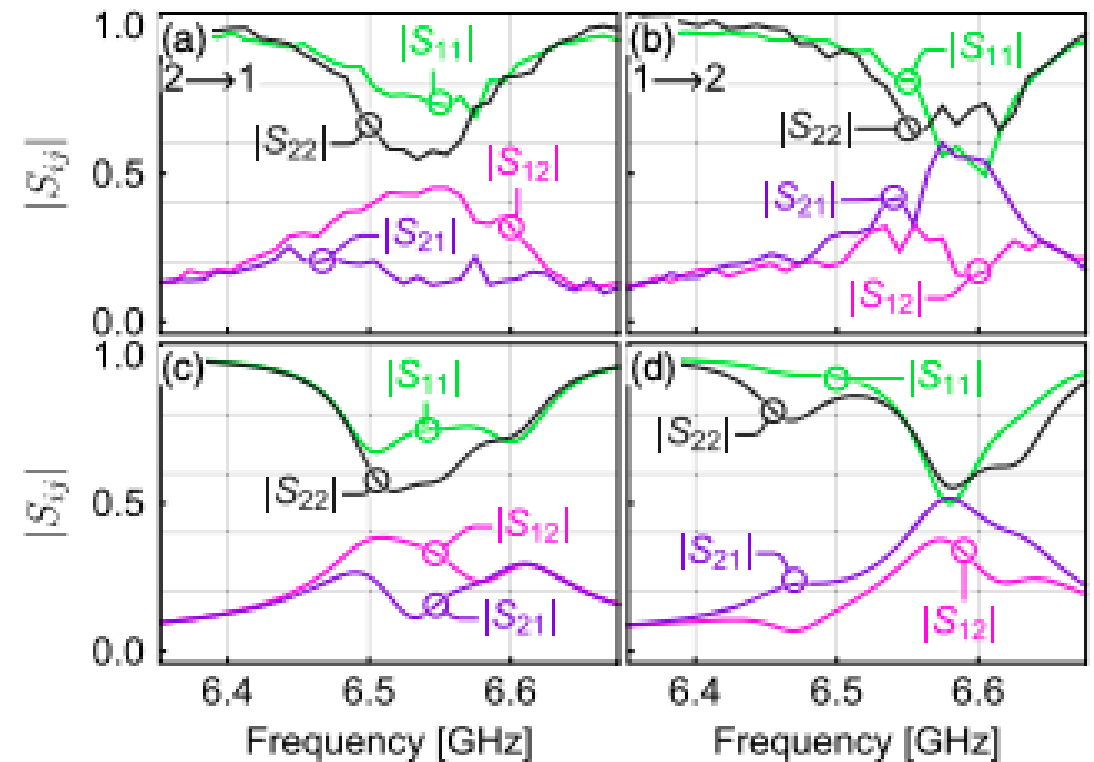
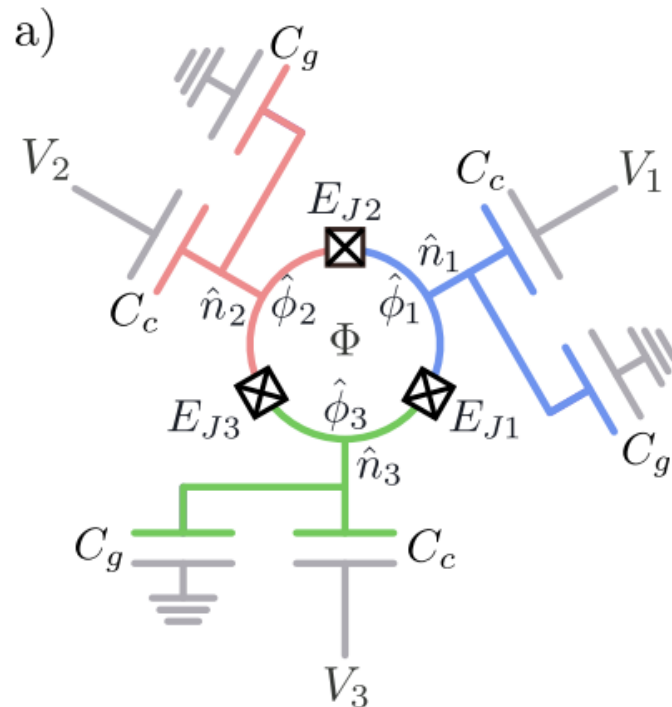
- Coler : quasiparticle configurations
- Line types : transition frequencies
- Line thickness : charge configurations

# Periodic dependence on applied charge bias



# S-matrix elements for two different charge-bias configurations. (fig.3)

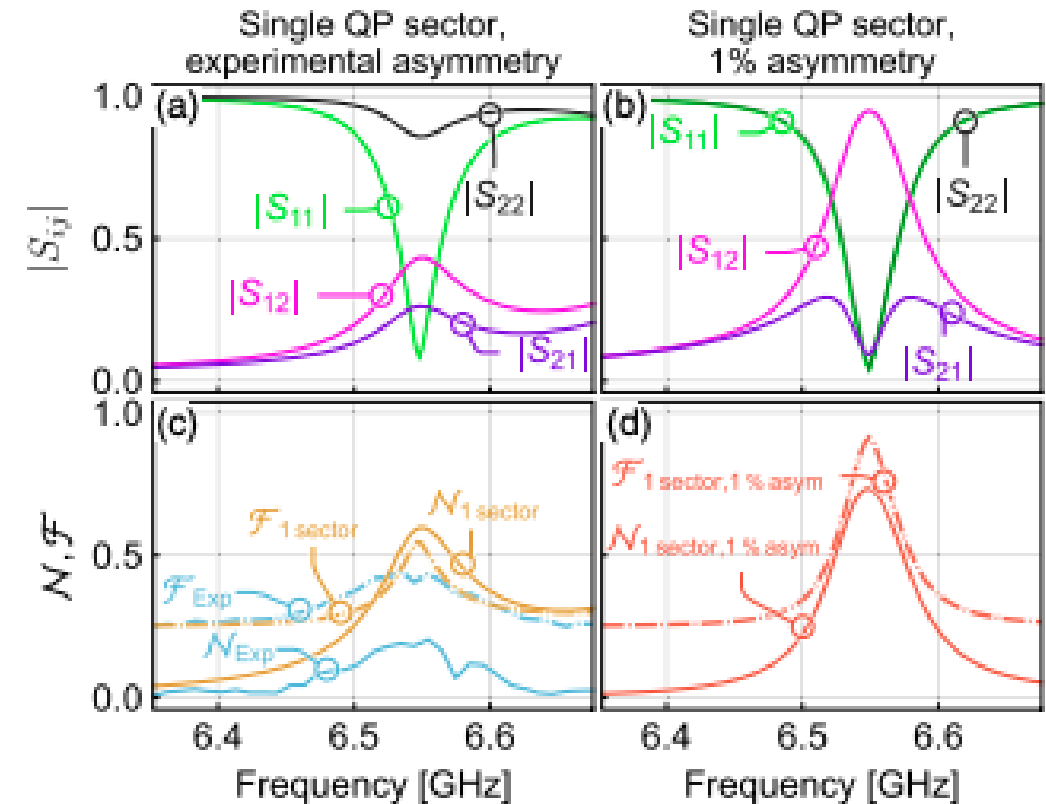
- The non-reciprocity can be changed by gate bias  $V_i$ .





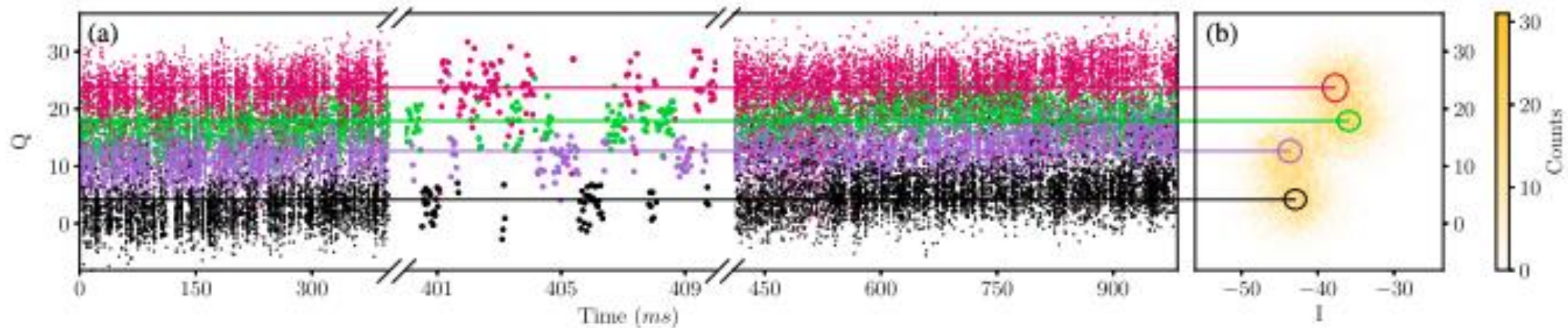
# Simulation of Asymmetry(fig.4)

- (a) Asymmetry in this experiment
- (b) 1% asymmetry
- (c) non-reciprocity and fidelity in this experiment
- (d) 1% asymmetry



# Detection of Quasiparticle Tunneling Using Hidden Markov Models(fig.5)

- Freq : 6.709GHz,  $\phi=1.9$
- identify the four quasi-particle states with HMM
- Time vs Re(S11), Im(S11) vs Re(S11)
- lifetime of the quasi-particle sector :  $\sim 200\mu\text{s}$ .

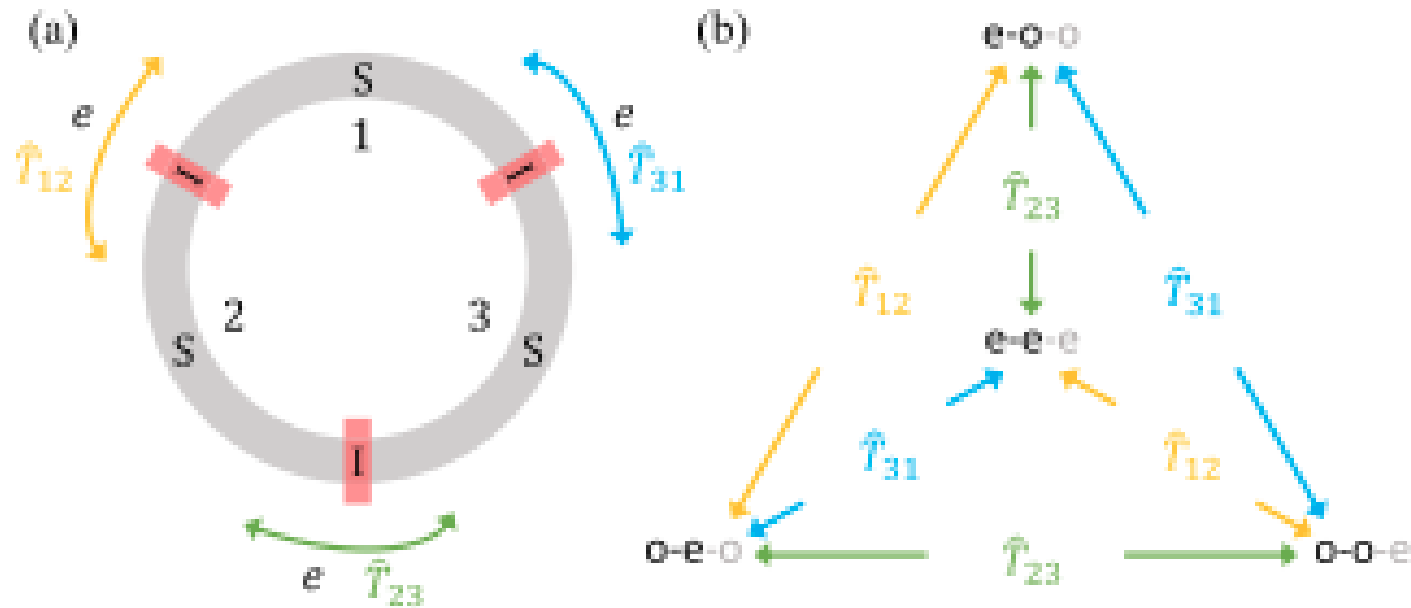


# Summary

- First demonstration of passive superconducting circulator operation.
- Non-reciprocity is tunable by changing charge bias and magnetic flux.
- High-fidelity operation expected by reducing junction asymmetry and quasiparticle density.

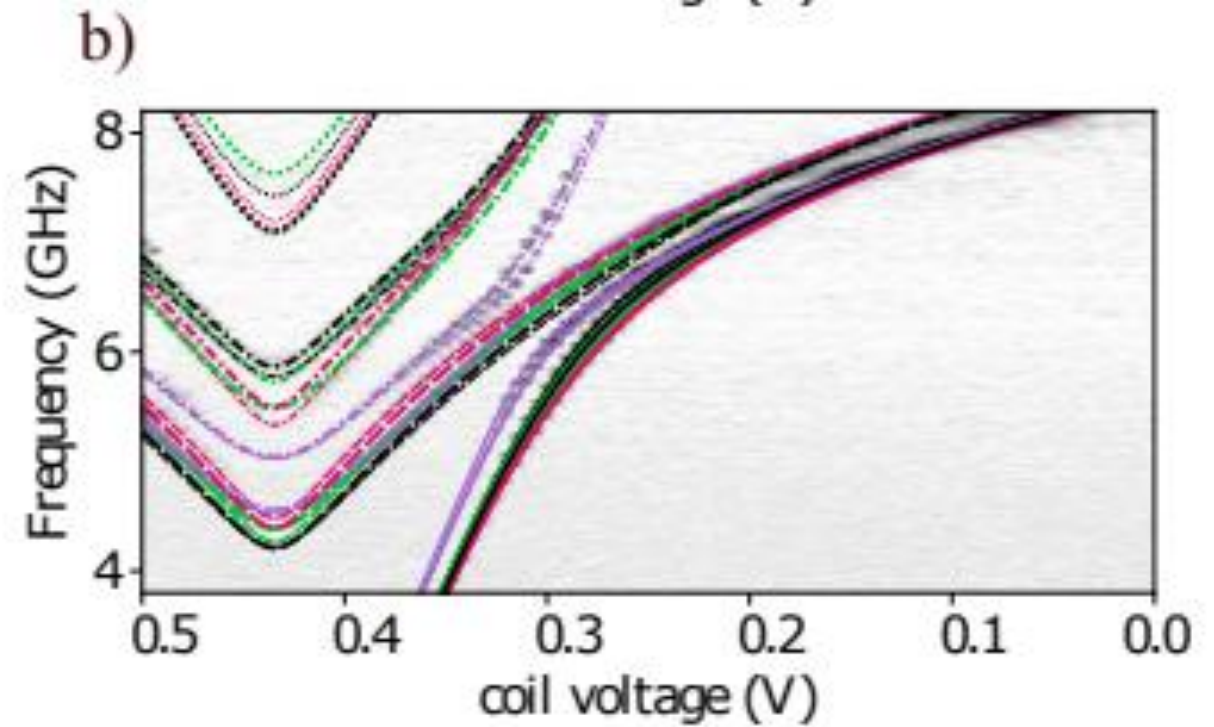
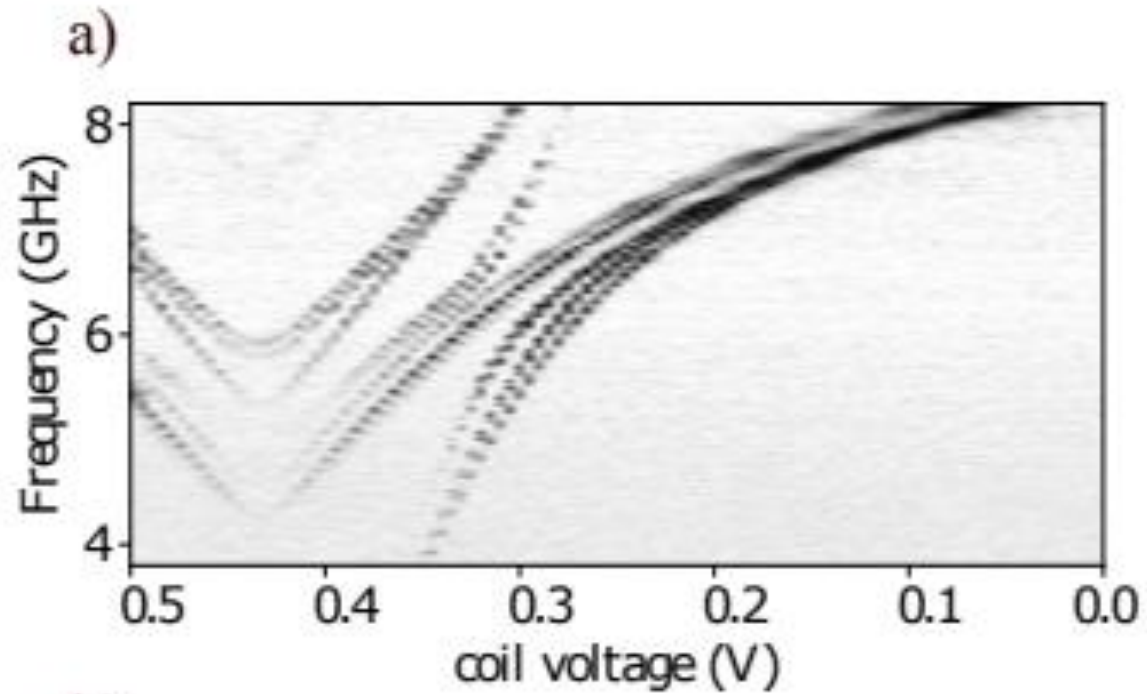
Back up

# Charge parity



[D. T. Le, C. Müller, R. Navarathna, A. Fedorov, and T. M. Stace, Operating a passive on-chip superconducting circulator: Device control and quasiparticle effects, Phys. Rev. Res. 3, 043211 \(2021\).](#)

# Full fits of fig.2



# HMM fitting

