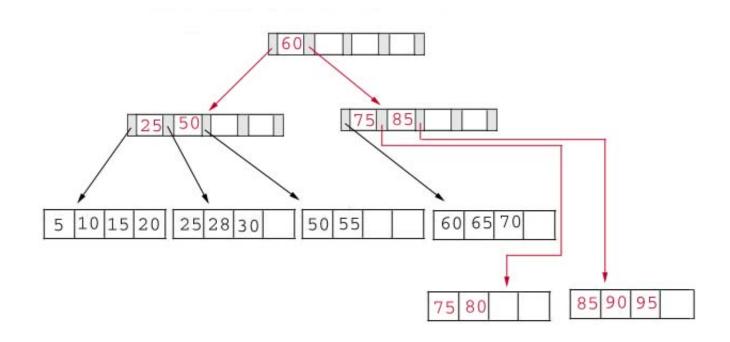
Data Structures and Algorithms

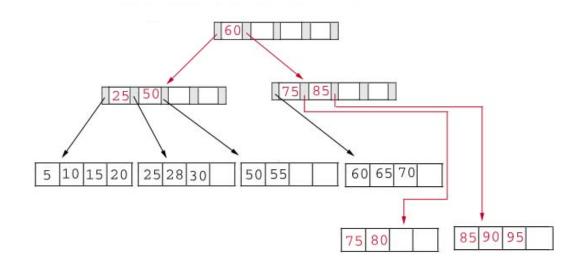
Lesson 8: Sometimes It Pays Not to Be Binary



B-Trees, Tries, Suffix Trees

Outline

- 1. B-Trees
- 2. Tries
- 3. Suffix Trees



B-Trees

- B-trees are balanced trees for fast search, finding successors and predecessors, insert, delete, maximum, minimum, etc.
- Not to be confused with binary trees
- They are designed to keep related data close to each other in (disk) memory to minimise retrieval time
- Important when working with large amount of data that is stored on secondary storage (e.g. disks)
- Used extensively in databases

When Big-O Doesn't Work

- An underlying assumption of Big-O is that all elementary operations take roughly the same amount of time
- This just isn't true of disk look-up
 - $\hfill\Box$ The typical time of an elementary operation on a modern processor is 10^{-9} seconds
 - But a typical hard disk might do 120 revolutions per second
 - $_{\square}$ The typical time it takes to locate a record is around 10ms or 10^7 times slower than an elementary operation

Accessing Data from Disk

- When accessing data from disk minimising the number of disk accesses is critical for good performance
- In database applications we want to store data as large sets
- Storing data in binary trees is disastrous as we typically need around $\log_2(n)$ disk accesses before we locate our data
- It is not unusual in databases for $n=10\,000\,000$ so that $\log_2(n)\approx 24$
- Using binary trees it would often take several seconds to find a record

Multiway-Trees

■ To remedy this we can use M-way trees (i.e. trees where each non-leaf node has M children) so that the access time is

$$\log_M(n) = \frac{\log_2(n)}{\log_2(M)}$$

- In practice we might use $M\approx 200\approx 2^8$ so we can reduce the depth of the tree by around a factor of 8
- The basic data structure for doing this is the B-tree
- There are many variants of B-trees, all trying to squeeze a bit more performance from the basic structure

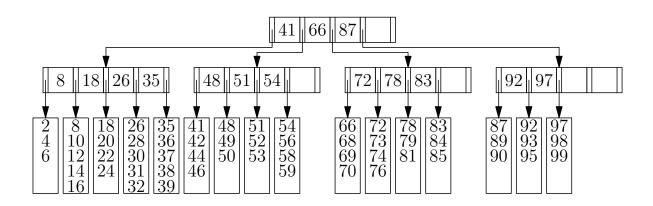
${f B}^+$ Tree

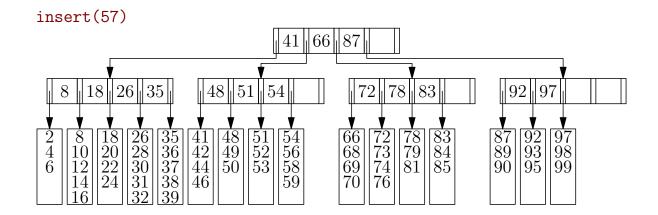
- A basic implementation would obey the following rules
 - 1. The data items are stored at leaves
 - 2. The non-leaf nodes store up to M-1 keys to guide the search: key i represents the smallest key in subtree i+1
 - 3. The root is either a leaf or has between 2 and M children
 - 4. All non-leaf nodes except the root have between $\lceil M/2 \rceil$ and M children
 - 5. All leaves except the root are at the same depth and have between $\lceil L/2 \rceil$ and L data entries

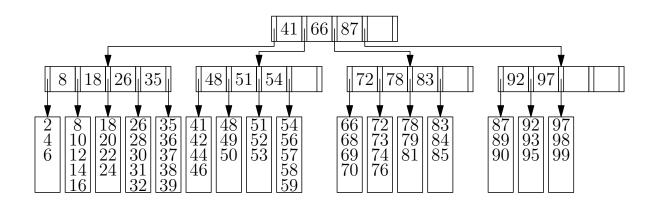
Choosing M and L

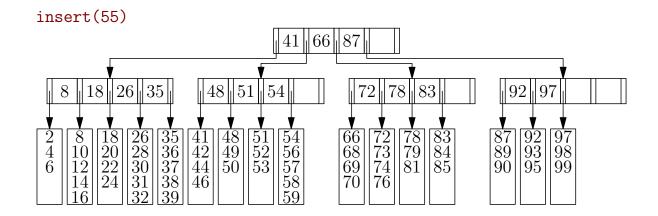
- The choice of M and L depends on the block size (the information read in one go from disk)
- It also depends on the type of data that is being stored (integer, reals, strings, etc.)
- lacksquare M and L might be in the hundreds or thousands
- In the examples below we consider tiny M=L=5 which is unrealistic, but drawable

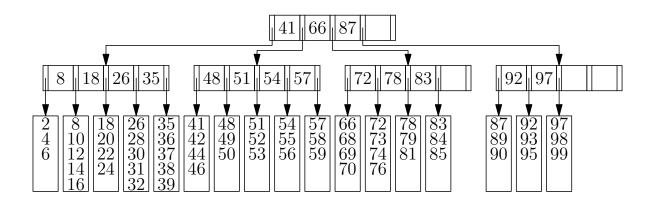
$$M = 5, L = 5$$

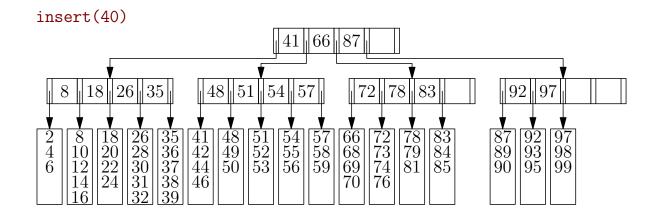


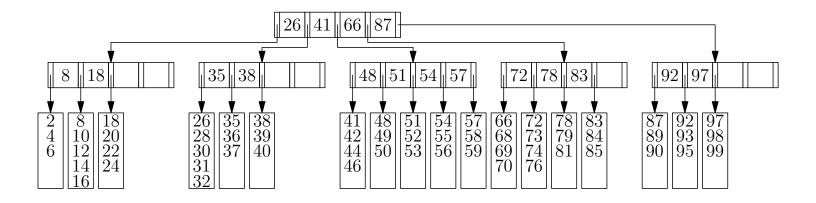












Other Changes

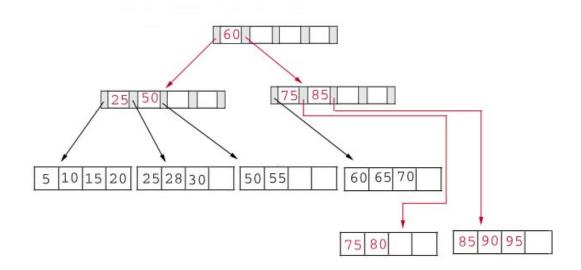
- If the root is full then it can be split into two and a new root created
- B-trees also have to allow the removal of records without losing their structure
- There are a number of strategies to further improve the performance (e.g. neighbouring nodes can adopt a child if the current node cannot expand any more)
- The actual implementation of B-trees is tricky because there are many special cases

B-Tree Summary

- B-trees are an important data structure for databases where reducing the number of disk searches is vital
- They tend to be much more complex than the other data structures we have seen
- The problem of disk access can be improved by replacing disk memory with solid-state drives (still slow compared to memory)
- For massive databases new data structures have been developed to allow faster (although less flexible) information access (e.g. NOSQL, MongoDB, Neo4j)

Outline

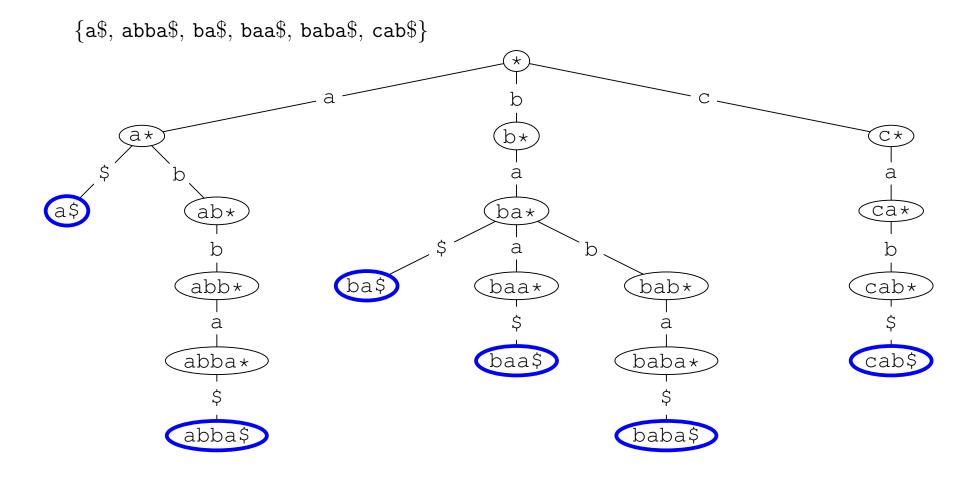
- 1. B-Trees
- 2. Tries
- 3. Suffix Trees



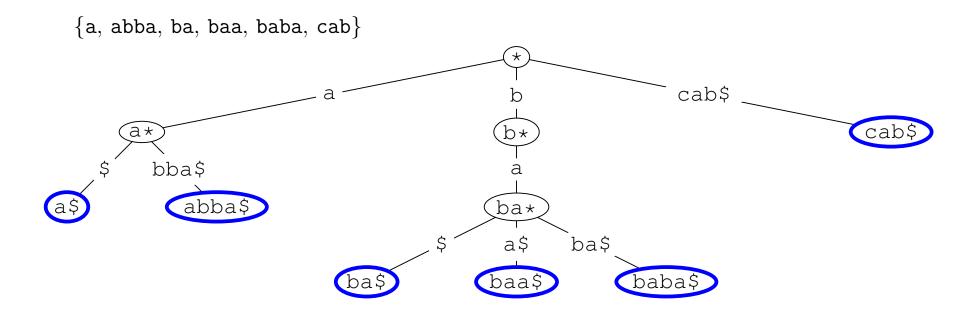
Tries

- A Trie (pron. 'try') or digital tree is a multiway tree often used for storing large sets of words
- They are trees with a possible branch for every letter of an alphabet
- Their names comes from the word retrieval
- All words end with a special letter "\$"
- Tries usually compactify the edges in the tree in order to remove
 - internal one-way branching (in the internal nodes),
 - external one-way branching (in the leaves)

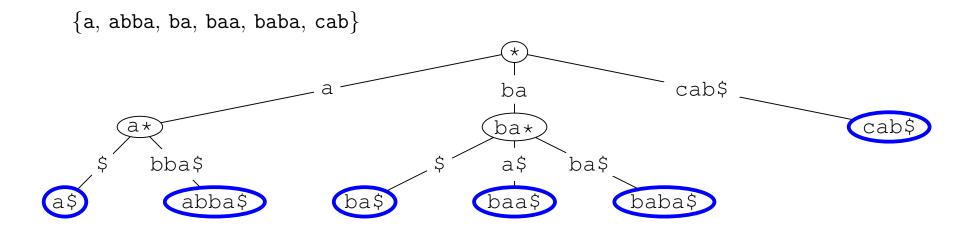
Trie



Trie



Trie



Uses of Tries

- Tries are yet another way of implementing sets
- They provide quick insertion, deletion and find
- Typically considerably quicker than binary trees and hash tables
- They are particularly good for spell checkers, completion algorithms, longest-prefix matching, hyphenation
- Each search finds the longest match between the words in the set and the query

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| \$ | | I\$ | | |
| A | A\$ | | HA* (3) | |
| В | | | | |
| С | | | | |
| D | | | | HAD\$ |
| E | | | | |
| F | | | | |
| G | | | | |
| Н | H* (2) | | | |
| I | I* (1) | | HIS\$ | |
| J | | | | |
| K | | | | |
| L | | | | |
| M | | | | |
| N | NOT\$ | IN\$ | | |
| O | | | | |
| Р | | | | |
| Q | | | | |
| R | | | | |
| S | | | | |
| Т | THAT\$ | IT\$ | | |
| U | | | | |
| V | | | | HAVE\$ |
| W | WITH\$ | | | |
| X | | | | |
| Y | | • | | |
| Z | | | | |

add("WHICH")

| | 0 | 1 | 2 | 3 | 4 |
|----|--------|------|---------|--------|---------|
| \$ | | I\$ | | | |
| A | A\$ | | HA* (3) | | |
| В | | | | | |
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| D | | | | HAD\$ | |
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| F | | | | | |
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| Н | H* (2) | | | | WHICH\$ |
| I | I* (1) | | HIS\$ | | WITH\$ |
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| S | | | | | |
| Т | THAT\$ | IT\$ | | | |
| U | | • | | | |
| V | | | | HAVE\$ | |
| W | W* (4) | | | | |
| X | | | | | |
| Y | | | | | |
| Z | | | | | |

add("HER")

| | 0 | 1 | 2 | 3 | 4 |
|----|--------|------|---------|--------|---------|
| \$ | | I\$ | | | |
| A | A\$ | | HA* (3) | | |
| В | | | | | |
| С | | | | | |
| D | | | | HAD\$ | |
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| F | | | | | |
| G | | | | | |
| Н | H* (2) | | | | WHICH\$ |
| I | I* (1) | | HIS\$ | | WITH\$ |
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| T | THAT\$ | IT\$ | | | |
| U | | | | | |
| V | | | | HAVE\$ | |
| W | W* (4) | | | | |
| X | | | | | |
| Y | | | | | |
| Z | | | | | |
| | ' | | | | |

add("HER")

| | 0 | 1 | 2 | 3 | 4 |
|----|--------|------|---------|--------|---------|
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| В | | | | | |
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| Η | H* (2) | | | | WHICH\$ |
| I | I* (1) | | HIS\$ | | WITH\$ |
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| U | | | | | |
| V | | | | HAVE\$ | |
| W | W* (4) | | | | |
| X | | | | | |
| Y | | | | | |
| Z | | | | | |

add("AT")

| | 0 | 1 | 2 | 3 | 4 |
|----|--------|------|---------|--------|---------|
| \$ | | I\$ | | | |
| A | A\$ | | HA* (3) | | |
| В | | | | | |
| С | | | | | |
| D | | | | HAD\$ | |
| E | | | HER\$ | | |
| F | | | | | |
| G | | | | | |
| Н | H* (2) | | | | WHICH\$ |
| I | I* (1) | | HIS\$ | | WITH\$ |
| J | | | | | |
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| M | | | | | |
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| T | THAT\$ | IT\$ | | | |
| U | | | | | |
| V | | | | HAVE\$ | |
| W | W* (4) | | | | |
| X | | | | | |
| Y | | | | | |
| Z | | | | | |
| | | | | | |

add("AT")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|------|
| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
| В | | | | | | |
| С | | | | | | |
| D | | | | HAD\$ | | |
| Ε | | | HER\$ | | | |
| F | | | | | | |
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| Н | H* (2) | | | | WHICH\$ | |
| I | I* (1) | | HIS\$ | | WITH\$ | |
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| N | NOT\$ | IN\$ | | | | |
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| S | | | | | | |
| Т | THAT\$ | IT\$ | | | | AT\$ |
| U | | | | | | |
| V | | | | HAVE\$ | | |
| W | W* (4) | | | | | |
| X | | | | | | |
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| Z | | | | | | |

add("IS")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|------|
| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
| В | | | | | | |
| С | | | | | | |
| D | | | | HAD\$ | | |
| E | | | HER\$ | | | |
| F | | | | | | |
| G | | | | | | |
| Н | H* (2) | | | | WHICH\$ | |
| I | I* (1) | | HIS\$ | | WITH\$ | |
| J | | | | | | |
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| N | NOT\$ | IN\$ | | | | |
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| V | | | | HAVE\$ | | |
| W | W* (4) | | | | | |
| X | | | | | | |
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| Z | | | | | | |

add("IS")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|------|
| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
| В | | | | | | |
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| D | | | | HAD\$ | | |
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| Н | H* (2) | | | | WHICH\$ | |
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| S | | IS\$ | | | | |
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| W | W* (4) | | | | | |
| X | | | | | | |
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| Z | | | | | | |

add("AND")

| | 0 | 1 | 2 | 3 | 4 | 5 |
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| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
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| C | | | | | | |
| D | | | | HAD\$ | | |
| E | | | HER\$ | | | |
| F | | | | | | |
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| Н | H* (2) | | | | WHICH\$ | |
| I | I* (1) | | HIS\$ | | WITH\$ | |
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| W | W* (4) | | | | | |
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| Z | | | | | | |

add("AND")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|-------|
| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
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| H | H* (2) | | | | WHICH\$ | |
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| Z | | | | | | |

add("BUT")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|-------|
| \$ | | I\$ | | | | A\$ |
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| W | W* (4) | | | | | |
| X | | | | | | |
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add("BUT")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|-------|
| \$ | | I\$ | | | | A\$ |
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| H | H* (2) | | | | WHICH\$ | |
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| W | W* (4) | | | | | |
| X | | | | | | |
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| Z | | | | | | |

add("THE")

| | 0 | 1 | 2 | 3 | 4 | 5 |
|----|--------|------|---------|--------|---------|-------|
| \$ | | I\$ | | | | A\$ |
| A | A* (5) | | HA* (3) | | | |
| В | BUT\$ | | | | | |
| C | | | | | | |
| D | | | | HAD\$ | | |
| E | | | HER\$ | | | |
| F | | | | | | |
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| H | H* (2) | | | | WHICH\$ | |
| I | I* (1) | | HIS\$ | | WITH\$ | |
| J | | | | | | |
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| M | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ |
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| S | | IS\$ | | | | |
| Т | THAT\$ | IT\$ | | | | AT\$ |
| U | | | | | | |
| V | | | | HAVE\$ | | |
| W | W* (4) | | | | | |
| X | | | | | | |
| Y | | | | | | |
| Z | | | | | | |

add("THE")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| С | | | | | | | |
| D | | | | HAD\$ | | | |
| E | | | HER\$ | | | | THE\$ |
| F | | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
| K | | | | | | | |
| L | | | | | | | |
| M | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | |
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| Q | | | | | | | |
| R | | | | | | | |
| S | | IS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | | | | | | |
| Z | | | | | | | |

add("FOR")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| С | | | | | | | |
| D | | | | HAD\$ | | | |
| Е | | | HER\$ | | | | THE\$ |
| F | | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
| K | | | | | | | |
| L | | | | | | | |
| M | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | |
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| Р | | | | | | | |
| Q | | | | | | | |
| R | | | | | | | |
| S | | IS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | | | | | | |
| Z | | | | | | | |

add("FOR")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| С | | | | | | | |
| D | | | | HAD\$ | | | |
| E | | | HER\$ | | | | THE\$ |
| F | FOR\$ | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
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| N | NOT\$ | IN\$ | | | | AND\$ | |
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| R | | | | | | | |
| S | | IS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | | | | | | |
| Z | | | | | | | |

add("ON")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| C | | | | | | | |
| D | | | | HAD\$ | | | |
| E | | | HER\$ | | | | THE\$ |
| F | FOR\$ | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
| K | | | | | | | |
| L | | | | | | | |
| M | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | |
| O | | | | | | | |
| P | | | | | | | |
| Q | | | | | | | |
| R | | | | | | | |
| S | | IS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | | | | | | |
| Z | | | | | | | |

add("ON")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| C | | | | | | | |
| D | | | | HAD\$ | | | |
| E | | | HER\$ | | | | THE\$ |
| F | FOR\$ | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
| K | | | | | | | |
| L | | | | | | | |
| M | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | |
| O | ON\$ | | | | | | |
| P | | | | | | | |
| Q | | | | | | | |
| R | | | | | | | |
| S | | IS\$ | | | | | |
| T | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | • | | | | | |
| Z | | | | | | | |

add("HE")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----|---------|------|---------|--------|---------|-------|--------|
| \$ | | I\$ | | | | A\$ | |
| A | A* (5) | | HA* (3) | | | | THAT\$ |
| В | BUT\$ | | | | | | |
| C | | | | | | | |
| D | | | | HAD\$ | | | |
| E | | | HER\$ | | | | THE\$ |
| F | FOR\$ | | | | | | |
| G | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | |
| J | | | | | | | |
| K | | | | | | | |
| L | | | | | | | |
| M | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | |
| O | ON\$ | | | | | | |
| P | | | | | | | |
| Q | | | | | | | |
| R | | | | | | | |
| S | | IS\$ | | | | | |
| T | TH* (6) | IT\$ | | | | AT\$ | |
| U | | | | | | | |
| V | | | | HAVE\$ | | | |
| W | W* (4) | | | | | | |
| X | | | | | | | |
| Y | | • | | | | | |
| Z | | | | | | | |

add("HE")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|----|---------|------|---------|--------|---------|-------|--------|-------|
| \$ | | I\$ | | | | A\$ | | HE\$ |
| A | A* (5) | | HA* (3) | | | | THAT\$ | |
| В | BUT\$ | | | | | | | |
| С | | | | | | | | |
| D | | | | HAD\$ | | | | |
| Ε | | | HE* (7) | | | | THE\$ | |
| F | FOR\$ | | | | | | | |
| G | | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | | |
| J | | | | | | | | |
| K | | | | | | | | |
| L | | | | | | | | |
| M | | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | | |
| О | ON\$ | | | | | | | |
| Р | | | | | | | | |
| Q | | | | | | | | |
| R | | | | | | | | HER\$ |
| S | | IS\$ | | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | | |
| U | | | | | | | | |
| V | | | | HAVE\$ | | | | |
| W | W* (4) | | | | | | | |
| X | | | | | | | | |
| Y | | | | | | | | |
| Z | | | | | | | | |

add("WAS")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|----|---------|------|---------|--------|---------|-------|--------|-------|
| \$ | | I\$ | | | | A\$ | | HE\$ |
| A | A* (5) | | HA* (3) | | | | THAT\$ | |
| В | BUT\$ | | | | | | | |
| С | | | | | | | | |
| D | | | | HAD\$ | | | | |
| Е | | | HE* (7) | | | | THE\$ | |
| F | FOR\$ | | | | | | | |
| G | | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | | |
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add("WAS")

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add("ARE")

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add("ARE")

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add("BY")

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add("BY")

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add("OR")

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add("OR")

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| W | W* (4) | | | | | | | | | |
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| Y | YOU\$ | | | | | | | | BY\$ | |
| Z | | | | | | | | | | |

add("FROM")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|---------|------|---------|--------|---------|-------|--------|-------|-------|------|
| \$ | | I\$ | | | | A\$ | | HE\$ | | |
| A | A* (5) | | HA* (3) | | WAS\$ | | THAT\$ | | | |
| В | B* (8) | | | | | | | | | |
| С | | | | | | | | | | |
| D | | | | HAD\$ | | | | | | |
| E | | | HE* (7) | | | | THE\$ | | BE\$ | |
| F | FOR\$ | | | | | | | | | |
| G | | | | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | THIS\$ | | | |
| J | | | | | | | | | | |
| K | | | | | | | | | | |
| L | | | | | | | | | | |
| M | | | | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | | | | ON\$ |
| О | O* (9) | | | | | | | | | |
| P | | | | | | | | | | |
| Q | | | | | | | | | | |
| R | | | | | | ARE\$ | | HER\$ | | OR\$ |
| S | | IS\$ | | | | AS\$ | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | | | | |
| U | | | | | | | | | BUT\$ | |
| V | | | | HAVE\$ | | | | | | |
| W | W* (4) | | | | | | | | | |
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| Y | YOU\$ | | | | | | | | BY\$ | |
| Z | | | | | | | | | | |

add("FROM")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|---------|------|---------|--------|---------|-------|--------|-------|-------|------|--------|
| \$ | | I\$ | | | | A\$ | | HE\$ | | | |
| A | A* (5) | | HA* (3) | | WAS\$ | | THAT\$ | | | | |
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| С | | | | | | | | | | | |
| D | | | | HAD\$ | | | | | | | |
| E | | | HE* (7) | | | | THE\$ | | BE\$ | | |
| F | F* (10) | | | | | | | | | | |
| G | | | | | | | | | | | |
| Н | H* (2) | | | | WHICH\$ | | | | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | THIS\$ | | | | |
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| L | | | | | | | | | | | |
| M | | | | | | | | | | | |
| N | NOT\$ | IN\$ | | | | AND\$ | | | | ON\$ | |
| O | O* (9) | | | | | | | | | | FOR\$ |
| P | | | | | | | | | | | |
| Q | | | | | | | | | | | |
| R | | | | | | ARE\$ | | HER\$ | | OR\$ | FROM\$ |
| S | | IS\$ | | | | AS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | | | | | |
| U | | | | | | | | | BUT\$ | | |
| V | | | | HAVE\$ | | | | | | | |
| W | W* (4) | | | | | | | | | | |
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| Y | YOU\$ | | | | | | | | BY\$ | | |
| Z | | | | | | | | | | | |

add("OF")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|---------|------|---------|--------|---------|-------|--------|-------|-------|------|--------|
| \$ | | I\$ | | | | A\$ | | HE\$ | | | |
| A | A* (5) | | HA* (3) | | WAS\$ | | THAT\$ | | | | |
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| Н | H* (2) | | | | WHICH\$ | | | | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | THIS\$ | | | | |
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| N | NOT\$ | IN\$ | | | | AND\$ | | | | ON\$ | |
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| Q | | | | | | | | | | | |
| R | | | | | | ARE\$ | | HER\$ | | OR\$ | FROM\$ |
| S | | IS\$ | | | | AS\$ | | | | | |
| Т | TH* (6) | IT\$ | | | | AT\$ | | | | | |
| U | | | | | | | | | BUT\$ | | |
| V | | | | HAVE\$ | | | | | | | |
| W | W* (4) | | | | | | | | | | |
| X | | | | | | | | | | | |
| Y | YOU\$ | | | | | | | | BY\$ | | |
| Z | | | | | | | | | | | |

add("OF")

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|---------|------|---------|--------|---------|-------|--------|-------|-------|------|--------|
| \$ | | I\$ | | | | A\$ | | HE\$ | | | |
| A | A* (5) | | HA* (3) | | WAS\$ | | THAT\$ | | | | |
| В | B* (8) | | | | | | | | | | |
| C | | | | | | | | | | | |
| D | | | | HAD\$ | | | | | | | |
| Е | | | HE* (7) | | | | THE\$ | | BE\$ | | |
| F | F* (10) | | | | | | | | | OF\$ | |
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| H | H* (2) | | | | WHICH\$ | | | | | | |
| I | I* (1) | | HIS\$ | | WITH\$ | | THIS\$ | | | | |
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| Т | TH* (6) | IT\$ | | | | AT\$ | | | | | |
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| W | W* (4) | | | | | | | | | | |
| X | | | | | | | | | | | |
| Y | YOU\$ | | | | | | | | BY\$ | | |
| Z | | | | | | | | | | | |

Disadvantage of Tries

- Tries typically waste large amounts of memory
 - Often tries are used for the first few layers, while lower levels use a less memory intensive data structure
- These days memory is less of a problem so tries are acceptable for some applications

Binary Tries

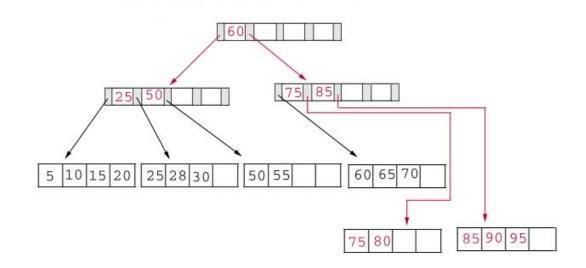
- One extreme (though not uncommon) solution to address memory issues is to build a bit-level trie so the resulting data structure is a binary tree
- It differs from a binary search tree in that the decision to go left or right depends on the current bit
- Although you lose the advantage of a multiway tree (of reducing the depth), it does find the longest match and it speeds up finds which fail

Why Tries?

- Tries are a classic example of a trade-off between memory and time complexity
- Tries are slightly specialist and tend to get used in very particular applications
 - Finding longest matches
 - Completion algorithms, spell checking, etc.
- A basic trie is not too complicated to implement, however . . .
- . . . more complex implementations are needed to overcome the difficulty of wasting too much memory

Outline

- 1. B-Trees
- 2. Tries
- 3. Suffix Trees



Suffix Trees

- A suffix tree is a trie of all suffixes of a string
- E.g. banana

{\$, a\$, na\$, ana\$, nana\$, anana\$, banana\$}

\$ banana\$ na banana\$

\$ na\$ banana\$

\$ na\$ nas\$

ana\$ anana\$

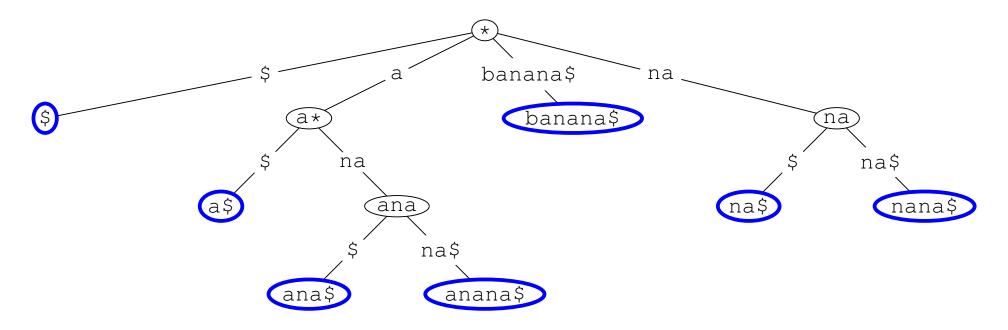
Importance of Suffix Tree

- Suffix trees (and the related suffix arrays) are relatively new data structures
- They are very important for string-based algorithms
- \blacksquare The classic application is finding a match for a query string, Q, in a text, T

String Matching

■ To find a match of a query string, Q, in a text, T, we can first construct the suffix tree of the string T; we then simply look up the query, Q, using the trie

{\$, a\$, na\$, ana\$, nana\$, anana\$, banana\$}



Complexity of Suffix Trees

- Using a regular trie for a suffix tree would typically use far too much memory to be useful
- However, by using pointers to the original text it is possible to build a suffix tree using O(n) memory where n is the length of the text
- Furthermore (and rather incredibly) there is a linear time (O(n)) algorithm to construct the trie
- The algorithm is, however, not trivial to understand

Uses of Suffix Trees

- Suffix trees are efficient whenever it is likely that you will do multiple searches
- Exact word matching is in itself a very important application
- Suffix trees in combination with dynamic programming (which we will eventually get to) can be used to do inexact matching (finding the match with the smallest edit distance)
- Suffix trees get used in bioinformatics, advanced machine learning algorithms, . . .

Lessons

- Multiway trees can considerably speed up search over binary trees
- They are very important in some specialised applications (e.g. databases, spell-checking, completion algorithms, word matching)
- They are not as general purpose as binary search trees and are more complicated to implement
- But they can give the best performance sometimes performance matters enough to make it worthwhile implementing multiway trees