homework16

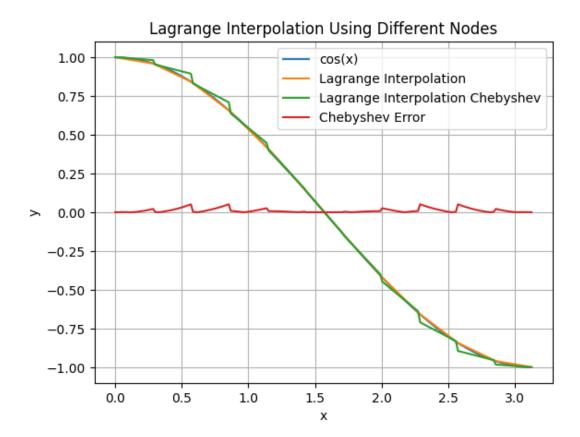
2025年4月17日

1 说明

- 第一张图包含等间距插值和用切比雪夫节点插值的结果,第二张图是使用 Cubicspline 插值的结果
- 切比雪夫插值的误差很明显,最后附上一张误差图

```
[19]: from math import cos, pi
      from scipy import interpolate
      import numpy as np
      import matplotlib.pyplot as plt
      point = np.linspace(0, pi, 12)
      chebypoint = 0.5 * (1 - np.cos((2 * np.arange(12) + 1) * pi / (2 * 12))) * pi
      oriresult = []
      lagresult = []
      lagresult_cheby = []
      cubiresult = []
      chebyerror = []
      x = np.linspace(0, pi, 200)
      def lagrange_interpolation(x_nodes, y_nodes, x_eval):
          f = interpolate.lagrange(x_nodes, y_nodes)
          return f(x_eval)
      def cubic_interpolation(x_nodes, y_nodes, x_eval):
          f = interpolate.CubicSpline(x_nodes, y_nodes)
          return f(x_eval)
      x_index = 0
      for loop in range(11):
          while x_index < len(x) and x[x_index] < point[loop + 1]:</pre>
              oriresult.append(cos(x[x_index]))
```

```
lagresult.append(lagrange_interpolation(point[loop:loop + 2],__
 →[cos(point[loop]), cos(point[loop + 1])], x[x_index]))
        cubiresult.append(cubic_interpolation(point[loop:loop + 2],__
 ⇔[cos(point[loop]), cos(point[loop + 1])], x[x_index]))
        lagresult_cheby.append(lagrange_interpolation(chebypoint[loop:loop +u
 42], [cos(chebypoint[loop]), cos(chebypoint[loop + 1])], x[x_index]))
        x index += 1
for i in range(0, 199):
    chebyerror.append(abs(oriresult[i] - lagresult_cheby[i]))
plt.plot(x[:len(oriresult)], oriresult, label='cos(x)')
plt.plot(x[:len(lagresult)], lagresult, label='Lagrange Interpolation')
plt.plot(x[:len(lagresult_cheby)], lagresult_cheby, label='Lagrange_
 →Interpolation Chebyshev')
plt.plot(x[:len(cubiresult)], chebyerror, label='Chebyshev Error')
plt.legend()
plt.title('Lagrange Interpolation Using Different Nodes')
plt.xlabel('x')
plt.ylabel('y')
plt.grid()
plt.show()
plt.savefig('lagrange_interpolation.png', dpi=600, bbox_inches='tight')
plt.figure()
plt.plot(x[:len(oriresult)], cubiresult, label='Cubic Interpolation')
plt.plot(x[:len(oriresult)], oriresult, label='cos(x)')
plt.legend()
plt.title('Cubic Interpolation')
plt.xlabel('x')
plt.ylabel('y')
plt.grid()
plt.show()
```



<Figure size 640x480 with 0 Axes>

