Artificial Intelligence Planning as Satisfiability

Russell and Norvig: Chapters 5, 11

we follow the following paper

Pushing the Envelope: Planning, Propositional Logic, and Stochastic Search

Kautz and Selman

http://www.cs.cornell.edu/home/selman/papers-ftp/plan.ps

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first-order logic (= situation calculus)

initial state goal state (= query)

EXISTS s

At(Home, s0) At(Home, s)

AND NOT Have(Milk, s0) AND Have(Milk, s)

AND NOT Have(Bananas, s0)

AND Have(Bananas, s)

AND Have(Drill, s0)

operators

FORALL a, s
Have(Milk, Result(a,s))
EQUIV
a = Buy(Milk) AND At(Supermarket, s)
OR
Have(Milk, s) AND NOT a = Drop(Milk)

AIPS-98 Planning Competition

Round	Planner	Av. Time	Solved	Shortest
Round 1	BLACKBOX HSP IPP STAN	1.49 35.48 7.40 55.41	63 82 63 64	55 61 49 47
Round 2	BLACKBOX HSP IPP STAN	2.46 25.87 17.37 1.33	8 9 11 7	6 5 8 4

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problems with first-order logic

- inefficient
- does not necessarily generate a GOOD plan

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propositional logic - initial and final situation

initial state goal state

At(Home,s9) At(Home,s9)

NOT At(SM,s0)

NOT At(HWS,s0)

NOT Have(Drill,s0) Have(Drill,s9) NOT Have(Milk,s0) Have(Milk,s9) NOT Have(Bananas,s0) Have(Bananas,s9)

notice:

these are not really predicates they are variables (for example, At(home,s0) could be replaced with x)

> we use knowledge to eliminate variables such as Sells(SM, Milk) from the encoding

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propositional logic - operators (2)

operators are just variables

Go(Home, SM, s0)

Go(Home, HWS, s0) Go(SM, Home, s0)

Go(SM, HWS, s0)

Go(HWS, SM, s0)

....

Buy(Drill, HWS, s0) Buy(Milk, SM, s0) Buy(Bananas, SM, s0) Buy(Drill, HWS, s1)

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propositional logic - operators (1)

different encodings are possible

here: - graphplan-based encodings

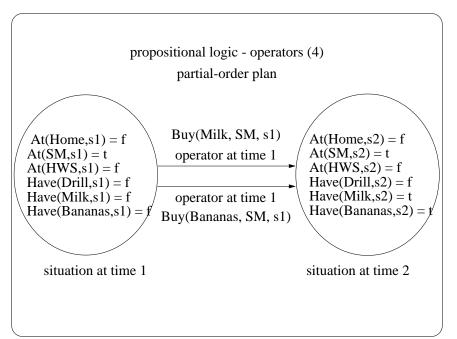
- linear encodings

- state-based encodings

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initial state	time 1	time 2
At(Home,s0) = t	At(Home,s1) = f	At(Home,s2) = f
At(SM,s0) = f	At(SM,s1) = t	At(SM,s2) = t
At(HWS,s0) = f	At(HWS,s1) = f	At(HWS,s2) = f
Have(Drill,s0) = f	Have(Drill,s1) = f	Have(Drill,s2) = f
Have(Milk,s0) = f	Have(Milk,s1) = f	Have(Milk,s2) = t
Have(Bananas,s0) = f	Have(Bananas,s1) = f	Have(Bananas,s2) = t
Go(Home, SM, s0) = t	Go(Home, SM, $s1$) = f	Go(Home, SM, s2)
Go(Home, HWS, s0) = f	Go(Home, HWS, s1) = f	Go(Home, HWS, s2)
Go(SM, Home, s0) = f	Go(SM, Home, s1) = f	Go(SM, Home, s2)
Go(SM, HWS, s0) = f	Go(SM, HWS, s1) = f	Go(SM, HWS, s2)
Go(HWS, SM, s0) = f	Go(HWS, SM, s1) = f	Go(HWS, SM, s2)
Buy(Drill, HWS, $s0$) = f	Buy(Drill, HWS, s1) = f	Buy(Drill, HWS, s2)
Buy(Milk, SM, $s0$) = f	Buy(Milk, SM, $s1$) = t	Buy(Milk, SM, s2)
Buy(Bananas, SM, $s0$) = f	Buy(Bananas, SM, s1) = t	Buy(Bananas, SM, s2)
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propositional logic - constraints (1)

Go(here, there) Precond: At(here)

Effect: At(there) AND NOT At(here)

Buv(x, store) MaintainAt(x)Precond: At(store) and Sells(store,x) Precond: At(x) Effect:

Effect: Have(x)

each fact (and its negation, respectively) at time t implies the disjunction of all the operators at time t-1 that have it as an add-effect (or delete-effect)

Have(Milk, s1) IMPLIES Buy(Milk, SM, s0) OR MaintainHave(Milk, s0) NOT Have(Milk, s1) IMPLIES MaintainNotHave(Milk,s0) At(SM, s2) IMPLIES Go(Home, SM, s1) OR Go(HWS, SM, s1) OR ...

propositional logic - operators (5)

For every fact (and its negation, respectively), we add a "maintain" operator that simply has that fact (or its negation, respectively) as a precondition

> MaintainAt(x)Precond: At(x)Effect:

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propositional logic - constraints (2)

Go(here, there) Precond: At(here)

Effect: At(there) AND NOT At(here)

Buv(x, store) MaintainAt(x)Precond: At(store) and Sells(store,x) Precond: At(x)Effect: Have(x) Effect:

operators imply their preconditions

Go(HWS, SM, s1) IMPLIES At(HWS, s1) Buy(Bananas, SM, s2) IMPLIES At(SM, s2)

propositional logic - constraints (3)

Go(here, there)
Precond: At(here)

Effect: At(there) AND NOT At(here)

Buy(x, store) MaintainAt(x)
Precond: At(store) and Sells(store,x) Precond: At(x)
Effect: Have(x) Effect:

conflicting actions cannot be executed at the same time

NOT Go(HWS, SM, s1) OR NOT Go(HWS, Home, s1) NOT Buy(HWS, Drill, s1) OR NOT Go(HWS, SM, s1)

...

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planning = solving SAT problem

we now have a huge propositional sentence we need to find an interpretation that makes it true

satisfiability problem (= SAT)

in general: NP hard

smaller sentences are easier to solve this is why we used knowledge to eliminate some predicates

Reasoning

knowledge-base

At(Home,s0) NOT At(SM,s0)

NOT At(HWS,s0) At(Home,s9)
NOT Have(Drill,s0) Have(Drill,s9)
NOT Have(Milk,s0) Have(Milk,s9)
NOT Have(Bananas.s0) Have(Bananas.s9)

Have(Milk, s1) IMPLIES Buy(Milk, SM, s0) OR MaintainHave(Milk, s0) NOT Have(Milk, s1) IMPLIES MaintainNotHave(Milk, s0) At(SM, s2) IMPLIES Go(Home, SM, s1) OR Go(HWS, SM, s1) OR ...

Go(HWS, SM, s1) IMPLIES At(HWS, s1) Buy(Bananas, SM, s2) IMPLIES At(SM, s2)

•••

NOT Go(HWS, SM, s1) OR NOT Go(HWS, Home, s1) NOT Buy(HWS, Drill, s1) OR NOT Go(HWS, SM, s1)

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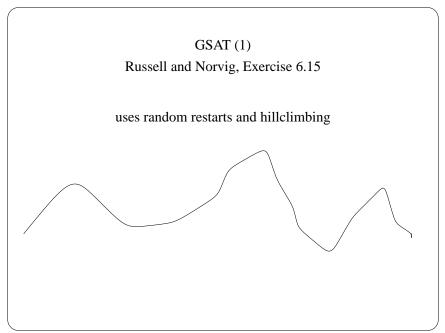
constraint satisfaction

SAT problems are search problems of a special kind. Why?

(P OR Q) AND (R OR NOT S)

$$P=?,\ Q=?,\ R=?,\ S=?$$
 set P to f set Q to f ... P=f, Q=t, R=?, S=? P=t, Q=?, R=?, S=? P=t, Q=f, R=?, S=? ...

- use systematic search methods here: - use heuristic methods



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GSAT (3)

function GSAT (sentence, max-restarts, max-climbs) returns a truth assignment or failure

for i := 1 to max-restarts

A := a randomly generated truth assignment

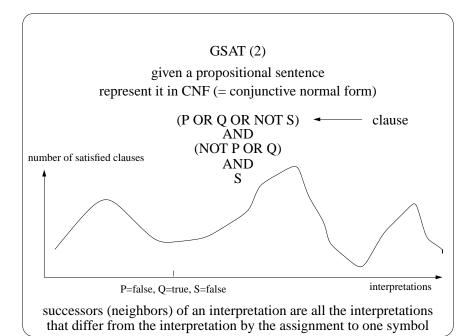
for j := 1 to max-climbs do

if A satisfies sentence then return A

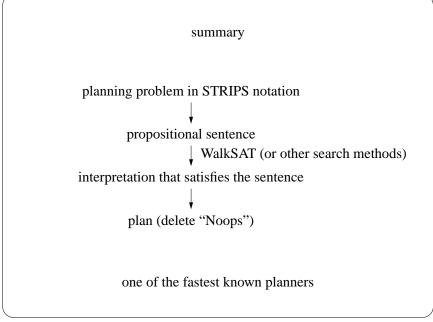
A := a random choice of one of the best successors of A return failure

completeness? soundness?

GSAT has been improved to WalkSAT



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