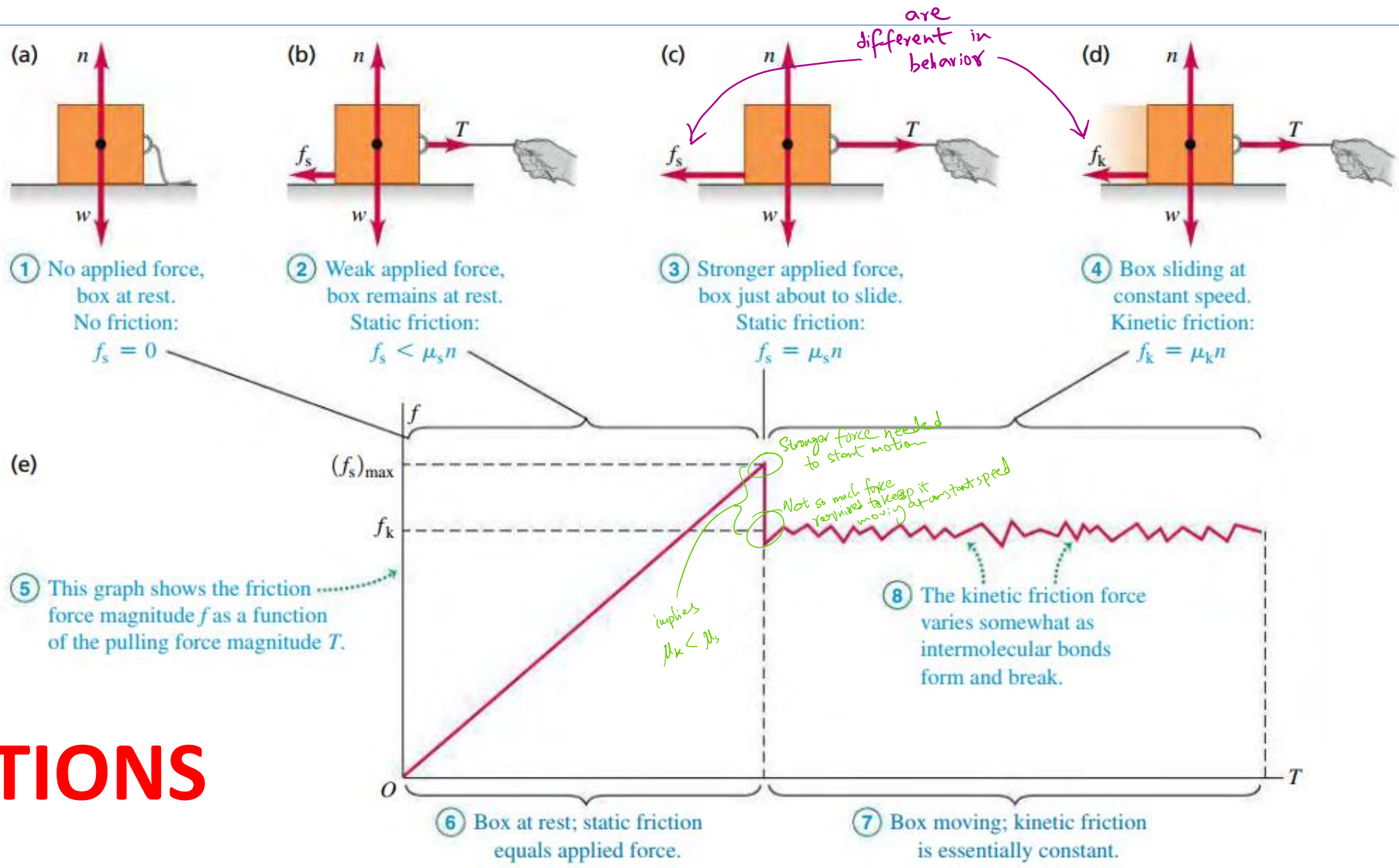
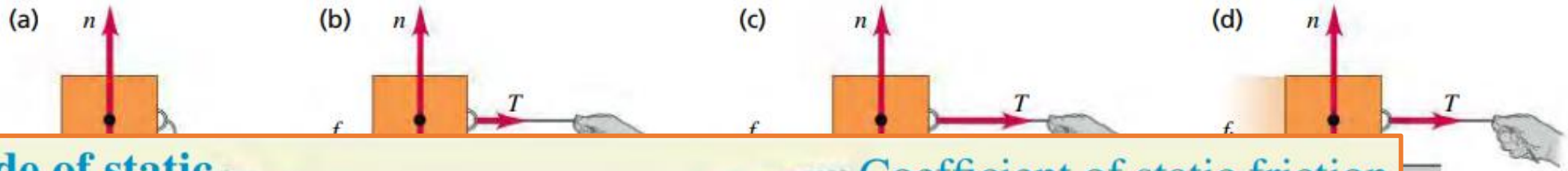


# Lecture 11

Our knowledge of nature of force of friction comes from experiments.



# FRICTIONS



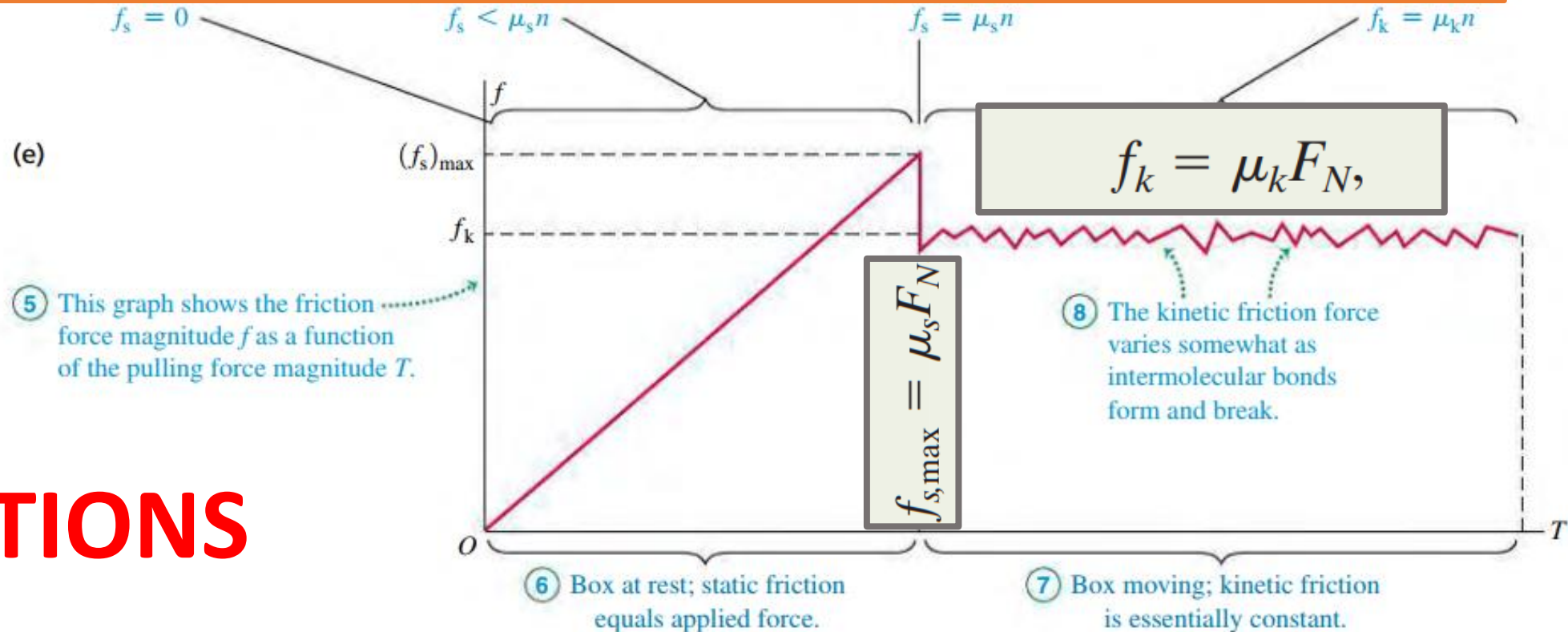
**Magnitude of static friction force**

Maximum static friction force

$$f_s \leq (f_s)_{\max} = \mu_s n$$

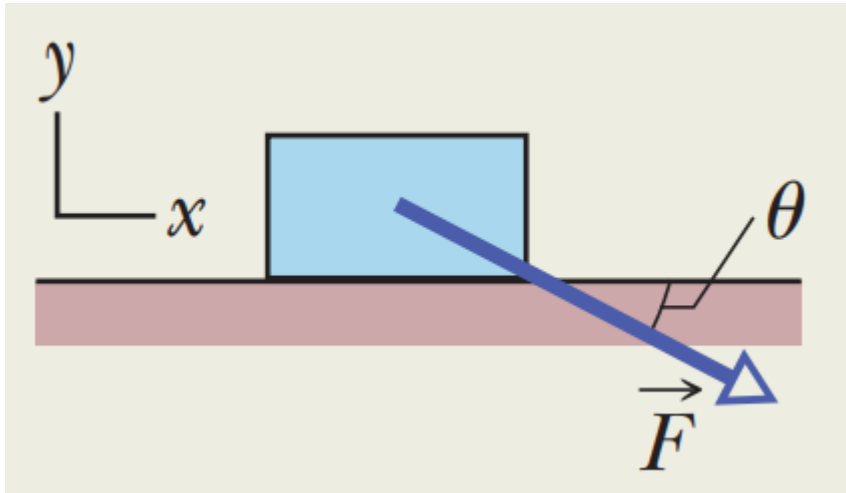
Coefficient of static friction

Magnitude of normal force



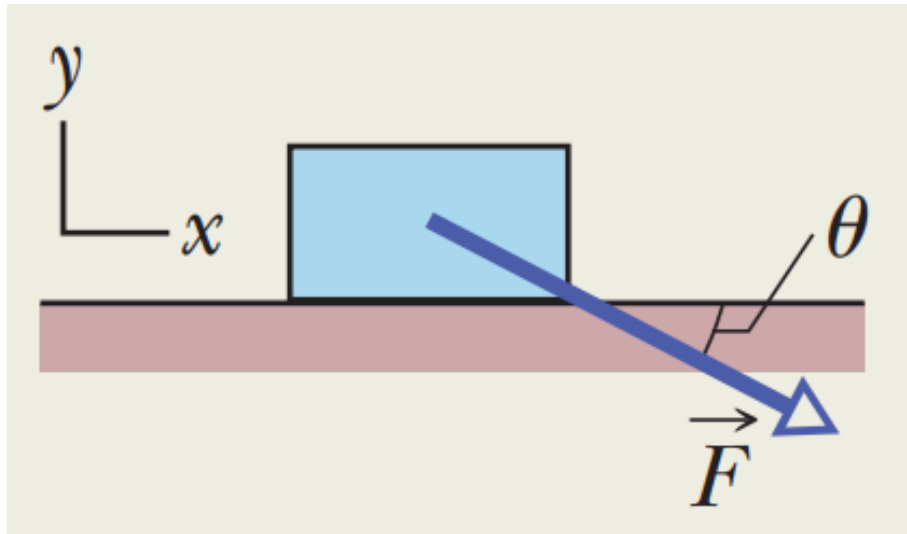
# FRICTIONS

12.0 N applied to an 8.00 kg block at a downward angle of  $\theta = 30.0^\circ$ . The coefficient of static friction between block and floor is  $\mu_s = 0.700$ ; the coefficient of kinetic friction is  $\mu_k = 0.400$ . Does the block begin to slide or does it remain stationary? What is the magnitude of the frictional force on the block?



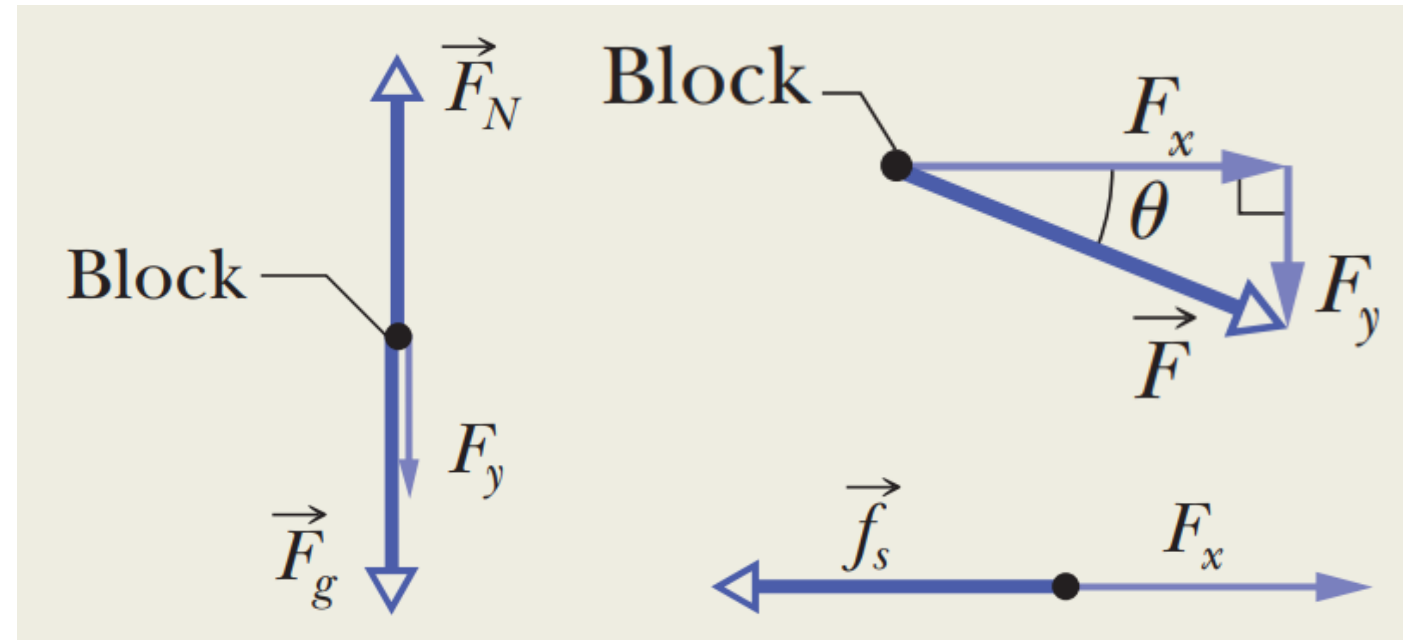
point out the condition  
you need to prove.

$$F_x \stackrel{?}{\geq} f_{s,\max}$$



$$F_x = F \cos \theta$$

$$= (12.0 \text{ N}) \cos 30^\circ = 10.39 \text{ N}.$$



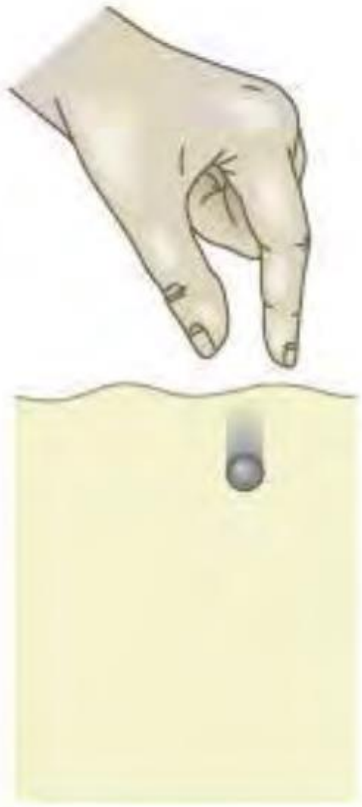
total  
vertical  
forces

$$F_N - mg - F \sin \theta = m(0),$$

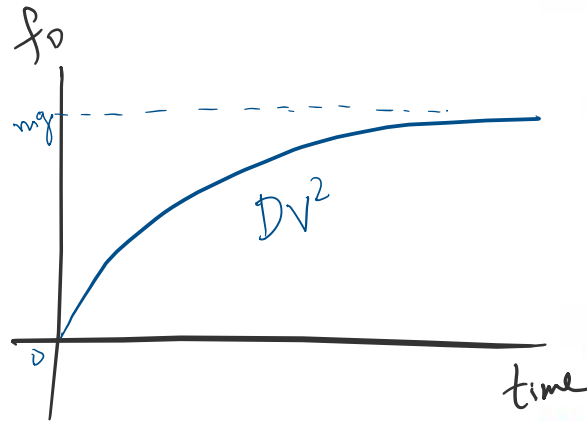
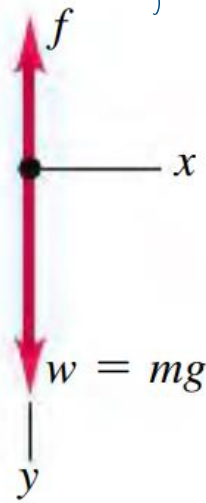
$$f_{s,\max} = \mu_s (mg + F \sin \theta)$$

$$= (0.700)((8.00 \text{ kg})(9.8 \text{ m/s}^2) + (12.0 \text{ N})(\sin 30^\circ))$$

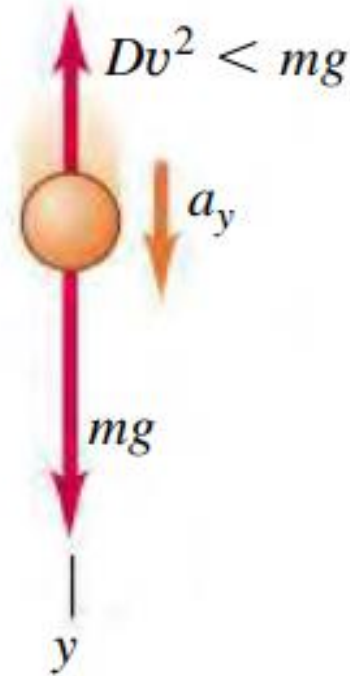
$$= 59.08 \text{ N.} \quad (6)$$



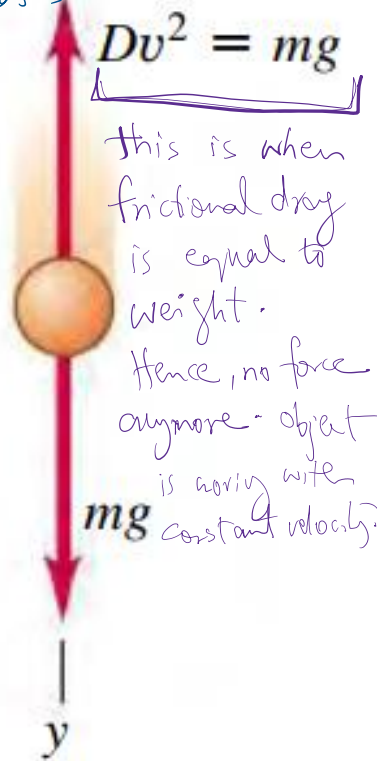
**Fluid Resistance:**  
occurs when fluid particles consecutively strike the solid object and resist motion.



As the object accelerates the velocity increases, therefore frictional drag also increases.



Before terminal speed: Object accelerating, drag force less than weight.

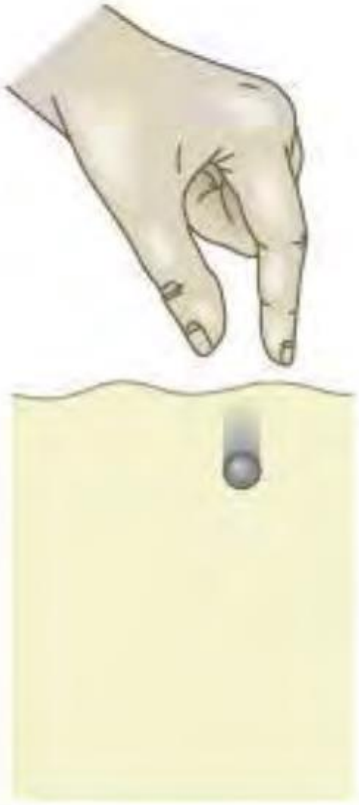


At terminal speed  $v_t$ : Object in equilibrium, drag force equals weight.

$$f = kv \quad (\text{fluid resistance at low speed})$$

$$f = Dv^2 \quad (\text{fluid resistance at high speed})$$

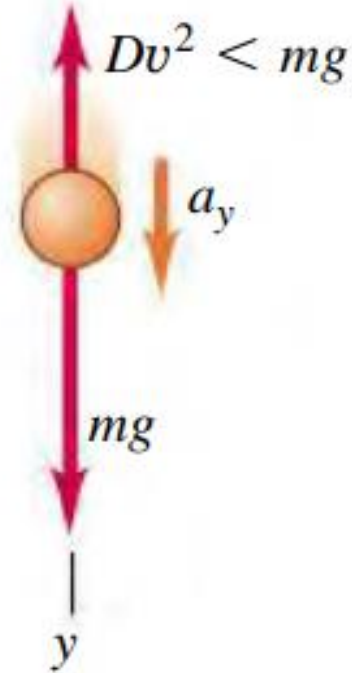
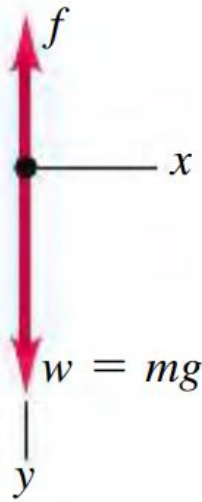




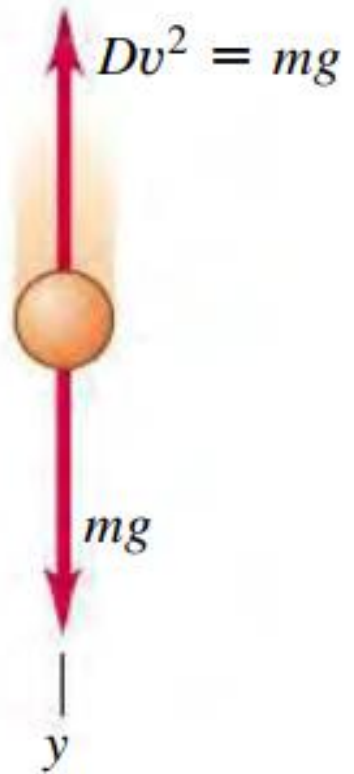
$$\Sigma F_y = mg + (-kv_y) = ma_y$$

$$v_t = \frac{mg}{k}$$

Terminal velocity  
at low speeds



Before terminal  
speed: Object  
accelerating, drag  
force less than  
weight.



At terminal speed  $v_t$ :  
Object in equilibrium,  
drag force equals  
weight.

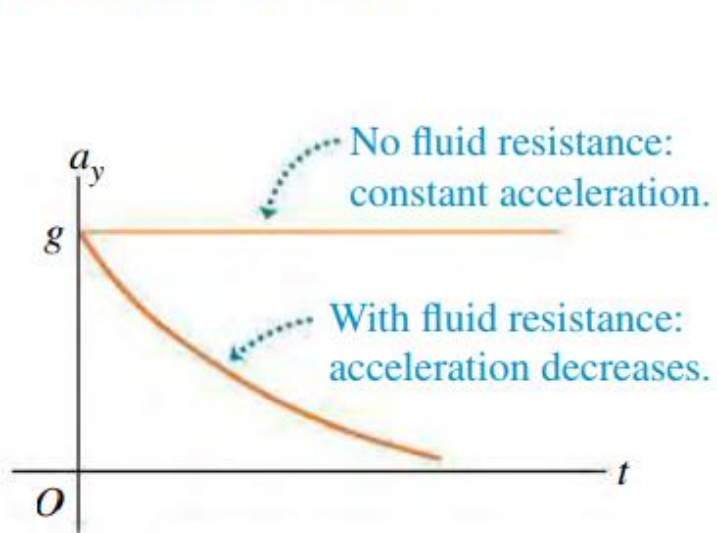
$f = kv$  (fluid resistance at low speed)

$f = Dv^2$  (fluid resistance at high speed)

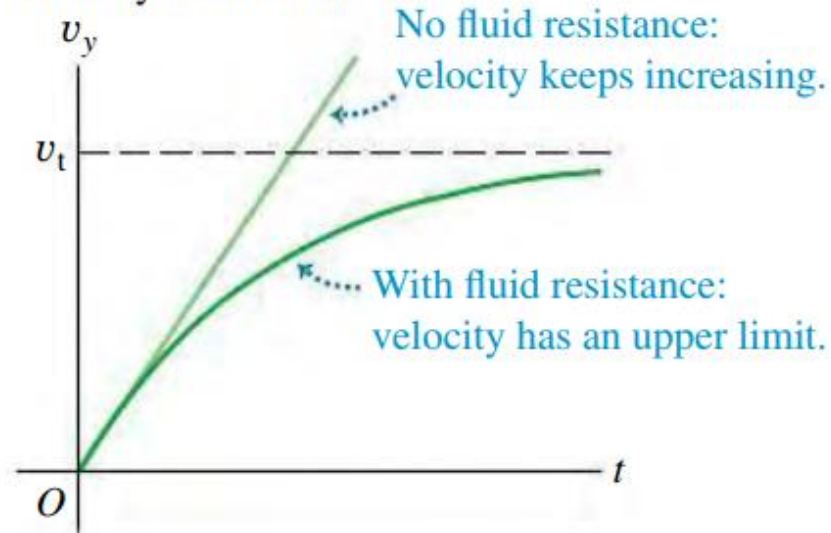
## Lecture 11

ignoring the friction gave us a very neat but unreal picture of motion.

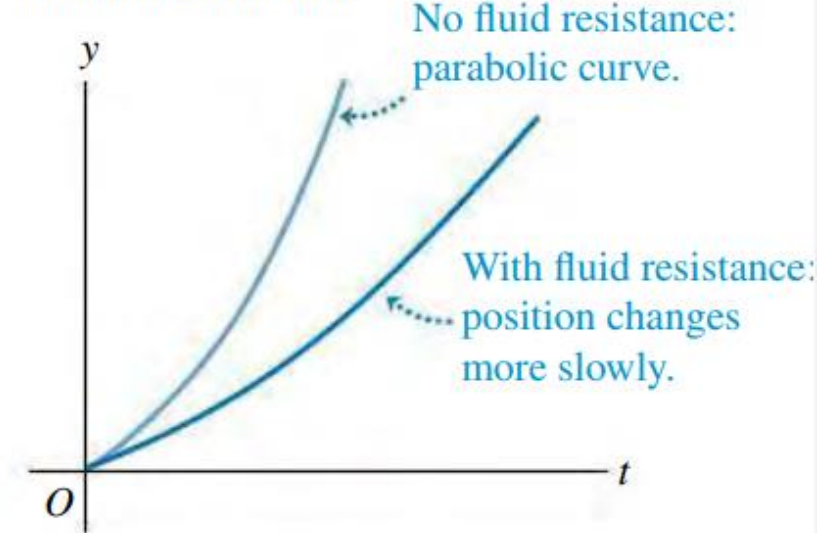
Acceleration versus time



Velocity versus time



Position versus time



Here, you'll see how acceleration, velocity and displacement change under fluid resistance.



centripetal  
acceleration is the resulting  
acceleration

$$-F_N - mg = m\left(-\frac{v^2}{R}\right).$$

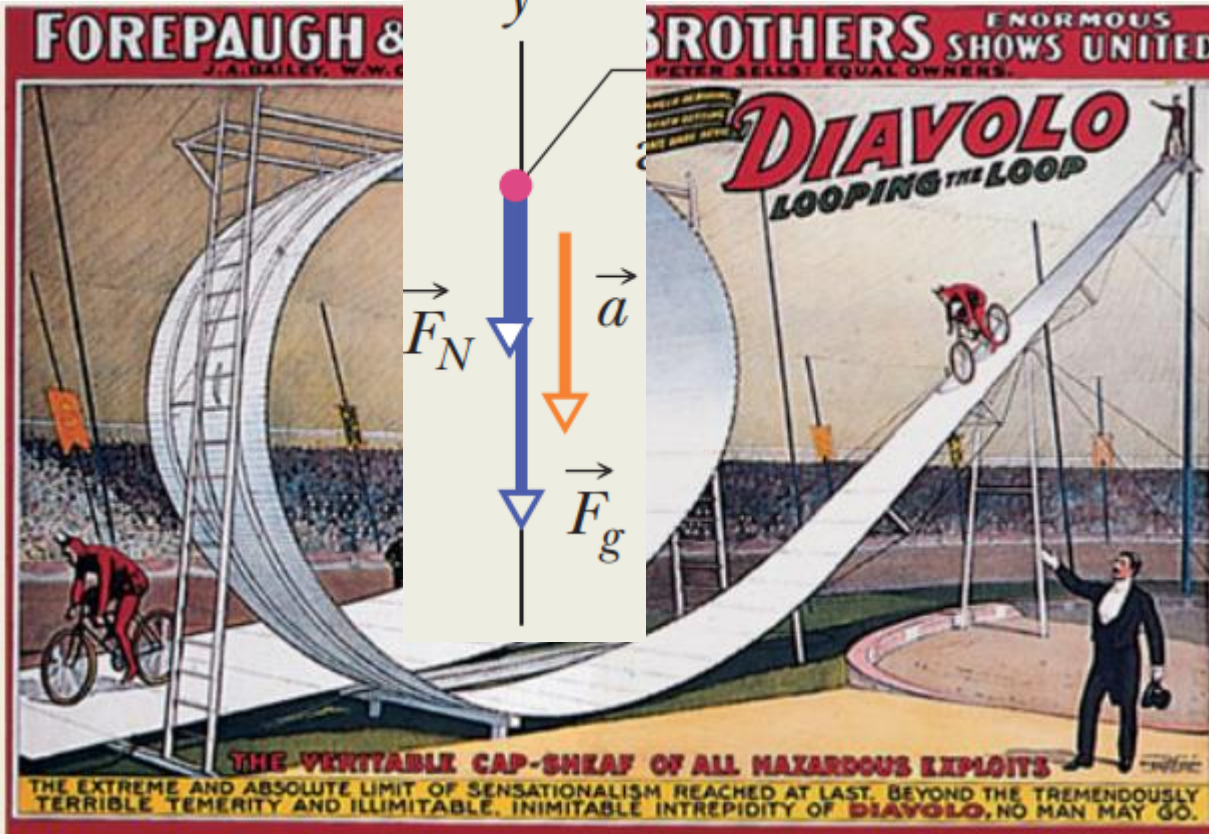
$\{F_N = 0\}$  just about to lose  
the surface contact

Minimum velocity to  
make this path

$$v = \sqrt{gR}$$

more velocity than this will  
only make it easier for Sonic





$$-F_N - mg = m\left(-\frac{v^2}{R}\right).$$

Minimum velocity to make this path

$$v = \sqrt{gR}$$

*independent of mass*

Weight of a body at the earth's surface ...  
... equals gravitational force the earth exerts on body.

$$w = F_g = \frac{Gm_E m}{R_E^2}$$

Gravitational constant  
Mass of the earth  
Mass of body  
Radius of the earth

will equal to 'ma'  
when only gravitational  
force is considered.

→ design of  
actual gravitational  
force



**Weight** of a body at  
the earth's surface ...

Gravitational constant

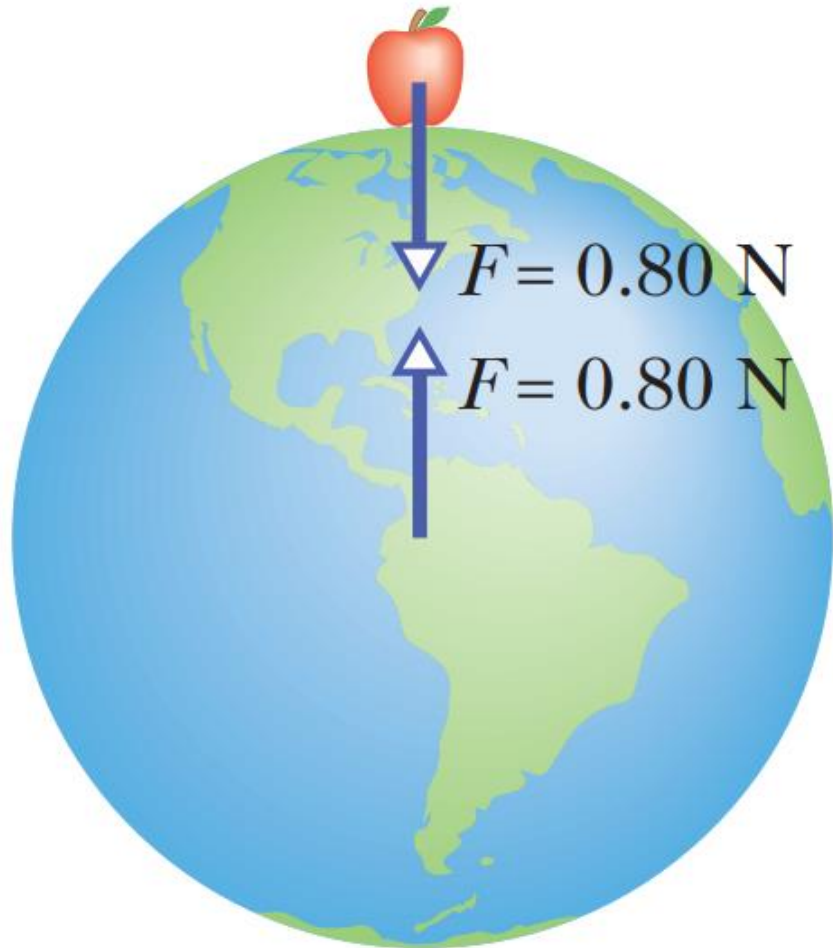
Mass of the earth

Mass of body

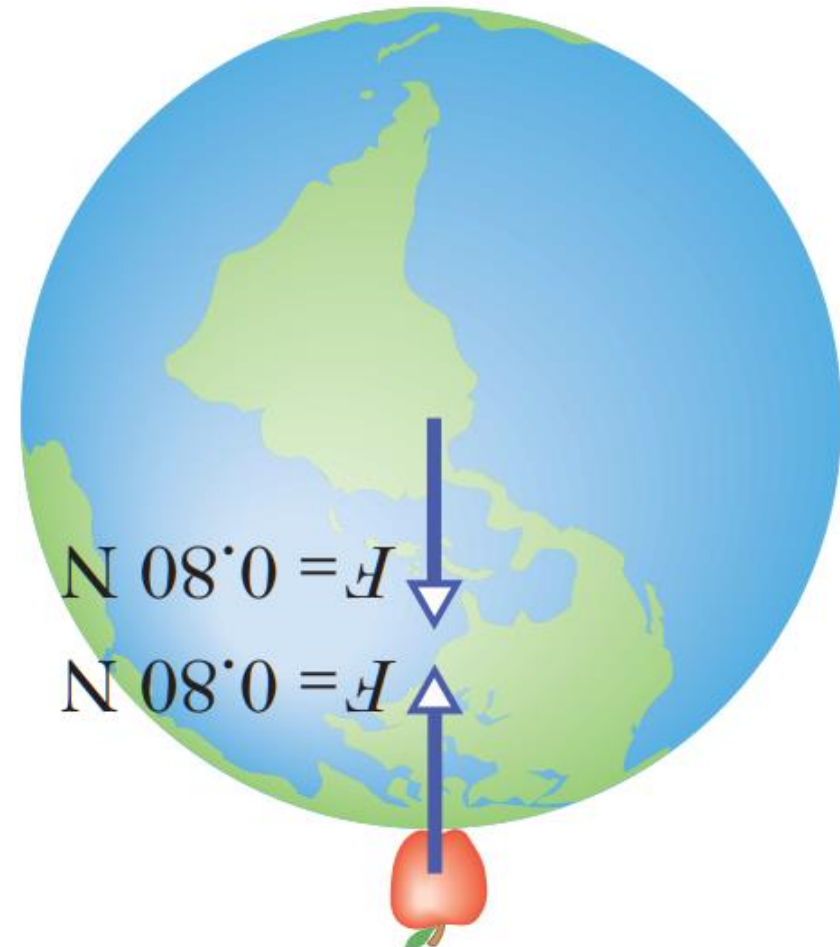
$$w = F_g = \frac{Gm_E m}{R^2}$$

l force  
dy.

th



=



**Weight** of a body at  
the earth's surface ...

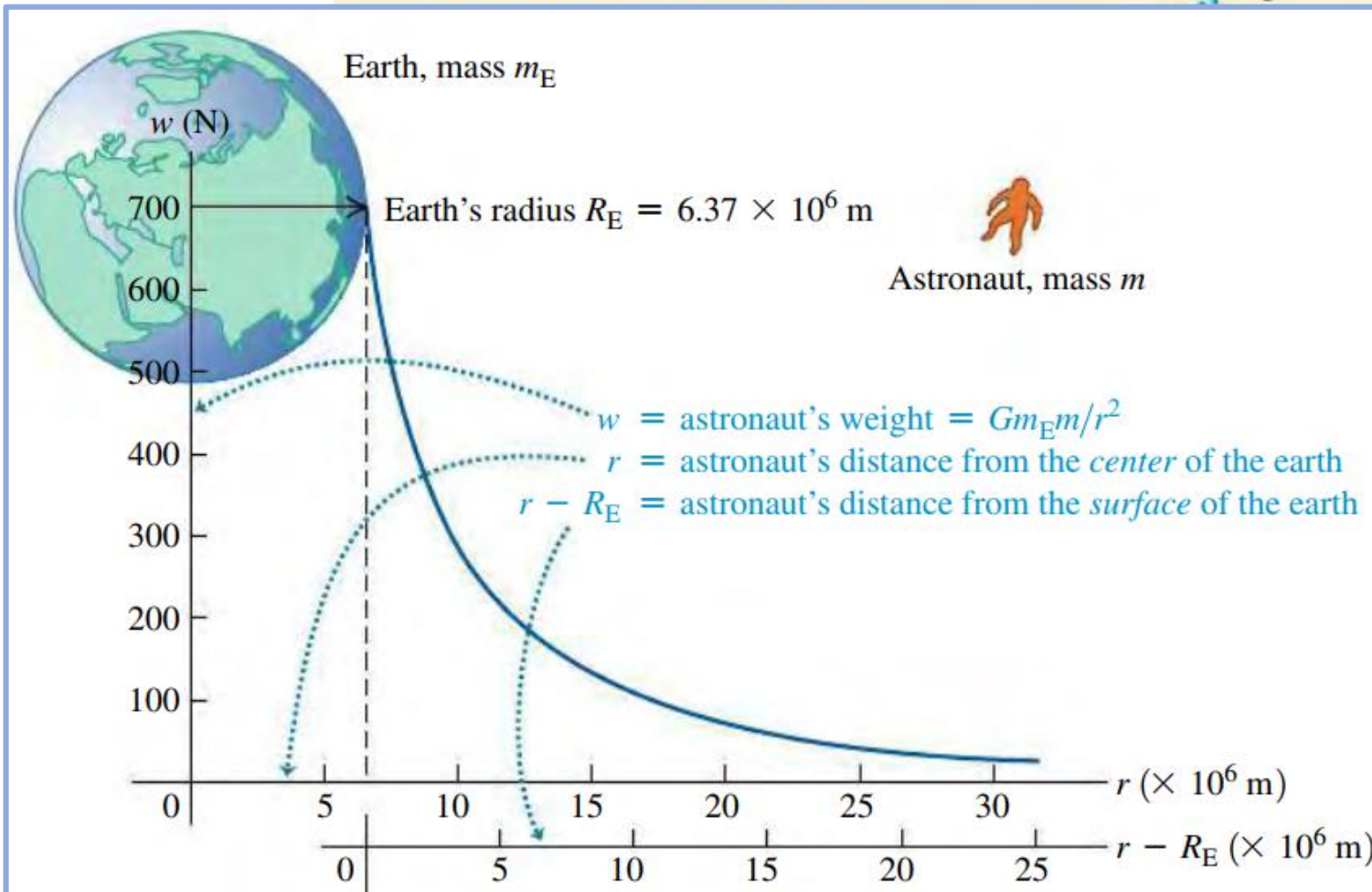
Gravitational constant

Mass of the earth

$$w = F_g = \frac{Gm_E m}{R_E^2}$$

Mass of body

Radius of the earth

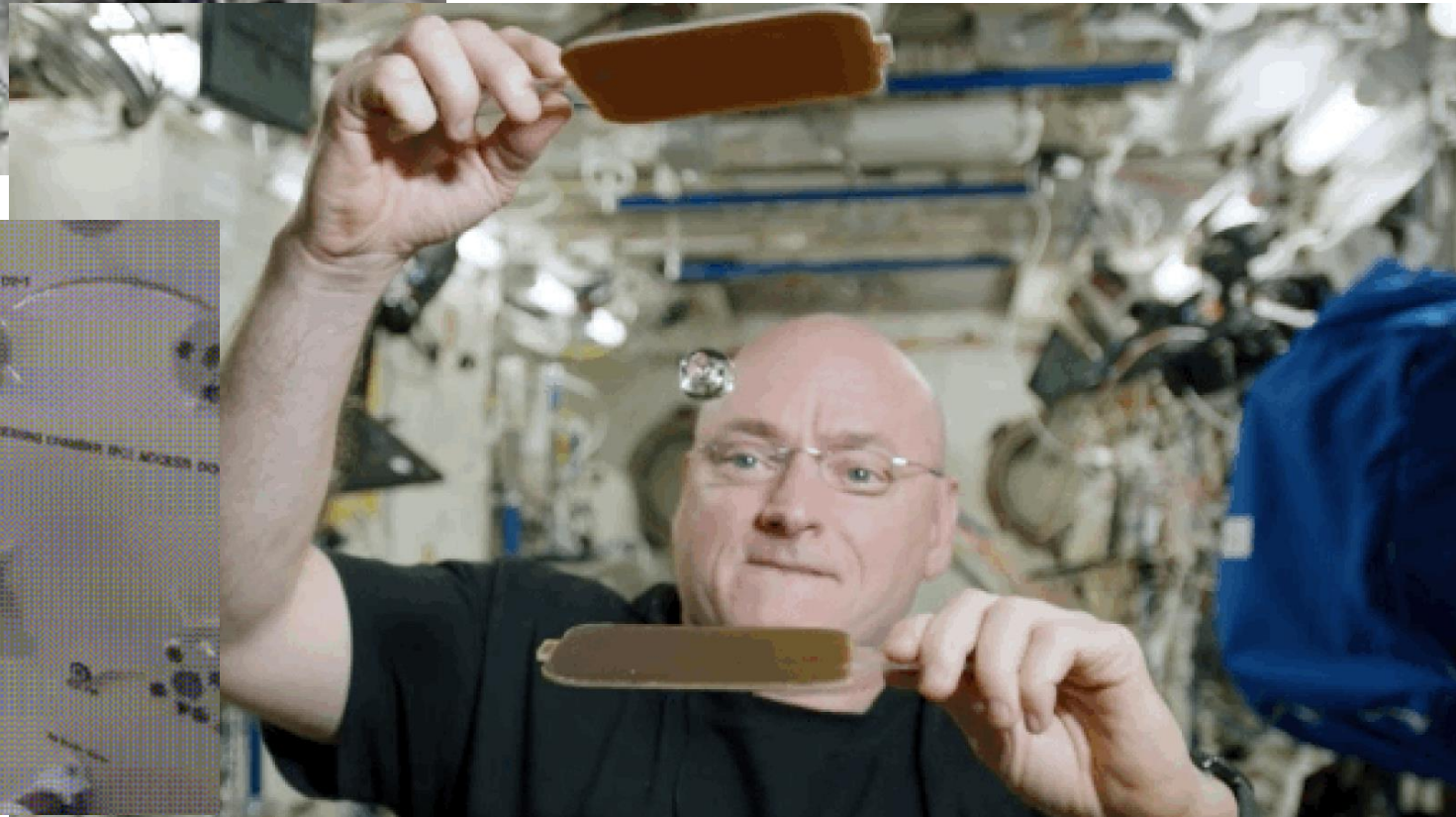
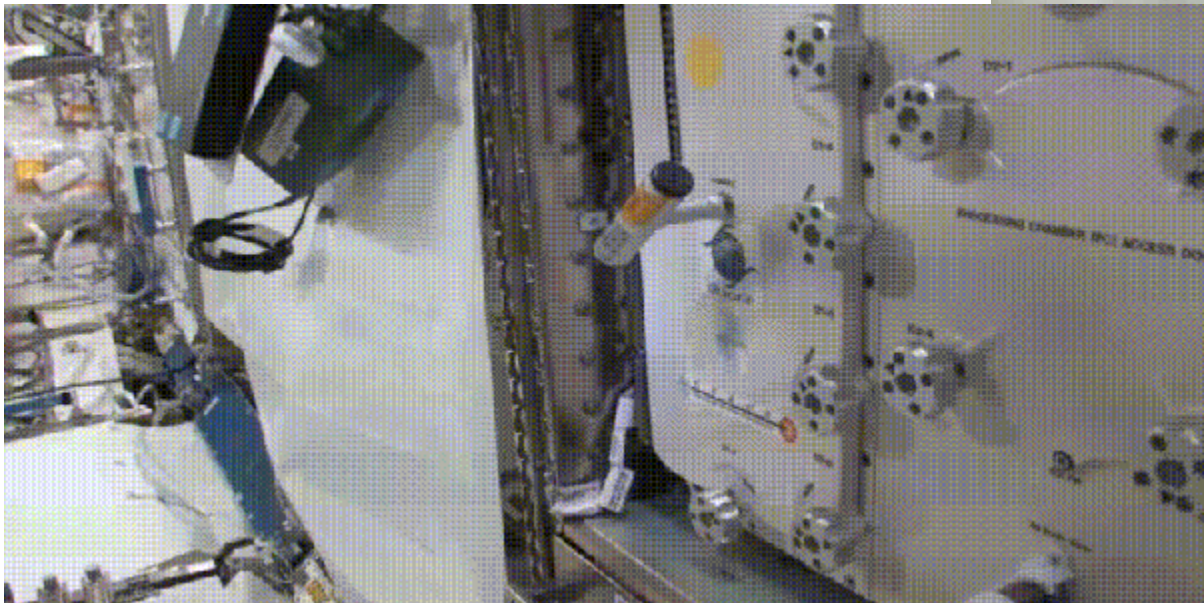


Curve shows how  
gravitational force  
decreases with distance





Astronauts doing weird things  
in ISS (International Space  
Station)







The diagram shows a cross-section of the Earth on the left, with a horizontal line indicating the radius. To the right of the Earth, several horizontal lines represent different altitudes and orbital zones. A red arrow points to the 215 km altitude line. The altitudes are listed in kilometers and miles. The orbital zones are labeled as LEO (Low Earth Orbit) and MEO (Medium Earth Orbit). The Sun-synchronous Satellites zone is also indicated.

Earth Radius 6378 Km / 3963 mi

0 km / mi - Sea Level.

37.6 km / 23.4 mi - Self Propelled Jet Aircraft Flight Ceiling (Record Set in 1977).

215 km / 133.6 mi - Sputnik-1 The first artificial satellite of earth.

340 km / 211.3 mi - International Space Station.

390 km / 242.3 mi - Former Russian Space Station MIR.

595 km / 369.7 mi - Hubble Space Telescope.

[700 - 1700 km] - Polar Orbiting Satellites.

[435 - 1056 mi]

LEO Zone  
(Low Earth Orbit)

MEO Zone  
(Medium Earth Orbit)

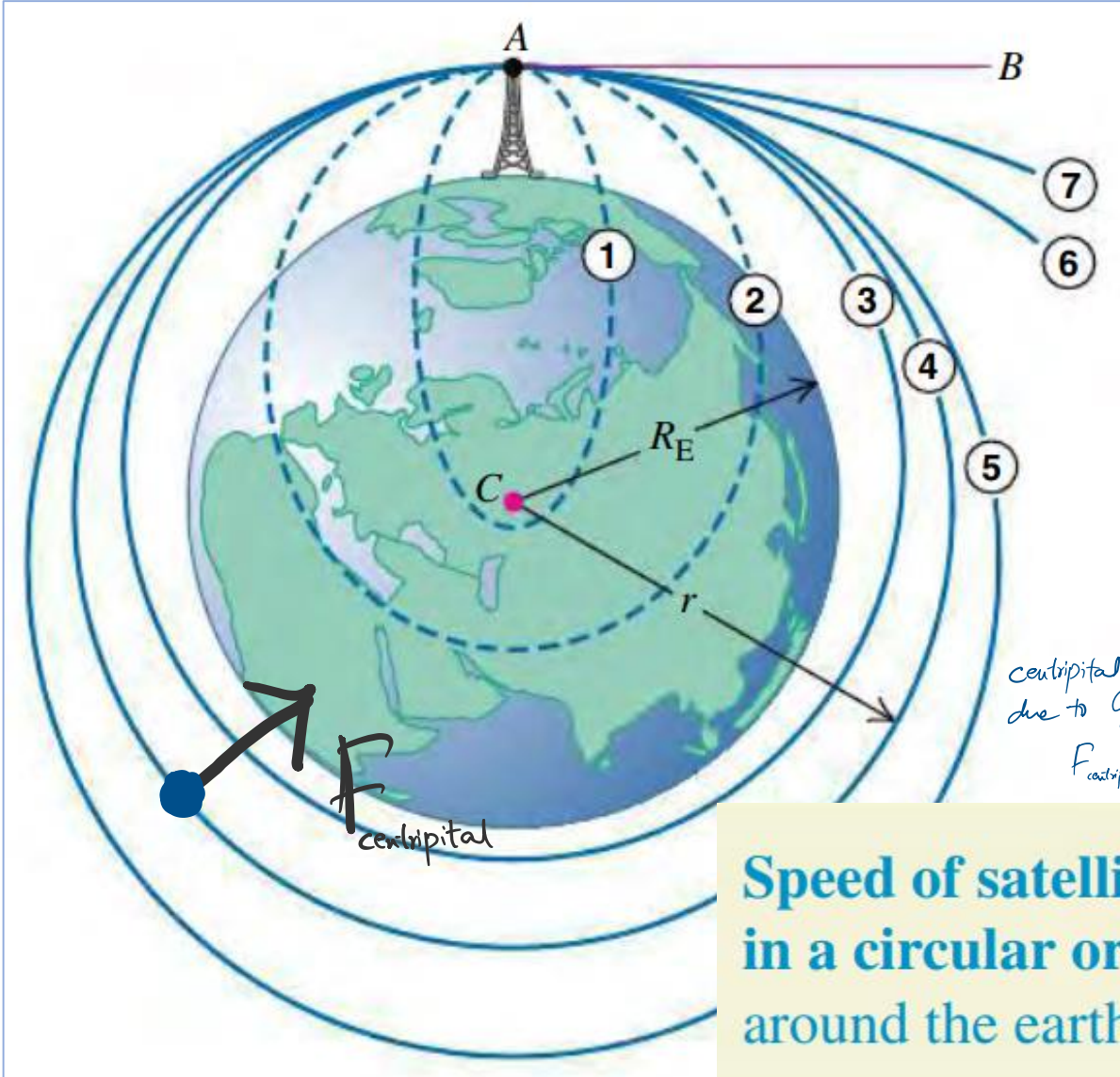
2000 Km / 1243.7 mi

600 - 800 km / 372.8 - 497.1 mi - Sun-synchronous Satellites

These satellites orbit the Earth in near exact polar orbits north to south. They cross the equator multiple times per day and each time they are at the same angle with respect to the sun. Satellites on these types of orbits are particularly useful for capturing images of the Earth's surface or images of the sun.



## Lecture 11



Gravitational constant  $G$  → Mass of the earth  $m_E$  → Mass of body  $m$  → Radius of the earth  $R_E$

$$w = F_g = \frac{Gm_E m}{R_E^2}$$

Force

centripetal acceleration is only due to Gravity

$$F_{\text{centripetal}} = F_{\text{gravity}} \Rightarrow \frac{m v^2}{r} = \frac{G m_E m}{r^2}$$

**Speed of satellite  
in a circular orbit  
around the earth**

Gravitational constant

Mass of the earth  $m_E$  → Radius of orbit  $r$

$$v = \sqrt{\frac{Gm_E}{r}}$$

At the north or south pole: apparent weight is the same as true weight.

$\vec{w}_0$  = true weight of object of mass  $m$

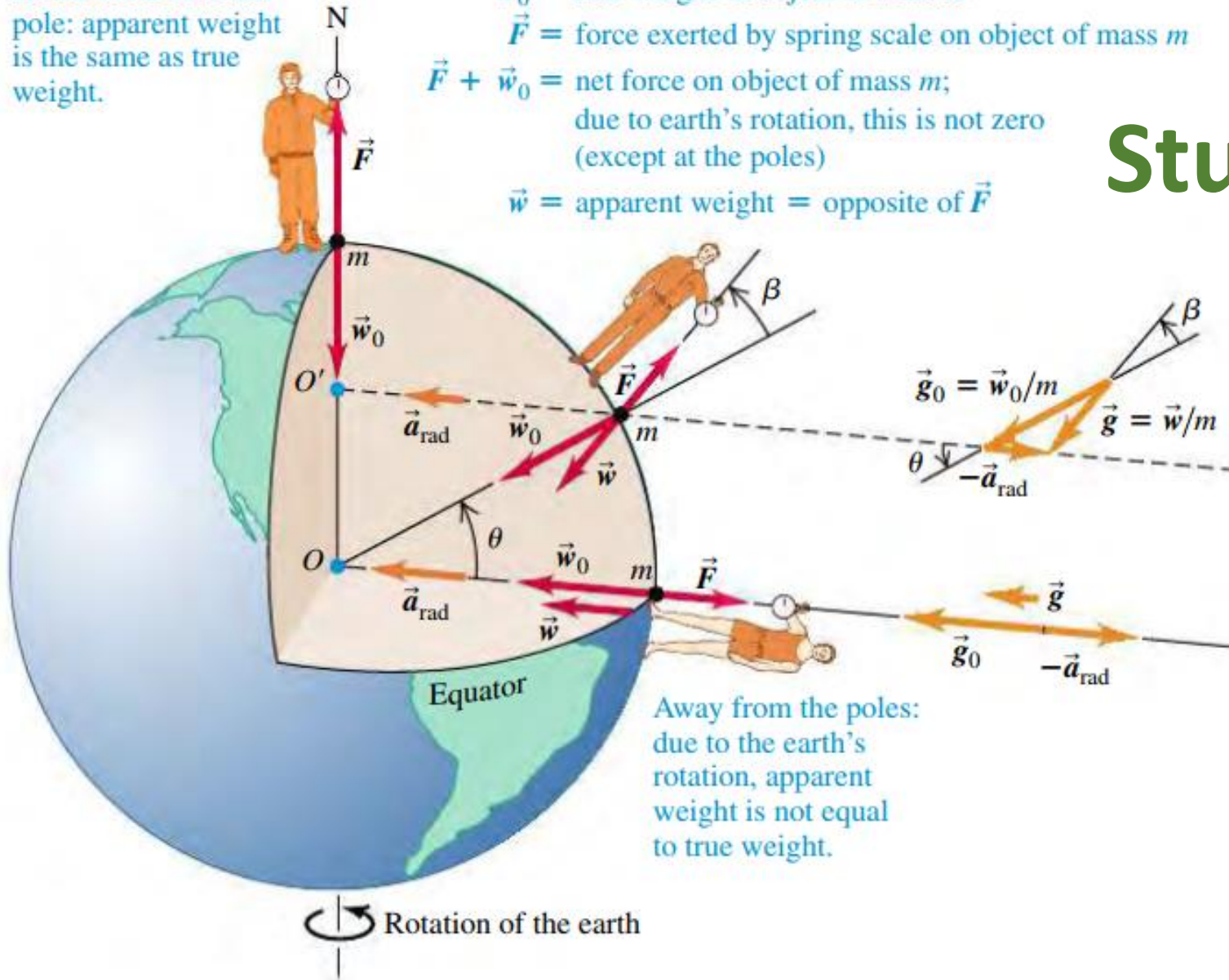
$\vec{F}$  = force exerted by spring scale on object of mass  $m$

$\vec{F} + \vec{w}_0$  = net force on object of mass  $m$ ;  
due to earth's rotation, this is not zero  
(except at the poles)

$\vec{w}$  = apparent weight = opposite of  $\vec{F}$

# Study Challenge

Read the diagram and understand how a false weight vector arises on the surface of the earth.





# Practice problems:

Problems from Fundamentals of Physics

-Jearl Walker

## Chapter 6 : Forces and Motion II

Page#114

Problems: **6,8,12,19,27,42,57**

sample prob: **5.06, 6.02**

Additional Problems