$\bigcirc \varphi(p)$

⊘ Correct

The answer is arphi(p-1) . Here is why. Let g be some generator of \mathbb{Z}_p^* and let $h=g^x$ for some x .

is a generator because if $g = h^y$ then any power of g can also be written as a power of h).

such x is the size of \mathbb{Z}_{p-1}^* which is precisely $\varphi(p-1)$.

It is not difficult to see that h is a generator exactly when we can write g as $g=h^y$ for some integer y (h

Since $y=x^{-1} mod p-1$ this y exists exactly when x is relatively prime to p-1. The number of