and the results are combined by computing $v \leftarrow u_1 + u_2$. \bigcirc party 1 returns $u_1 \leftarrow u^{a_1}$, party 2 returns $u_2 \leftarrow u^{a_2}$ and the results are combined by computing $v \leftarrow u_1 - u_2$. \bigcirc party 1 returns $u_1 \leftarrow u^{-a_1}$, party 2 returns $u_2 \leftarrow u^{-a_2}$ and the results are combined by computing $v \leftarrow u_1 \cdot u_2$. **⊘** Correct Indeed, $v=u_1\cdot u_2=g^{a_1+a_2}=g^a$ as needed for decryption. Note that the secret key was never re-constructed for this distributed decryption to work. **10.** Suppose Alice and Bob live in a country with 50 states. Alice is 1/1 point currently in state $a \in \{1, \dots, 50\}$ and Bob is currently in state $b \in \{1, \dots, 50\}$. They can communicate with one another and Alice wants to test if she is currently in the same state as Bob. If they are in the same state, Alice should learn that fact and otherwise she should learn nothing else about Bob's location. Bob should learn nothing about Alice's location. They agree on the following scheme: • They fix a group G of prime order p and generator g of G• Alice chooses random x and y in \mathbb{Z}_p and sends to Bob $(A_0,A_1,A_2)=\left(g^x,\;g^y,\;g^{xy+a}\right)$ • Bob choose random r and s in \mathbb{Z}_p and sends back to Alice $(B_1,B_2)=\left(A_1^rg^s,\ (A_2/g^b)^rA_0^s\right)$ What should Alice do now to test if they are in the same state (i.e. to test if a=b)? Note that Bob learns nothing from this protocol because he simply recieved a plain ElGamal encryption of g^a under the public key g^x . One can show that if $a \neq b$ then Alice learns nothing else from this protocol because she recieves the encryption of a random value. \bigcirc Alice tests if a=b by checking if $B_2B_1^x=1$. \bigcirc Alice tests if a=b by checking if $B_2^xB_1=1$. lacksquare Alice tests if a=b by checking if $B_2/B_1^x=1$. O Alice tests if a=b by checking if $B_1/B_2^x=1$.

The pair (B_1,B_2) from Bob satisfies $B_1=g^{yr+s}$ and $B_2=(g^x)^{yr+s}g^{r(a-b)}$. Therefore, it is a

plain ElGamal encryption of the plaintext $g^{r(a-b)}$ under the

nothing about b other than the fact that $a \neq b$.

public key (g,g^x) . This plaintext happens to be 1 when a=b.

The term B_2/B_1^x computes the ElGamal plaintext and compares it to 1.

Note that when a
eq b the r(a-b) term ensures that Alice learns

Indeed, when a
eq b then r(a-b) is a uniform non-zero element of

The only change to the analysis is that N-arphi(N) is now

product of two primes making the attack less effective.

on the order of $N^{2/3}$. Everything else stays the same. Plugging

11. What is the bound on d for Wiener's attack when N is a product of **three** equal size distinct primes?

in this bound gives the answer. Note that the bound is weaker in this case compared to when N is a

1/1 point

⊘ Correct

 \mathbb{Z}_p .

 $\bigcirc \ d < N^{1/3}/c$ for some constant c.

 $igotimes d < N^{1/6}/c$ for some constant c.

 $\bigcirc \ \ d < N^{1/4}/c$ for some constant c.

 $\bigcirc \ \ d < N^{1/5}/c$ for some constant c.