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No.

Date

BSLC Statistics 2

① A college found that 20% of its student left after first year without completing the introductory Statistics course. Assume that 20 students registered for the course & the probability of leaving college follows a binomial distribution, compute

$n = 20$	$q = 1 - p$
$p = 20/100$	$q = 4/5$

a) Expected number of withdrawals

$$= n \cdot p$$
$$= 20 \cdot 20\%$$

$$= 4 \Rightarrow \text{expected number of withdrawals}$$

b) Probability that exactly 3 students withdraw

$$P(X=3) = {}^{20}C_3 \cdot (1/5)^3 \cdot (4/5)^{17}$$
$$= \frac{20!}{(20-3)! \cdot 3!} \cdot (1/5)^3 \cdot (4/5)^{17}$$

$$= 0.205$$

c) The probability that more than 3 student withdraw ($X > 3$)

$$P(X > 3) = 1 - [{}^{20}C_0 \cdot (1/5)^0 \cdot (4/5)^{20} + {}^{20}C_1 \cdot (1/5)^1 \cdot (4/5)^{19} + {}^{20}C_2 \cdot (1/5)^2 \cdot (4/5)^{18} + {}^{20}C_3 \cdot (1/5)^3 \cdot (4/5)^{17}]$$
$$= 1 - (0.016 + 0.058 + 0.137 + 0.205)$$
$$= 1 - 0.416$$

$$= 0.584$$

② During the period of a time that a local uni takes phone in regis calls comes in rate of one every 2 min
 $t_1 = 2 \text{ min}$ $\lambda = 1$

a) Expected number of calls in an hour

$$\frac{\lambda_2}{\lambda_1} = \frac{t_2}{t_1}$$

$$\lambda = 30 \text{ calls}$$

$$\frac{\lambda_2}{1} = \frac{60}{2}$$

The expected number of calls in an hour is 30 calls

b) Probability of getting 3 calls in 5 min

$$\frac{\lambda_2}{\lambda_1} = \frac{t_2}{t_1}$$

$$\frac{\lambda_2}{1} = \frac{5}{2}$$

$$\lambda_2 = 2.5 \text{ calls}$$

$$x = 3$$

$$P(x=3) = \frac{\lambda^x e^{-\lambda}}{x!}$$

$$= \frac{2.5^3 e^{-2.5}}{3!}$$

$$= 0.2137$$

The probability of getting 3 calls in 5 minute is 21.38%

c) Probability of getting 0 calls in 5 min

$$P(x=0) = \frac{\lambda^x e^{-\lambda}}{x!}$$

$$= \frac{2.5^0 e^{-2.5}}{0!}$$

$$= 0.08208$$

$$= 0.0821$$

The probability of getting 0 calls in 5 minute is 8.21%