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No.

Date

6SLC Statistics 2

① A college found that 20% of its student left after first year without completing the introductory statistics course. Assume that 20 students registered for the course & the probability of leaving college follows a binomial distribution. Compute

$$\begin{array}{|c|c|} \hline n & = 20 \\ p & = 0.20 \\ q & = 1 - p \\ q & = 0.80 \\ \hline \end{array}$$

a) Expected number of withdrawals

$$\begin{aligned} &= n \cdot p \\ &= 20 \cdot 20\% \end{aligned}$$

= 4 = expected number of withdrawals

b) Probability that exactly 3 students withdraw

$x = 3$

$$\begin{aligned} P(\text{exactly 3 student}) &= 20C_3 \cdot (1/5)^3 \cdot (4/5)^{17} \\ &= \frac{20!}{(20-3)! 20!} \cdot (1/5)^3 \cdot (4/5)^{17} \\ &= 0.020205 \end{aligned}$$

c) The probability that more than 3 student withdrew ($x > 3$)

$$\begin{aligned} P(\text{more than 3 student}) &= 1 - [20C_0 \cdot (1/5)^0 \cdot (4/5)^{20} + \\ &\quad 20C_1 \cdot (1/5)^1 \cdot (4/5)^{19} + \\ &\quad 20C_2 \cdot (1/5)^2 \cdot (4/5)^{18} + \\ &\quad 20C_3 \cdot (1/5)^3 \cdot (4/5)^{17}] \\ &= 1 - (0.016 + 0.058 + \\ &\quad 0.137 + 0.205) \\ &= 1 - 0.416 \\ &= 0.584 \end{aligned}$$

② During the period of a time that a local uni takes phone in regis calls comes in rate of one every 2 min
 $t_1 = 2 \text{ min}$ $\lambda_1 = 1$

a) Expected number of calls in an hour

$$\frac{\lambda_1}{\lambda_1} = \frac{t_1}{t_1} \quad [2 = 30 \text{ calls}]$$

$$\frac{\lambda_2}{\lambda_1} = \frac{60}{2} \quad [\text{The expected number of calls in an hour is } 30 \text{ calls}]$$

b) Probability of getting 3 calls in 5 min

$$\frac{\lambda_2}{\lambda_1} = \frac{t_2}{t_1} \quad \left. \begin{aligned} P(X=3) &= \frac{\lambda^x e^{-\lambda}}{x!} \\ &= \frac{2,5^3 e^{-2,5}}{3!} \end{aligned} \right\}$$

$$\lambda_2 = 2,5 \text{ calls}$$

$$x = 3$$

$\rightarrow 2,5^3 \cdot 0,2137$
 The probability of getting 3 calls in 5 minute is 21,38%

c) Probability of getting 0 calls in 5 min

$$P(X=0) = \frac{\lambda^x e^{-\lambda}}{x!}$$

$$\begin{aligned} &= \frac{2,5^0 e^{-2,5}}{0!} \\ &= 0,08208 \\ &\approx 0,0821 \end{aligned}$$

\rightarrow The probability of getting 0 calls in 5 minute is 8,21%