



**Figure S3:** The possible choices for the embedding dimensionality  $d=\{11,15\}$  were determined by identifying the first and second elbow-point (Zhu and Ghodsi, 2006), respectively, on the scree plot of singular values.