

Some examples of global threshold utilization:

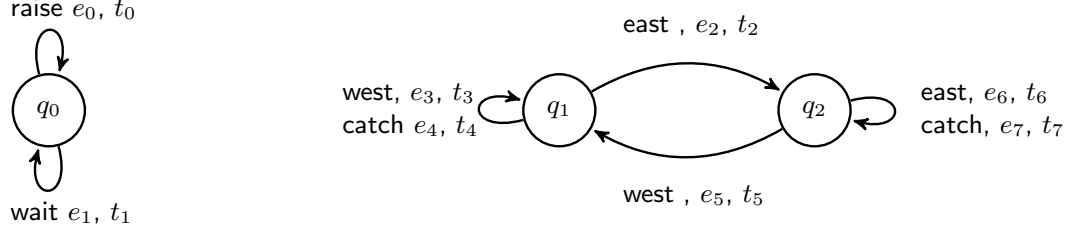


Figure 1: Automata  $A_0$  on the left and  $A_1$  on the right

$\{\text{raise, west, east, wait, catch}\}$  are all possible actions.  $e_i$  and  $t_i$  are respectively the semiring value and the threshold associated to the corresponding transition. Each automaton has a global threshold  $T_{A_i}$  such that  $A|_{T_{A_i}}$  is the restriction of the automaton to all transition involving semiring values below  $T_{A_i}$ . In the next figure, some values have been associated with each  $e_i$  and  $t_i$

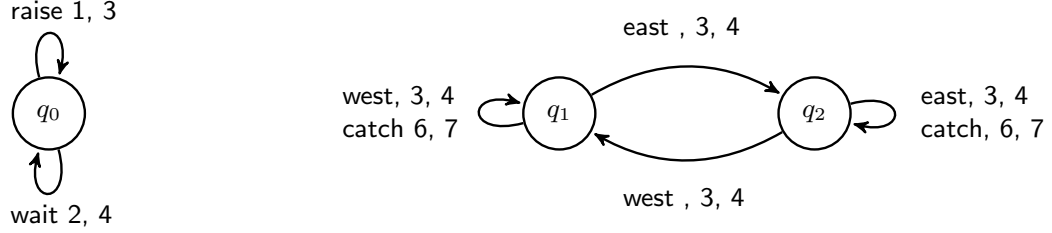


Figure 2: Automata  $A_0$  on the left and  $A_1$  on the right

Let  $T_{A_0} = 3$  and  $T_{A_1} = 5$ . We assume that raise can only compose with catch, and wait can only compose with west or east. There are now two possibilities to compose  $A_1$  and  $A_0$ . Either :

$$A = (A_0 \otimes A_1)|_{T_{A_0} \otimes T_{A_1}}$$

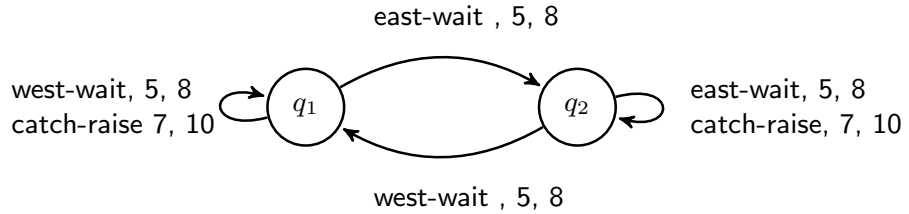


Figure 3: Automata  $A = (A_0 \otimes A_1)|_{T_{A_0} \otimes T_{A_1}}$  with  $T_A = 8$

Or :

$$A = A_{0|T_{A_0}} \otimes A_{1|T_{A_1}}$$

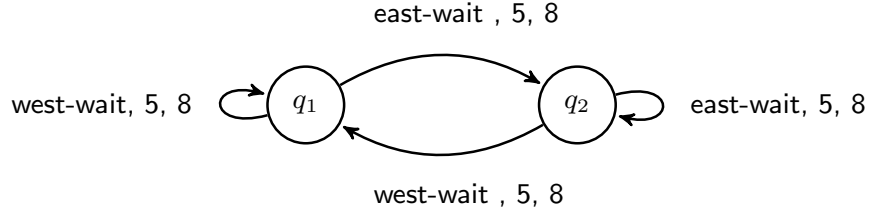


Figure 4: Automata  $A = A_{0|T_{A_0}} \otimes A_{1|T_{A_1}}$  with  $T_A = 8$

This threshold can be usefull to separate composition of *internal* actions and *external* actions. An action can be defined as *internal* if it involves a single agent (west or east action). An action is called *external* if it needs some other agents to be allowed (catch for instance). In this scope, internal actions have low semiring values, and external actions have high semiring values. By defining a global threshold  $T_A$ , and a restriction of the Automaton regarding the threshold, we allow only composition of internal action, or internal and external actions.