



Fig. 1: A black box is an irrational component; a white box is a rational component. Channels are pictured by different edge styles. Nodes are depicted by black dots, merging incoming ports $a_1 \dots a_n$ and replicating to outgoing ports $b_1 \dots b_m$.

1 Preliminaries (2 pages)

We model autonomous systems as compositions of primitive components. We superficially regard two kinds of components: rational components and irrational components. Intuitively, only the behavior of the former can be finitely represented; the latter not. Components cannot recognize themselves or others as being rational or irrational. We use irrational components as primitives to model unpredictable environments.

Components Each component has a fixed number of ports. A port can be thought of as a gateway, passing data in and out. Components without ports are sealed and can no longer be composed. Semantically, we define behavior of a component as a (non-well-founded) relation between ports. Only rational components harbor a finite representation of its behavior. See figure 1a for a picture.

Studying ports is important. One could stand—quite literally—next to a port and observe all data that is passed along. Sometimes one observes no activity at all, which we denote by $*$. Other times one observes a datum, which we leave uninterpreted. Ports are characterized by the set of streams of its activity. For example, we write $a = (*, d_1, *, *, d_2, \dots)$ where d_1 is the first datum observed and d_2 is the second datum observed, and so on.

This work is based on Reo: a language for modeling agents as components. The most important elements of this language are channels, nodes and compositions. Channels and nodes are primitive components through which data *flows* between ports. We will later give two examples of the channels in figure 1b. Nodes are used to link multiple channels together, see figure 1c. Finally, composition identifies the ports in complex constructions of channels and nodes.

Protocols We introduce protocols as a fundamental formalism for modeling systems. Formal protocols are a generalization of formal languages, in the sense that formal languages defines word membership, and that formal protocols defines stream membership. We now give some more details.

By Σ we denote some countably infinite alphabet of symbols. A finite sequence, or *word*, is formed by juxtaposing symbols from Σ . The set of all words is denoted Σ^* . A formal language \mathcal{L} is a subset of the set of all words, i.e. $\mathcal{L} \subseteq \Sigma^*$.

An infinite sequence, or *stream*, is formed by an infinite juxtaposing of symbols from Σ . The set of all streams is denoted Σ^ω . A stream is isomorphic to a function $\sigma : \mathbb{N} \rightarrow \Sigma$, and a σ can be given by defining $\sigma(0)$ and the *stream derivative* σ' . Streams are informally described as infinite tuples, in the shape (x_0, x_1, x_2, \dots) where x_i are elements of Σ . A formal protocol \mathcal{P} is a subset of the set of all streams, i.e. $\mathcal{P} \subseteq \Sigma^\omega$.

Ports Let V denote a countably infinite set of port variables, and let D denote a set of data that contains some fixed constant $*$ $\in D$. The meaning of each datum $d \in D$ other than $*$ is application-specific. By D^ω we mean a single stream of observations, called a *data stream*. Next, we consider a rational component C . Let V_C denote the finite set of port variables corresponding to C . If V_C is empty then the component is sealed. Let $n = |V_C|$ be the number of ports of C .

We characterize the behavior of a rational component by a relation on data streams. An n -ary relation R on data streams can be seen as a set of tuples of data streams, e.g. $(\sigma_1, \sigma_2, \dots, \sigma_n) \in R$. We obtain the sets of data streams by projection: we define $\sigma_i \in \Pi_i R$ if and only if $(\sigma_1, \dots, \sigma_i, \dots, \sigma_n) \in R$. Equivalently, and more convenient for our purposes, let R be sets of streams of n -ary tuples of data. That is, we let R be a formal protocol with alphabet $\Sigma = D^n$.

Intuitively, one can compare our treatment to relational algebra, where the attribute names of n -ary relations are our port variables. By convention we identify a rational component C and the relation specifying its behavior. The ports V_C are attributes of the $|V_C|$ -ary relation. We now characterize a port $v \in V_C$ by the set of data streams $\Pi_v C$.

Channels We consider two channels: synchronous and asynchronous, as depicted in figure 1b respectively on top and bottom. Let a and b be two ports. We specify the behavior of a synchronous channel between a and b , denoted $S(a, b) \subseteq (D^2)^\omega$, as the largest relation such that:

$$\sigma \in S(a, b) \Leftrightarrow [\forall d \in D. \sigma(0) = (d, d)] \wedge \sigma' \in S(a, b)$$

that is, the two ports have equal data streams. We now specify the behavior of an asynchronous channel, denoted $A(a, b) \subseteq (D^2)^\omega$, as the largest relation:

$$\begin{aligned} \sigma \in A(a, b) \Leftrightarrow \forall d \in D. \sigma(0) = (d, *) \wedge \\ \exists i. \sigma(i) = (*, d) \wedge [\forall j < i. \sigma(j) = (*, *)] \wedge \\ \sigma^{(i+1)} \in A(a, b) \end{aligned}$$

where $\sigma^{(0)} = \sigma$ and $\sigma^{(n+1)} = (\sigma^{(n)})'$ defines the repeated stream derivative. Intuitively, an asynchronous channel is either inactive or passes a datum in a delayed fashion. Let $i = 0$ and see $\sigma(0) = (*, *)$. If port a offers a datum d then port b takes the same datum at some time later, while both ports remain inactive in the mean time. Note that when a and b are also connected by a synchronous channel, the behavior collapses into the singleton set accepting only $(*, *, \dots)$.

Nodes Finally, we specify the node as depicted in 1c. Nodes have $n + m$ number of ports with $n, m \geq 1$. Its input ports are denoted $a^\rightarrow = a_1, \dots, a_n$ and output ports $b^\rightarrow = b_1, \dots, b_m$. Note that by $\sigma(0)_i$ we denote the i -th projection of the initial element of the stream σ containing tuples $(a_1, \dots, a_n, b_1, \dots, b_m)$. The behavior of nodes are characterized by the $(n + m)$ -ary relation $N(a^\rightarrow, b^\rightarrow)$, defined as the largest relation such that:

$$\begin{aligned} \sigma \in N(a^\rightarrow, b^\rightarrow) \Leftrightarrow \forall d \in D. [\exists i \leq n. \sigma(0)_i = d \wedge [\forall i' \leq n. i' \neq i \rightarrow \sigma(0)_{i'} = *] \\ \forall j \leq m. \sigma(0)_{n+j} = d] \wedge \\ \sigma' \in N(a^\rightarrow, b^\rightarrow) \end{aligned}$$

where i, i', j are non-zero. Intuitively, nodes are synchronous channels that merge and replicate data. Merge specifies that at most one of the n channels can offer a datum, and all others n channels are inactive. Replication specifies that all of the m channels takes the datum offered. Also, all ports of a node can be inactive.

2 SCA : 2 pages

Constraints

Preferences

States and Transitions

Operational Semantic

LTS

State assignment

Constraint solving

3 Streams : 2 pages

Relation as stream

Equivalence with SCA

Composition

Counter example

4 Coproduct : 2 pages

Coproduct definition

Uninterpreted expression

Runtime composition

Quotient

Example

5 Simplification : 2 pages

Single state SCA

Constraint as Boolean semiring value

Semiring automaton

Optimisation and future work

References

1. Farhad Arbab and Francesco Santini. *Preference and Similarity-Based Behavioral Discovery of Services*, pages 118–133. Springer Berlin Heidelberg, Berlin, Heidelberg, 2013.
2. Stefano Bistarelli. *Semiring for Soft Constraint Solving and Programming*. Springer, 2004.
3. Tobias Kappé, Farhad Arbab, and Carolyn L. Talcott. A component-oriented framework for autonomous agents. pages 20–38, 2017.