

Homework Set: HW4

Momentum, Impulse, and 2D Collisions

Problem 1: Perfectly Inelastic 2D Collision + Impulse + Post-Collision Motion

Two low-friction carts collide on a horizontal air table and stick together (perfectly inelastic collision). Take +x to be east and +y to be north. External horizontal forces during the collision are negligible.

Cart A has mass $m_A = 0.45 \text{ kg}$ and moves at speed 6.2 m/s at an angle of 25° *north of east* just before impact.

Cart B has mass $m_B = 0.70 \text{ kg}$ and moves at speed 4.5 m/s at an angle of 40° *south of east* just before impact.

After they stick, the combined carts slide off the air table onto a rough surface and come to rest after traveling a distance of 3.5 m . Assume the rough surface provides a kinetic friction force with coefficient μ_k (unknown). Use $g = 9.81 \text{ m/s}^2$.

- (a) **Vector momentum setup.** Write the initial velocity vectors \vec{v}_A and \vec{v}_B in component form (x- and y-components).
- (b) **Post-collision velocity (2D).** Use conservation of momentum in x and y to find the combined velocity vector \vec{v}_f immediately after the collision. Report:
 - (i) v_{fx} and v_{fy} ,
 - (ii) the speed v_f ,
 - (iii) the direction as an angle measured from +x (east), with correct quadrant.
- (c) **Kinetic energy change.** Calculate the total kinetic energy before the collision and just after the collision, then determine:
 - (i) the kinetic energy lost in the collision, $\Delta K = K_i - K_f$,
 - (ii) the fraction of kinetic energy lost, $\Delta K/K_i$.
- (d) **Impulse and average collision force.** The sticking collision lasts $\Delta t = 0.035 \text{ s}$.
 - (i) Find the impulse vector on cart A, \vec{J}_A . Note $J = \Delta p = F\Delta t$.
 - (ii) Find the impulse vector on cart B, \vec{J}_B .

- (iii) Hence find the average force on each cart during the collision, $\vec{F}_{\text{avg}} = \vec{J}/\Delta t$ (give components).
- (e) **Friction estimate from stopping distance.** After the collision, the combined carts (mass $m_A + m_B$) enter the rough surface with initial speed v_f (from part b) and stop after 3.5 m. Assuming kinetic friction is the only horizontal force on the rough surface, determine μ_k .
- (f) **Direction reasoning (short explanation).** In 1–2 sentences, explain why the final direction in part (b) must lie between the initial directions of A and B.