## Assignment 14

## K.A. Raja Babu

Download all python codes from

https://github.com/ka-raja-babu/Matrix-Theory/ tree/main/Assignment14

and latex-tikz codes from

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## 1 Question No. 6.17

A person plays a game of tossing a coin thrice. For each head, he is given Rs 2 by the organiser of the game and for each tail,he has to give Rs 1.50 to the organiser. Let X denote the amount gained or lost by the person. Show that X is a random variable and exhibit it as a function on the sample space of the experiment.

## 2 Solution

Let  $X_1, X_2, X_3$  be the three tosses of the coin and X be the total amount such that

$$X = X_1 + X_2 + X_3 \tag{2.0.1}$$

where

$$X_i = \{2, -1.5\} \tag{2.0.2}$$

- : Tossing a coin three times follows binomial distribution.
  - $\therefore X$  follows binomial distribution.

Now, assuming a fair coin, the probability mass function of *X* is given by

$$p_X(k) = {}^{n}C_k p^k (1-p)^{n-k}$$
 (2.0.3)

where

$$n = 3, p = \frac{1}{2}, k = 0, 1, 2, 3$$
 (2.0.4)

From eq.(2.0.1), value of X is given by

$$X = x \in \{-4.5, -1, 2.5, 6\}$$
 (2.0.5)

Now, using least square method of curve fitting, PMF of X in terms of x is given by

$$p_X(x) = 0.4005 + 0.0153x - 0.0102x^2$$
 (2.0.6)

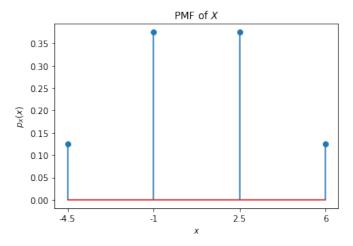


Fig. 2.1: PMF of *X*