

# Assignment 14

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Download all python codes from

<https://github.com/ka-raja-babu/Matrix-Theory/tree/main/Assignment14>

and latex-tikz codes from

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## 1 QUESTION No. 6.17

A person plays a game of tossing a coin thrice. For each head, he is given Rs 2 by the organiser of the game and for each tail, he has to give Rs 1.50 to the organiser. Let  $X$  denote the amount gained or lost by the person. Show that  $X$  is a random variable and exhibit it as a function on the sample space of the experiment.

## 2 SOLUTION

Let  $X_1, X_2, X_3$  be the three tosses of the coin and  $X$  be the total amount such that

$$X = X_1 + X_2 + X_3 \quad (2.0.1)$$

where

$$X_i = \{2, -1.5\} \quad (2.0.2)$$

Assuming a fair coin, the probability mass function of  $X$  is given by

$$\Pr(r, n, p) = \frac{n!}{r!(n-r)!} p^r q^{n-r} \quad (2.0.3)$$

where

$$n = 3, p = \frac{1}{2}, q = \frac{1}{2}, r = 0, 1, 2, 3 \quad (2.0.4)$$

| $r$      | 0             | 1             | 2             | 3             |
|----------|---------------|---------------|---------------|---------------|
| $\Pr(r)$ | $\frac{1}{8}$ | $\frac{3}{8}$ | $\frac{3}{8}$ | $\frac{1}{8}$ |

TABLE 2.1: PMF of  $X$

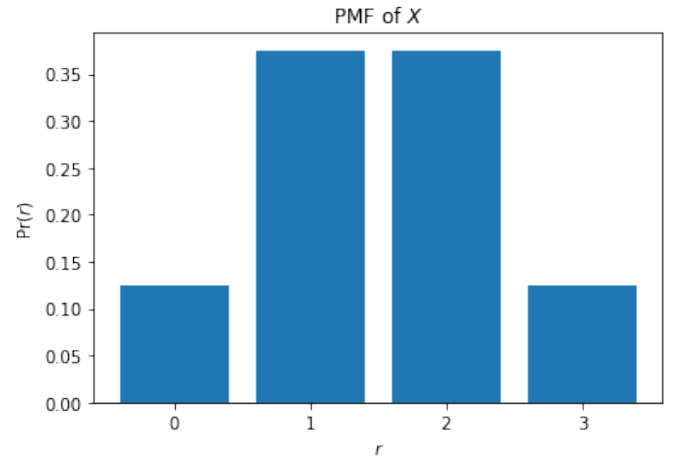


Fig. 2.1: PMF of  $X$