

Date

Problem 1

Topic / Description

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Engr 65

H.W 1

9.4.22

a. If charge flow is expressed as  $q(t) = (14t^2 + 8t - 2)C$ , determine the current flow↳ recall that  $i \triangleq \frac{dq}{dt}$ ;  $q = 14t^2 + 8t - 2)C$ 

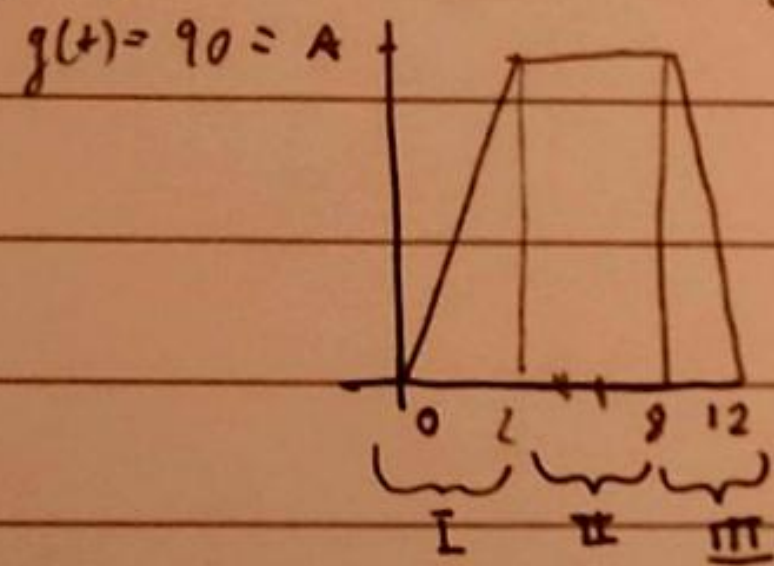
$$\rightarrow i = \frac{d}{dt} [14t^2 + 8t - 2) = 28t + 8 \checkmark$$

b. Charge flow is expressed as  $q(t) = (11e^{-t} - 21e^{-2t})nC$ ↳  $i \triangleq \frac{dq}{dt}$ ;  $q = 11e^{-t} - 21e^{-2t}$ 

$$\rightarrow i = \frac{d}{dt} (11e^{-t}) - \frac{d}{dt} (21e^{-2t})$$

$$\rightarrow -11e^{-t} - (-42e^{-2t})$$

$$\rightarrow -11e^{-t} + 42e^{-2t} = i \checkmark$$

c. Given the charge entering the terminal of elements demonstrated by picture below, given  $A = 90$ , find the current at 1ms, 6ms, 10msI. ↳  $[0, 2]$ , Consider positive relationship

$$\rightarrow \frac{90-0}{2-0} = 45 \text{ mC/ms}$$

$$\rightarrow 45 \text{ C/s}; q(t) = 45t$$

$$\rightarrow \text{Consider current } (i = \frac{dq}{dt}); i = \frac{d(45t)}{dt} = 45$$

↳ Thus, at 1ms there is 45A ✓

II. ↳  $[2, 8]$ , Consider that slope interval is constant; thereby, no changes.

$$\rightarrow i \triangleq \frac{dq}{dt} = \frac{d(90)}{dt} = 0$$

↳ thereby, at 6ms, there is 0A ✓

III ↳  $[8, 12]$ , Consider decline relationship, find slope.

$$\rightarrow \frac{0-90}{12-8} = -\frac{90}{4} = -22.5 \text{ C}$$

$$\rightarrow \text{Consider } q(t) = -22.5t + (C)$$

$$\rightarrow \text{recall that } i \triangleq \frac{dq}{dt}; i = \frac{d(-22.5t)}{dt} = -22.5 \text{ A}$$

↳ Thus, at 10ms, there is -22.5A



## Problem 2

a. 1 kW toaster takes 6 min to heat up 1 slice of bread. Find cost of toaster usage if it is used twice per day for 2 weeks. Consider energy cost 9 cents/kWh

$$\rightarrow \frac{6 \text{ min}}{60} \cdot 2 \cdot 14 \left( \frac{.09}{1 \text{ kWh}} \right)$$

$$\rightarrow (2.8)9 = 25.2 \text{ Cent}$$

b. How much energy does a 7-hp motor deliver in 30 min

$\rightarrow$  Consider desired answer is energy which is measured in Joules; Also, consider  $1 \text{ W} = 1 \frac{\text{J}}{\text{sec}}$

$\rightarrow$  Given that  $1 \text{ hp} = 746 \text{ W}$

$\rightarrow 7 \text{ hp} \rightarrow \text{Watts} \rightarrow \text{Joules/sec}$

$$\rightarrow 7 \cdot 746 (30 \text{ min} \cdot 60 \text{ sec}) \quad \# \text{ Consider the } E = P(T)$$

$$\rightarrow 939600 = 9.399600 \cdot 10^6 \text{ Joules}$$

c. Graph depicts energy drawn by a plant from 8:00 A.M. to 8:30 A.M. Calculate the total energy in kWh consumed by plant.

$\rightarrow$  Consider that  $P = E(T)$

$$\rightarrow \text{from } 8:00-:05 = 5(S), 8:05-:10 = 4(S), 8:10-:15 = 3(S), 8:15-:20 = 8(S)$$

$$8:20-:25 = 5(S), 8:25-:30 = 5(S)$$

$$\rightarrow 5(S) + 4(S) + 3(S) + 8(S) + 5(S) + 0$$

$$\rightarrow \frac{140}{60} = 2.33 \text{ Mwh}$$



### Problem 3

Given that  $i$  entering positive terminal is  $i(t) = 13e^{-2t} \text{ mA}$  and the voltage across the device is  $v(t) = 6 \frac{di}{dt} \text{ V}$

a. Calculate the power absorbed by the device

↳ Consider the fact that  $p(t) = v(t)i(t)$

↳ Given  $v(t) = 6 \frac{di}{dt} \text{ V}$  ;  $i(t) = 13e^{-2t} \text{ mA}$

$$\rightarrow 6 \left( \frac{di}{dt} (13e^{-2t} \cdot 10^{-3}) \right) (13e^{-2t} \cdot 10^{-3})$$

$$6 \cdot 13 \cdot 13 \cdot 10^{-6} \cdot e^{-2t} \cdot \frac{d}{dt}(e^{-2t})$$

$$\rightarrow (1.014 \cdot 10^{-3} \cdot e^{-2t}) 2e^{-2t}$$

$$\rightarrow -2.028 \cdot 10^{-3} \cdot e^{-4t}$$

$$\rightarrow -2.028 \cdot e^{-4t} \text{ mW}$$

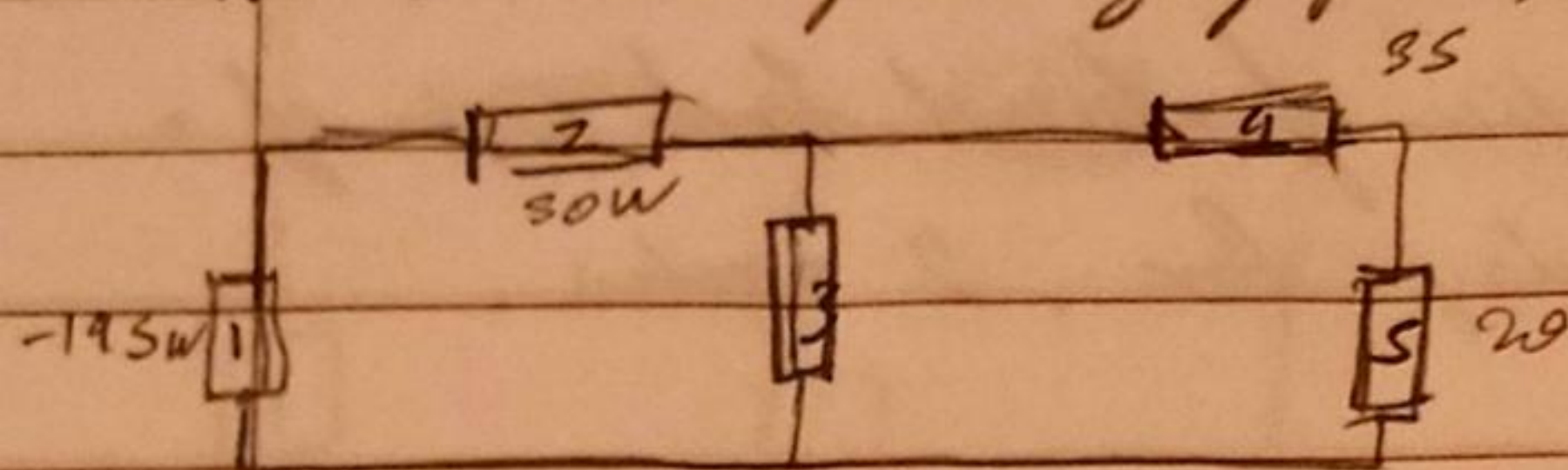
b. Calculate energy absorbed in 3 seconds

Consider  $E = \int_{t_0}^{t_f} P dt$  , ↳ consider  $-2.028 \cdot e^{-4t}$  ;  $t=3 \Rightarrow \int_0^3 (-2.028 \cdot 10^{-3} e^{-4t}) dt = -5.00 \cdot 10^{-4} \text{ J}$  ✓

↳  $2.028 \cdot 10^{-3} \left[ -\frac{1}{4} e^{-4t} \right]_0^3$



4. Consider the following figure,



Consider, Given  $P_1 = -195W$

$$P_2 = 50W$$

$$P_4 = 35W$$

$$P_5 = 20W$$

a. Calculate  $P_3 = \text{Total of } P = 0$

$$\rightarrow \text{Consider } -195 + 50 + 35 + 20 + P_3 = 0$$

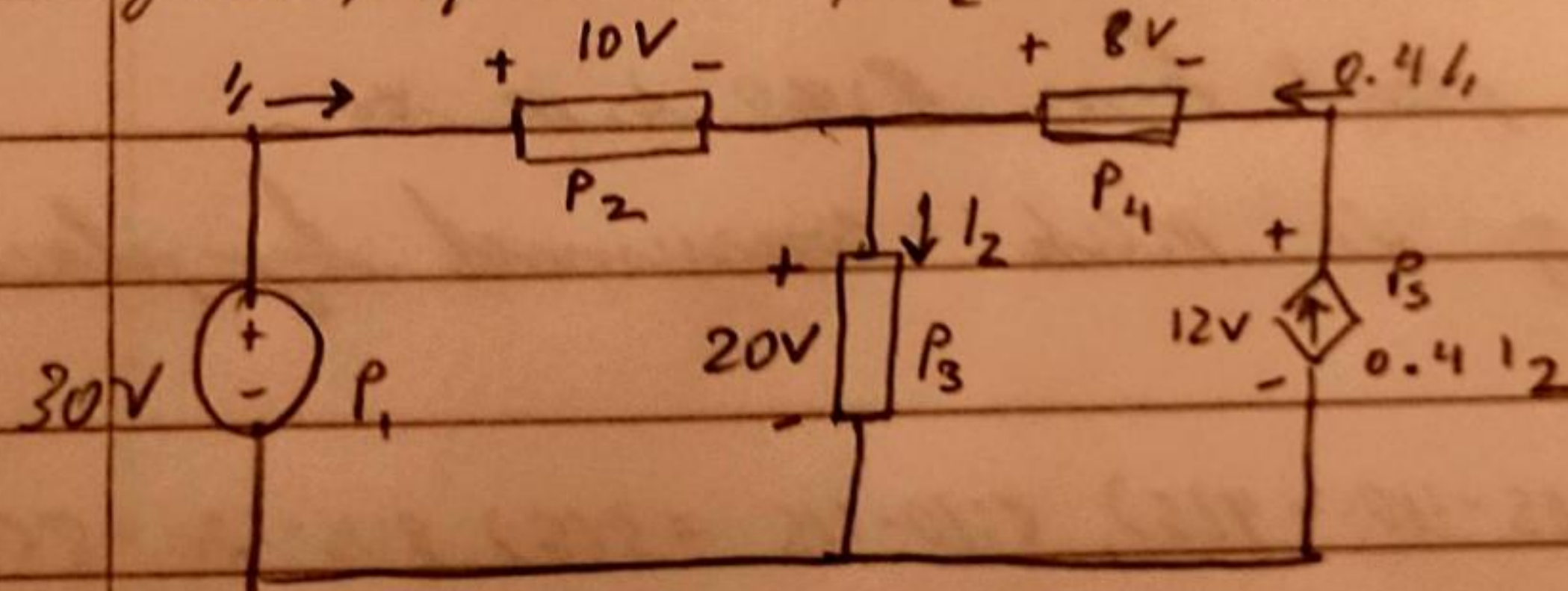
$$\rightarrow -95 + P_3 = 0$$

$$\rightarrow (-95 = -P_3) \rightarrow$$

$$\rightarrow P_3 = 95W$$

b. Find the power absorbed by elements in given fig,

given,  $I_1 = 13.00A$ ,  $I_2 = 18.20A$



Consider  $P = Vi$

$$\rightarrow \text{Thereby, } P_1 = 13A(30V) \cdot \text{Negative } \tau = -390W$$

$$P_2 = 13A(10V) \cdot \text{Positive } \tau = 130W$$

$$P_3 = 18.20A(20V) \cdot \text{Positive } \tau = 364W$$

$$P_4 = -4(13.00A)(8V) \cdot \text{Negative } \tau = -41.6W$$

$$P_5 = -0.4(13.00A)(12V) \cdot \text{Negative } \tau = -62.4W$$