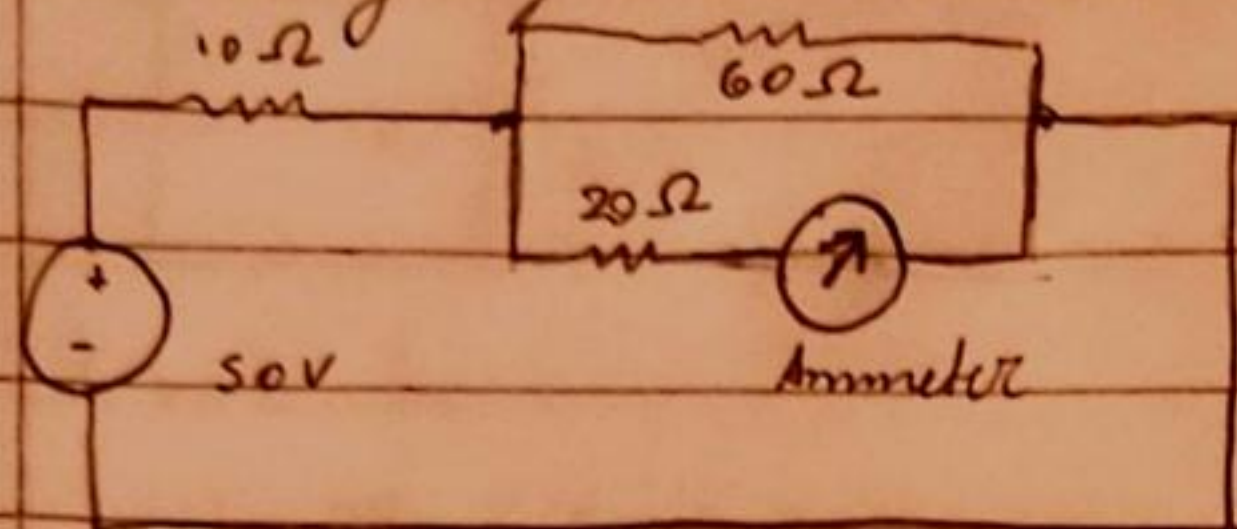


# Engr 65 Homework

## 1. Reading of the Ammeter



A. Consider KCL

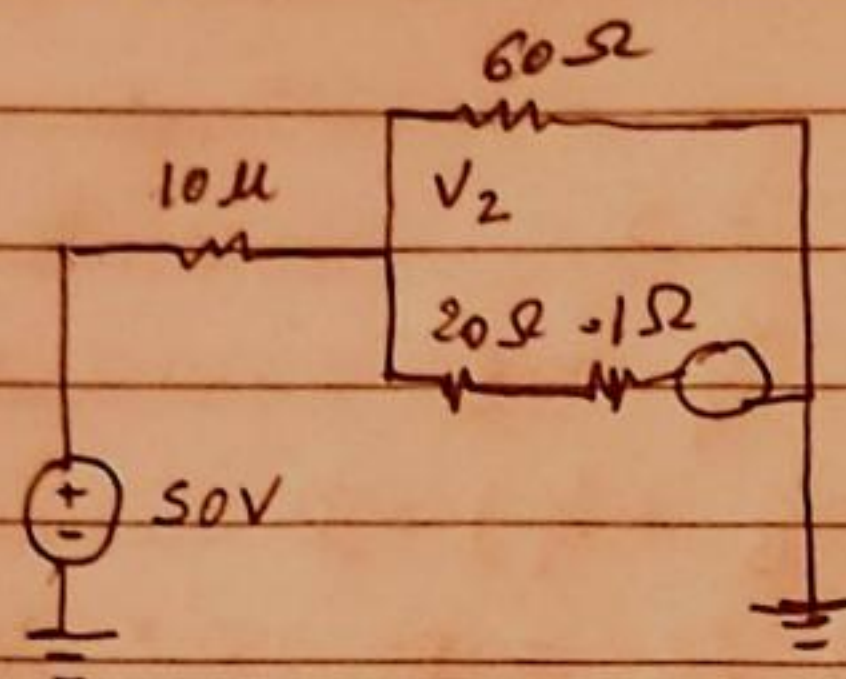
$$\frac{I_m - 50}{10} + \frac{I_m}{20} + \frac{I_m}{60} = 0$$

$$\rightarrow \frac{6(I_m - 50)}{60} + \frac{3(I_m)}{60} + \frac{I_m}{60} = 0$$

$$\rightarrow \frac{6I_m - 300 + 3I_m + I_m}{60} = 0$$

$$\rightarrow \frac{10I_m - 300}{60} = 0$$

B. Consider



• kVL

$$\rightarrow \text{Consider } \frac{I_m - 50}{10} + \frac{I_m}{60} + \frac{I_m}{20 + 0.1} = 0$$

$$\frac{V_x}{10} - \frac{50}{10} + \frac{V_x}{60} + \frac{V_x}{20 + 0.1} = 0$$

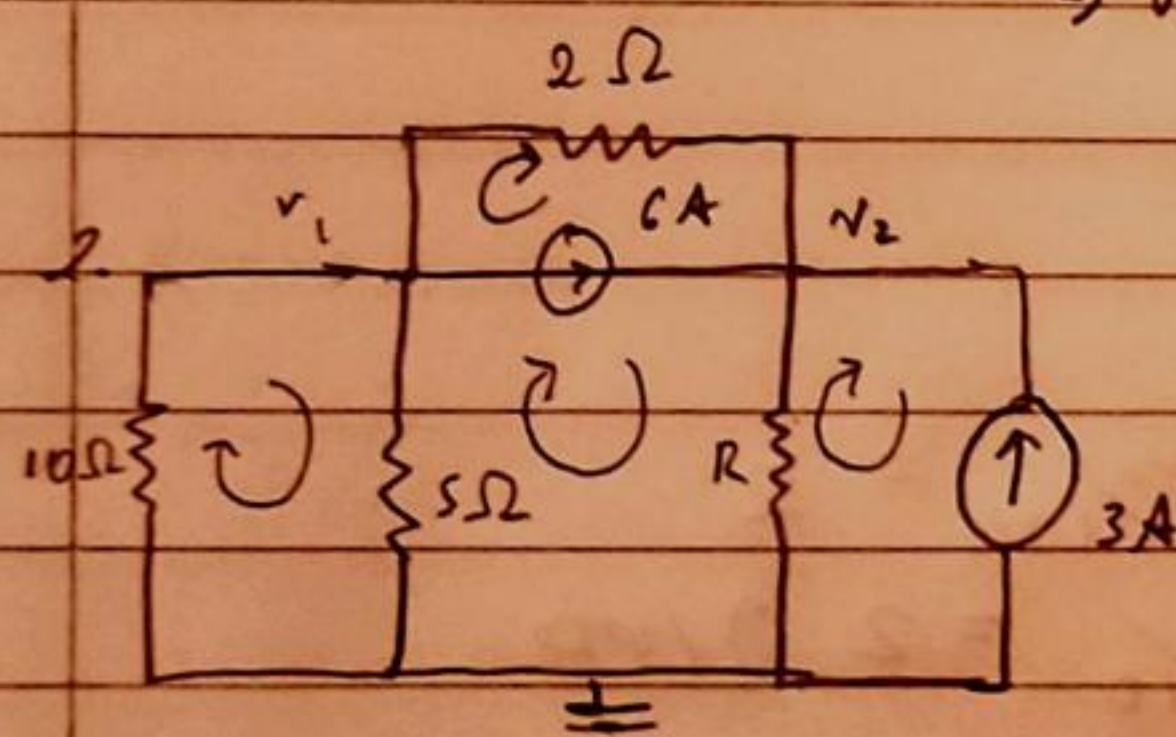
$$\rightarrow \left( \frac{V_x}{10} + \frac{10V_x}{60} + \frac{10V_x}{20.1} \right) = 50$$

$$\rightarrow V_x + \frac{1}{6} + \frac{100}{20.1} = 500$$

$$\rightarrow V_x + 0.16V_x + 4.97 = 500$$

$$\rightarrow 1.1635V_x = 500 = 300.5710V$$

$$\text{Consider } I = \frac{V_x}{20.1} = \frac{300.57}{20.1} = 14.95V$$



$$\text{I. kVL } \left( \frac{V_1}{10} + \frac{V_1}{5} + \frac{V_1 - V_2}{2} + 6 = 0 \right)$$

→

$$-V_1 + 2V_1 + 5V_1 - 5V_2 + 60 = 0$$

$$\rightarrow 8V_1 - 5V_2 + 60 = 0$$

$$\text{II. kVL } \left( \frac{V_2}{8} + \frac{V_2 - V_1}{2} = 3 + 6 \right)$$

$$\rightarrow V_2 + 4V_2 - 4V_1 = 72$$

$$\rightarrow 5V_2 - 4V_1 = 72$$

$$\text{III. } 8V_1 - 5V_2 + 60 = 72$$

$$4V_1 + 5V_2 + 0 = 0$$

$$4V_1 + 60 = 72 ; V_1 = 3V$$

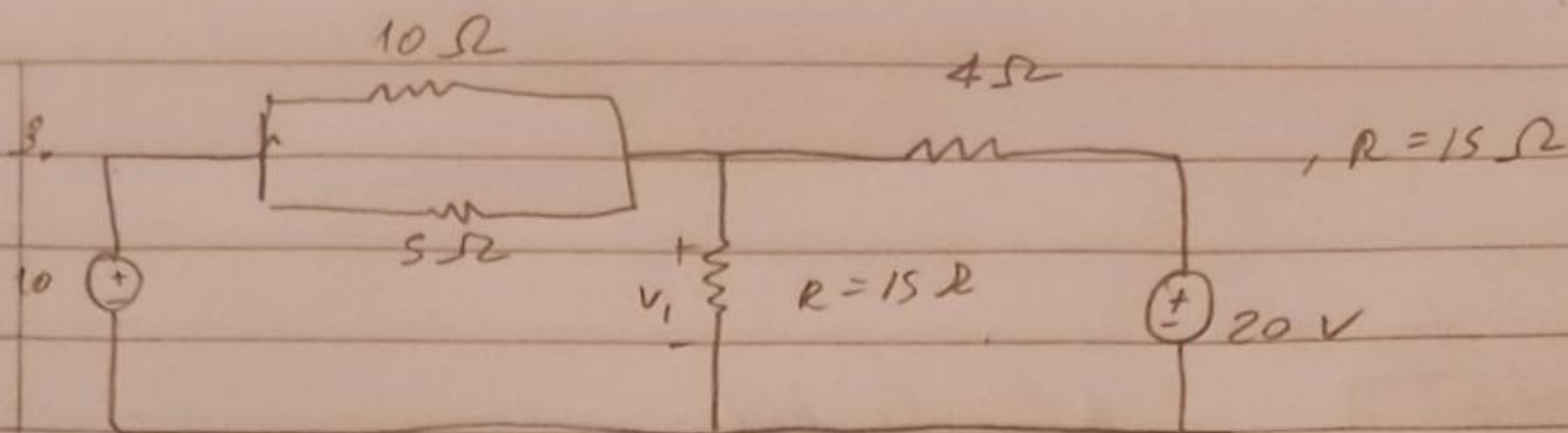
$$\rightarrow 5V_2 - 4(3) = 72$$

$$\rightarrow 5V_2 = 84$$

$$V_2 = \frac{84}{5} = 16.8$$

$$\text{Thus, } V_1 = 3V \text{ and } V_2 = 16.8V$$





$$1. \text{ KVL at } V_1: \frac{15(V_1 - 10)}{10 \parallel 5} + \frac{V_1 - 0}{4} + \frac{V_1 - 20}{15} = 0 \quad \text{KVL}$$

$$\Rightarrow \frac{15(V_1 - 10)}{50} + \frac{V_1}{4} + \frac{V_1 - 20}{15} = 0$$

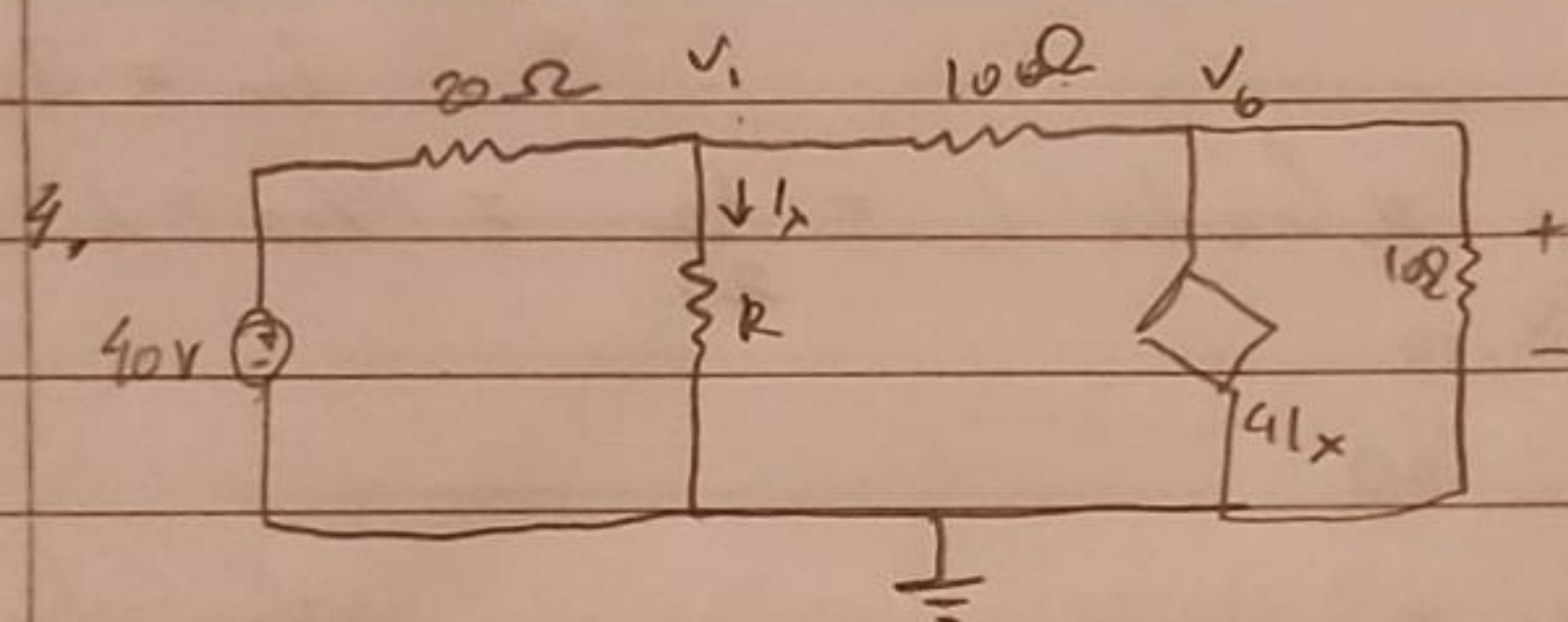
$$\Rightarrow \frac{15}{50} V_1 - 3 + \frac{V_1}{4} + \frac{V_1}{15} = 0$$

$$\Rightarrow \frac{3}{10} V_1 + \frac{V_1}{4} + \frac{V_1}{15} = 3$$

$$\Rightarrow V_1 \left( \frac{3}{10} + \frac{1}{15} + \frac{1}{4} \right) = 3$$

$$\Rightarrow V_1 \cdot \frac{37}{60} = 3$$

$$\Rightarrow V_1 = \frac{3 \cdot 60}{37} = 4.86 \text{ V}$$



1. KVL at  $V_1$

$$\Rightarrow \frac{V_1 - 40}{20} + \frac{V_1}{25} + \frac{V_1 - V_0}{100} = 0$$

$$\Rightarrow V_1 \left[ \frac{1}{20} + \frac{1}{25} + \frac{1}{100} \right] - \frac{V_0}{100} = 2$$

$$\Rightarrow \left( V_1 \left( \frac{19}{100} \right) - \frac{V_0}{100} = 2 \right) \cdot 100$$

$$\Rightarrow V_1 (19) - V_0 = 200$$

II. KVL at  $V_0$

$$\Rightarrow \frac{V_0 - V_1}{10} - 4I_x + \frac{V_0}{100} = 0$$

$$\Rightarrow \frac{V_0}{10} - \frac{V_1}{10} - 4 \left[ \frac{V_1}{25} \right] + \frac{V_0}{100} = 0$$

$$\text{III. } V(19) - 10(1.3V_1) = 200 \quad \Rightarrow \frac{V_0}{10} - \frac{V_1}{10} - 4 \frac{V_1}{25} + \frac{V_0}{100} = 0$$

$$\Rightarrow V_1 (19) - 13V_1 = 200$$

$$V_1 (6) = 200 = 33.3 \text{ V}$$

IV. V

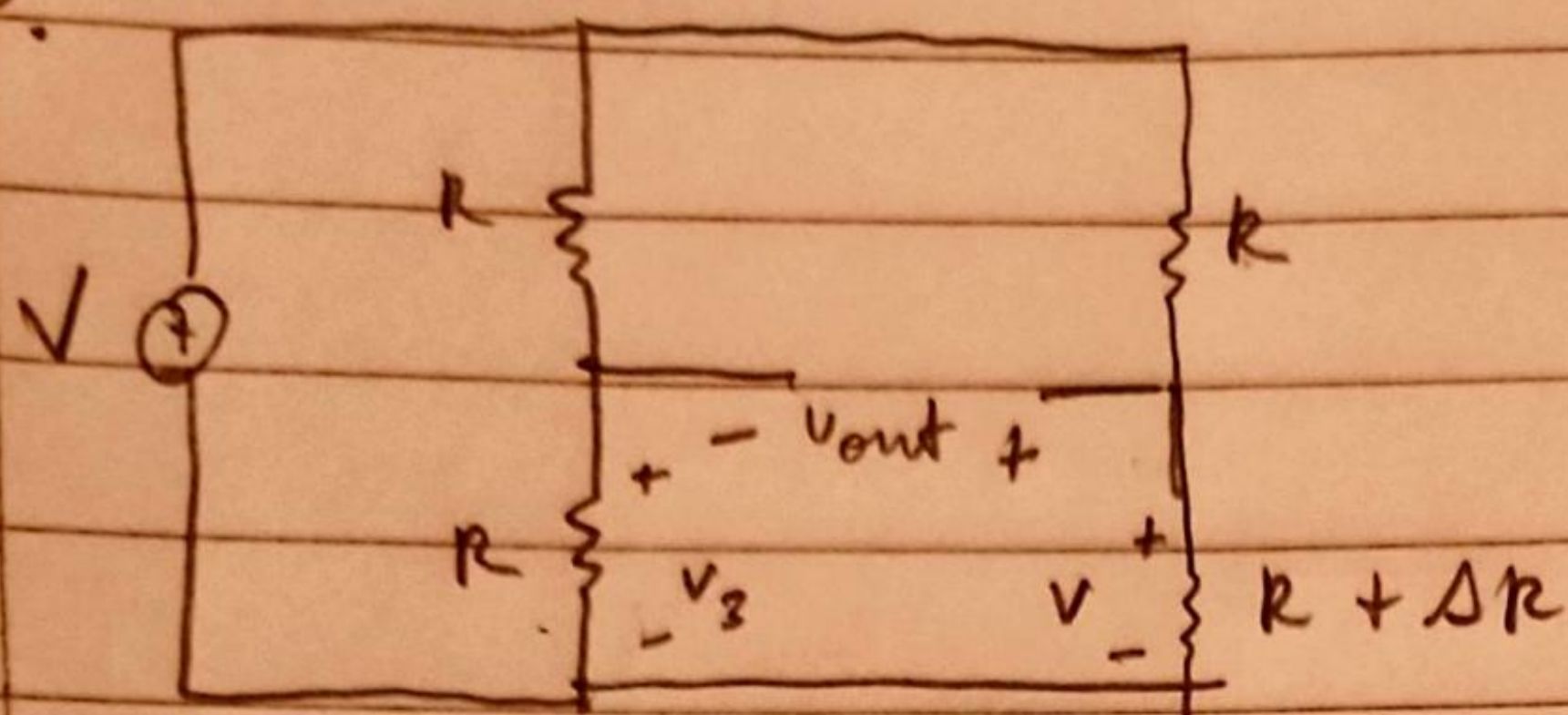
$$V_0 = 1.3(33.3) = V_0$$

$$\Rightarrow V_0 = 43.3 \text{ V}$$

$$V. i = \frac{V_1}{R} = \frac{33.3}{25} = 1.33 \text{ A}$$



5.



I. KVL in loop

$$\rightarrow -V_3 - V_{out} + V_x = 0$$

$$\rightarrow V_{out} = V_x - V_3$$

II. Consider division

$$a) V_x = V \left( \frac{R + \Delta R}{R + R + \Delta R} \right) = V \left( \frac{R + \Delta R}{2R + \Delta R} \right)$$

$$b) V_3 = V \left( \frac{R}{R + R} \right) = \frac{VR}{2R} = \frac{V}{2}$$

$$III. \text{ Thus, } V_{out} = V \left( \frac{R + \Delta R}{2R + \Delta R} \right) - \frac{V}{2}$$

$$\rightarrow V \left( \frac{R + \Delta R}{2R + \Delta R} - \frac{1}{2} \right) = V \left( \frac{2R + 2\Delta R - 2R - \Delta R}{2(2R + \Delta R)} \right)$$

$$\rightarrow \text{ Thus, } V_{out} = V \left[ \frac{\Delta R}{4R + \Delta R} \right] \checkmark$$