

$n = 5$  [Initial no. of buckets]

$b = 2$  [bucket capacity]

$bfs = 0.75$  [bucket fill factor]

$h_j(k) = k \bmod 2^j n$

Elements to insert into an empty hash table:-

200, 325, 405, 389, 188, 101, 500, 57, 82.  
120, 133, 48, 436, 461, 369, 223, 228, 199,  
123, 42, 23

Step	Inserted Key	Hash Function Used	Bucket Affected	Bucket Contents After Insert	Splitting Pointer (s)	Number of Buckets (N)	Average Load	Split Performed
1	200	$h_0(k) = k \bmod 5$ $h_0(k) = k \bmod 5$	0	0: [200]	0	5	0.2	No
2	325	$h_0(k) = k \bmod 5$ $h_0(k) = k \bmod 5$	0	0: [200, 325]	0	5	0.4	No
3	405	$h_0(k) = k \bmod 5$ $h_0(k) = k \bmod 5$	0	0: [200, 325, 405] (Overflow)	0	5	0.6	No
4	389	$h_0(k) = k \bmod 5$ $h_0(k) = k \bmod 5$	4	4: [389]	0	5	0.8	Yes (Split Bucket 0)
		$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	0, 5	0: [200], 5: [325, 405]	1	6	0.6667	
5	188	$h_0(k) = k \bmod 5$ $h_0(k) = k \bmod 5$	3	3: [188]	1	6	0.8333	Yes (Split Bucket 1)
		$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	1	1: Empty Bucket	2	7	0.7143	
6	101	$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	1	1: [101]	2	7	0.8571	Yes (Split Bucket 2)
		$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	2	2: Empty Bucket	3	8	0.75	
7	500	$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	0	0: [200, 500]	3	8	0.875	Yes (Split Bucket 3)
		$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	3, 8	3: Empty Bucket, 8: [188]	4	9	0.7778	
8	57	$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	7	7: [57]	4	9	0.8889	Yes (Split Bucket 4)
		$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	4, 9	4: Empty Bucket, 9: [389]	5	10	0.8	
9	82	$h_1(k) = k \bmod 10$ $h_1(k) = k \bmod 10$	2	2: [82]	5	10	0.9	Yes (Increment Level to $j=1$ )
		$h_2(k) = k \bmod 20$ $h_2(k) = k \bmod 20$	-	Level increased to 1, splitting pointer reset	0	10	0.9	

10	120	$h1(k)=k \bmod 10$	$h1(k)=k \bmod 10$	0	0: [200, 500, 120] ( <b>Overflow</b> )	0	10	<b>0.9</b>	Yes (Split Bucket 0)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	0, 10	0: [200, 120], 10: [500]	1	11	0.8182	
11	133	$h1(k)=k \bmod 10$	$h1(k)=k \bmod 10$	3	3: [133]	1	11	<b>0.9091</b>	Yes (Split Bucket 1)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	1, 11	<u>1: [101], 11: Empty Bucket</u>	2	12	0.8333	
12	48	$h1(k)=k \bmod 10$	$h1(k)=k \bmod 10$	8	8: [188, 48]	2	12	<b>0.9167</b>	Yes (Split Bucket 2)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	2, 12	<u>2: [82], 12: Empty Bucket</u>	3	13	0.8462	
13	436	$h1(k)=k \bmod 10$	$h1(k)=k \bmod 10$	6	6: [436]	3	13	<b>0.9231</b>	Yes (Split Bucket 3)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	3, 13	<u>3: Empty Bucket, 13: [133]</u>	4	14	0.8571	
14	461	$h1(k)=k \bmod 10$	$h1(k)=k \bmod 10$	1	1: [101, 461]	4	14	<b>0.9286</b>	Yes (Split Bucket 4)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	4	<u>4: Empty Bucket</u>	5	15	0.8667	
15	364	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	4	4: [364]	5	15	<b>1</b>	Yes (Split Bucket 5)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	5, 15	<u>5: [325, 405], 15: Empty Bucket</u>	6	16	0.9375	
16	223	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	3	3: [223]	6	16	<b>1</b>	Yes (Split Bucket 6)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	6, 16	<u>6: [436], 16: Empty Bucket</u>	7	17	0.9412	
17	228	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	8	8: [188, 48, 228] ( <b>Overflow</b> )	7	17	<b>1</b>	Yes (Split Bucket 7)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	7, 17	<u>7: [57], 17: Empty Bucket</u>	8	18	0.9444	
18	199	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	19	19: [199]	8	18	<b>1</b>	Yes (Split Bucket 8)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	8, 18	<u>8: [188, 48, 228], 18: Empty Bucket</u>	9	19	0.9474	
19	123	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	3	3: [223, 123] ( <b>Overflow</b> )	9	19	<b>1</b>	Yes (Split Bucket 9)
		$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	9, 19	9: [389], 19: [199]	10	20	0.95	
20	42	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	2	2: [82, 42]	10	20	<b>1</b>	Yes (Increment Level to j=2)
		$h3(k)=k \bmod 40$	$h3(k)=k \bmod 40$	-	<b>Level increased to 2, splitting pointer reset</b>	0	20	1	
21	23	$h2(k)=k \bmod 20$	$h2(k)=k \bmod 20$	3	3: [223, 123, 23] ( <b>Overflow</b> )	0	20	<b>1.05</b>	Yes (Split Bucket 0)
		$h3(k)=k \bmod 40$	$h3(k)=k \bmod 40$	0, 20	0: [200, 120], 20: [500]	1	21	1	

Final Hash table states :-

Bucket 0 :- [200, 120]

Bucket 1 :- [101, 461]

Bucket 2 :- [82, 42]

Bucket 3 :- [223, 123, 23] (**Overflow**)

Bucket 4 :- [364]

Bucket 5 :- [325, 405]

Bucket 5 : [2, 7, 10, 11]

Bucket 6 : [ ]

Bucket 7 : [ ]

" 8 :- [188, 48, 228] (overflow)

Bucket 9 : [389]

Bucket 10 : [ ]

Bucket 11 : [ ]

Bucket 12 : [ ]

Bucket 13 : [133]

Bucket 14 : [ ]

Bucket 15 : [ ]

Bucket 16 : [436]

Bucket 17 : [57]

Bucket 18 : []

Bucket 19 : [199]

Bucket 20 : [500]