

# Fys4150

## Project 4 Figures and stuff

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<https://github.com/kaaja/fys4150>

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4b

mcs	Eavg	absMavg	Cv	chi
100	-2.000000	1.000000	0.000000	0.000000
1000	-1.972000	0.991500	0.220864	0.022711
10000	-1.991000	0.996950	0.071676	0.009263
100000	-1.995180	0.998475	0.038467	0.004321
1000000	-1.995904	0.998634	0.032701	0.004093
10000000	-1.995942	0.998643	0.032401	0.004074

Table 1: Estimated quantities

mcs	Eavg	absMavg	Cv	chi
100	0.201300	0.134106	-100.000000	-100.000000
1000	-1.201518	-0.717034	588.428762	466.254675
10000	-0.249606	-0.171303	123.412688	130.949678
100000	-0.040185	-0.018598	19.901104	7.728200
1000000	-0.003912	-0.002677	1.928037	2.039441
10000000	-0.002028	-0.001736	0.994274	1.573251

Table 2: Percentage deviations from analytical results

1 4c

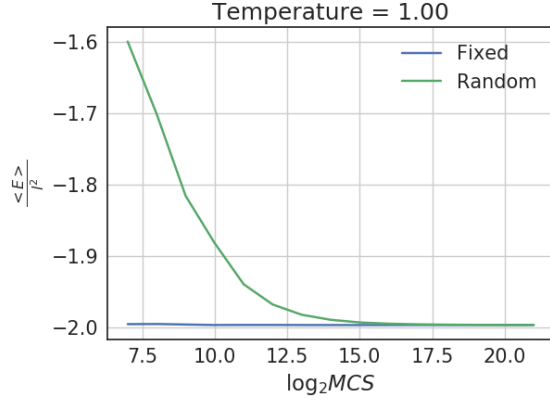


Figure 1: Expected Energy divided by  $L^2$ .  $T = 1.0$ .  
Equilibrium reached after  $2^{20}$  Monte Carlo cycles.

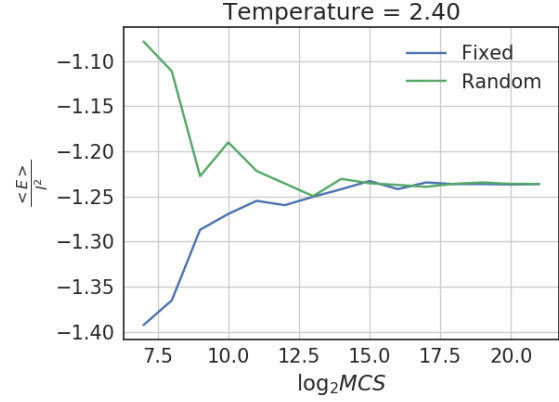


Figure 2: Expected Energy divided by  $L^2$ .  $T = 2.4$ .  
Equilibrium reached at same point as for  $T = 1$ .

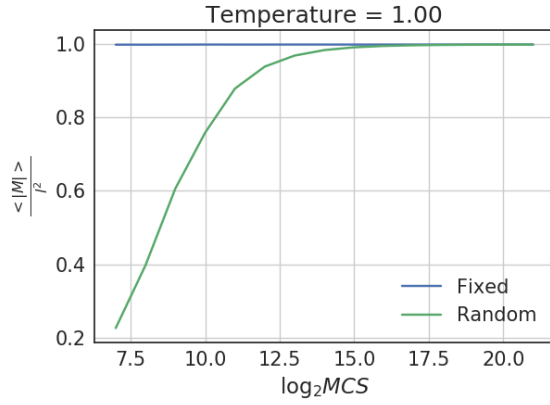


Figure 3: Expected absolute magnetic momentum divided by  $L^2$ .  $T = 1.0$ .  
Equilibrium reached at same point as for the energy.

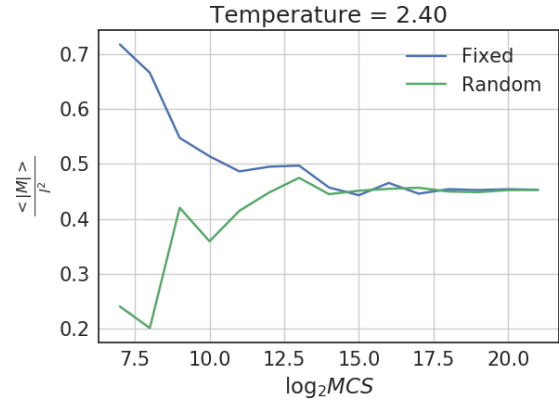


Figure 4: Expected absolute magnetic momentum divided by  $L^2$ .  $T = 2.4$ .  
Equilibrium reached at same point as for the others.

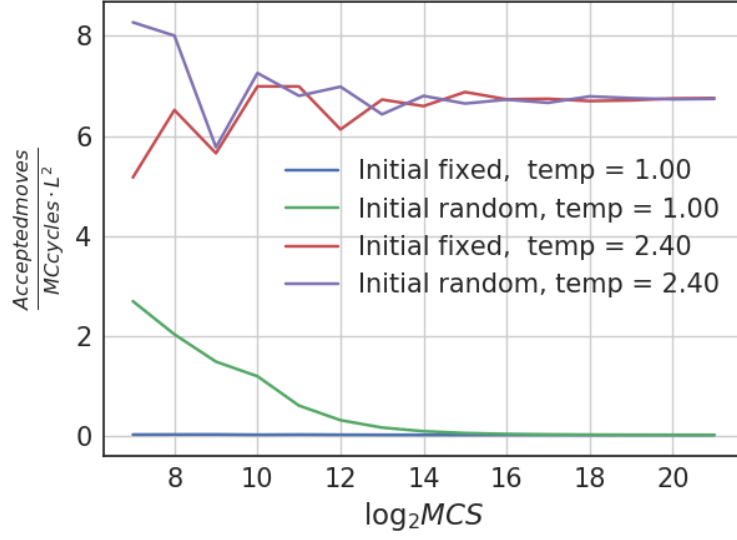


Figure 5: Accepted moved divided by  $L^2$ .

## 2 4d

$\log_2 MCS$	T	$\mu_E/L^2$	$\langle E \rangle / L^2$	$(\frac{\mu_E/L^2}{\langle E \rangle / L^2} - 1) \cdot 100$	$\sigma_E^2/L^2$	$\frac{\langle E^2 \rangle - \langle E \rangle^2}{L^2}$	$(\frac{\sigma_E^2/L^2}{1/L^2(\langle E^2 \rangle - \langle E \rangle^2)} - 1) \cdot 100$	$\langle  M  \rangle / L^2$	$\frac{\langle  M ^2 \rangle / L^2 - \langle  M  \rangle^2}{L^2}$	$Cv/L^2$	$\chi/L^2$
20.0	1.0	-1.997172	-1.997172	-8.152091e-07	0.023281	0.023281	1.080300e-06	0.999279	0.001560	0.023281	0.001560
20.0	2.4	-1.236940	-1.236940	3.699787e-06	8.185407	8.185407	-4.893184e-07	0.453954	21.269744	1.421077	8.862393

Table 3: Statistics. Fixed initial config.

$\log_2 MCS$	T	$\mu_E/L^2$	$\langle E \rangle / L^2$	$(\frac{\mu_E/L^2}{\langle E \rangle / L^2} - 1) \cdot 100$	$\sigma_E^2/L^2$	$\frac{\langle E^2 \rangle - \langle E \rangle^2}{L^2}$	$(\frac{\sigma_E^2/L^2}{1/L^2(\langle E^2 \rangle - \langle E \rangle^2)} - 1) \cdot 100$	$\langle  M  \rangle / L^2$	$\frac{\langle  M ^2 \rangle / L^2 - \langle  M  \rangle^2}{L^2}$	$Cv/L^2$	$\chi/L^2$
20.0	1.0	-1.997043	-1.997043	4.680687e-07	0.039074	0.039074	-3.837571e-07	0.999040	0.065137	0.039074	0.065137
20.0	2.4	-1.236217	-1.236217	2.899155e-06	8.114528	8.114527	3.297618e-07	0.452284	21.282545	1.408772	8.867727

Table 4: Statistics. Random initial config.

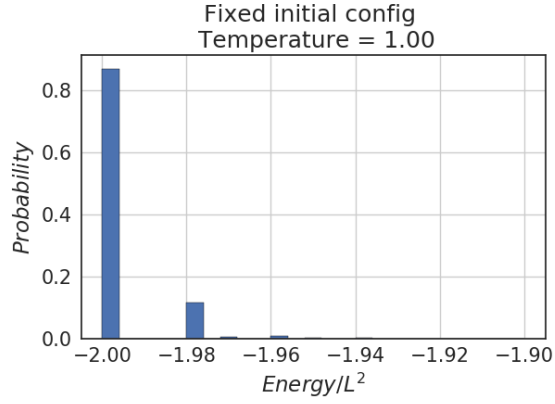


Figure 6: Probability distribution. Fixed initial  $T = 1$ .

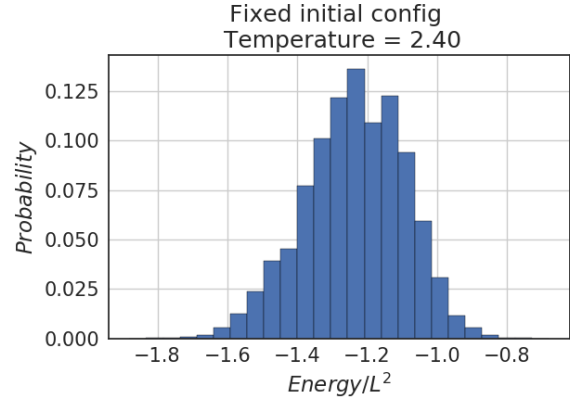


Figure 7: Probability distribution. Fixed initial  $T = 2.4$ .

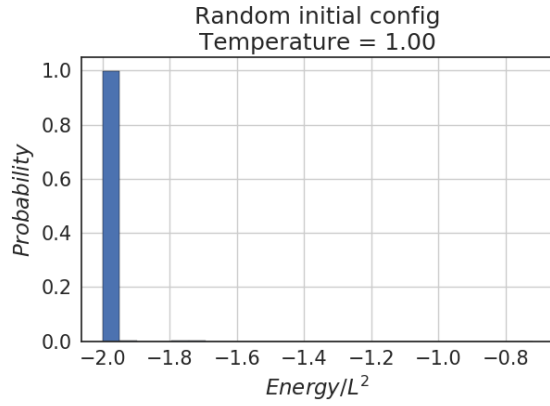


Figure 8: Probability distribution. Random initial  $T = 1$ .

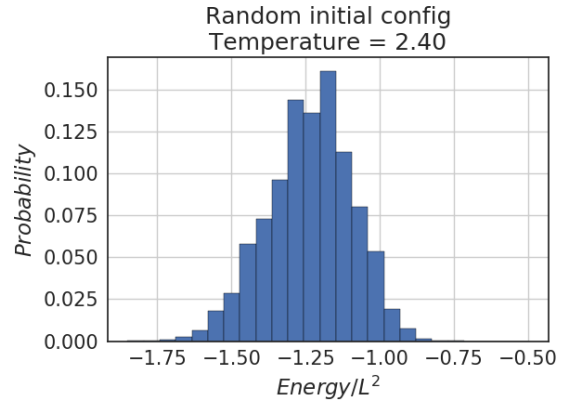


Figure 9: Probability distribution. Random initial  $T = 2.4$ .

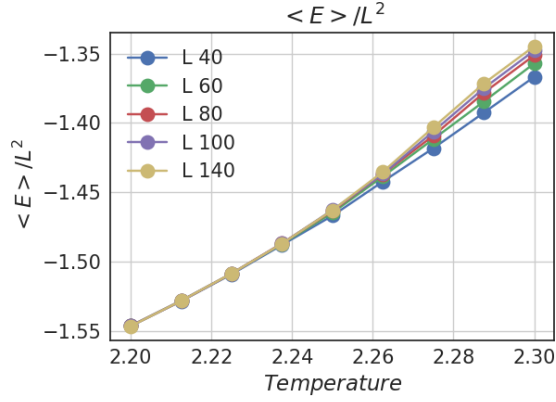


Figure 10: Expected value energy.

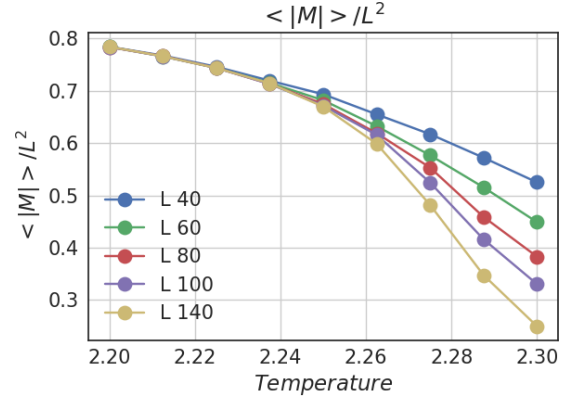


Figure 11: Expected value magnetic moment.

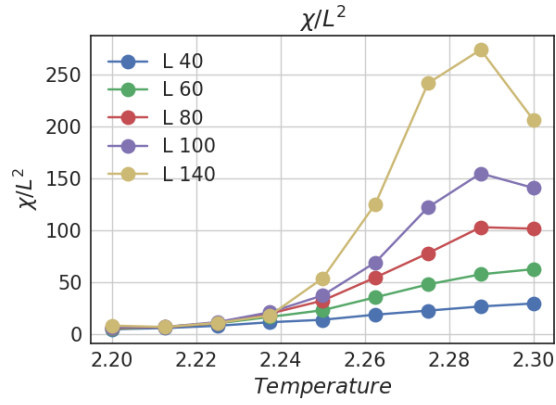


Figure 12: Susceptibility

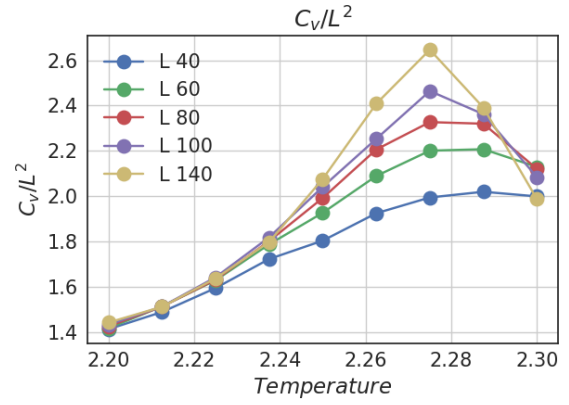


Figure 13: Specific heat capacity

Spin combos	$T_c^{Estimate}(L = \infty)$	$(\frac{T_c^{Estimate}(L=\infty)}{T_{c,exact}} - 1) \cdot 100$
[40, 60]	2.2875	0.80710401536
[40, 60, 100]	2.27916666667	0.439865020769
[40, 60, 100, 140]	2.27708333333	0.348055272121

Table 5: Estimated  $T_C$ .