Kaan Eren Yuwa Homework-2 090200348 1-) Let 5 be a parametized surface given by parametization & parametization all-rad coefficients of first fundamental and second fund. forms of the synthe 6) Fond the Gaussian and Mean curvalure of the surface s c) Fond umbilical points of S. all Determent hyperboles, ellepter, and paraboles posses of surface S. e) find the asymptotic lines a) = (-spauseny, cosustau, 0) , = (cosucos, spaucos, -spav) E= sint sint contestate = sint, G= costicost +sint cost +sint F=-SPAUSTAV COSU COSV + COSUSPAV SPAUCOSU = 0 ルースvxマー = マンママー = マリカレ Comsenv O 1 0 (-cosy sin2 ) CUSUCOSY STRUCESY -STRY [ -J ( STRT STRU) +16 STATUSTANCOSV - COSTUSTANCOSV) 2 x2= P(-cosusin2)-J(sin2vsinu)-k(senucosu) | | x | = | cost spor + = (sqn2 (sqn2+cbs2) = sqnv N= (-cosustav, -stavstav, -cosv) Zu= (-cosustav, + Staustav, 0), Zu= (-cosustav, -staustav, -cosu) Zu= (-5900 cosv, cosu cosv (0) e= 人力、えいラ= cos いとちかいちゃからかっちゃかか f= 2 D , Zuy > = cosus Prucosusenv - Spregnucosucusu = 0 g= < D, x v > = cos 2 sen 2 + seño sen 2 + cos 2 = 1

P) K= 68- 67 =100 (K= det (JDp) = k1. k2) Gauss corv. det(dDp) = det (011 012) = 011 022 - 012 021 H= -1 brace (d)p)=-1 (an 2022)=-1 [4F-e6 + FF-3E]
Mean
Coro. H= 1 ( gE -2f F +e6) = 1 (sent + sent) = 1 (2) = 1 e) If known at the popular popular prencipal curvatures hold the equation. 62-2HE+K=0 62-2 (Eg-2Ff +eG) 12+ eg- f2 = 0 (E6-F2) 12- (Eg-2FF+E6) 1 + (eg-f2)=6 5+12 12 + 25+12 / + 5+12 2U 12-21/1=0 |21=12=1 princepal corratures equal each d) since the Gaussian correture 12 of the surface 2(0,1) ps positive (K=1>0) then all points are elleptic. e) Tp=0=> e(Ju)2+2f dudv+9(dv)2=0 6902/W7+0V=0 ( ov ) = - senz Sou = - 5 dx u = - Scardy U=-(-Inlesev+cotv++c) U=Inlesev+cotv+c

2) \$(6, v) = (t+v, t-v, 464+t4) a) Show that the surface of Ps a ruled surface b) Fond the line of straction of the ruled surface ? a) Food the de trubbean parameter of 2. a) = (bw)=(t+v,t-v,46v+E+1 =(b, b, b+1) + V(1,-1, 4t) = 2(6) + v. 2(6) where 2(6) = (6,6,611) and ひ(t)=(1,-1, hb) This オ (hv) ps a foled surface generated by bre famely (a(t), ひ(も)) り〕は(も) = 文(も) - イン(カップは(も) We already know 2(6) (2(6) x'(E) = (1,1,1), 3'(E)=(0,0,4) 了(七)= 文(七) - とないでうる(七)= (七,七十1)+ 1(1,-1,46) < a', a'> B(E)=(E+ =, E-=, 12++1) =( (+ =) (-4) - (+-=) (4) +(2++1) 10) =-4E-1-4E+1=-8E 1 12= 16

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-63

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3) Let U= [(U,V) & R24 U>0, 0= V= 20 11 1, lal = 13 Let 5 and 5 be two parametrised surfaces, respectively given by だいしつらースし) 、ス(いい)=(ucosV, usqnv, 5) and えいいうらースト(い) \* (UN) = (aucos (\*), auso(\*), Ti-az u) Show that 5 and 5 are \$ = (cosv, senv, 0), \$v= (-usenv, ucosv, 0) E=1, F=0, G= 13802 + 12803 = 12 2 = (a cos(x), a sen(x), 101-02) = ( usen( ), ucos( ), 0) E= a2+1-a2=1, F=0, G= U3800(2)+02(cost(2)=0) Sence E=E\*=1, F=F\*=0, G=G\*= 12 then S and S are locally promotive. 4.) Let == 2(u,v) be a regular parametrized surface and assume that \$7 is Psothermal. Then proved that \$200 + \$200 = 2x2 + \$300 where \$2 = 2x2 + \$300 where Theorem let == = (u,v) be a parametrized surface and assume that = 95 9 sothernal. Then 200+200=2×H, H=HR Proof: By the realhermal parametritation イマン、マンフ = Cマン、マンフ ; イマン、マンマ=0 6 多くえいスレアニョンマスフ イマル、シットイマン、マル>= ムマレノ、メントイマン、マレン 2 < x2, , 2, >= 2 < x2, xy7 () F三と対し、元マニロ ることが、マントとない、マントとないでですこの Zマッ、マッキースマッスット コンズルナズルノズッ>=0 (3)

とえ、ス>=<え、ス> こくな、丸つこうとえなっ =>2とマルノス>=2とマンノストラの F= とえし、スマ=0 =7 2 と×リメンラ=0 とえいノスンフ=ーとえいえいフ From 4 and 5 => 4xuv, xu> = 47vv, 7v> = -4xu, xw> ∠Zuy +xv, Zy >=0 € From Zut Zv, Zu>=0 } and (zu, zu) ETp(s)

Zzu+ Zv, Zv>=0 } togent rectors. torgent rectors. Zu + Zu = M N for son fireton m H= 1 ( = G - 2FF + 9 E) and resolvermal parametrization
EG-F2 and F= G, F= 0 H= 1 (e+9) => ; by assumption G= <2, x>= x2 2 × 1+ = e+9 = とえい、ガフナとス、レ、ガラ = 2 2 m + 2 m , 2 > = M < 2, 2 > 2 x2 H=M Then 7w + 71= 2 12 HD 13

5.) Show that the cutenors given by the parametrization R(u,v)=(acosh cosu, cacosh spru, av), BEU = 2m, IVICOD PS
rsothermal and the catenord PS management A parametrized surface & To acilled Toothamal of E=G,F=O and the coordinate system luivius aqued Toothamal coordinates on S. xu = (-acoshusenu, acoshucosu, 0) Ry = (astato cosu, astato senu a) E= a2cosh2vsen2u+ a2cosh2v costv = a2cosh2v F= - a2 coshustahu staucosa + a2 cos mustahucusustau = 0 G = atsenhircostu + cisenhir seniv +ai = aisenhirai = ai (senhir1) = aicoshir E=G, F=O \$ 95 950 thermal. Xu = (- acoshveosu, -ercoshvepnu, 0) xvv = (acoshvcosu (acoshvsenu, O) XUU+XW= 0 If x (up) es harmones, then from the corollary \$ (u,v) es menind (ordlary ) Let \$(u,v) be rsothermal. Then , 7 as mineral of and only of the components of xiviz of \$(u,v) thre harmonia.