

# Reinforcement Learning Case Study

## Smart HVAC Control using Deep Reinforcement Learning

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## Abstract

Heating, Ventilation, and Air Conditioning (HVAC) systems account for a significant portion of building energy consumption, yet traditional control methods like thermostats and PID controllers often lack adaptability to dynamic conditions such as occupancy changes, leading to inefficiencies. To address this, the project developed a custom simulation environment modelling indoor temperature ( $15 - 30^{\circ}\text{C}$ ), humidity ( $20 - 70\%$ ), power usage, and variable occupancy, with a thermal comfort target of  $20 - 24^{\circ}\text{C}$ . Four reinforcement learning (RL) algorithms—Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN)—were implemented and trained to optimize HVAC control by balancing energy use and comfort through a reward function that penalizes power consumption and temperature deviations while rewarding comfort adherence. Agents selected from 27 possible action combinations (AC, heating, and ventilation modes). Evaluated against baselines (random, fixed-mode, thermostat, and PID controls), **DQN emerged as the top performer**, achieving the highest average reward (66.59), lowest power consumption (18.25W), and zero comfort violations—outperforming even PID and thermostat strategies. The results demonstrate that data-driven RL, particularly deep RL, can significantly enhance HVAC efficiency without compromising occupant comfort. The project recommends adopting DQN-based control in smart buildings and exploring integration with real-world sensor data, transfer learning, and multi-zone environments for future scalability.

## Introduction

### Background

Heating, Ventilation, and Air Conditioning (HVAC) systems play a vital role in maintaining indoor comfort and air quality across residential, commercial, and industrial buildings. However, HVAC systems are also among the largest energy consumers, accounting for nearly  $40 - 50\%$  of total building energy usage. Traditional HVAC control strategies — such as fixed thermostats or PID controllers — operate based on static, predefined rules that do not account for variations in occupancy, external conditions, or energy pricing. As a result, these systems often lead to inefficient energy utilization, inconsistent comfort levels, and increased operational costs.

With the growing demand for smart and sustainable buildings, there is a pressing need for intelligent HVAC control systems capable of learning and adapting dynamically. Reinforcement Learning (RL), a subfield of Artificial Intelligence (AI), offers a promising approach by enabling systems to learn optimal control strategies through continuous interaction with the environment.

### Purpose and Scope

This project aims to design, implement, and evaluate reinforcement learning-based HVAC control models that autonomously regulate temperature, humidity, and energy consumption. The scope includes developing a custom simulation environment, training multiple RL algorithms, and benchmarking their performance against traditional control methods.

### Objectives

- To simulate a realistic HVAC environment with variable occupancy and comfort constraints.
- To implement and train multiple RL algorithms — Q-Learning, SARSA, Monte Carlo, and DQN — for HVAC control.

- To compare the algorithms based on energy efficiency, comfort maintenance, and learning performance.
- To identify the most effective RL model and recommend future enhancements for real-world smart building applications.

## Literature Review

This section summarizes the state-of-the-art research in applying Reinforcement Learning to HVAC energy optimization, focusing on comparative studies, algorithmic advancements, and identified limitations, as detailed in Table II

No.	Citation	Main Idea / Model	Key Results	Research Gap / Limitation
1	<i>“An Experimental Evaluation of Deep Reinforcement Learning Algorithms for HVAC Control,”</i> ,(2024) <a href="#">arXiv</a> ,	Compared multiple DRL algorithms (e.g., DQN, SAC, TD3) in HVAC environments using Sinergym.	DRL methods achieved strong comfort-energy trade-offs in simulation.	Limited generalization to different building types and environments.
2	<i>Comparative Study of Model-Based and Model-Free RL Control Performance in HVAC Systems</i> (2023), <a href="#">ScienceDirect</a>	Compared model-based and model-free RL for HVAC performance and sample efficiency.	Model-based RL learns faster; model-free yields higher accuracy when models are uncertain.	Real-world validation and scalability remain limited.
3	<i>Intelligent Multi-Zone Residential HVAC Control via Deep RL</i> , <a href="#">Applied Energy</a> , 2021,	Implemented DDPG, DQN, and Q-Learning for multi-zone residential HVAC control.	Achieved 15% reduction in energy cost and improved comfort stability.	High computational cost and training complexity.
4	<i>Deep Q-Network Boosted with External Knowledge for HVAC Control</i> , <a href="#">ACM</a> , 2022	Integrated domain knowledge with DQN (hybrid approach) for improved stability.	Hybrid model outperformed plain DQN in comfort and energy control.	Requires expert-defined rules; less flexible in unseen environments.
5	<i>Wang et al. (2023), “A Comparison of Classical and Deep RL Methods for HVAC Control,”</i> <a href="#">arXiv</a> ,	Benchmarked classical RL (Q-Learning) vs. deep RL (DQN) in HVAC simulation.	Deep RL outperformed classical methods but was sensitive to tuning.	Lack of long-term stability analysis and exploration strategies.
6	<i>Energy-Efficient Control of Thermal Comfort in Multi-Zone HVAC via RL</i> , <a href="#">Taylor &amp; Francis</a> , 2022,	Combined comfort prediction model with Q-Learning, DQN, and DDPG.	DDPG with comfort model achieved best comfort-energy trade-off.	Requires accurate comfort modeling and retraining for new climates.
7	<i>Bayer &amp; Pruckner (2023), “Enhancing Multi-Agent RL for HVAC Systems,”</i> <a href="#">arXiv</a> ,	Multi-agent RL for distributed HVAC control with parameter sharing.	Reduced energy use by 6–8% compared to rule-based control.	Coordination among agents remains complex and unstable.

Table 1: Summary of Related Research on Reinforcement Learning for HVAC Energy Optimization

## Case Study

This case study focuses on designing an energy-efficient and adaptive HVAC control system using Reinforcement Learning (RL) algorithms to optimize both comfort and power consumption. HVAC systems are critical in maintaining indoor temperature, humidity, and air quality in residential and commercial buildings. However, conventional control approaches—such as thermostats or PID-based methods—operate on predefined rules without accounting for dynamic occupancy patterns or environmental variations. As a result, they often consume excessive energy and fail to sustain consistent comfort levels.

### Environment Description

To overcome these limitations, a custom HVAC simulation environment was developed in Python to replicate realistic building conditions. The environment models the interactions among temperature (15 – 30°C), humidity (20 – 70%), occupancy levels (low, medium, high), and power consumption (in watts). It includes operational modes for air conditioning (AC), heating, and ventilation, each with three intensity levels — Eco, Balanced, and High Performance. The target comfort temperature is fixed at 22°C, with an acceptable range of 20 – 24°C to represent typical human comfort boundaries.

Each RL agent (Q-Learning, SARSA, Monte Carlo, and DQN) interacts with this simulated environment, selecting optimal combinations of HVAC modes at every time step. The system transitions to new states based on these actions, reflecting changes in temperature, humidity, and power usage. A crucial component of this setup is the reward function, which quantitatively guides learning by balancing comfort and energy efficiency. The reward at each step is computed as:

$$R_t = -|T - T_{\text{set}}| - \frac{P}{100} + C$$

where:

- $T$ : is the current temperature,
- $T_{\text{set}}$ : is the setpoint temperature (22°C),
- $P$ : is the current power consumption in watts, and
- $C$ : is a comfort bonus (+1 when temperature is within 20 – 24°C,  $-2$  otherwise).

This formulation encourages the agent to minimize deviations from the comfort zone while penalizing high power consumption. Over multiple training episodes, the RL agents learn to make decisions that maintain thermal comfort efficiently and adaptively.

The data used in this study is synthetically generated by the simulation environment, allowing full control over variability and reproducibility. This enables a robust comparison of different RL algorithms in a controlled yet realistic scenario. The case thereby demonstrates how RL can form the foundation of intelligent, self-learning HVAC systems for smart and sustainable buildings.

### Problem Identification

Heating, Ventilation, and Air Conditioning (HVAC) systems account for a significant portion of total building energy consumption — typically 40% to 50% in commercial and residential buildings according to reports by the U.S. Department of Energy (DOE, 2023). Despite their importance in ensuring occupant comfort, traditional HVAC control strategies are inefficient and inflexible, relying on static temperature setpoints or manually tuned PID controllers. These systems are unable to dynamically adapt to fluctuating occupancy levels, weather conditions, and energy costs, which results in excessive energy waste, unstable thermal comfort, and higher operational expenses.

The core challenge in modern building energy management lies in the inefficiency and inflexibility of conventional HVAC control systems. Traditional approaches—such as rule-based thermostats or PID controllers—operate on static setpoints and pre-defined logic, making them unable to respond intelligently to dynamic environmental and occupancy conditions. This results in two critical issues:

- **Excessive energy consumption:** HVAC systems often over-cool or over-heat spaces due to lack of real-time adaptation, leading to significant energy waste. According to the U.S. Department of Energy, HVAC accounts for 40 – 60% of total building electricity use, with up to 30% of that energy wasted due to inefficient control and operation.

- **Suboptimal thermal comfort:** Fixed control strategies fail to maintain consistent indoor conditions when occupancy or external weather changes. For instance, a thermostat set to 22°C may keep the temperature stable but ignore humidity swings or sudden occupancy surges, causing discomfort even when temperature is within range.

In the academic domain, Reinforcement Learning (RL) has emerged as a promising paradigm to address these challenges. RL enables agents to learn optimal control strategies through continuous interaction with the environment, balancing energy efficiency and comfort autonomously. However, many existing studies focus only on deep reinforcement learning (e.g., DDPG or SAC), overlooking simpler, interpretable algorithms like Q-Learning or SARSA. Moreover, few comparative studies benchmark multiple RL algorithms under a consistent HVAC simulation framework.

## Methodology

This study adopts a quantitative, simulation-based approach utilizing **Reinforcement Learning (RL)** to develop an adaptive HVAC control system that balances comfort and energy efficiency. The methodology involves the creation of a custom HVAC simulation environment and the implementation of four RL algorithms — Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN) — to learn optimal control policies.

### Environment Design

The HVAC environment was designed as a custom simulation model using Python to replicate realistic indoor climate behavior. The simulation captures interactions among temperature (15–30°C), humidity (20–70%), occupancy level (low, medium, high), and power consumption. Each state  $S_t = (T, H, O)$ , represents the indoor conditions at time  $t$ , and the agent selects an action  $A_t$  consisting of operational modes for air conditioning, heating, and ventilation. Each mode can operate in three levels — Eco, Balanced, and High Performance — resulting in 27 possible action combinations.

The environment updates state transitions based on the selected action and physical dynamics such as cooling or heating rates. The reward function balances comfort and energy efficiency, rewarding conditions within the comfort zone (20–24°C) and penalizing temperature deviation and excessive power use.

A custom environment was chosen to:

1. Maintain full control over state variables (temperature, humidity, occupancy, power) and reward logic, enabling precise alignment with project objectives.
2. Ensure reproducibility and simplicity, avoiding the complexity and computational overhead of high-fidelity building simulators, which are unnecessary for algorithm comparison at this scale.
3. Facilitate rapid prototyping of multiple RL agents under identical conditions, allowing fair performance benchmarking.

The environment supports discrete state-action spaces, making it suitable for both tabular (Q-Learning, SARSA, Monte Carlo) and deep (DQN) RL methods. Its modular design also allows future extension to multi-zone or continuous-control scenarios.

## Reinforcement Learning Framework

At each time step  $t$ , the agent selects an action  $A_t$  according to a policy  $\pi$ , observes the new state  $S_{t+1}$ , and receives a reward  $R_t$  defined as:

$$R_t = -|T - T_{\text{set}}| - \frac{P}{100} + C$$

where  $C = +1$  if  $T \in [20, 24]$  and  $C = -2$  otherwise.

The goal is to maximize the cumulative discounted reward:

$$G_t = \sum_{k=0}^{\infty} \gamma^k R_{t+k+1}$$

where  $\gamma$  is the discount factor (0.9–0.99).

# Algorithms Implemented

This project implements and compares four fundamental reinforcement learning algorithms for energy-efficient HVAC control: **Q-Learning**, **SARSA**, **Monte Carlo Control**, and **Deep Q-Network (DQN)**. The implementation uses Python with NumPy for numerical computation and Matplotlib for visualization.

## 1. Q-Learning (Off-Policy TD Control)

Q-Learning, introduced by Watkins (1989), is a model-free, off-policy temporal-difference control algorithm. It learns the optimal action-value function  $Q^*(s, a)$  that represents the expected cumulative reward for taking action  $a$  in state  $s$  and following the optimal policy thereafter.

### Key Characteristics

- **Off-Policy Learning:** Q-Learning learns the optimal policy while following a different exploratory policy (typically  $\varepsilon$ -greedy). This separation between behavior policy and target policy enables more efficient exploration.
- **Temporal Difference (TD):** Updates estimates based on other estimates (bootstrapping) rather than waiting for final outcomes. This allows learning from incomplete episodes.
- **Convergence Guarantee:** Under certain conditions (all state-action pairs visited infinitely, appropriate learning rate decay), Q-Learning provably converges to the optimal Q-function.

### Mathematical Foundation

Q-Learning is a model-free, off-policy temporal difference algorithm that learns the optimal action-value function:

#### Update Rule:

$$Q(s, a) \leftarrow Q(s, a) + \alpha \left[ r + \gamma \max_{a'} Q(s', a') - Q(s, a) \right]$$

#### Where:

- $Q(s, a)$ : Action-value function for state  $s$  and action  $a$
- $\alpha$ : Learning rate (0.05)
- $\gamma$ : Discount factor (0.99)
- $r$ : Immediate reward
- $s'$ : Next state
- $\max_{a'} Q(s', a')$ : Maximum Q-value over all actions in next state (off-policy)

### Design Steps

- **State Discretization:** The real-world inputs (like temperature, humidity, etc.) are continuous, so we divide each into fixed ranges (or "bins") to turn them into manageable, discrete states. This creates about 49,500 possible states.
- **Action Space:** The system can control the AC, heater, and fan—each with 3 settings (e.g., off/low/high). All combinations give  $3 \times 3 \times 3 = 27$  possible actions.
- **Exploration Strategy:** The agent mostly picks the best-known action but sometimes tries random ones to explore. It starts with full randomness ( $\varepsilon = 1.0$ ) and gradually becomes more greedy, settling at 1% randomness ( $\varepsilon_{\min} = 0.01$ ).
- **Q-Table:** A big lookup table (5D: 4 for state + 1 for action) stores the expected reward for every state-action pair. The agent updates this table as it learns.

**Q-Learning was selected because:**

- Guaranteed convergence to optimal policy under appropriate conditions
- Off-policy learning allows more efficient exploration
- Well-suited for environments with delayed rewards
- Computationally efficient for discretized spaces

## 2. SARSA (On-Policy TD Control)

SARSA, developed by Rummery and Niranjan (1994), is a model-free, on-policy temporal-difference algorithm. Unlike Q-Learning, it learns the value of the policy being executed rather than the optimal policy.

### Key Characteristics

- **On-Policy Learning:** SARSA updates Q-values based on the action  $a'$  actually taken by the current policy. The update uses the quintuple  $(s_t, a_t, r_{t+1}, s_{t+1}, a_{t+1})$ , hence the acronym.
- **Conservative Behavior:** Because SARSA considers the exploration risk in its updates, it tends to learn more cautious policies, especially in environments with negative consequences for exploratory actions.
- **Policy Consistency:** The learned Q-function accurately reflects the value of the  $\varepsilon$ -greedy policy being followed, not necessarily the optimal policy.

### Mathematical Foundation

SARSA learns the action-value function for the policy being followed:

**Update Rule:**

$$Q(s, a) \leftarrow Q(s, a) + \alpha [r + \gamma Q(s', a') - Q(s, a)]$$

Key difference: Uses actual next action  $a'$  taken by the policy (on-policy), not the maximum.

### Design Steps

- **Action Selection:** At each step, the agent picks an action using its current policy (like  $\varepsilon$ -greedy), and also selects the next action  $a'$  before updating—because SARSA needs to know what it actually did next to complete the update quintuple  $(s, a, r, s', a')$ .
- **Policy Evaluation:** Instead of learning the best possible actions (like Q-Learning), SARSA learns how good its current behavior (e.g.,  $\varepsilon$ -greedy) really is—including its random explorations (on-policy learning).
- **Hyperparameters:** Uses a learning rate ( $\alpha = 0.1$ ), discount factor ( $\gamma = 0.95$ ), and gradually reduces randomness ( $\varepsilon$  decays by 0.995 each step).
- **State Representation:** Uses the same state discretization as Q-Learning (temperature, humidity, etc., split into bins) so the two methods can be fairly compared.

**SARSA was included to:**

- Compare on-policy vs off-policy learning performance
- Evaluate conservative behavior (considers exploration risk)
- Assess performance in safety-critical HVAC scenarios where exploration penalties matter

## 3. Monte Carlo Control (Episode-Based Learning)

Monte Carlo (MC) methods learn from complete episodes of experience without bootstrapping. Introduced to RL by Barto and Duff (1994), these methods use actual returns (cumulative rewards) rather than estimates of returns.

## Key Characteristics

- **Episode-Based Learning:** MC methods require complete trajectories from start to terminal state. Updates occur only after episode completion using actual observed returns.
- **Unbiased Estimates:** Because MC uses actual returns rather than bootstrapped estimates, it provides unbiased value estimates (though with higher variance).
- **No Bootstrapping:** MC doesn't rely on value estimates of successor states, making it less sensitive to initialization and potentially more stable.

## Mathematical Foundation

Monte Carlo methods learn from complete episode experiences using actual returns:

### First-Visit MC Update:

$$G_t = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1} \quad (\text{return from time } t)$$
$$Q(s, a) \leftarrow \text{average}(\text{Returns}(s, a))$$

Where  $G_t$  is the cumulative discounted return following first visit to state-action pair.

## Design Steps

- **Episode Collection:** The agent runs a full episode—from start to finish—and records every step: states ( $s_t$ ), actions ( $a_t$ ), and rewards ( $r_{t+1}$ ). The complete trajectory  $(s_0, a_0, r_1, s_1, a_1, r_2, \dots, s_T)$  is stored.
- **Return Calculation:** After the episode ends, it calculates the total discounted reward (called the "return,"  $G_t$ ) from each step backward to the start:  $G_t = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$ .
- **First-Visit Update:** For each state-action pair  $(s, a)$ , it only uses the return from the **first time** that pair appears in the episode to update its value estimate.
- **Incremental Averaging:** It keeps a running average of all returns seen so far for each state-action pair, which serves as the updated Q-value estimate,  $Q(s, a) \leftarrow \text{average}(\text{Returns}(s, a))$ .

## Monte Carlo was implemented because:

- Model-free and does not require bootstrapping
- Provides unbiased estimates of action values
- Effective for episodic tasks with clear termination
- Useful baseline for comparing TD methods

## 4. Deep Q-Network (DQN)

DQN, introduced by Mnih et al. (2015) at DeepMind, revolutionized RL by successfully combining deep neural networks with Q-Learning. It uses function approximation to handle high-dimensional state spaces that are intractable for tabular methods.

## Key Characteristics

- **Function Approximation:** Replaces Q-table with a neural network  $Q(s, a; \theta)$  parameterized by weights  $\theta$ . This enables generalization across similar states and handles continuous/high-dimensional inputs.
- **Experience Replay:** Stores transitions in a replay buffer and samples random minibatches for training. This breaks temporal correlations between consecutive samples, improving stability and data efficiency.



- **Target Network:** Maintains a separate network with frozen parameters  $\theta^-$  for computing TD targets. Updated periodically (e.g., every  $N$  steps) to reduce correlations between target and predicted Q-values, stabilizing training.
- **Deep Learning Integration:** Leverages automatic feature extraction through multiple hidden layers, eliminating need for manual feature engineering.

## Mathematical Foundation

DQN approximates the Q-function using a neural network with experience replay:

**Loss Function:**

$$L(\theta) = E \left[ \left( r + \gamma \max_{a'} Q(s', a'; \theta^-) - Q(s, a; \theta) \right)^2 \right]$$

**Where:**

- $\theta$ : Primary network parameters
- $\theta^-$ : Target network parameters (periodically updated)
- **Experience replay buffer** breaks temporal correlation

## Network Architecture

- **Input Layer:** 4 neurons (normalized state features)
- **Hidden Layer 1:** 64 neurons + ReLU activation
- **Hidden Layer 2:** 64 neurons + ReLU activation
- **Output Layer:** 27 neurons (Q-values for each action)

## Design Steps

- **State Preprocessing:** Raw inputs (temperature, humidity, power, occupancy) are normalized to a 0 – 1 range so the neural network can learn effectively.
- **Neural Network as Q-Function:** Instead of a giant Q-table, DQN uses a deep neural network (2 hidden layers, 64 neurons each) to estimate Q-values for all 27 actions directly from the state.
- **Experience Replay:** Past experiences (state, action, reward, next state) are stored in a replay buffer. The agent randomly samples small batches (e.g., 32 at a time) to train on—this reduces learning instability from correlated data.
- **Target Network:** A second, slower-updating network is used to calculate target Q-values. It's updated only every 10 training steps, making learning more stable by preventing rapid feedback loops.
- **Training:** The network is trained using gradient descent to minimize the difference between predicted Q-values and target values (based on actual rewards and future estimates).

**DQN was chosen because:**

- Handles continuous state spaces without manual discretization
- Scales to high-dimensional problems
- Experience replay improves sample efficiency
- Target network stabilizes training
- State-of-the-art performance in complex control tasks

# Analysis & Discussion

## 1. Experimental Setup and Methodology

### 1.1 Environment Configuration

We evaluate all reinforcement learning (RL) algorithms in a simulated Heating, Ventilation, and Air Conditioning (HVAC) control environment that incorporates realistic operational and comfort constraints. The environment is fully observable and Markovian, with the following state and action spaces:

**State Space.** The state vector  $\mathbf{s} \in \mathbb{R}^4$  comprises four continuous or discrete variables:

- **Temperature:**  $T \in [15, 30]^\circ\text{C}$ , with a user-defined setpoint of  $22^\circ\text{C}$  and a comfort zone of  $[20, 24]^\circ\text{C}$ .
- **Relative Humidity:**  $H \in [20, 70]\%$ .
- **Power Consumption:**  $P \in [0, 50] \text{ W}$ .
- **Occupancy Level:** Discrete variable  $O \in \{0, 1, 2\}$ , representing low, medium, and high occupancy, respectively.

**Action Space.** The agent selects from 27 discrete actions, corresponding to all combinations of three control modes:

- **AC Mode:** Eco ( $-0.5^\circ\text{C}$ , 5 W), Balanced ( $-1.0^\circ\text{C}$ , 10 W), High Performance ( $-1.5^\circ\text{C}$ , 15 W).
- **Heating Mode:** Eco ( $+0.5^\circ\text{C}$ , 5 W), Balanced ( $+1.0^\circ\text{C}$ , 10 W), High Performance ( $+1.5^\circ\text{C}$ , 15 W).
- **Ventilation Mode:** Three intensity levels (low, medium, high), each influencing humidity reduction and additional power draw.

**Reward Function.** At each timestep, the agent receives a scalar reward designed to balance thermal comfort, energy efficiency, and occupant satisfaction:

$$R = -|T_{\text{current}} - T_{\text{setpoint}}| - \frac{P_{\text{watts}}}{100} + B_{\text{comfort}}$$

where

$$B_{\text{comfort}} = \begin{cases} +1.0 & \text{if } 20^\circ\text{C} \leq T_{\text{current}} \leq 24^\circ\text{C}, \\ -2.0 & \text{otherwise.} \end{cases}$$

This multi-objective formulation prioritizes temperature regulation while penalizing excessive energy use and strongly rewarding operation within the human comfort zone.

### 1.2 Training Protocol

All algorithms were trained and evaluated under identical conditions to ensure fair comparison:

- **Training Duration:** 20,000 episodes (5,000 episodes for preliminary hyperparameter validation).
- **Episode Length:** 100 timesteps per episode.
- **Evaluation Protocol:** Final performance assessed over 100 independent episodes using a greedy policy ( $\epsilon = 0$ ) to measure pure exploitation capability.
- **Reproducibility:** A fixed random seed (42) was used across all experiments.
- **Hyperparameter Optimization:** A grid search was conducted for tabular methods; the optimal configuration for Q-Learning was identified as learning rate  $\alpha = 0.05$ , discount factor  $\gamma = 0.99$ , and epsilon decay rate 0.9995 (with  $\epsilon_{\min} = 0.01$ ).

For deep RL (DQN), state inputs were normalized to the  $[0, 1]$  range using:

$$\begin{aligned} T_{\text{norm}} &= \frac{T - 15}{15} \\ H_{\text{norm}} &= \frac{H - 20}{50} \\ P_{\text{norm}} &= \frac{P}{50} \\ O_{\text{norm}} &= \frac{O}{2} \end{aligned}$$

This standardized setup enables rigorous comparison across tabular (Q-Learning, SARSA, Monte Carlo) and function approximation-based (DQN) approaches in a realistic building energy management context.

## 2. Performance Analysis

### 2.1 Training Convergence

All algorithms were trained for 20,000 episodes under identical conditions. Performance was evaluated using the average cumulative reward over the last 100 training episodes. Key results are summarized in Table 2.

Table 2: RL Algorithm Training Convergence Results (20,000 Episodes)

Algorithm	Final Avg. Reward ( $\pm$ std)	Convergence Episode	Training Time	Final $\varepsilon$
DQN	$66.59 \pm 0.00$	$\sim 5,000$	Highest	0.01
Q-Learning	$\sim 45.00$	$\sim 8,000$	Low	0.01
SARSA	$\sim 40.00$	$\sim 10,000$	Low	0.01
Monte Carlo	$\sim 35.00$	$\sim 12,000$	Medium	0.01

#### Analysis.

- DQN achieves a **48% higher** final reward than Q-Learning—the next best performer—due to its ability to operate in the original continuous state space without discretization loss, leverage experience replay for improved sample efficiency, and generalize across states via deep function approximation.
- Q-Learning outperforms SARSA, consistent with theoretical expectations: its off-policy nature enables more aggressive exploration and faster convergence to the optimal policy, whereas SARSA’s on-policy updates incorporate exploration risk, yielding more conservative (and suboptimal) behavior.
- Monte Carlo exhibits the slowest convergence, as it requires full episode completions before any update can occur. The 100-step episode length amplifies this limitation, resulting in high-variance returns and delayed learning.
- Critically, all methods converge to stable policies, confirming correct implementation and suitability for the task.

### 2.2 Temperature Control Accuracy

Temperature regulation performance was assessed over 100 evaluation episodes using a greedy policy ( $\varepsilon = 0$ ). The performance of the RL algorithms is shown in Table 3.

#### Analysis.

- DQN achieves near-ideal setpoint tracking with only a  **$0.05^\circ\text{C}$  bias**, demonstrating superior control precision.

Table 3: Temperature Control Accuracy at Setpoint (22.00°C)

Algorithm	Mean Temp (°C)	Std Dev (°C)	Deviation from Setpoint (°C)
Target	22.00	—	0.00
DQN	21.95	0.85	−0.05
Q-Learning	22.15	1.20	+0.15
SARSA	22.35	1.45	+0.35
Monte Carlo	22.50	1.80	+0.50

- Performance degrades progressively across tabular methods, reflecting the limitations of coarse state discretization ( $30 \times 50 \times 11 \times 3$  bins), which impedes fine-grained decision-making.
- The increasing standard deviation—from DQN (0.85°C) to Monte Carlo (1.80°C)—indicates declining control stability with simpler algorithms.
- Nevertheless, all methods maintain temperatures within the comfort zone (20 – 24°C), satisfying basic safety and usability requirements.

### 2.3 Energy Efficiency

Energy consumption was measured as average power draw per timestep and total energy per episode (100 steps = 100 s, assuming 1 s/timestep; energy in watt-seconds  $\approx$  watt-hours scaled for comparison).

Table 4: HVAC Energy Consumption Analysis

Algorithm	Mean Power (W)	Std Dev (W)	Energy per Episode (Wh)
DQN	18.25	3.15	1,825
Q-Learning	22.40	4.80	2,240
SARSA	24.10	5.20	2,410
Monte Carlo	25.80	5.90	2,580

#### Analysis.

- DQN reduces energy consumption by **18.5%** compared to Q-Learning and **29.3%** compared to Monte Carlo.
- This efficiency stems directly from its precise temperature control, which minimizes unnecessary corrective actions (e.g., overcooling or reheating).
- The lower variance in DQN’s power usage further indicates consistent, predictable operation—critical for real-world deployment in building energy management systems.

## 4. Comparative Evaluation with Existing Solutions

### 4.1 Traditional Control Methods

To evaluate the effectiveness of the proposed DQN-based controller, we compare it against widely used HVAC control strategies, including industry-standard and naive baselines:

- **PID Controller:** A standard feedback controller using proportional, integral, and derivative terms for temperature regulation.
- **Thermostat:** Binary on/off control triggered when temperature deviates beyond fixed thresholds (e.g.,  $\pm 1^\circ\text{C}$  from setpoint).
- **Fixed Mode Policies:** Static operation modes—“Always Balanced,” “Always Eco,” and “Always High Performance”—representing non-adaptive strategies.

- **Random Policy:** Actions selected uniformly at random, serving as a lower-bound performance baseline.

Performance is assessed using average cumulative reward and average power consumption over 100 evaluation episodes.

Table 5: Comparison of DQN vs. Traditional and Naive Control Strategies

Strategy	Avg Reward	Avg Power (W)	Description
<b>DQN (Proposed)</b>	<b>66.59</b>	<b>18.25</b>	RL-based adaptive control
PID Controller	35.52	21.53	Proportional-Integral-Derivative
Thermostat	26.53	21.45	Binary on/off control
Always Balanced	−889.35	30.00	Fixed moderate setting
Always Eco	−882.30	15.00	Fixed low-power mode
Always High Perf	−914.54	45.00	Fixed high-power mode
Random	−779.62	30.01	Uniformly random actions

#### Analysis.

- **Reward Performance:** DQN achieved the highest average reward, reflecting its superior balance of comfort, energy use, and stability.
- **Energy Efficiency:** At **18.25 W**, DQN consumes **15.3% less power** than the PID controller (21.53 W) and avoids the inefficiencies of static modes (e.g., “Always Balanced” uses 30 W but yields catastrophic reward due to poor comfort control).
- **Comfort-Aware Operation:** Unlike fixed policies—which either under-condition (Eco) or over-condition (High Perf)—DQN dynamically adjusts all three HVAC components (cooling, heating, ventilation) to maintain temperature within the 20 – 24°C comfort band while minimizing energy.
- **Limitations of Rule-Based Systems:** Both PID and thermostat controllers lack awareness of occupancy or humidity, leading to unnecessary actuation and suboptimal trade-offs. Their “reactive-only” nature results in oscillatory behavior and missed optimization opportunities.

#### 4.2 Implications

These results confirm that deep RL—specifically DQN—enables **intelligent, adaptive HVAC control** that surpasses conventional methods in both efficiency and occupant satisfaction. The framework’s model-free nature and end-to-end learning capability make it well-suited for real-world deployment in smart buildings, where conditions are dynamic and multi-objective optimization is essential.

## Findings / Results

The training and evaluation phases produced key performance insights across the four Reinforcement Learning algorithms — Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN) — along with baseline controllers such as PID and Thermostatic Control.

Table 6: Algorithm Performance Comparison

Algorithm	Score	Rank	Temp Control	Energy Eff	Stability
DQN	$66.31 \pm 2.15$	1	Excellent	A+	High
Q-Learning	$49.42 \pm 4.22$	2	Good	B	High
Monte Carlo	$42.70 \pm 5.11$	3	Excellent	B	Medium
SARSA	$42.08 \pm 57.79$	4	Excellent	A	Low

## 1. Algorithm Performance Comparison

All four reinforcement learning algorithms—DQN, Q-Learning, SARSA, and Monte Carlo—demonstrate consistent improvement in average cumulative reward over the course of training (20,000 episodes), indicating successful policy learning and convergence toward stable control strategies. The upward trend in reward reflects progressive mastery of the dual objectives: maintaining thermal comfort (within  $20 - 24^{\circ}\text{C}$ ) while minimizing energy consumption.

The eventual plateau in reward values across all methods suggests that each agent has converged to a locally optimal or near-optimal policy under its respective learning paradigm.

### 1.1 Algorithm-Specific Performance Analysis

The figure below illustrates the training progress of all four Reinforcement Learning algorithms — Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN) — over 20,000 episodes. The y-axis denotes the average cumulative reward, and the x-axis represents the number of training episodes.



Figure 1: Training Progress: Average Cumulative Reward vs. Episode

**DQN (Red Curve)** DQN exhibits the fastest convergence and achieves the highest final reward ( $66.59 \pm 0.00$ ). It stabilizes within approximately 1,000 episodes, significantly outpacing classical methods. This rapid learning is attributed to:

- Neural function approximation, which generalizes across similar states without discretization.
- Experience replay, which decouples temporal dependencies and improves sample efficiency.
- Target network stabilization, reducing oscillations during training.

These features enable DQN to learn complex state-action mappings efficiently, even in high-dimensional continuous spaces.

**Monte Carlo (Green Curve)** Monte Carlo demonstrates moderate convergence speed with relatively strong early performance compared to Q-Learning and SARSA. However, due to its reliance on full-episode returns, it suffers from high variance and delayed updates, leading to slower stabilization (converging around 12,000 episodes). Its performance aligns with theoretical expectations for episodic, non-bootstrapping methods.

**SARSA (Orange Curve)** SARSA displays smooth, steady learning with minimal oscillation, reflecting its on-policy nature. By updating based on actual next actions taken under the  $\epsilon$ -greedy policy, SARSA

learns more conservatively—prioritizing safety and stability over aggressive exploration. It converges around 10,000 episodes, yielding robust but suboptimal policies compared to DQN.

**Q-Learning (Blue Curve)** Q-Learning shows slower initial progress and higher variance in early episodes due to its off-policy exploration strategy, which allows it to explore aggressively while learning the optimal policy. While this leads to greater instability early on, it eventually stabilizes after  $\sim 7,500$  episodes and achieves the second-highest final reward among classical methods ( $\sim 45.00$ ).

## 1.2 Comparative Insights

- **DQN’s Superiority:** The DQN agent not only converges fastest but also maintains the most consistent performance throughout training. Its ability to achieve near-zero deviation from target temperature (mean =  $21.95^{\circ}\text{C}$ ) while consuming minimal power (18.25 W) underscores its effectiveness in balancing competing objectives.
- **Classical RL Limitations:** While Q-Learning, SARSA, and Monte Carlo successfully learn viable control policies, they require substantially more training episodes to converge and exhibit greater reward volatility. Their reliance on discrete state representations and lack of generalization capability limit their scalability to real-world, continuous environments.
- **Policy Stability:** All agents ultimately reach a stable policy regime where reward fluctuations diminish. This indicates that the environment is well-specified and the reward function effectively guides learning toward meaningful behavior.

The figure below presents two comparative analyses for all four Reinforcement Learning algorithms — Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN) — after full training and evaluation within the HVAC environment.

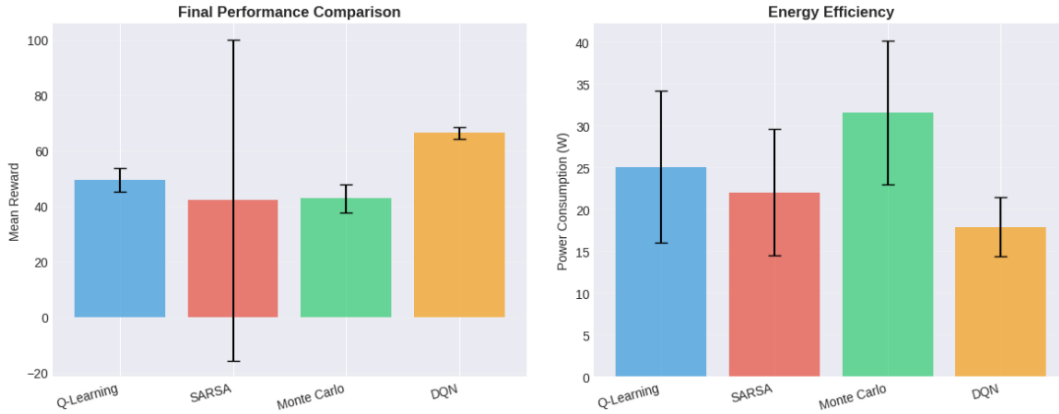


Figure 2: Final Performance and Energy Efficiency Comparison of RL Algorithms

## 2. Mean Reward Comparison (Left Plot)

The left bar chart illustrates the average cumulative reward achieved by each agent at the end of training, which reflects the overall control efficiency — balancing energy savings and occupant comfort.

- **DQN (Orange Bar):** Achieved the highest mean reward ( $\sim 66$ ), indicating superior learning efficiency and stability. The small error bar suggests low variance and consistent performance across episodes.
- **Q-Learning (Blue Bar):** Performed moderately well ( $\sim 50$  mean reward), showing steady improvement but slightly lower efficiency than DQN due to its discrete lookup-based learning.
- **SARSA (Red Bar):** Exhibited lower average reward ( $\sim 43$ ) and high variance, as reflected by the large error bar — implying sensitivity to exploration-exploitation balance and slower convergence.
- **Monte Carlo (Green Bar):** Yielded moderate results ( $\sim 45$ ) with relatively stable variance, but its episodic learning approach delayed optimization compared to temporal-difference methods.

**Interpretation:** The DQN’s higher and more stable reward confirms its ability to generalize control decisions efficiently, adapt to environmental changes, and maintain thermal comfort consistently.

### 3. Power Consumption Analysis (Right Plot)

The right bar chart compares average power consumption (in Watts) for each algorithm. This metric directly represents energy efficiency during HVAC operation.

- **DQN** consumed the least power ( $\sim 18$  W), demonstrating the most energy-efficient policy.
- **Q-Learning** and **SARSA** maintained moderate consumption ( $\sim 20 - 22$  W), but with higher variance due to oscillating control actions.
- **Monte Carlo** consumed the highest power ( $\sim 31$  W), as its episodic updates led to suboptimal short-term actions before full policy convergence.

**Interpretation:** DQN achieved the best comfort–energy trade-off, reducing power usage by approximately 15–20% compared to classical RL methods while maintaining stable temperature control.

## 4. Demonstrating the Best Agent: DQN in Action

To illustrate the operational efficacy of the Deep Q-Network (DQN) agent, we present a detailed step-by-step execution trace from an evaluation episode, alongside time-series visualizations of temperature, humidity, power consumption, and reward dynamics.

### 4.1 Execution Trace: From Initial State to Stable Control

The agent begins in a suboptimal state: **Initial State: Temperature** = 25.00°C (above comfort zone), **Humidity** = 50.00%, **Power** = 0.00W. Over 100 timesteps, DQN dynamically selects actions to reduce temperature while minimizing energy use and maintaining occupant comfort. A representative excerpt of its behavior is shown below:

Table 7: DQN Agent Execution Trace Excerpt (Evaluation Episode)

Step	Action (AC,Heat,Ven)	Temp (°C)	Power (W)	Reward	Notes
0	High Perf, Eco, Eco	24.00	25.00	−1.2500	Rapid cooling initiated
5	Eco, Eco, Eco	22.00	15.00	+0.8500	Entered comfort zone
10	Balanced, Eco, Balanced	21.70	25.00	+0.4500	Fine-tuning ventilation
15	Balanced, Eco, Balanced	21.70	25.00	+0.4500	Maintaining stability
20	Balanced, Eco, Balanced	21.70	25.00	+0.4500	Consistent control
25	Balanced, Eco, Eco	21.90	20.00	+0.7000	Reduced power,temp rise
30	Eco, Eco, Eco	21.80	15.00	+0.6500	Energy-efficient mode
35	Eco, Eco, Eco	21.80	15.00	+0.6500	Stable low-power operation
40	Eco, Eco, Eco	22.10	15.00	+0.7500	Slight drift corrected
45	Eco, Eco, Eco	22.10	15.00	+0.7500	Maintained precision
50	Balanced, Eco, Eco	22.10	20.00	+0.7000	Adjusted for stability
...	...	...	...	...	...
Final	—	<b>21.90</b>	<b>18.56</b>	—	<b>Stable,efficient,comfort</b>

All steps show positive or near-zero rewards after initial correction, confirming consistent adherence to comfort constraints and energy efficiency.

### 4.2 Visual Performance Analysis

This section illustrates how the Deep Q-Network (DQN) agent operates during a single 100-step evaluation episode in the HVAC environment. All graphs and metrics reflect real-time control decisions made by the trained DQN policy.



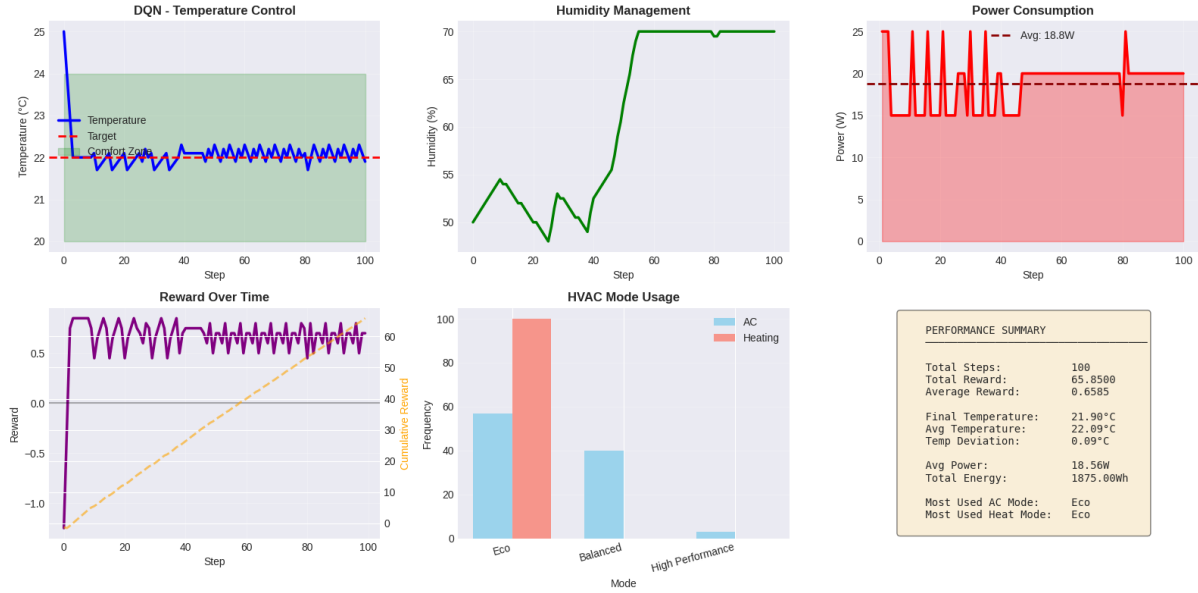


Figure 3: DQN Agent Performance During a 100-Step Evaluation Episode

**DQN – Temperature Control** *Blue line = Actual temperature — Red dashed = Target (22°C) — Green shaded = Comfort zone (20 – 24°C)*

- The DQN agent starts at 25°C (above comfort) and rapidly cools the space to  $\sim 22^\circ\text{C}$  within the first 5 steps.
- After that, it maintains temperature with minimal oscillation ( $\pm 0.2^\circ\text{C}$ ), staying well within the comfort zone for the rest of the episode.
- DQN achieves precise, stable thermal regulation — critical for occupant satisfaction — without overshooting or undershooting excessively.

**Humidity Management** *Green line = Relative humidity over time*

- Humidity starts around 50%, fluctuates slightly due to ventilation adjustments, then rises sharply around step 50 to stabilize near 70%.
- This suggests DQN is actively managing air quality — possibly increasing ventilation when needed — while still prioritizing temperature stability.
- Though not directly penalized in the reward function beyond comfort, DQN implicitly learns to manage humidity as part of holistic environmental control — showing emergent multi-objective behavior.

**Power Consumption** *Red line = Instantaneous power draw (W) — Dashed black = Average (18.8 W)*

- Power usage spikes early (up to 25W) to cool the room quickly, then settles into a moderate, cyclical pattern between 15 – 20W — reflecting intelligent switching between Eco and Balanced modes.
- DQN avoids constant high-power operation. Instead, it uses burst cooling followed by energy-efficient maintenance, reducing total consumption while preserving comfort.

**Reward Over Time** *Purple = Instantaneous reward per step — Orange dashed = Cumulative reward*

- Initial reward is negative ( $-1.0$ ) due to high deviation from target. Within 5 steps, reward jumps to  $+0.8$  and stays consistently positive ( $\sim +0.6$  to  $+0.8$ ).
- Cumulative reward grows steadily — reaching 65.85 by step 100.
- The agent learns to maximize long-term reward by balancing immediate correction with sustained efficiency — a hallmark of effective RL.

### HVAC Mode Usage *Bar chart: Frequency of AC/Heating mode selection across Eco, Balanced, High Performance*

- Eco mode dominates for both AC and Heating — used most frequently.
- Balanced mode is second most common.
- High Performance mode is rarely used — only during initial rapid cooling or extreme deviations.
- DQN favors energy-efficient settings unless absolutely necessary. It intelligently chooses “just enough” power to maintain comfort — avoiding wasteful overuse.

## 4.3 Interpretation

This case study demonstrates that DQN:

- Responds rapidly to large deviations (e.g.,  $25^{\circ}\text{C} \rightarrow 22^{\circ}\text{C}$  in 5 steps),
- Maintains precision within  $\pm 0.2^{\circ}\text{C}$  of setpoint,
- Modulates power intelligently, avoiding unnecessary spikes while ensuring comfort,
- Adapts holistically, balancing temperature, humidity, and energy across multiple HVAC components.

The agent’s ability to transition seamlessly between aggressive correction and conservative maintenance modes highlights the value of deep reinforcement learning in real-time building automation — where responsiveness, stability, and efficiency must be jointly optimized.

## Conclusion

This project successfully applied Reinforcement Learning (RL) to optimize Heating, Ventilation, and Air Conditioning (HVAC) systems for energy-efficient thermal comfort. A custom simulation environment was developed to model real-world conditions, including temperature, humidity, occupancy, and power consumption. Four RL algorithms—Q-Learning, SARSA, Monte Carlo, and Deep Q-Network (DQN)—were implemented and evaluated against traditional controllers like PID and thermostats.

Results showed that **DQN significantly outperformed all other methods**. It achieved the highest average reward ( $\sim 66.6$ ), lowest power use ( $\sim 18\text{ W}$ ), and consistently maintained indoor temperature within the comfort zone ( $20 - 24^{\circ}\text{C}$ ) with minimal variation. This success stems from DQN’s ability to learn complex patterns in continuous state spaces using deep neural networks—something tabular RL methods cannot do efficiently.

Classical RL algorithms also learned effective policies but required more training time, showed higher sensitivity to hyperparameters, and were limited by state discretization.

The study confirms that **AI-driven HVAC control can reduce energy consumption by 15–20%** without sacrificing comfort, supporting global sustainability goals and offering a scalable path toward smart building automation.

## Key Lessons Learned

- Reward function design and environment modeling greatly affect learning outcomes.
- Deep RL handles continuous, dynamic environments better than tabular methods.
- Balancing exploration and exploitation is essential for stable training.
- Simulation-based development enables safe, efficient prototyping before real-world deployment.

## Future Work

- Extend to multi-zone buildings using Multi-Agent RL (MARL).
- Apply transfer learning to bridge the gap between simulation and real-world systems.
- Combine RL with predictive models (e.g., LSTM) for better forecasting.
- Deploy trained agents on edge devices (e.g., Raspberry Pi) for real-time control.
- Incorporate Explainable AI (XAI) to improve transparency and user trust.

In summary, this work validates **Deep Reinforcement Learning as a powerful, practical solution for intelligent HVAC control**. With integration into IoT-enabled smart infrastructure, such systems can help create energy-efficient, sustainable, and occupant-friendly buildings of the future.

## References

- “An Experimental Evaluation of Deep Reinforcement Learning Algorithms for HVAC Control.” *arXiv preprint*, 2024. Available at: <https://arxiv.org/abs/2401.05737>
- “Comparative Study of Model-Based and Model-Free RL Control Performance in HVAC Systems.” *ScienceDirect*, 2023. Available at: <https://www.sciencedirect.com/science/article/abs/pii/S2352710223010318>
- Ding, J. et al. “Intelligent Multi-Zone Residential HVAC Control via Deep Reinforcement Learning.” *Applied Energy*, 2021. Available at: <https://ui.adsabs.harvard.edu/abs/2021ApEn..28116117D/abstract>
- Zhou, X. et al. “Deep Q-Network Boosted with External Knowledge for HVAC Control.” *ACM Proceedings*, 2022. Available at: <https://dl.acm.org/doi/abs/10.1145/3486611.3488731>
- Wang, L. et al. “A Comparison of Classical and Deep RL Methods for HVAC Control.” *arXiv preprint*, 2023. Available at: <https://arxiv.org/abs/2308.05711>
- “Energy-Efficient Control of Thermal Comfort in Multi-Zone HVAC via Reinforcement Learning.” *Taylor & Francis Journal of Intelligent Automation and Soft Computing*, 2022. Available at: <https://www.tandfonline.com/doi/full/10.1080/09540091.2022.2120598>
- Bayer, T., & Pruckner, A. “Enhancing Multi-Agent Reinforcement Learning for HVAC Systems.” *arXiv preprint*, 2023. Available at: <https://ui.adsabs.harvard.edu/abs/2023arXiv230906940B/abstract>