

# Cheap Talk Games with two types

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## So far messages were costly...

- *Example:*
  - Acquiring additional years of education was a costly signal (message) potential employees use to reveal their innate productivity (type).
  - Duel in the Wild West: Drink beer for breakfast as a signal of your strength. Uff!
- What if messages were costless?
  - Talk is cheap!

# Costless messages

- Examples:
  - Your doctor tells you that you should go through an expensive MRI test.
  - Your investment analyst recommends you to buy/sell stocks of a particular company.
  - A lobbyist (expert on a particular topic) informs a politician about the current conditions in a given industry, high schools, natural parks, etc.
- Are there situations in which you would believe that whatever comes out of his/her mouth is the truth? Yes! *The problem*
- **Reading reference:** Harrington, pp. 359-373.

# Costless messages

- We are interested in "information transmission":
- That is, we are searching for separating equilibria where:
  - the doctor tells you to take the test only when necessary;
  - your investment analyst recommends to buy only when the prospects of the firm are good;
  - the lobbyist informs the politician about the true state of the industry, or any other topic.

## Stages in a cheap talk game:

- First, nature chooses the sender's type.
- Second, the sender learns her type and chooses a message.
- Third, the receiver observes the sender's message, modifies his beliefs about the sender's type, and chooses an action (response).

# Payoffs in a cheap talk game:

- **Sender:**

- The payoff of the sender depends on his type  $\theta$ , and on the action of the receiver (response),  $a_R$ ,
- His payoff does not depend on his message,
- That is, the sender's utility function is of the form  $u_S(a_R, \theta)$ , where his message  $m$  is not an argument.

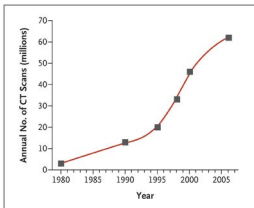
# Payoffs in a cheap talk game:

- **Receiver:**

- Similarly, the payoff of the receiver depends on his own response to the sender's message and on the sender's type (e.g., it depends on the true state of the world).
- However, his payoff does not depend on the particular message he receives from the sender.
- That is, the receiver's utility function is of the form  $u_R(a_R, \theta)$ , where the message he received  $m$  is not an argument.
- The message only affects his beliefs (potentially affecting his response) but not his payoff, i.e.,  $u_R(a_R, \theta)$ .

## Example 1: Defensive medicine

- "In a recent survey of physicians 93% reported altering their clinical behavior...
  - Of them, 43% reported using imaging technology (such as MRIs) in clinically unnecessary circumstances."



- From the article:
  - "Defensive Medicine Among High-Risk Specialist Physicians in a Volatile Malpractice Environment," *Journal of the American Medical Association*, 293 (2005), pp. 2609-17.



## Example 1: Defensive medicine

- Nature moves first determining the value of a test (MRI) to a patient:
  - with prob  $\frac{1}{3}$  the test is beneficial,
  - with prob  $\frac{2}{3}$  it is useless for his condition.
- The value of the test is only known by the doctor.
- After determining the value of the test for the patient, the doctor decides to recommend/not recommend the test.
- The patient then chooses whether to undertake the test or not, after receiving his doctor's recommendation/non-recommendation of taking the test.

$$\begin{array}{c} D \\ \hline p = \frac{1}{3} \end{array} \quad N \quad \begin{array}{c} N \\ \hline p = \frac{2}{3} \end{array}$$

$D = \text{Disease}$   
 $N = \text{No}$

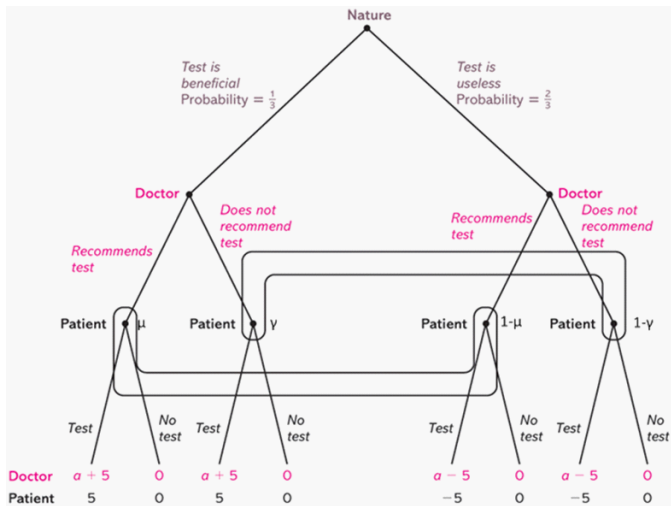
## Example 1: Defensive medicine

- **Payoffs:**
- Regarding the *patient*, he only wants to take the test when the test is beneficial:
  - If the patient takes the test when such test was beneficial, his payoff is 5.
  - If the patient takes the test when such test was useless, his payoff is -5 (time, money, etc.).
  - If the patient doesn't take the test, his payoff is 0, regardless of its true benefits.
    - (This is a simplification, but you could modify the game so that the patient's payoff is 0 when he doesn't take the test and it was useless, but -10 when he doesn't take the test but such a test was beneficial).

## Example 1: Defensive medicine

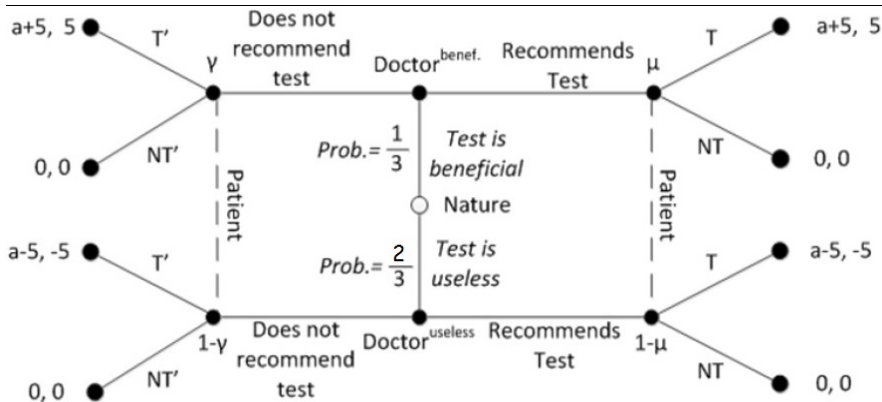
- **Payoffs:**
- Regarding the *doctor*, his payoffs are:
  - If the patient takes the test when such test was beneficial, the doctor's payoff is  $a + 5$ .
  - If the patient takes the test when such test was useless, the doctor's payoff is  $a - 5$ .
  - If the patient doesn't take the test, the doctor's payoff is 0.
- Notice that if  $a = 0$ , then the interests of the doctor and the patient coincide, i.e., preferences are aligned.
- The doctor has a bias towards conducting tests (he obtains a benefit  $a$ ) even if they are not really necessary.
  - e.g., doing so might avoid potential malpractice suits.
- Figure

# Example 1: Defensive medicine



## Example 1: Defensive medicine

- We can alternatively depict the game tree in a more familiar way as follows:



## Example 1: Defensive medicine

- Let us start checking if a pooling equilibrium can be sustained.
  - In the literature on cheap-talk games, the pooling equilibrium is often referred to as "babbling" equilibrium, since all messages from the sender are uninformative.
  - Your doctor is babbling!: anything that comes out of his mouth is uninformative for you.
  - You can think about him as the Swedish Chef in The Muppets (watch a video in YouTube).

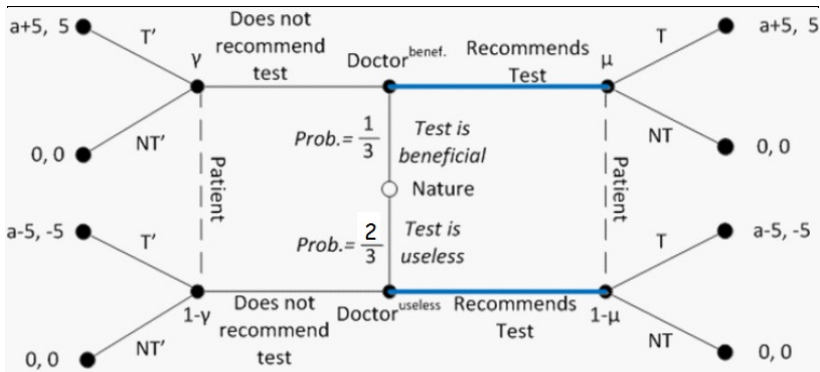


## Example 1: Defensive medicine

- Let us check the pooling strategy profile where the doctor recommends to take the test regardless of its true benefits.
  - (See next figure where, as usual, we shaded the appropriate branches).

## Example 1: Defensive medicine

- Pooling (babbling) equilibrium:** The doctor recommends the test regardless of its benefits





## Example 1: Defensive medicine

- **Patient (responder):**
- *Beliefs:*
  - After observing that the doctor "Recommends test", the patient's beliefs coincide with the priors, i.e.,  $\mu = \frac{1}{3}$ .

## Example 1: Defensive medicine

- **Patient (responder):**

- *Response:*

- Hence, the patient decides whether or not to take the test by comparing the expected utilities:

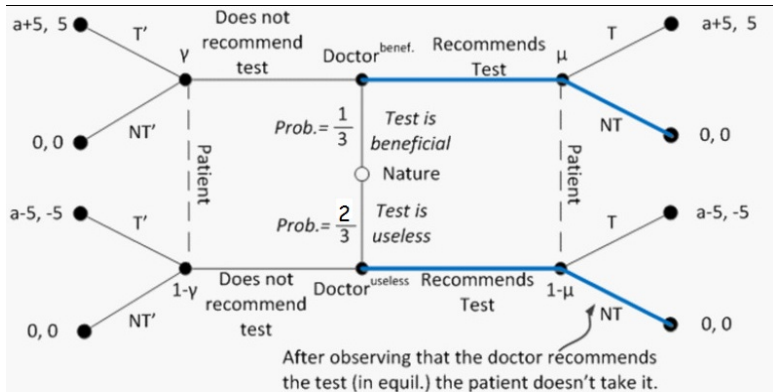
$$EU_{Patient}(T|Recomm.) \geq EU_{Patient}(NT|Recomm.)$$

$$\frac{1}{3}5 + \frac{2}{3}(-5) > \frac{1}{3}0 + \frac{2}{3}0 \iff -\frac{5}{3} < 0$$

inducing the patient to Not take the test.

- (This branch is shaded in the next figure)

- Pooling (babbling) equilibrium (con't)



## Example 1: Defensive medicine

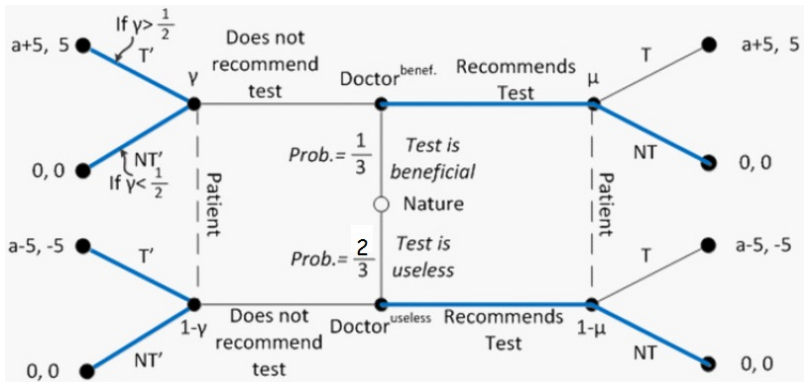
- **Patient (responder):**
- *Response:* After observing that the doctor "Does not recommend the test" (off-the-equilibrium), the patient compares

$$EU_{Patient} (T|NoRecomm.) \geqslant EU_{Patient} (NT|NoRecomm..)$$

$$\begin{aligned}\gamma 5 + (1 - \gamma)(-5) &> \gamma 0 + (1 - \gamma)0 \\ 10\gamma &> 5 \iff \gamma > \frac{1}{2}\end{aligned}$$

- The patient takes the test after iff  $\gamma > \frac{1}{2}$ .
- (Shade this in the figure, one case for  $\gamma > \frac{1}{2}$ , and another case for  $\gamma < \frac{1}{2}$ ).
- (Harrington only presents the case in which  $\gamma$  is exactly equal to  $\frac{1}{3}$ ).

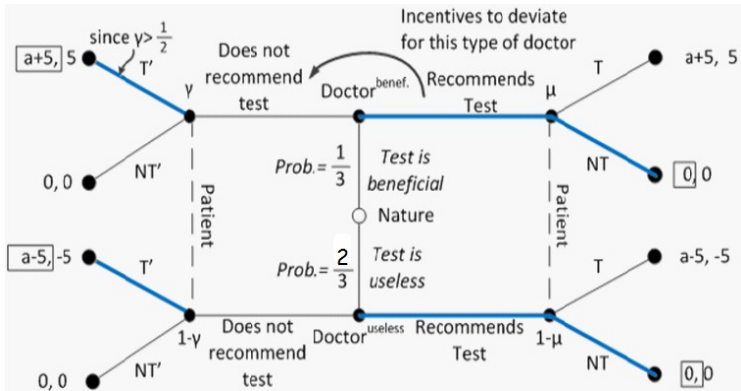
- Pooling (babbling) equilibrium (con't)



## Example 1: Defensive medicine

- **Doctor (sender):** First case:  $\gamma > \frac{1}{2}$ .
- If the test is beneficial, he obtains:
  - 0 from recommending it (since the patient responds not taking the test), and
  - $a + 5$  from not recommending it (since the patient takes the test after no recommendation, given that  $\gamma > \frac{1}{2}$  in this case).
  - The doctor then prefers to **not** recommend the test...
    - and the pooling strategy profile cannot be sustained as a PBE.
- (No need to check if the doctor wants to recommend the test when such test is useless)

- Summary of the First case:  $\gamma > \frac{1}{2}$



## Example 1: Defensive medicine

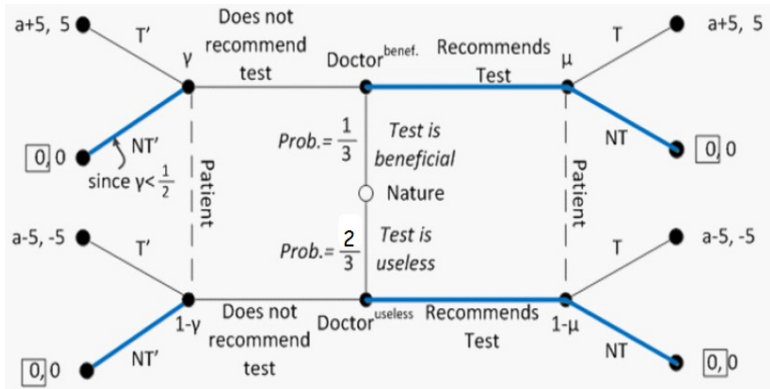
- **Doctor (sender):** Second case:  $\gamma < \frac{1}{2}$  (e.g.,  $\gamma = \frac{1}{3}$ )
- If the test is beneficial, he obtains:
  - 0 from recommending it (since the patient responds by not taking the test), and
  - he also obtains 0 if he doesn't recommend the test (since the patient now does not take the test after no recommendation, given  $\gamma < \frac{1}{2}$ ).
  - The doctor is then indifferent between R/NR the test.



## Example 1: Defensive medicine

- **Doctor (sender):** Second case:  $\gamma < \frac{1}{2}$  (e.g.,  $\gamma = \frac{1}{3}$ )
- If the test is useless, he obtains:
  - 0 from recommend it (since the patient responds by not taking the test), and
  - he obtains 0 if he doesn't recommend the test (since the patient now does not take the test after no recommendation, given  $\gamma < \frac{1}{2}$ ).
  - The doctor is then indifferent between R/NR the test.
- The pooling (babbling) strategy profile can be sustained as a PBE when  $\gamma < \frac{1}{2}$ .

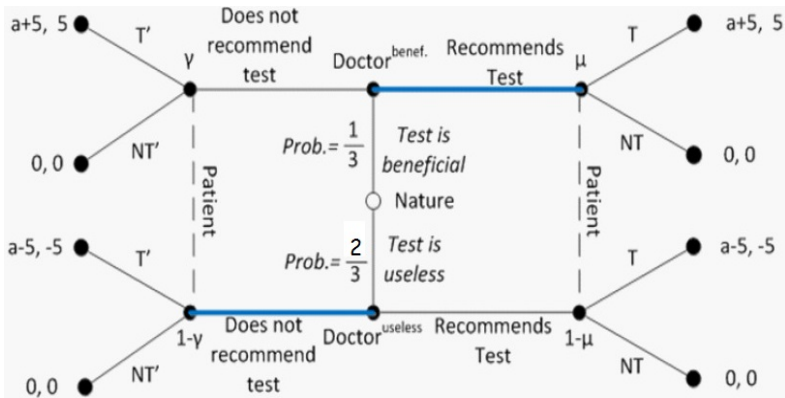
- Summary of the Second case:  $\gamma < \frac{1}{2}$



## Example 1: Defensive medicine

- Unfortunately, in the pooling (babbling) equilibrium we just found, no information is being transmitted from the doctor to the patient!!
  - There is a Pareto improvement to be made if they communicate better.
- **Can we support some more information transmission in this game?**
- Yes!
- We can find a separating equilibrium where the doctor only recommends the test if it is beneficial for the patient.

- **Separating (informative) equilibrium:** the test is only recommended when it is beneficial.



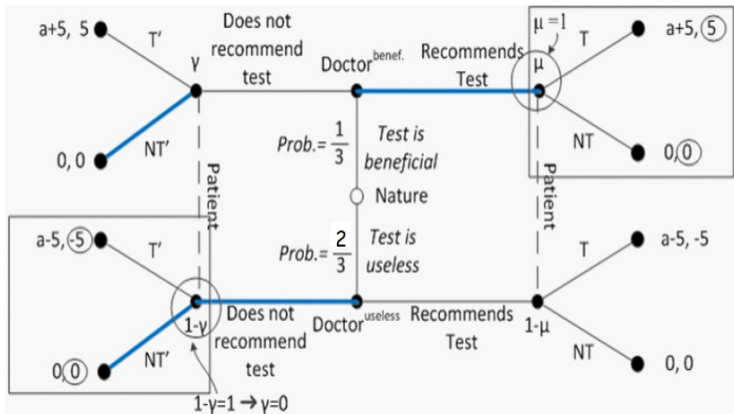
## Example 1: Defensive medicine

- **Patient (responder):**
- *Beliefs:*
  - Beliefs are  $\mu = 1$  after observing a recommendation, and
  - $\gamma = 0$  after observing no recommendation.

## Example 1: Defensive medicine

- **Patient (responder):**
- *Response after Recomm.:*
  - After observing the recommendation of the test, he assigns full probability to the test being beneficial, and he takes it, since  $5 > 0$ .
- *Response after NoRecomm.:*
  - After observing no recommendation of taking the test, he assigns full probability to the test being useless, and he does not take it, since  $-5 < 0$ .
- These branches are shaded in the next figure.

- Separating (informative) equilibrium (cont.)

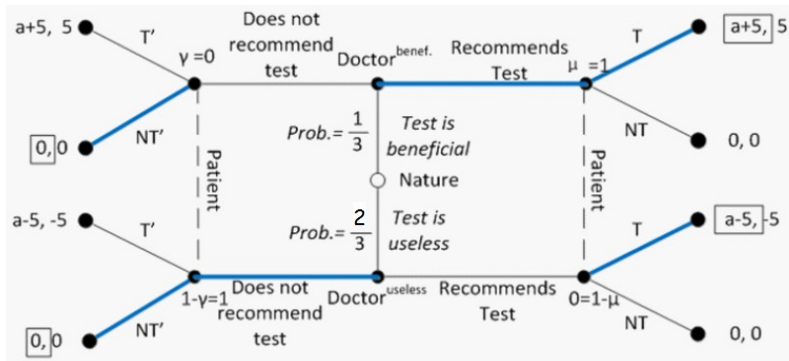


## Example 1: Defensive medicine

- **Doctor (sender):**
- When the test is beneficial, he recommends it if and only if  $a + 5 > 0$  (which holds since  $a > 0$ ).
- When the test is useless, he doesn't recommend the test if and only if  $a - 5 < 0$ , i.e., if  $a < 5$ .
  - Otherwise, he recommends the test, and this separating strategy profile cannot be supported as PBE.



- Summary of the separating (informative) PBE:



## Example 1: Defensive medicine

- **Intuition:**

- The difference in the preferences of the patient and the doctor, captured by parameter  $a$ , must be relatively small ( $a < 5$ ) for a separating PBE to be supported.
- Otherwise, only pooling (babbling) PBEs are sustained, in which the doctor recommends the test regardless of its utility for the patient's condition.
  - These are uninformative equilibria, since the uninformed patient cannot infer any information about his condition from observing that his doctor has just recommended the test.
- We can then interpret separating PBEs as equilibria where information is transmitted from the informed to the uninformed party.