

# Supplementary materials

## Article: Four-dimensional reassignment

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### 1 A comparison of different cross-sections of the W2DFT and four-dimensional reassignment

Figure 1 presents different cross-sections of the W2DFT and four-dimensional reassignment for two chirps with the SNR = 10 dB. The results are for three cuts for  $t = 20, 50, 80$ ,  $r = 20, 50, 80$ , and for the frequency bins of  $\omega = 20, 128, 220$  and  $\eta = 20, 128, 220$ . The distribution had 101 samples in  $t$  and  $r$ , and 256 points of the Fourier transform in  $\omega$  and  $\eta$ . The comparison was made such that the displayed results are grouped in sets of four for the same indices of the cross-sections, i.e. the first index for  $t$ , the first index for  $r$ , the first index for  $\omega$ , and the first index for  $\eta$ , for example,  $t = 20$ ,  $r = 20$ ,  $\omega = 20$ , and  $\eta = 20$ . Subsequent comparisons follow for the second index, i.e.  $t = 50$ ,  $r = 50$ ,  $\omega = 128$ , and  $\eta = 128$ , and for the third index,  $t = 80$ ,  $r = 80$ ,  $\omega = 220$ , and  $\eta = 220$ . The outcomes clearly show that the four-dimensional reassignment is not a super-resolution method, but efficiently concentrates the energy on local maxima.

Figure 1: A comparison of various selected cross-sections through the W2DFT (left-hand side animation) and its concentrated version (the right-hand side animation). The animation can be run using Adobe Reader. If the animation does not work, it can be downloaded from [https://github.com/kabratkiewicz/W2D-FT/blob/main/documents/supplementary\\_materials.pdf](https://github.com/kabratkiewicz/W2D-FT/blob/main/documents/supplementary_materials.pdf).

### 2 Full radar range-Doppler map

Figure 2 presents the full range-Doppler map of the radar signal analyzed in Section III B in the main article. Due to the limited scope of the work, this result was not presented.

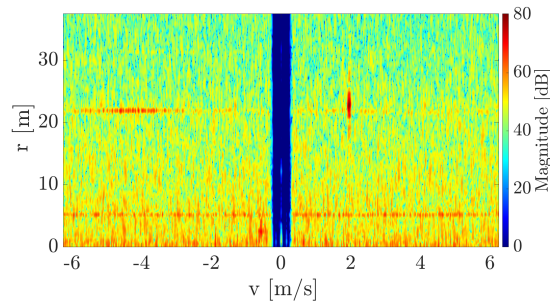


Figure 2: Full range-Doppler map of the signal analyzed in the article.

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