

## 1 西腊字母

$$\ln 2 + \ln 3 = \ln 6$$

## 2 点到直线

$$\frac{|AX_0+BX_0+C|}{\sqrt{A^2+B^2}}$$

## 3 和差化积

$$\sin \alpha + \sin \beta = 2 \sin \left( \frac{\alpha + \beta}{2} \right) \cos \left( \frac{\alpha - \beta}{2} \right)$$

$$\sin \alpha - \sin \beta = 2 \cos \left( \frac{\alpha + \beta}{2} \right) \sin \left( \frac{\alpha - \beta}{2} \right)$$

$$\cos \alpha + \cos \beta = 2 \cos \left( \frac{\alpha + \beta}{2} \right) \cos \left( \frac{\alpha - \beta}{2} \right)$$

$$\cos \alpha - \cos \beta = -2 \sin \left( \frac{\alpha + \beta}{2} \right) \sin \left( \frac{\alpha - \beta}{2} \right)$$

## 4 积化和差

$$\sin \alpha \cos \beta = \frac{1}{2} [\sin(\alpha + \beta) + \sin(\alpha - \beta)]$$

$$\cos \alpha \sin \beta = \frac{1}{2} [\sin(\alpha + \beta) - \sin(\alpha - \beta)]$$

$$\cos \alpha \cos \beta = \frac{1}{2} [\cos(\alpha + \beta) + \cos(\alpha - \beta)]$$

$$\sin \alpha \sin \beta = -\frac{1}{2} [\cos(\alpha + \beta) - \cos(\alpha - \beta)]$$

## 5 万能公式

$$\begin{aligned}\sin \alpha &= \frac{2 \tan \frac{\alpha}{2}}{1 + \tan^2 \frac{\alpha}{2}} \\ \cos \alpha &= \frac{1 - \tan^2 \frac{\alpha}{2}}{1 + \tan^2 \frac{\alpha}{2}} \\ \tan \alpha &= \frac{2 \tan \frac{\alpha}{2}}{1 - \tan^2 \frac{\alpha}{2}}\end{aligned}$$

## 6 半角公式

$$\begin{aligned}\sin \left( \frac{\alpha}{2} \right) &= \pm \sqrt{\left( \frac{1 - \cos \alpha}{2} \right)} \\ \cos \left( \frac{\alpha}{2} \right) &= \pm \sqrt{\left( \frac{1 + \cos \alpha}{2} \right)} \\ \tan \left( \frac{\alpha}{2} \right) &= \pm \sqrt{\left( \frac{1 - \cos \alpha}{1 + \cos \alpha} \right)}\end{aligned}$$

## 7 函数对称

$f(x)$  关于  $x=T$  对称 充要条件  
 $f(x)=f(2T-x)$  ;  $f(T+x)=f(T-x)$

## 8 奇函数与偶函数的表达

奇  $F(x)=f(x)-f(-x)$   
 偶  $F(x)=f(x)+f(-x)$   
 任意  $f(x)=1/2[f(x)-f(-x)]+1/2[f(x)+f(-x)]$

## 9 最大值 & 最小值

$\text{Max}f(x),g(x)=1/2[f(x)+g(x) +|f(x)-g(x)|]$   
 $\text{Min}f(x),g(x)=1/2[f(x)+g(x)-|f(x)-g(x)|]$

## 10 反函数

$f(x)$   $g(x)$  互为反函数

$$f(g(x))=x \rightarrow g(f(x))$$