

$$P(A|B) = \frac{P(AB)}{P(B)}, P(A) = \sum_{k=1}^n P(A|B_k)P(B_k), P(B_i|A) = \frac{P(A|B_i)P(B_i)}{\sum_{k=1}^n P(A|B_k)P(B_k)}$$

$$f_X(x) = P(X = x), E(H(X)) = \sum_x H(x)f_X(x), \\ Var(X) = E((X - E(X))^2) = EX^2 - (EX)^2$$

$$P(|X - \mu| \geq c\sigma) \leq 1/c^2 \\ \hat{E}X = \frac{X_1+X_2+\dots+X_n}{n}, \hat{V}X = \frac{X_1^2+X_2^2+\dots+X_n^2}{n-1} - \frac{(X_1+X_2+\dots+X_n)^2}{n(n-1)}$$

$$G_X(z) = E(z^X), G'_X(1) = EX, G''_X(1) + G'_X(1) - (G'_X(1))^2 = VX$$

$$f_{XY}(x,y) = P(X = x, Y = y), f_X(x) = \sum_y f_{XY}(x,y), f_Y(y) = \sum_x f_{XY}(x,y) \\ E(H(X,Y)) = \sum_x \sum_y H(x,y)f_{XY}(x,y)$$

$$Cov(X,Y) = E((X-\mu_x)(Y-\mu_y)) = E(XY) - E(X)E(Y), \rho_{XY} = \frac{Cov(X,Y)}{\sqrt{VarX}\sqrt{VarY}} \\ f_{X|Y}(x) = f_{X|Y=y}(x) = \frac{f_{XY}(x,y)}{f_Y(y)}$$

$$U_n: f_X(x) = \frac{1}{n}, G_X(e^t) = \frac{\sum_{k=1}^n e^{tx_k}}{n}, EX = \frac{\sum_{k=1}^n x_k}{n}, VX = \frac{\sum_{k=1}^n x_k^2}{n} - \left(\frac{\sum_{k=1}^n x_k}{n} \right)^2$$

$$Be: f_X(x) = p^x(1-p)^{1-x}, G_X(e^t) = q + pe^t, EX = p, VX = p(1-p)$$

$$Ge: f_X(x) = (1-p)^{x-1}p, G_X(e^t) = \frac{pe^t}{1-qe^t}, EX = \frac{1}{p}, VX = \frac{q}{p^2}$$

$$Bi: f_X(x) = \binom{n}{x}p^x(1-p)^{n-x}, G_X(e^t) = (q + pe^t)^n, EX = np, VX = npq$$

$$NegBi: f_X(x) = \binom{x-1}{r-1}p^r(1-p)^{x-r}, G_X(e^t) = \frac{(pe^t)^r}{(1-qe^t)^r}, EX = \frac{r}{p}, VX = \frac{rq}{p^2}$$

$$HG: f_X(x) = \frac{\binom{r}{x}\binom{N-r}{n-x}}{\binom{N}{n}}, G_X(e^t) = , EX = n\frac{r}{N}, VX = n\frac{r}{N}\frac{N-r}{N}\frac{N-n}{N-1}$$

$$Po: f_X(x) = \frac{e^{-k}k^x}{x!}, G_X(e^t) = e^{k(e^t-1)}, EX = k, VX = k$$

$$P(a \leq X \leq b) = \int_a^b f(x)dx,$$

$$F(x) = P(X \leq x) = \int_{-\infty}^x f(t)dt,$$

$$P(a \leq X \leq b) = F(b) - F(a)$$

$$E(H(x)) = \int_{-\infty}^{\infty} H(x)f(x)dx$$

$$\text{Ако } Y = g(X), f_Y(y) = f_X(g^{-1}(y)) \left| \frac{dg^{-1}(y)}{dy} \right|,$$

Непрекъснато равномерно разпределение:

$$f(x) = \frac{1}{b-a}, \quad a < x < b; \quad E(e^{tX}) = \frac{e^{tb} - e^{ta}}{t(b-a)}; \quad EX = \frac{a+b}{2}; \quad VX = \frac{(b-a)^2}{12}$$

Експоненциално разпределение:

$$f(x) = \frac{1}{\beta} e^{-x/\beta}, \quad x, \beta > 0; \quad E(e^{tX}) = \frac{1}{1-\beta t}; \quad EX = \beta; \quad VX = \beta^2;$$

Нормално разпределение:

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}; \quad E(e^{tX}) = e^{\mu t + \frac{\sigma^2 t^2}{2}}; \quad EX = \mu; \quad VX = \sigma^2$$

Точкови оценки. Неизместеност: $E(\hat{\theta}) = \theta$

k-ти емпиричен момент: $M_k = \sum_{i=1}^n \frac{X_i^k}{n}$

Функция на правдоподобие: $L(\theta) = \prod_{i=1}^n f(x_i)$

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i, \quad S^2 = \frac{1}{n-1} \sum_{i=1}^n (X_i - \bar{X})^2$$

Интервална оценка: $[L_1, L_2]$, такъв, че $P(L_1 \leq \theta \leq L_2) = 1 - \alpha$ се нарича $100(1 - \alpha)\%$ -ен доверителен интервал за параметъра θ .

Ако X_1, \dots, X_n е случайна извадка от $N(\mu, \sigma^2)$:

$$\bar{X} \sim N(\mu, \sigma^2/n), \quad \bar{X} \pm z_{\alpha/2} \sigma / \sqrt{n};$$

$$(n-1)S^2/\sigma^2 \sim \chi_{n-1}^2, \quad [(n-1)S^2/\chi_{\alpha/2}^2, (n-1)S^2/\chi_{1-\alpha/2}^2];$$

$$\frac{\bar{X} - \mu}{S/\sqrt{n}} \sim T_{n-1}, \quad \bar{X} \pm t_{\alpha/2} S / \sqrt{n}$$

Хипотези:

$$\alpha = P(\text{се отхвърли } H_0 | H_0 \text{ е вярна}), \quad \beta = P(\text{не се отхвърли } H_0 | H_1 \text{ е вярна})$$