

Prediction of Flight Categories using LSTM Deep Learning

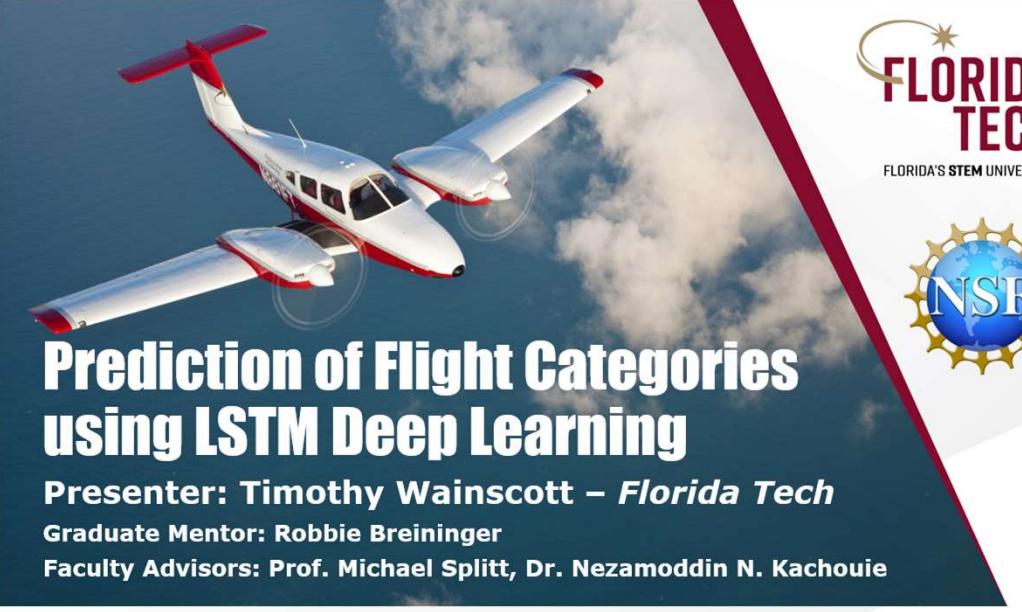
Presenter: Timothy Wainscott – *Florida Tech*

Graduate Mentor: Robbie Breininger

Faculty Advisors: Prof. Michael Splitt, Dr. Nezamoddin N. Kachouie

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**Prediction of Flight Categories
using LSTM Deep Learning**

Presenter: Timothy Wainscott – *Florida Tech*
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NSF

1. Introduction

Weather Effects on Flight

Part 91 = GA = General Aviation – private and recreational flying in small aircraft

Part 135 = Commuter and on-demand flying (government, corporate, and helicopter operations)

G

Part 91 Weather-Related Accidents 2008-2022

White Out/Fla 0%
General Wx 7%
Updrafts/Downdrafts 1%
Turbulence Wind 2%
Carburetor Icing 3%
Structural Icing 3%

	Weather-Related	Non-Weather Related	Total	Weather-Related Percentage
Accidents	4,341	15,197	19,538	22%
Fatal Accidents	990	2,586	3,576	28%

D.Eick / J.Thomas NTSB 2024

Identified
41%
Reduced visibility
Reduced winds
Flat light
Icing (Dark)
Sleet
NTSB

Eich, D. (2024, April). NTSB Weather Related Accidents. In FPAW 2024 Spring Meeting

Flight Rules

- Pilots operate under two different sets of procedures and practices while flying:

Visual Flight Rules (VFR) – primarily visual-based flying

- limited communication with ATC
- navigation is pilot-controlled

Instrument Flight Rules (IFR) – primarily instrument-based flying

- constant communication with ATC
- navigation is ATC-controlled

Flight Categories

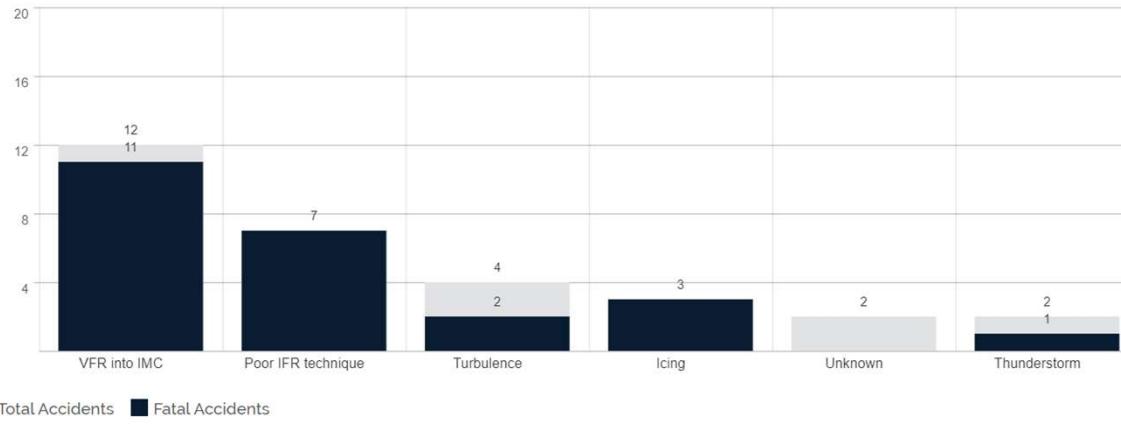
- Surface-based weather conditions divide flight rules into four flight categories (FCATs):
 - **VFR**, **MVFR**, **IFR**, **LIFR**

Category	Ceiling		Visibility
Visual Flight Rules VFR (green sky symbol)	greater than 3,000 feet AGL	and	greater than 5 miles
Marginal Visual Flight Rules MVFR (blue sky symbol)	1,000 to 3,000 feet AGL	and/or	3 to 5 miles
Instrument Flight Rules IFR (red sky symbol)	500 to below 1,000 feet AGL	and/or	1 mile to less than 3 miles
Low Instrument Flight Rules LIFR (magenta sky symbol)	below 500 feet AGL	and/or	less than 1 mile

https://www.faasafety.gov/gslac/alc/libview_printerfriendly.aspx?id=9091

Flight Rules

- Aircraft need to have certain instruments to be IFR certified
- Pilots need to be trained to be IFR certified
- Aircraft and/or pilots not rated to fly in IFR conditions (IMC) need to divert to



How can we predict flight category if not already readily available?

Method 1 – Educated Guess

Applied Cognitive Psychology, Appl. Cognit. Psychol. **30:** 532–543 (2016)
Published online 8 April 2016 in Wiley Online Library (wileyonlinelibrary.com) DOI: 10.1002/acp.3225

Cognitive Biases in Visual Pilots' Weather-Related Decision Making

STEPHEN WALMSLEY and ANDREW GILBEY*

School of Aviation, Massey University, Palmerston North, New Zealand

- Pilots interpret weather differently based on previous information
- Pilots do not favor disconfirming evidence over confirming evidence
- Pilots would replicate a flight into IMC conditions if the outcome was favorable



Method 1 – Educated Guess

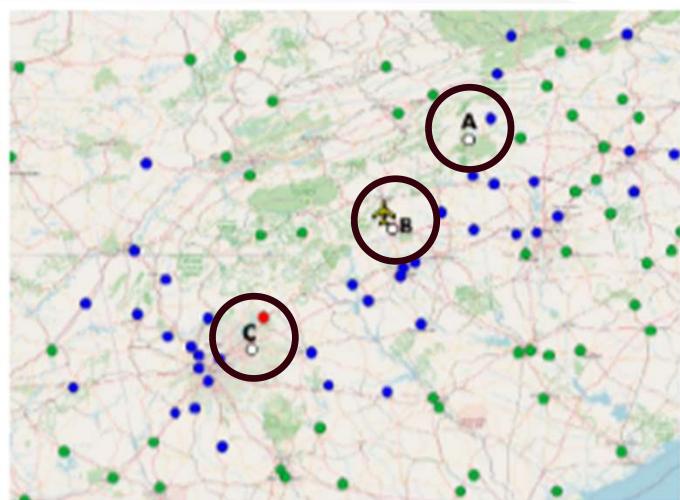
Effects of Weather Information Observability and Uncertainty on Pilot Assessment of Weather Conditions and Decision Making

Barrett S. Caldwell, PhD^{1,2}, Michael E. Split, MA³, and A. N. “Evv” Boerwinkle¹

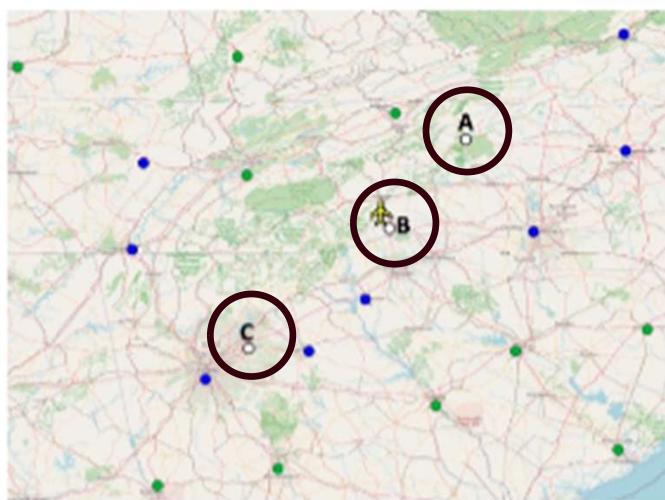
¹School of Industrial Engineering, Purdue University, West Lafayette, IN

²School of Aeronautics and Astronautics, Purdue University, West Lafayette, IN

³College of Aeronautics, Florida Institute of Technology, Melbourne, FL



(a)



(b)

Location A	VFR	MVFR	IFR	LIFR
LOW OBS	14	10	0	0
MED OBS	23	1	0	0
HIGH OBS	0	23	1	0

Location B	VFR	MVFR	IFR	LIFR
LOW OBS	20	4	0	0
MED OBS	16	8	0	0
HIGH OBS	2	22	0	0

Location C	VFR	MVFR	IFR	LIFR
LOW OBS	21	3	0	0
MED OBS	3	17	3	1
HIGH OBS	0	11	13	0

Method 2 – Nearest Neighbor (“Dummy”) Forecast

- See when a nearby station has a reported FCAT and see what are the chances that another station has the same FCAT

	Station 1	Station 2	VFR Count	VFR Percentage	IFR Count	IFR Percentage	Total Count
1	GEV	MKJ	5054	0.94	298	0.06	5352
2	GEV	VJI	5093	0.99	63	0.01	5156
3	GEV	JFZ	5282	0.97	144	0.03	5426
4	JFZ	MKJ	5663	0.96	265	0.04	5928
5	JFZ	VJI	5909	0.97	182	0.03	6091
6	JFZ	GEV	5282	0.97	144	0.03	5426
7	MKJ	JFZ	5663	0.96	265	0.04	5928
8	MKJ	GEV	5054	0.94	298	0.06	5352
9	MKJ	VJI	5524	0.96	222	0.04	5746
10	VJI	JFZ	5909	0.97	182	0.03	6091
11	VJI	GEV	5093	0.99	63	0.01	5156
12	VJI	MKJ	5524	0.96	222	0.04	5746

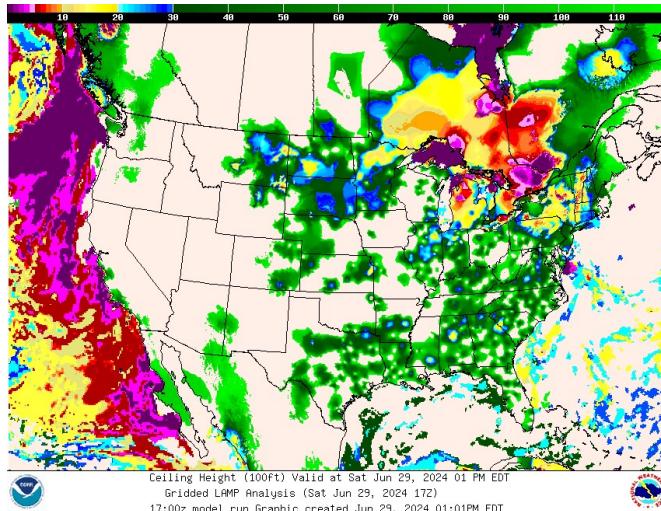
Method 3 – Numerically Predict Ceiling Height & Visibility

A Comparative Verification of Localized Aviation Model Output Statistics Program (LAMP) and Numerical Weather Prediction (NWP) Model Forecasts of Ceiling Height and Visibility

DAVID E. RUDACK AND JUDY E. GHIRARDELLI

*Meteorological Development Laboratory, Office of Science and Technology, NOAA/NWS,
Silver Spring, Maryland*

(Manuscript received 18 November 2009, in final form 3 March 2010)



- Uses numeric models to predict ceiling height and visibility
- Accurate from 0 h future to 25 h future
- Is a complex way to solve our main research question

Method 4 – Our Objective

Use Neural Networks to
Predict Flight Rules

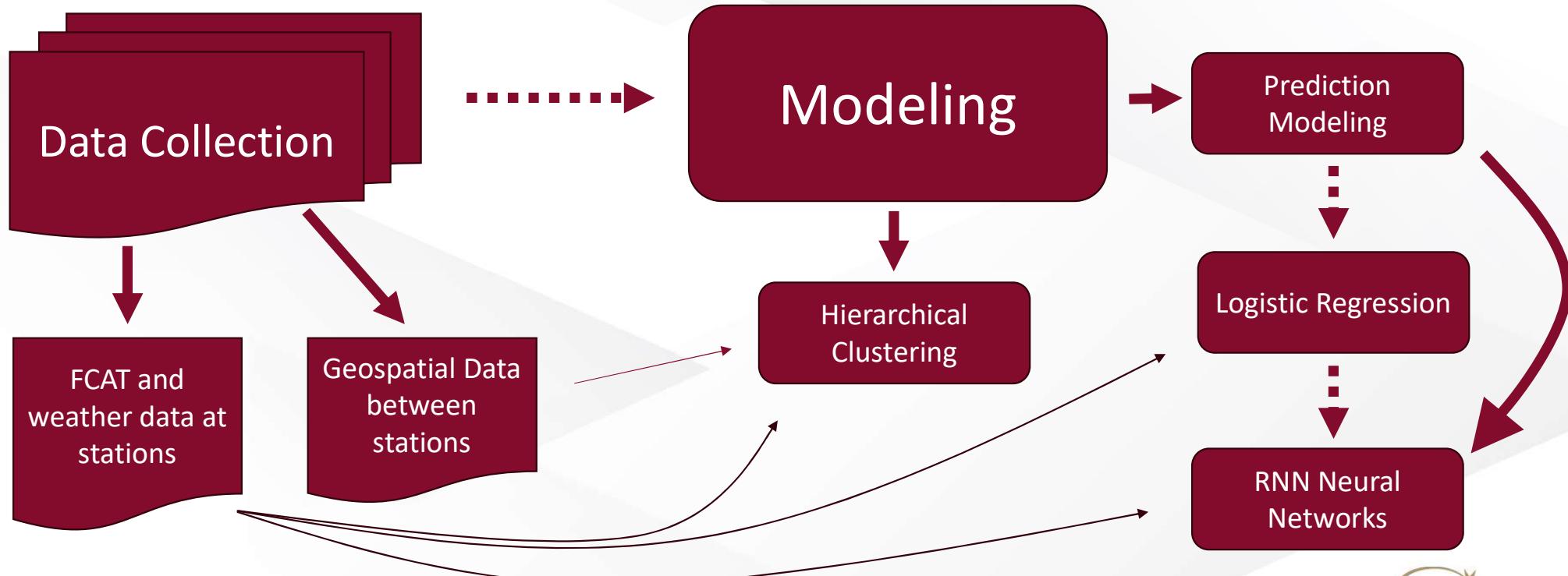
Method 4 – Our Objective

Use Neural Networks to Predict Flight Rules

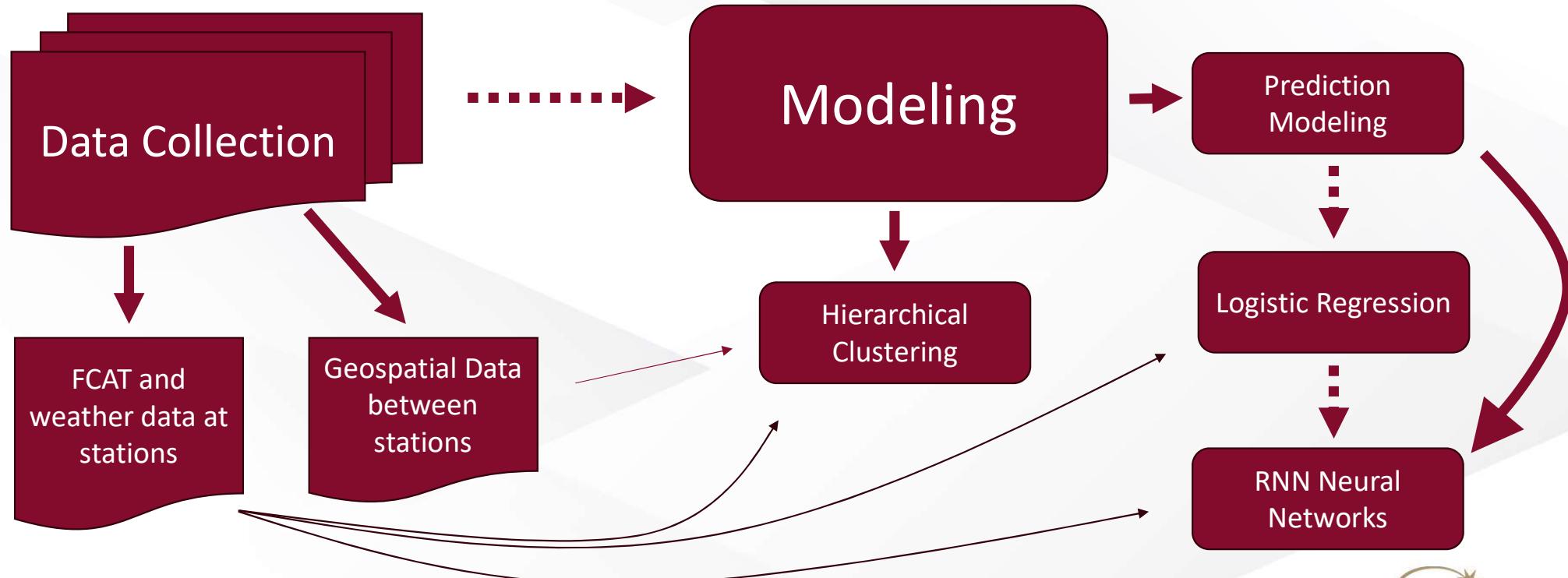
Hypothesis:

LSTM NNs will accurately predict Flight Categories

Schematics – Overall Work of REU



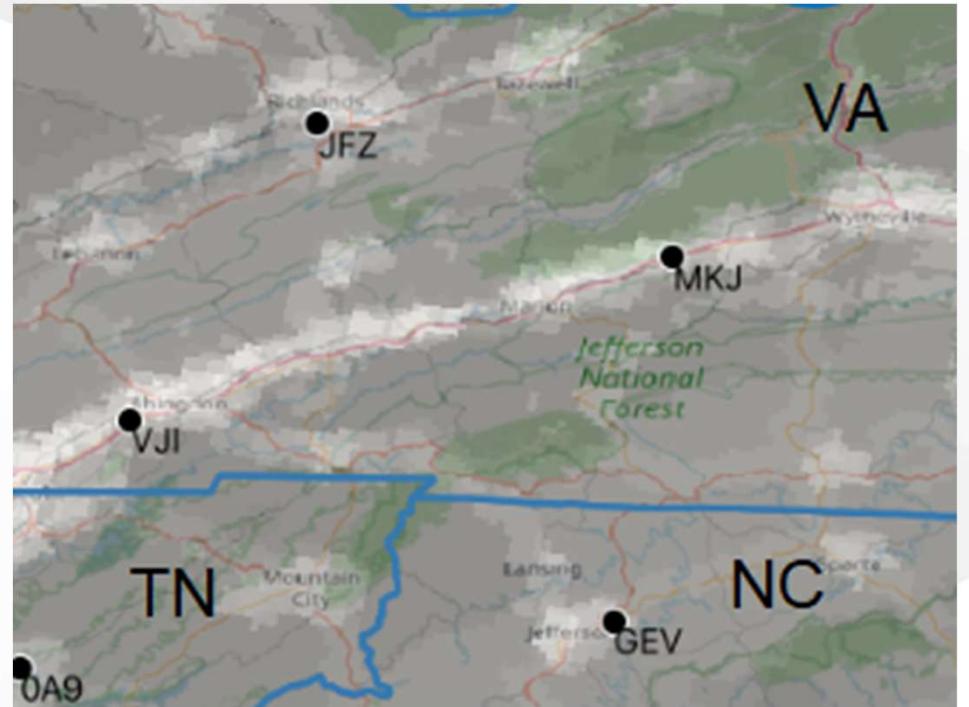
Schematics – Presented Work of REU



2. Data

Sample Size

- 194 total airports (stations) in the Appalachian region
- Neural network model uses 4 equidistant stations from sample



First Data Source

- AWOS/ASOS sites give hourly updates of weather including:
 - Visibility
 - Cloud Ceiling
 - Air Temperature
 - Dew Point
 - Relative Humidity
 - Wind Speed
- These will be our predictors for our prediction model



<https://mesotech.com/pages/awos-3pt>

Neural Network Data

- For predictors, we use
 - FCATs (reported)
 - Air Temp (°C)
 - Dew Point (°C)
 - Relative Humidity (%)
 - and Wind Speed (kts)

```
> flight_data_more
   Station     Date      Time CFCAT VFCAT FCAT Air Temp Dew Point Rel Humid Wind Speed
 1  BCB 01/01/2019 01:00:00  MVFR    VFR MVFR    15     13    88      5
 2  BCB 01/01/2019 02:00:00  MVFR    VFR MVFR    16     13    82      7
 3  BCB 01/01/2019 03:00:00  MVFR    VFR MVFR    17     14    82      5
 4  BCB 01/01/2019 04:00:00    VFR    VFR VFR    17     13    77      7
 5  BCB 01/01/2019 05:00:00    VFR    VFR VFR    17     13    77      8
 6  BCB 01/01/2019 06:00:00    VFR    VFR VFR    16     13    82      7
 7  BCB 01/01/2019 07:00:00    VFR    VFR VFR    15     13    88      6
 8  BCB 01/01/2019 08:00:00  MVFR    VFR MVFR    15     14    94      7
 9  BCB 01/01/2019 10:00:00    VFR    VFR VFR    13     11    88      6
10  BCB 01/01/2019 11:00:00    VFR    VFR VFR    12      9    82      8
11  BCB 01/01/2019 12:00:00    VFR    VFR VFR    12      8    76      5
12  BCB 01/01/2019 13:00:00    VFR    VFR VFR    12      8    76      7
13  BCB 01/01/2019 14:00:00    VFR    VFR VFR    12      8    76      4
14  BCB 01/01/2019 15:00:00  MVFR    VFR MVFR    13      9    77      6
```

Data Preparation – Neural Network

- Take FCATs of four stations and merge them according to date and timer
- Remove date, time, weather predictors (optional), and missing data

FCAT JFZ	Date	Time	Temp (C)	Rel Humid	Wind Sp	FCAT MKJ	FCAT GEV	FCAT VJI
0	1 2020-03-01	1900-01-01 00:00:00	-3.0	54.0	3.0	1	1	1
1	1 2020-03-01	1900-01-01 01:00:00	-3.0	54.0	6.0	1	1	1
2	1 2020-03-01	1900-01-01 02:00:00	-3.0	54.0	6.0	1	1	1
3	1 2020-03-01	1900-01-01 03:00:00	-3.0	54.0	6.0	1	1	1
4	1 2020-03-01	1900-01-01 04:00:00	-3.0	54.0	5.0	1	1	1
6	1 2020-03-01	1900-01-01 05:00:00	-4.0	58.0	5.0	1	1	1
7	1 2020-03-01	1900-01-01 06:00:00	-4.0	58.0	4.0	1	1	1
8	1 2020-03-01	1900-01-01 07:00:00	-4.0	58.0	4.0	1	1	1
9	1 2020-03-01	1900-01-01 08:00:00	-4.0	58.0	3.0	1	1	1
10	1 2020-03-01	1900-01-01 09:00:00	-4.0	58.0	3.0	1	1	1
11	1 2020-03-01	1900-01-01 10:00:00	-4.0	58.0	0.0	1	1	1
12	1 2020-03-01	1900-01-01 11:00:00	-5.0	63.0	0.0	1	1	1

Data Preparation – Neural Network

- Separate response variable from predictor variable
- Split data sets into training and testing data sets

Response		Predictors					
Training	Testing	Training	Testing	FCAT MKJ	FCAT GEV	FCAT VJI	1.]
[1]	FCAT JFZ	[1]					
[1]		[1]					
[1]	0	1	[1]				
[1]			[1]				
[1]	1	1	[1]				
[1]			[1]				
[1]	2	1	[1]				
[1]			[1]				
[1]	3	1	[0]				
[1]			[1]				
[1]	4	1	[1]				
[1]			[1]				
[1]	6	1	[0]				
[1]			[1]				
[1]	7	1	[1]				
[1]			[0]				
[1]	8	1	[1]				
[1]			[1]				
[1]	9	1	[1]				
[1]			[1]				
[1]	10	1	[1]				
[1]			[1]				
[1]	11	1	[1]				
[1]			[1]				
[1]	12	1	[1]				

Data Preparation – Neural Network

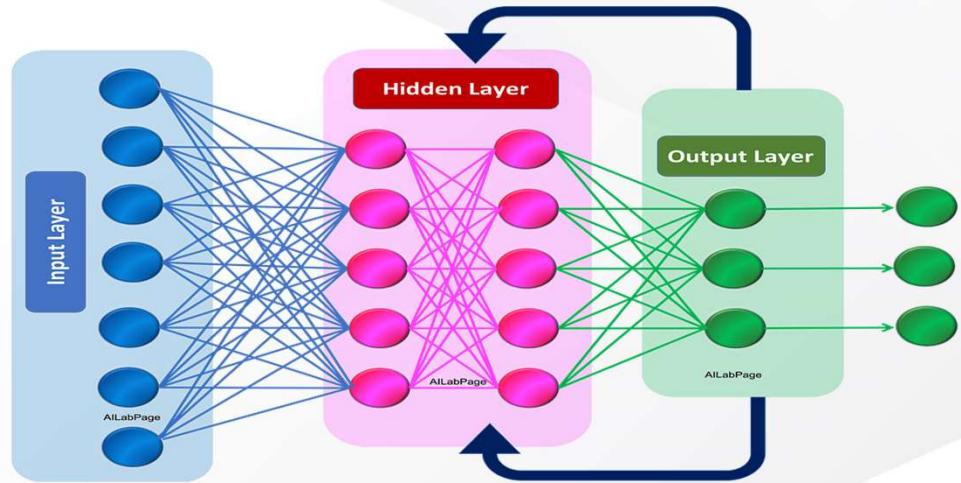
- Multiple questions as to how to format data for future work
 - Training-testing data split?
 - Date and time?
 - Missing data?
 - Weather predictors?
 - Geospatial/Cluster predictors?

3. Methodology

Recurrent Neural Networks

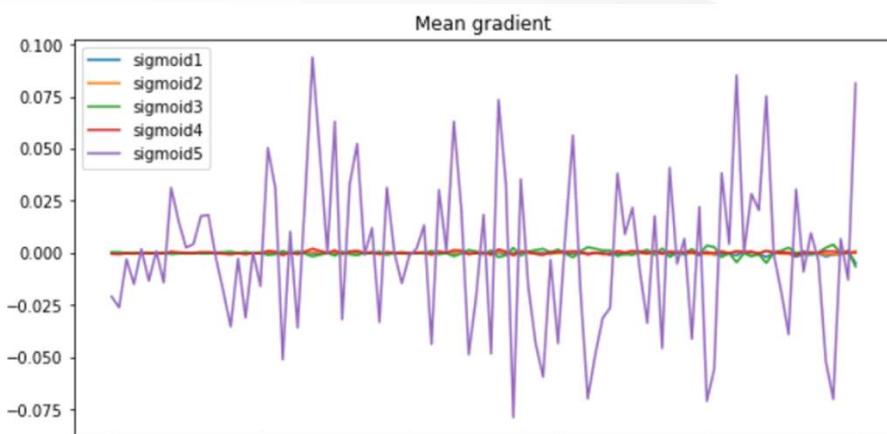
- Neural network that uses previous information in the next sequential data
- Commonly used in time series data
- Is the basis of our prediction model

Recurrent Neural Networks

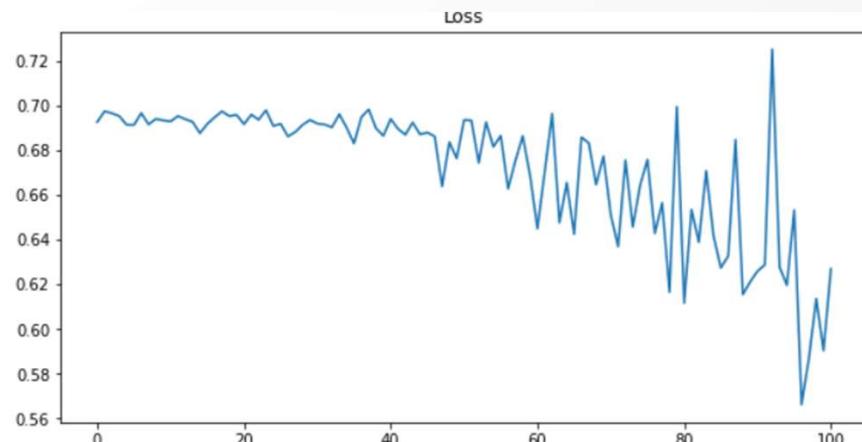


Recurrent Neural Networks – Main Issue

- Difficult with large datasets
- Gradients (rate of change in loss) can either vanish or explode

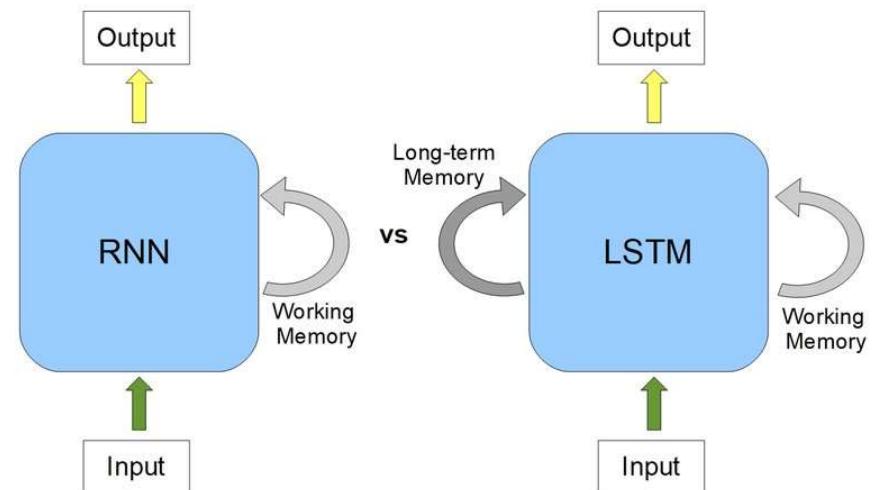


<https://machinelearningmastery.com/visualizing-the-vanishing-gradient-problem/>



Long Short-Term Memory Neural Networks

- Solves the problem of exploding and vanishing gradients
- Uses gates to keep and forget certain information
- Can be made to go sequentially or bidirectionally

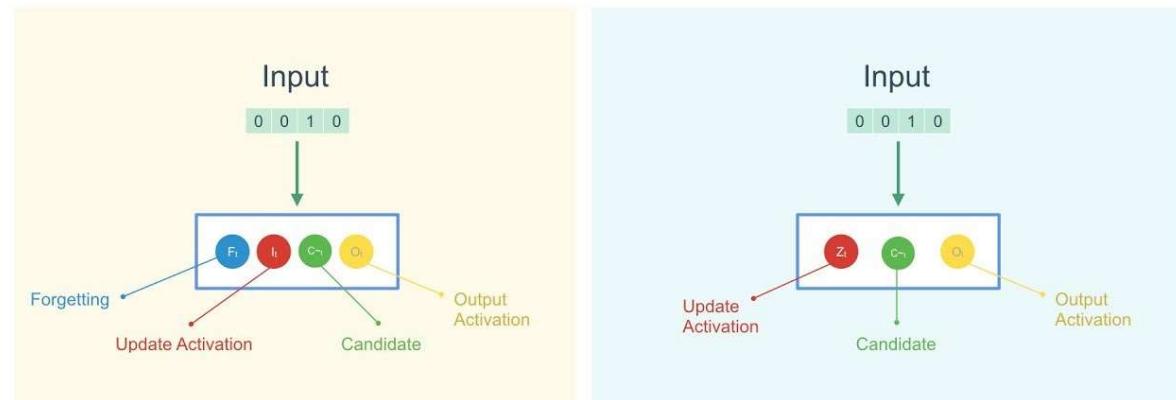


<https://www.analyticsvidhya.com/blog/2022/01/the-complete-lstm-tutorial-with-implementation/>

Gated Recurrent Units

- Also solves vanishing and exploding gradient problem
- Combines “forget” and “remember” gate in LSTM into one “update” gate

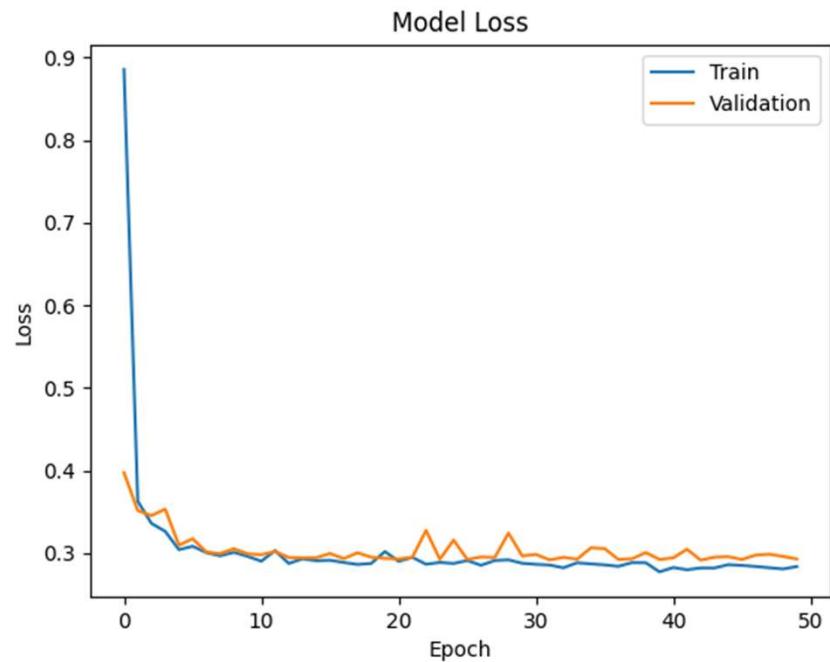
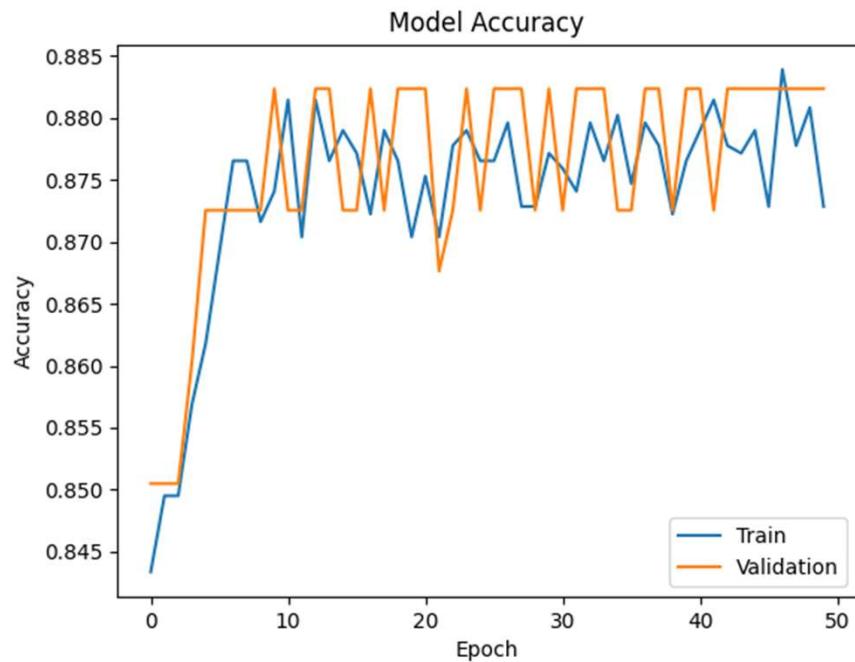
LSTMs and GRUs



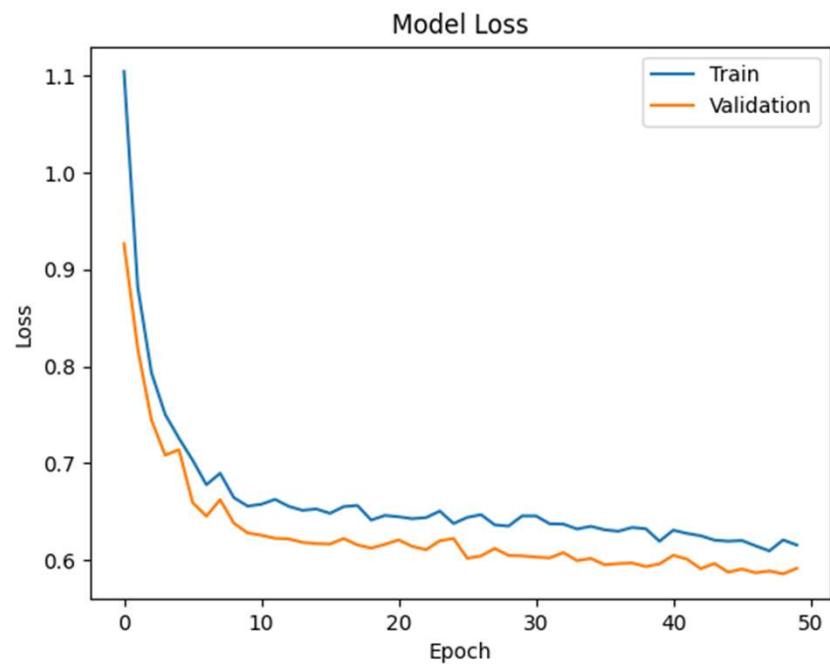
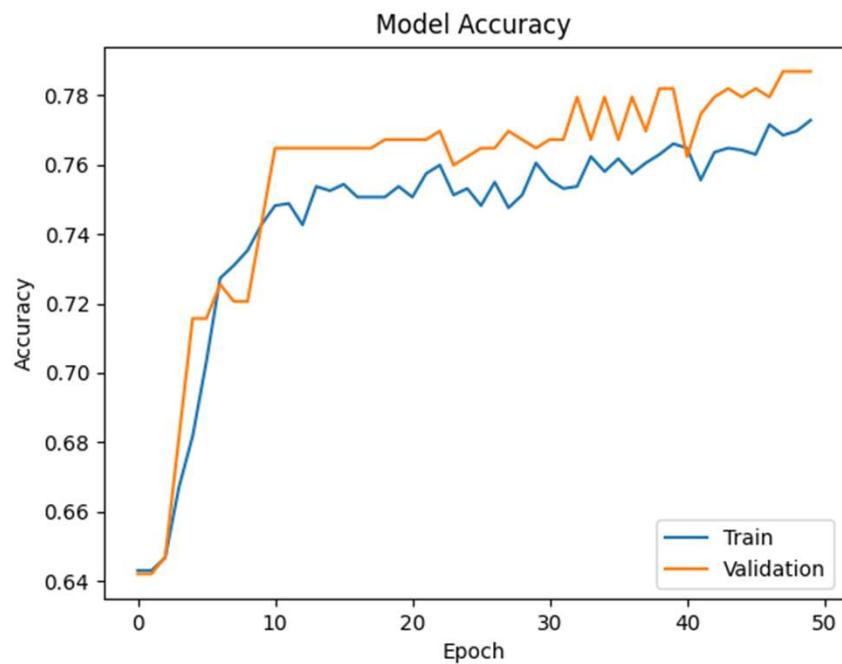
<https://www.youtube.com/watch?app=desktop&v=4F69m3krMhw>

4. Results

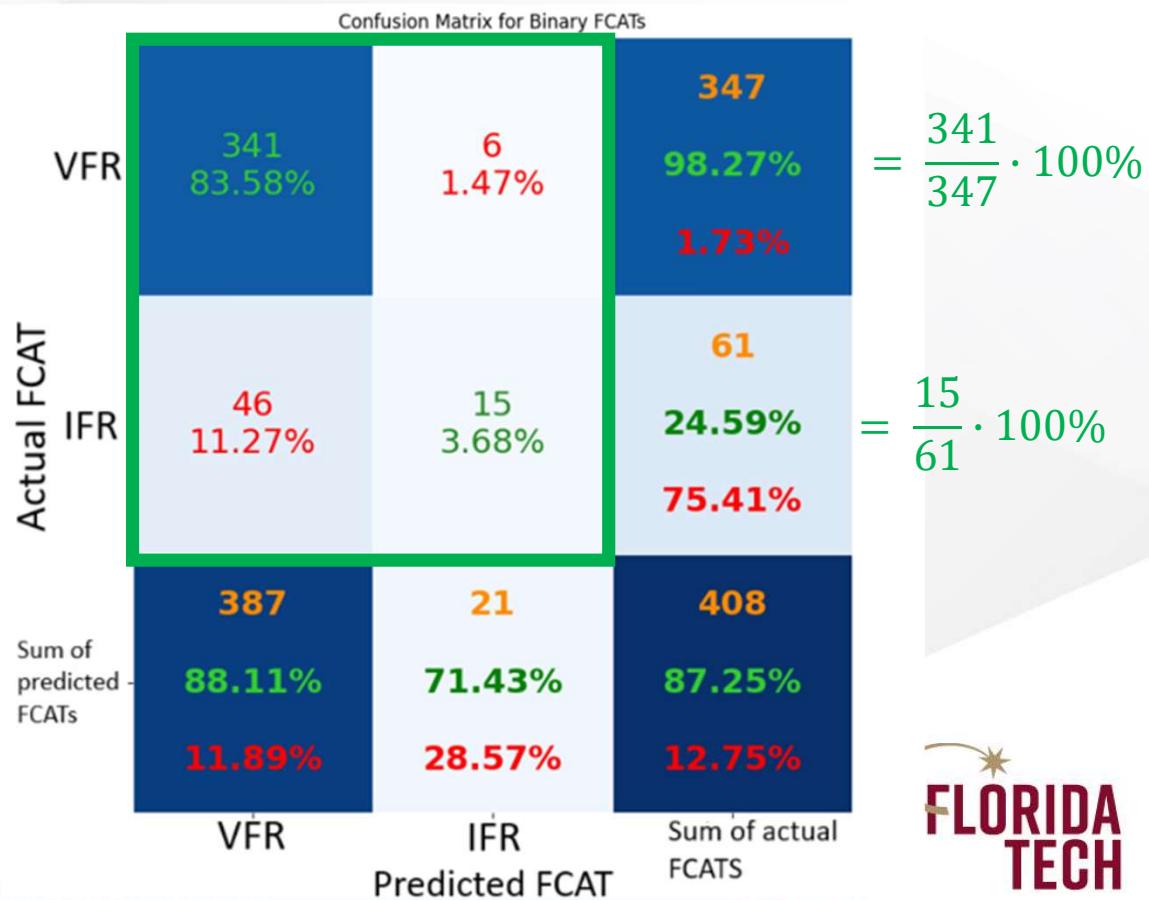
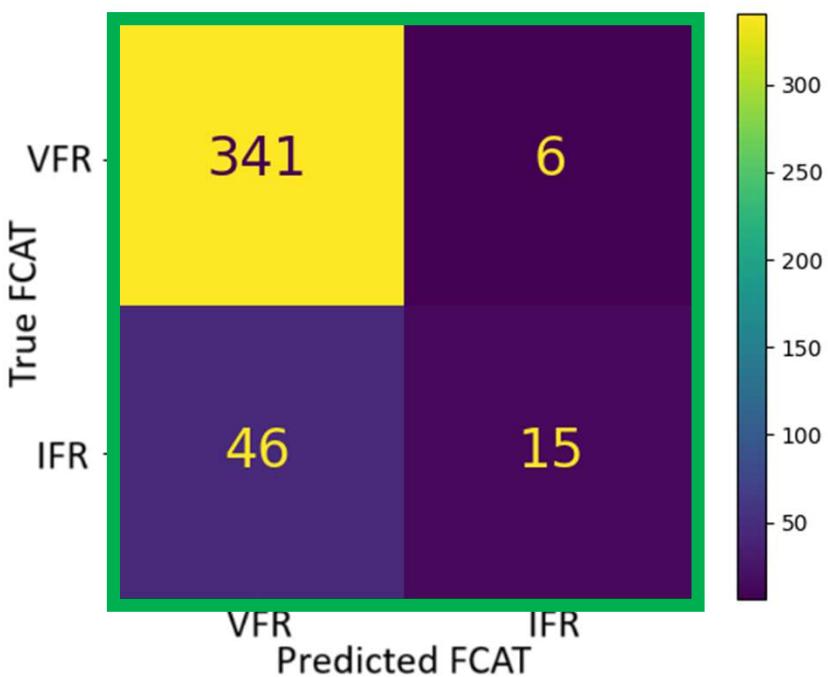
Results – LSTM: Binary



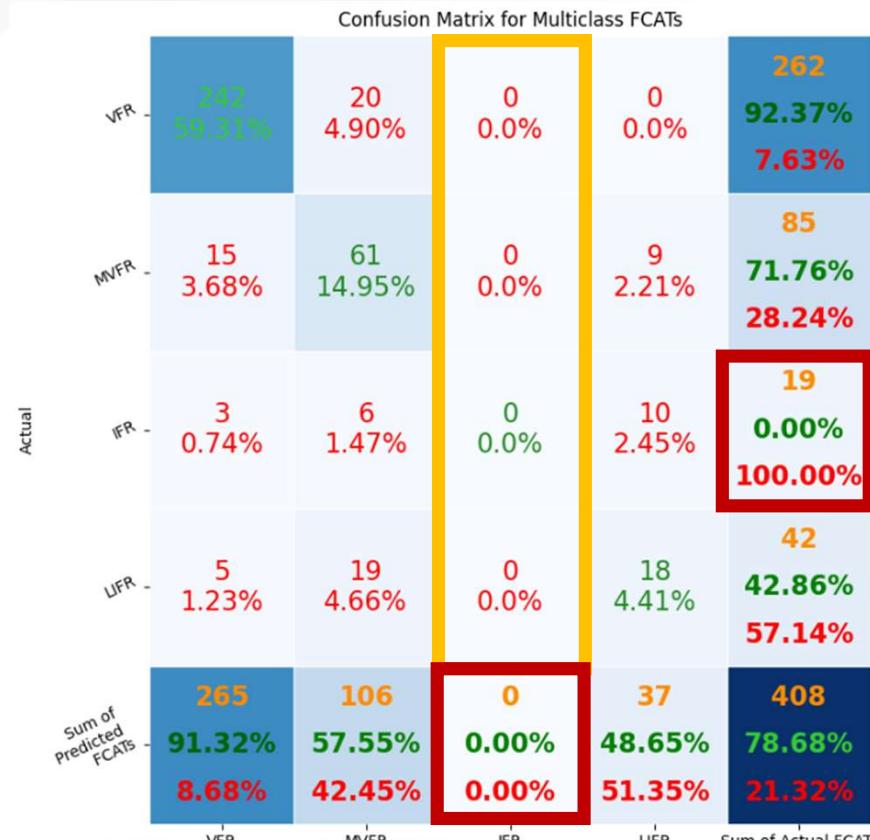
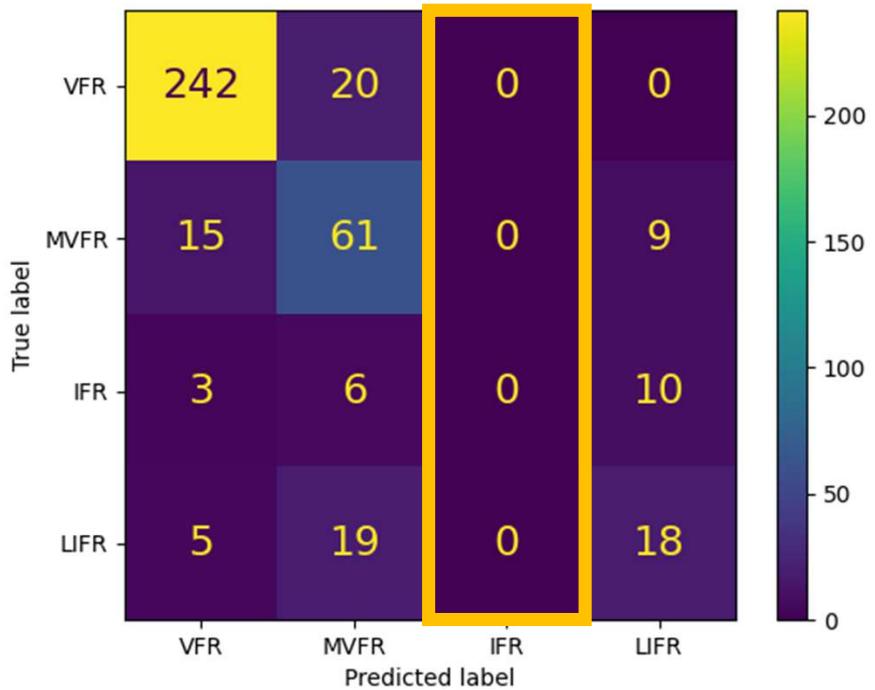
Results – LSTM: Multiclass



Confusion Matrices – LSTM: Binary



Confusion Matrices – LSTM: Multiclass



Models	Accuracy (%)		Loss	
	MKJ	VJI	MKJ	VJI
RNN	86.06	93.35	0.3080	0.1828
GRU	85.96	93.43	0.3085	0.1823
LSTM	85.96	93.38	0.3081	0.1824

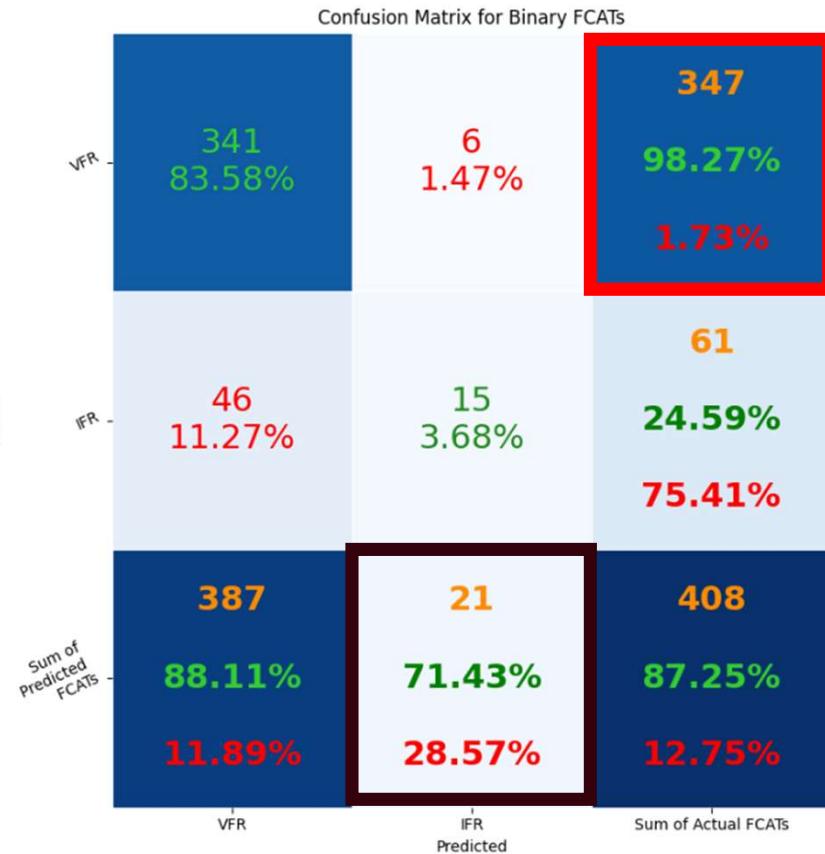
Table 13: Twenty-run average accuracy and loss for all stations (binary, 1 year data length)

Models	Accuracy (%)		Loss	
	MKJ	VJI	MKJ	VJI
RNN	74.60	83.29	0.6592	0.4683
GRU	74.96	83.34	0.6548	0.4651
LSTM	74.54	83.20	0.6570	0.4675

Table 14: Twenty-run average accuracy and loss for all stations (multi-class, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Rate (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	88.62	94.58	95.65	98.51
	GRU	89.61	94.50	93.95	98.39
	LSTM	88.70	94.43	95.38	98.74
IFR	RNN	65.53	65.42	38.17	32.22
	GRU	62.86	64.80	44.54	33.25
	LSTM	64.99	66.67	38.75	30.16

Table 15: Twenty-run average prediction and actual FCAT accuracy for all stations (binary, 1 year data length)



FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Rate (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	88.62	94.58	95.65	98.51
	GRU	89.61	94.50	93.95	98.39
	LSTM	88.70	94.43	95.38	98.74
IFR	RNN	65.53	65.42	38.17	32.22
	GRU	62.86	64.80	44.54	33.25
	LSTM	64.99	66.67	38.75	30.16

Table 15: Twenty-run average prediction and actual FCAT accuracy for all stations (binary, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Rate (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	88.62	94.58	95.65	98.51
	GRU	89.61	94.50	93.95	98.39
	LSTM	88.70	94.43	95.38	98.74
IFR	RNN	65.53	65.42	38.17	32.22
	GRU	62.86	64.80	44.54	33.25
	LSTM	64.99	66.67	38.75	30.16

Table 15: Twenty-run average prediction and actual FCAT accuracy for all stations (binary, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Accuracy (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	83.07	90.66	94.42	94.62
	GRU	84.75	90.76	93.40	94.60
	LSTM	84.82	90.68	93.16	94.64
MVFR	RNN	63.74	62.54	50.57	58.35
	GRU	64.26	62.83	50.69	58.19
	LSTM	62.59	62.32	51.51	58.02
IFR	RNN	45.52	33.99	33.38	30.32
	GRU	40.88	39.07	40.60	39.22
	LSTM	39.15	39.67	40.07	36.51
LIFR	RNN	38.13	34.66	24.24	26.25
	GRU	35.70	38.05	26.00	23.51
	LSTM	38.03	36.21	21.29	23.75

Table 16: Twenty-run average prediction and actual FCAT accuracy for all stations (multi-class, 1 year data length)

Models	Accuracy (%)		Loss	
	MKJ	VJI	MKJ	VJI
RNN	86.06	93.35	0.3080	0.1828
GRU	- 0.10	+ 0.08	+ 0.0005	- 0.0005
LSTM	- 0.10	+ 0.03	+ 0.0001	- 0.0004

Table 17: Comparing accuracies and losses between RNN, GRU, and LSTM, with RNN as the baseline (binary, 1 year data length)

Models	Accuracy (%)		Loss	
	MKJ	VJI	MKJ	VJI
RNN	74.60	83.29	0.6592	0.4683
GRU	+ 0.36	+ 0.05	+ 0.0044	- 0.0032
LSTM	- 0.06	- 0.09	- 0.0022	- 0.0008

Table 18: Comparing accuracies and losses between RNN, GRU, and LSTM, with RNN as the baseline (multi-class, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Rate (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	88.62	94.58	95.65	98.51
	GRU	+ 0.99	+ 0.08	- 1.70	- 0.12
	LSTM	+ 0.08	- 0.15	- 0.27	+ 0.23
IFR	RNN	65.53	65.42	38.17	32.22
	GRU	- 2.67	- 0.62	+ 6.37	+ 1.03
	LSTM	- 0.54	+ 1.25	+ 0.58	- 2.06

Table 19: Comparing average prediction and actual FCAT accuracy for all stations between RNN, GRU, and LSTM, with RNN as the baseline (binary, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)		True Pos/Neg Accuracy (%)	
		MKJ	VJI	MKJ	VJI
VFR	RNN	83.07	90.66	94.42	94.62
	GRU	+1.68	+0.10	-1.02	-0.02
	LSTM	+1.75	+0.02	-1.26	+0.02
MVFR	RNN	63.74	62.54	50.57	58.35
	GRU	+0.52	+0.29	-0.12	-0.16
	LSTM	+1.15	-0.24	+0.94	-0.33
IFR	RNN	45.52	33.99	33.38	30.32
	GRU	-4.64	+5.08	+7.22	+8.90
	LSTM	-6.37	+5.68	+6.69	+6.19
LIFR	RNN	38.13	34.66	24.24	26.25
	GRU	-2.40	+3.39	+1.76	-2.74
	LSTM	-0.10	+1.55	-2.95	-2.50

5. Conclusions

Conclusions

- Binary has higher accuracy than multiclass, but loss doesn't decrease with validation data
- All three models have similar binary accuracy
- Models struggle with predicting rare events
- There are problems with certain stations having better/worse predictions than others

6. Future Work

Future Work

- Continue to test our prediction model
 - Data splits
 - Different models
 - Predictors
 - Architecture
- Incorporate hierarchical clustering and/or geospatial data into our model

Research Team

(photo taken on Space Mountain at Disney World)



Timothy Wainscott
Florida Tech



Dr. Nezamoddin N. Kachouie
Dept. of Mathematical Sciences



Robbie Breininger
Graduate Student Assistant



Prof. Michael Splitt
College of Aeronautics



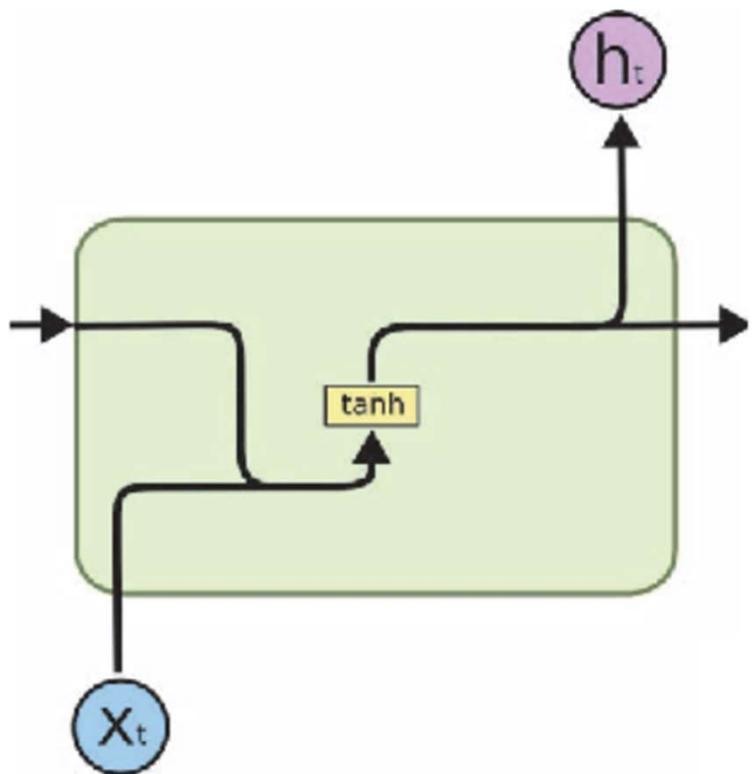
Thanks! Questions?



Appendix

Methodology

RNN Structure

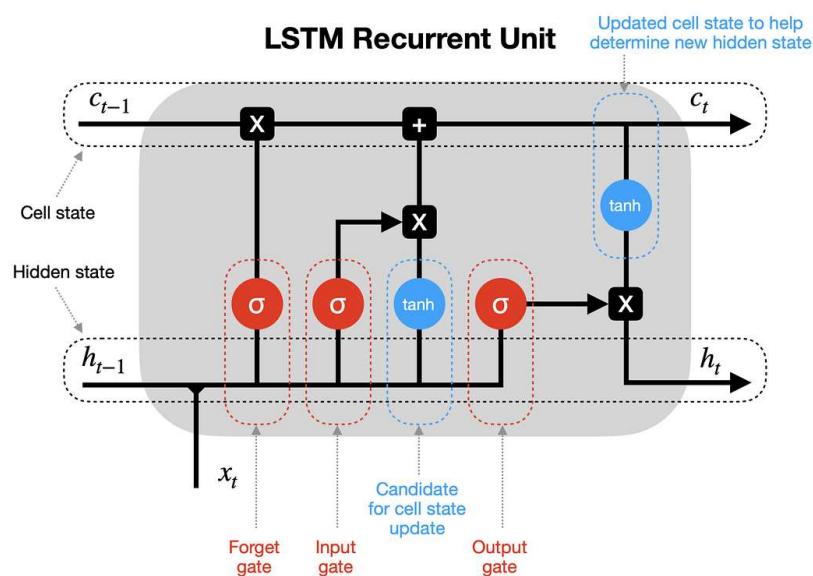


<https://towardsdatascience.com/grus-and-lstm-s-741709a9b9b1>



LSTM Structure

LONG SHORT-TERM MEMORY NEURAL NETWORKS



<https://towardsdatascience.com/lstm-recurrent-neural-networks-how-to-teach-a-network-to-remember-the-past-55e54c2ff22e>

GRU Structure

Results

Models	Accuracy (%)				Loss			
	MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
RNN	86.06	86.61	93.35	86.78	0.3080	0.3653	0.1828	0.3574
GRU	85.96	86.60	93.43	86.78	0.3085	0.3654	0.1823	0.3582
LSTM	85.96	86.61	93.38	86.76	0.3081	0.3652	0.1824	0.3577

Table 5: Twenty-run average accuracy and loss for all stations (binary, 1 year data length)

Models	Accuracy (%)				Loss			
	MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
RNN	74.60	69.81	83.29	75.07	0.6592	0.7902	0.4683	0.6936
GRU	74.96	69.80	83.34	74.91	0.6548	0.7893	0.4651	0.6915
LSTM	74.54	69.79	83.20	74.91	0.6570	0.7893	0.4675	0.6947

Table 6: Twenty-run average accuracy and loss for all stations (multi-class, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)				True Pos/Neg Rate (%)			
		MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
VFR	RNN	88.62	88.91	94.58	88.97	95.65	95.62	98.51	96.44
	GRU	89.61	89.00	94.50	89.05	93.95	95.55	98.39	96.27
	LSTM	88.70	89.00	94.43	89.01	95.38	95.55	98.74	96.36
IFR	RNN	65.53	68.50	65.42	60.54	38.17	44.39	32.22	31.12
	GRU	62.86	68.42	64.80	59.69	44.54	44.98	33.25	31.82
	LSTM	64.99	68.42	66.67	60.11	38.75	44.98	30.16	31.47

Table 7: Twenty-run average prediction and actual FCAT accuracy for all stations (binary, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)				True Pos/Neg Accuracy (%)			
		MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
VFR	RNN	83.07	79.91	90.66	83.15	94.42	85.10	94.62	94.81
	GRU	84.75	79.96	90.76	82.55	93.40	85.13	94.60	94.90
	LSTM	84.82	80.08	90.68	82.81	93.16	84.71	94.64	94.64
MVFR	RNN	63.74	42.92	62.54	45.05	50.57	37.99	58.35	36.58
	GRU	64.26	41.54	62.83	45.35	50.69	37.87	58.19	37.89
	LSTM	62.59	41.99	62.32	44.75	51.51	39.07	58.02	39.53
IFR	RNN	45.52	52.92	33.99	45.24	33.38	64.90	30.32	40.73
	GRU	40.88	53.62	39.07	47.76	40.60	63.82	39.22	38.01
	LSTM	39.15	53.58	39.67	48.43	40.07	64.36	36.51	37.13
LIFR	RNN	38.13	-	34.66	-	24.24	0.00	26.25	0.00
	GRU	35.70	-	38.05	1.82	26.00	0.00	23.51	2.04
	LSTM	38.03	-	36.21	-	21.29	0.00	23.75	0.00

Table 8: Twenty-run average prediction and actual FCAT accuracy for all stations (multi-class, 1 year data length)

Models	Accuracy (%)				Loss			
	MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
RNN	86.06	86.61	93.35	86.78	0.3080	0.3653	0.1828	0.3574
GRU	- 0.10	- 0.01	+ 0.08	± 0.00	+ 0.0005	+ 0.0001	- 0.0005	+ 0.0008
LSTM	- 0.10	± 0.00	+ 0.03	- 0.02	+ 0.0001	- 0.0001	- 0.0004	+ 0.0003

Table 9: Comparing accuracies and losses between RNN, GRU, and LSTM, with RNN as the baseline (binary, 1 year data length)

Models	Accuracy (%)				Loss			
	MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
RNN	74.60	69.81	83.29	75.07	0.6592	0.7902	0.4683	0.6936
GRU	+ 0.36	- 0.01	+ 0.05	- 0.16	+ 0.0044	- 0.0009	- 0.0032	+ 0.0021
LSTM	- 0.06	- 0.02	- 0.09	- 0.16	- 0.0022	- 0.0009	- 0.0008	+ 0.0011

Table 10: Comparing accuracies and losses between RNN, GRU, and LSTM, with RNN as the baseline (multi-class, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)				True Pos/Neg Rate (%)			
		MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
VFR	RNN	88.62	88.91	94.58	88.97	95.65	95.62	98.51	96.44
	GRU	+ 0.99	+ 0.09	+ 0.08	+ 0.08	- 1.70	- 0.07	- 0.12	- 0.14
	LSTM	+ 0.08	+ 0.09	- 0.15	+ 0.04	- 0.27	+ 0.07	+ 0.23	- 0.08
IFR	RNN	65.53	68.50	65.42	60.54	38.17	44.39	32.22	31.12
	GRU	- 2.67	- 0.08	- 0.62	- 0.85	+ 6.37	+ 0.59	+ 1.03	+ 0.70
	LSTM	- 0.54	- 0.08	+ 1.25	- 0.43	+ 0.58	+ 0.59	- 2.06	+ 0.35

Table 11: Comparing average prediction and actual FCAT accuracy for all stations between RNN, GRU, and LSTM, with RNN as the baseline (binary, 1 year data length)

FCAT	Models	Pos/Neg Prediction Accuracy (%)				True Pos/Neg Accuracy (%)			
		MKJ	GEV	VJI	JFZ	MKJ	GEV	VJI	JFZ
VFR	RNN	83.07	79.91	90.66	83.15	94.42	85.10	94.62	94.81
	GRU	+1.68	+0.05	+0.10	-0.60	-1.02	+0.03	-0.02	+0.09
	LSTM	+1.75	+0.17	+0.02	-0.34	-1.26	-0.39	+0.02	-0.17
MVFR	RNN	63.74	42.92	62.54	45.05	50.57	37.99	58.35	36.58
	GRU	+0.52	-1.38	+0.29	+0.30	-0.12	-0.12	-0.16	+1.31
	LSTM	+1.15	-0.93	-0.24	-0.30	+0.94	+1.08	-0.33	+2.95
IFR	RNN	45.52	52.92	33.99	45.24	33.38	64.90	30.32	40.73
	GRU	-4.64	+0.70	+5.08	+2.52	+7.22	-1.08	+8.90	-2.72
	LSTM	-6.37	+0.66	+5.68	+3.19	+6.69	-0.54	+6.19	-3.60
LIFR	RNN	38.13	-	34.66	-	24.24	0.00	26.25	0.00
	GRU	-2.40	-	+3.39	+1.82	+1.76	± 0.00	-2.74	+2.04
	LSTM	-0.10	-	+1.55	-	-2.95	± 0.00	-2.50	± 0.00

Table 12: Comparing average prediction and actual FCAT accuracy for all stations between RNN, GRU, and LSTM, with RNN as the baseline (multi-class, 1 year data length)