

Adobe  
Goldman Sachs

Q There are  $N$  doors  $\rightarrow$  (1 to  $N$ ) & a person is standing in front of every door. Initially all doors are closed

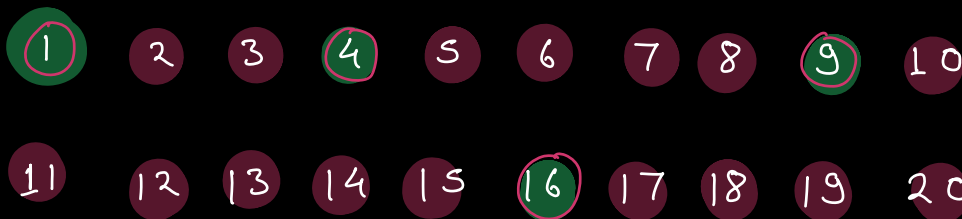
1<sup>st</sup> person  $\rightarrow$  1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup> - - - -  $N^{\text{th}}$  (open)

2<sup>nd</sup> person  $\rightarrow$  2<sup>nd</sup>, 4<sup>th</sup>, 6<sup>th</sup>, 8<sup>th</sup> - - - - (toggle)

3<sup>rd</sup> person  $\rightarrow$  3<sup>rd</sup>, 6<sup>th</sup>, 9<sup>th</sup> - - - -

4<sup>th</sup> person  $\rightarrow$  4<sup>th</sup>, 8<sup>th</sup>, 12<sup>th</sup> - - - -

Return which all doors will be open finally.



9  $\rightarrow$  1, 3, 9  
15  $\rightarrow$  1, 3, 5, 15  
18  $\rightarrow$  1, 2, 3, 6, 9, 18

Every door will be toggled by its factor.

C  $\xrightarrow{1^{\text{st}}}$  O  $\xrightarrow{2^{\text{nd}}}$  C  $\xrightarrow{3^{\text{rd}}}$  O  $\xrightarrow{4^{\text{th}}}$  C  $\xrightarrow{5^{\text{th}}}$  O

If the no. of factors is odd then the final state  $\Rightarrow$  Open

$$24 \Rightarrow \underline{1}, \underline{2}, 3, 4, 6, 8, \underline{12}, \underline{24}$$

$$\begin{array}{lcl} 9 & \Rightarrow & 1, \textcircled{3}, 9 \\ 16 & \Rightarrow & 1, 2, \textcircled{4}, 8, 16 \\ 25 & \Rightarrow & 1, \textcircled{5}, 25 \end{array} \quad \left. \vphantom{\begin{array}{lcl} 9 \\ 16 \\ 25 \end{array}} \right\}$$

All perfect sq/s will have odd no. of factors.

$$\underline{i \times i = N}$$

$$N = 100$$

$$\underline{\underline{N}}$$

$$\left. \begin{array}{lcl} 1 \times 1 & = & 1 \\ 2 \times 2 & = & 4 \\ 3 \times 3 & = & 9 \\ 4 \times 4 & = & 16 \\ \vdots & & \\ 9 \times 9 & = & 81 \\ \textcircled{10} \times 10 & = & \underline{100} \end{array} \right\}$$

$$\Rightarrow 11 \times 11 = \textcircled{121} > 100$$

Amazon

N<sup>th</sup> Magical No.

Given a no. N. Return N<sup>th</sup> magical no.

Magical No: A no. that can be expressed as a  
sum of unique powers of 5.

$$= 5^1 + 5^2 + 5^4 + 5^{10}$$

$$N = 1 \Rightarrow 5^1$$

$$N = 2 \Rightarrow 10 \Rightarrow 5^1 + 5^1 \times$$
$$25 \Rightarrow 5^2$$

$$N = 3 \Rightarrow 5^1 + 5^2 \Rightarrow 30 \checkmark$$

$$30 = 5^2 + 5^1$$

$$\begin{array}{cccccc} 5, & 25, & 30, & 125, & 130 \\ 1 & 2 & 3 & 4 & 5 \end{array}$$

$$130 = 5^3 + 5^1$$

$\textcircled{N}$   
 $1^{st} \quad 5 \quad s^1$   
 $2^{nd} \quad 25 \quad s^2$   
 $3^{rd} \quad 30 \quad \boxed{s^2 + s^1}$   
 $4^{th} \quad \begin{array}{l} 125 \\ \hline \end{array} \quad \boxed{s^3}$   
 $5^{th} \quad \begin{array}{l} 130 \\ \hline \end{array} \quad \begin{array}{l} s^3 + s^1 \\ \hline \end{array}$   
 $6^{th} \quad \begin{array}{l} 150 \\ \hline \end{array} \quad \begin{array}{l} s^3 + s^2 \\ \hline \end{array}$   
 $7^{th} \quad 155 \quad s^3 + s^2 + s^1$

3	2	1	
0	0	$s^1$	0 0 $\textcircled{1}$
0	$s^2$	0	0 $\textcircled{1}$ 0
0	$s^2$	$s^1$	0 $\textcircled{1}$ $\textcircled{1}$
$s^3$	0	0	$\textcircled{1}$ 0 0
$s^3$	0	$s^1$	1 0
$s^3$	$s^2$	0	1 1 0
$s^3$	$s^2$	$s^1$	1 1

$N = 11$

$11 \Rightarrow \begin{array}{cccc} 4 & 3 & 2 & 1 \\ 1 & 0 & 1 & 1 \end{array}$   
 $s^4 + 0 + s^2 + s^1 \Rightarrow \underline{\underline{655}}$

## Google Majority Element

Q Given an array of size  $N$ , (true no)

Return, if there exists a no. with frequency  $> N/2$   
[Without any extra space  $SC: O(1)$ ]

A: 1, 6, 1, 1, 2, 1  $N = 6$

$\Rightarrow 1$

$$N/2 = 3$$

Quiz

3, 4, 3, 6, 1, 3, 2, 5, 3, 3, 3  $N = 11$

$\Rightarrow 3$

$$\frac{11}{2} = 5$$

$$(5-1)$$

Quiz

4, 6, 5, 3, 4, 5, 6, 4, 4, 4  $N = 10$

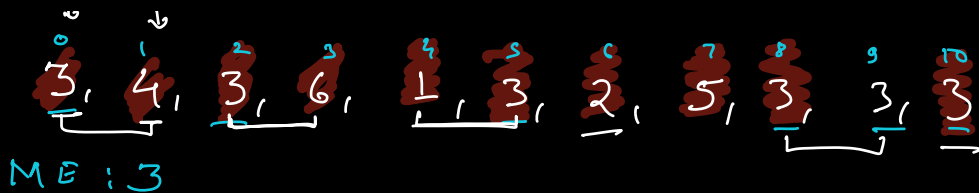
No ME

$$Majority = 6$$

-1

$O(N^2)$   $\Rightarrow$   $f_n(i=0 \rightarrow N)$   
 $f_n(j=0 \rightarrow N)$   
if  $(a[i] == a[j])$   
     $freq_i++$   
     $freq_j++$   
if  $freq_i > N/2$  return  $a[i]$ .





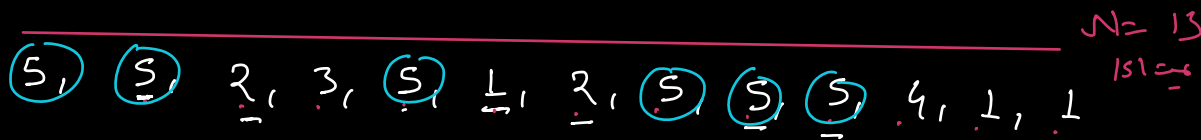
N	ME
11	6
9	5
7	4
5	3
3	2
1	1

Moore's Voting Algo

[ME: ~~3~~ ~~3~~ ~~1~~ ~~2~~ 3]

Count: ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ 3

Can be a ME.  
Iterate over the array & confirm if it is.



ME: ~~5~~ ~~5~~ ~~2~~ ~~3~~ 5

Count: ~~1~~ ~~2~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~0~~ ~~1~~ ~~2~~ ~~1~~ ~~0~~ 1

Iterate over the array & confirm it is in majority

TC:  $O(N)$  (  $N$  finding a ME by Moore Voting +  $N$  confirm by counting the occurrence of ME )  
 SC:  $O(1)$  (Extra)

Q

ME  $\Rightarrow$  Count  $> N/3$

An array can have 2 ME.

[ME1 - Count1] | [ME2 - Count2]

Tricky Case

War - Stories ?

Josephus (Jewish)

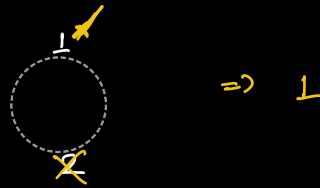
If there are  $N$  people in the circle,

What should be the position where Josephus should stand in order to save his life.

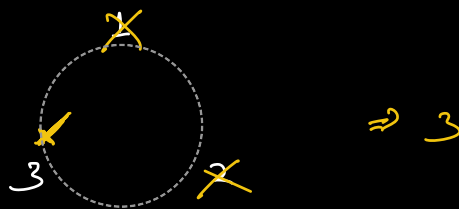
$N = 1$

0 X

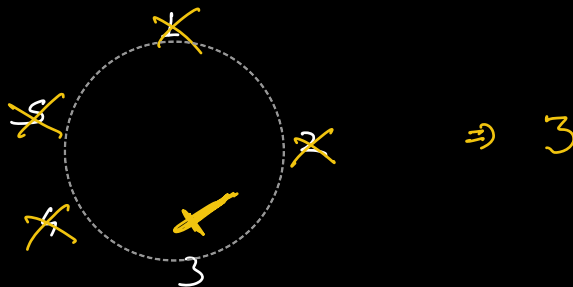
$N = 2$



$N = 3$

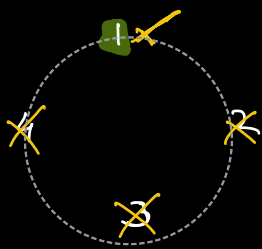


$N = 5$

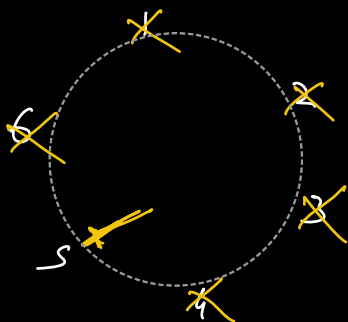




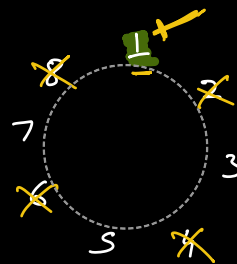
$$N = 4$$



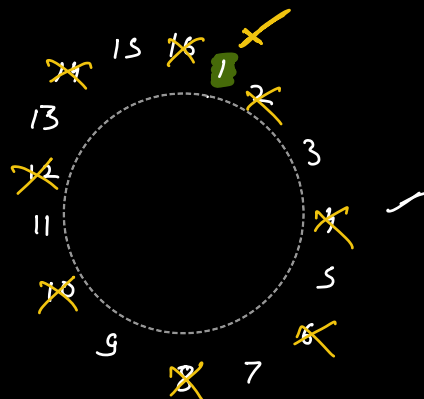
$$N = 6$$



$$N = 8$$



$$N = 16$$



$N$		
2	→	1
4	→	1
8	→	1
16	→	1
32	→	1
64	→	1
128	→	1

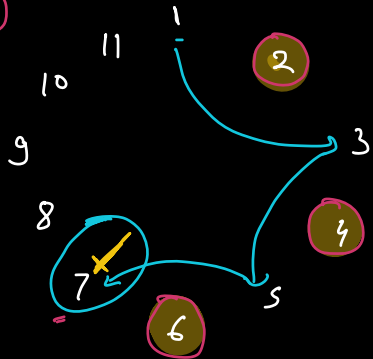
If no. of people is a power of 2

$$N = 2^k$$

Then, the person who starts the Kelly  
wins

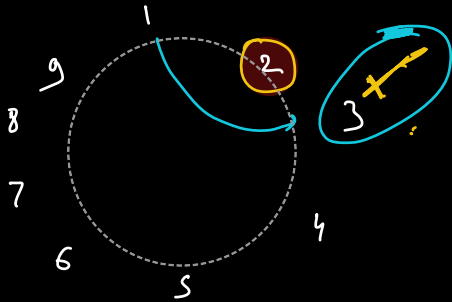
$$N = 11 \quad 2^3 \Rightarrow 8$$

$$11 - 8 = 3$$



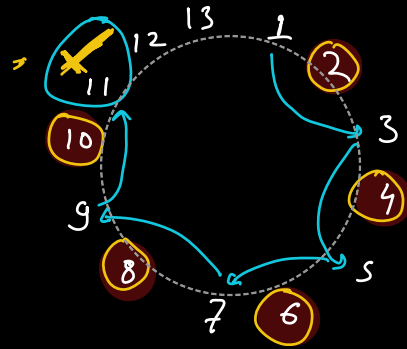
7

$$N = 9$$



$$N = 13$$

$$13 - 8 = 5$$



After killing of  $x$  people  
position of sword is  $2x + 1$

$$N = 100$$

$x$  ?

$x = N - \text{Nearest Power of } 2$

$$x = 100 - 64$$

$$x = 36$$

After 36 killings, pos of sword is 73