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## 2-Sum problem

Given an array & a no. K.

indices  
↑

Return true if there exists a pair (i, j) in the array

Such that

$$a[i] + a[j] = K$$

$$i \neq j$$

0 1 2 3 4  
2, 7, 11, 15, 7

$$K = 18 \rightarrow (1, 2) \Rightarrow \text{True}$$

$$K = 14 \rightarrow (1, 4) \Rightarrow \text{True}$$

$$K = 20 \rightarrow \text{False}$$

0 1 2 3  
i j

for (i=0; i < N; i++) {

(0,0), (0,1), (0,2), (0,3)  
(1,0), (1,1), (1,2), (1,3)  
(2,0), (2,1), (2,2), (2,3)  
(3,0), (3,1), (3,2), (3,3)

for (j=i+1; j < N; j++) {  
if (a[i] + a[j] == K)  
return true;  
}

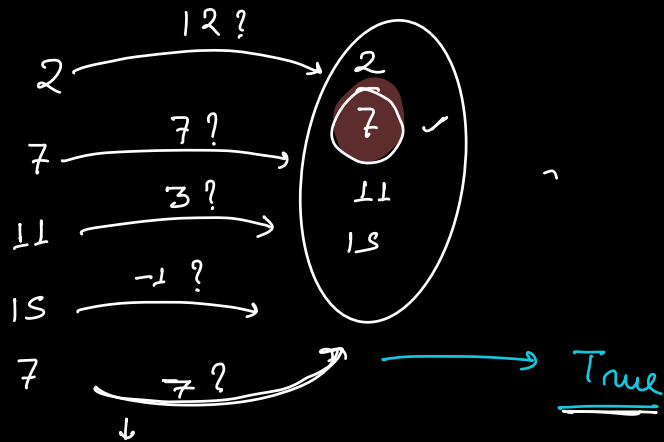
TC:  $O(N^2)$

$a[i] + a[j] = K$   
 $\Rightarrow a[j] = K - a[i]$  ] Check if a[j] is present

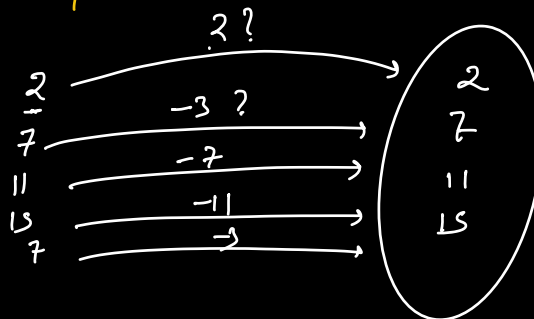
$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 2, & 7, & 11, & 15, & 7 \end{matrix}$

$$a[i] = \boxed{K - a[i]}$$

$$K = 14$$



$\begin{matrix} 0 & 1 & 2 & 3 & 4 \\ 2, & 7, & 11, & 15, & 7 \end{matrix}$   
 $K = 4$

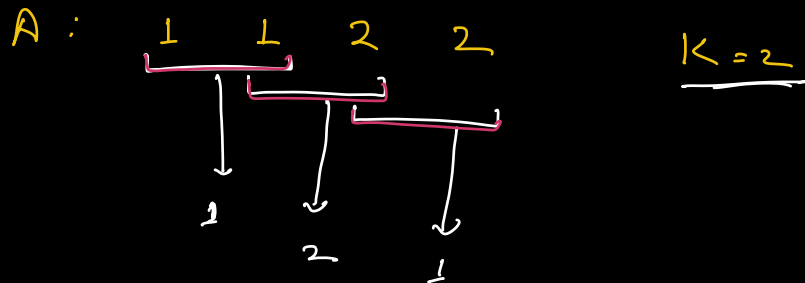


Step I Check if  $K - a[i]$   
 is present in set

Step II insert  $a[i]$  to set

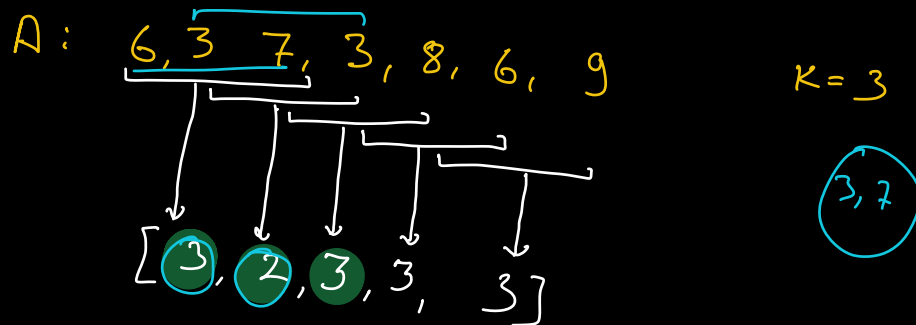
What if  $\Rightarrow$  Think 30 min

Q Given  $N$  array elements. Calculate the no. of distinct elements in every window of size  $K$ .



return :  $[1, 2, 1]$

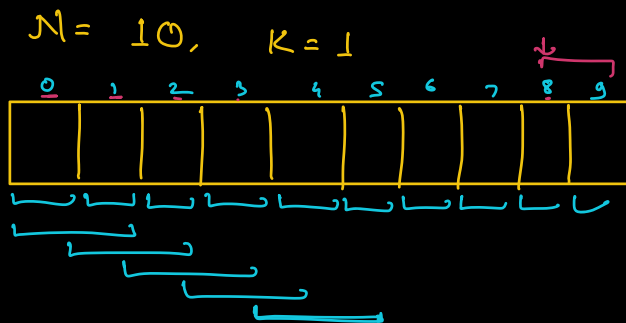
Quiz 1



$\Rightarrow$  For every window of size  $K \Rightarrow \underline{N-K+1}$

- Add all  $K$  elements to an empty set  $\Rightarrow K$
- Add size of the set to ans array.

Quiz



$\Rightarrow N \Rightarrow 10$

$\# \text{ iterations} = K(N-K+1)$

$K = N/2$

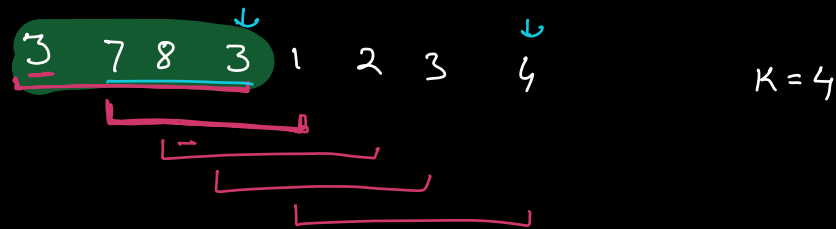
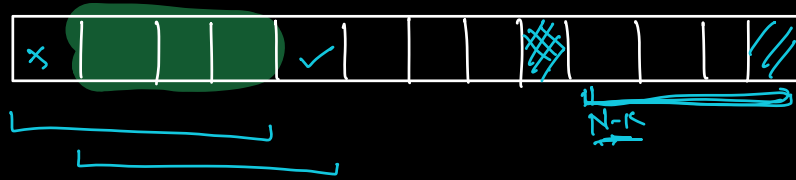
$\frac{N}{2} (N - \frac{N}{2} + 1)$

$\frac{N}{2} (\frac{N}{2} + 1)$

$O(N^2)$

(N)

K	Start of last window	# of window
1	0, N-1	N
2	N-2	N-1
3	N-3	N-2
$\vdots$	$\vdots$	$\vdots$
K	<u>N-K</u>	N-K+1



Map

3 : 1, 2, 1

3, 4, 4, 3, 4

4 : 1

1 : 1

2 : 1

(I)

Process the first window of size K  
 $\Rightarrow$  Build the freq map

(II)

Iterate over remaining windows

$\Rightarrow$  Remove 1st element of prev window

$\Rightarrow$  Add new element.

// Build the freq map

```
for (i=0; i<K; i++) {
```

```
    if (map.containsKey(A[i])) {
        map.put(A[i], map.get(A[i]) + 1);
    }
```

$\Rightarrow$  # iterations = K

```
    else
        map.put(A[i], 1);
}
```

// Sliding window

```
for (i=0; i<N-K; i++) {
```

// Remove A[i]

```
    map.put(A[i], map.get(A[i]) - 1);
```

```
    if (map.get(A[i]) == 0)
```

```
        map.remove(A[i]);
```

// Add A[i+K]

```
    if (map.containsKey(A[i+K])) {
```

```
        map.put(A[i+K], map.get(A[i+K]) + 1);
```

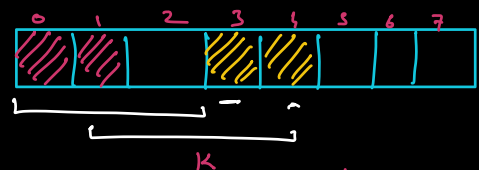
# iterations = N-K

```
    else
```

```
        map.put(A[i+K], 1);
```

```
}
```

Total # of iterations = K + N-K  $\Rightarrow$  N  $\Rightarrow$   $O(N)$   
 SC:  $O(N)$



Remove  
index

add  
index

$\rightarrow 0 \xleftarrow{K} 3$

$- 1 \xleftarrow{K} 4$

$2 \xleftarrow{K} 5$

$\vdots$

$i \xleftarrow{\quad} \underline{i+K}$

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Q Given an array. Find the length of largest  
sequence which can be rearranged to  
form a seq of consecutive no.

A: 100, (4), 200, (1), (3), (2)

4, 1, 3, 2  $\Rightarrow$  1, 2, 3, 4  
 $\Rightarrow$  4.

Quiz

-1, 8, 2, 7, 1, 4, 9, 3

1, 2, 3, 4  $\Rightarrow$  4  
7, 8, 9

Quiz

5, 9, 100, 1, -1, 2, 3, 99, 98, 11, 101, 15, 102

1, 2, 3

100, 99, 98, 101, 102  $\Rightarrow$  5

-1, 8, 2, 7, 1, 4, 9, 3

-1, 1, 2, 3, 4, 7, 8, 9  
1 2 3 1 2 3

Max  $\neq$  4

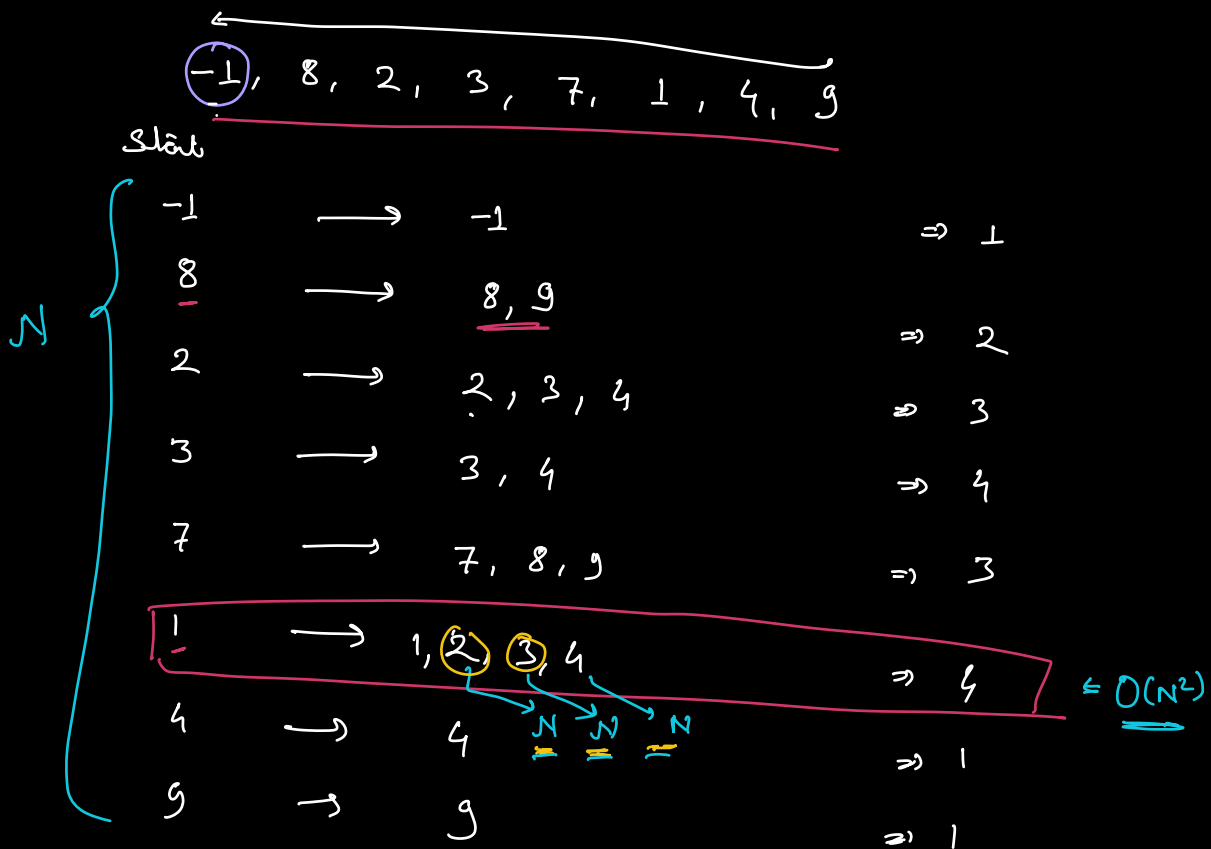
3, 100, 99, 4, 100, 3, 2, 101, 102

2, 3, 3, 4, 99, 100, 100, 101, 102  
C 1 2 2 3 1 2 2 3 4

Man ✗ ✗ ✗ 4

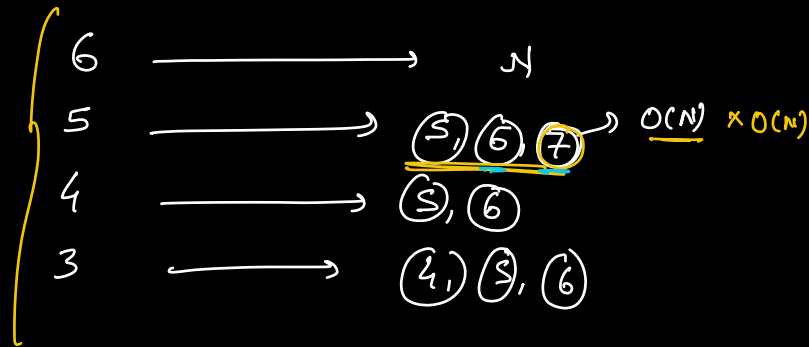
TC:  $O(N \log N) + O(N) \Rightarrow O(N \log N)$

SC: Depends on sorting algo  
(Extra)



TC:  $O(N^3)$

6, 5, 4, 3, 2, 1



// Build the set

Set = {}

for (i=0; i<N; i++) {

Set.add(a[i]);

}

} O(N)

// Count sq length for every element as a start

ans = 0;

~~for (i=0; i<N; i++) {~~ for every a[i] in Set:

length = 1; K = 1;

if (!Set.contains(a[i]-1)) {

while (Set.contains(a[i] + K)) {  
length++;  
K++;  
}  
ans = max(length, ans);

}

}



1, 2, 2, 3, 4, 5, 5, 6, 7, 8, 9, 10, 11

$\Rightarrow$  ①  $\Rightarrow$  2, 3, 4, 5, 6, ⑦ 8, 9, 10, 11, ~~12~~  $\Rightarrow O(N)$   
 $\Rightarrow$  ②  $\Rightarrow$  3, 4, 5, 6, 7, 8, 9, 10, 11, ~~12~~  $\Rightarrow O(N)$   
 $\Rightarrow$  ③  $\Rightarrow$  3, 4, 5, 6, 7, 8, 9, 10, 11, ~~12~~  $\Rightarrow O(N)$

$O(N^2)$

① 2, 3, 4, 5, 6, 7, 8, 9, 10, 11

6, 6, 6, 6, 6, 6, 7, 8, 9, 10, 11, 12

① for any  $a[i]$ ,

if  $a[i] - 1$  is present.

$\Rightarrow$  Stop checking the length of seq starting from  $a[i]$

②

Iterate over set (Not array)  
to avoid duplicate start point.

x 6, 6, 6, 6, 6, 6, 7, 8, 9, 10, 11, 12

9 → is 8 present? →  $O(1)$

10 → is 9 present?  $O(1)$

11 → is 10 present?  $O(1)$

8 → is 7 present?  $O(1)$

7 →

6 → is 5 present? x

7, 8, 9, 10, 11, 12, ~~6~~

12 → is 11 present?

9, 10, 11  
8, 7, 6  
12

# of iterations =  $2N$

↑ Because every element being visited at most 2 times.

TC :  $O(N)$

SC :  $O(N)$

TC :  $N^3 \longrightarrow \begin{pmatrix} N^2 \\ N \end{pmatrix} \longrightarrow \begin{pmatrix} N \\ N \end{pmatrix}$

SC :

1

