

$$\textcircled{5} \begin{bmatrix} 3 & 6 & 1 & | & 1 \\ 5 & 5 & 3 & | & 1+\lambda \\ 6+\lambda & 4 & 6-\lambda & | & 3 \end{bmatrix}$$

$$\begin{aligned} \det(A) &= 15(6-\lambda^2) + 12(6+\lambda^2) + 20 \\ &\quad - 5(6+\lambda^2) - 36 - 30(6-\lambda^2) \\ &= -15(6-\lambda^2) + 12(6+\lambda^2) - 16 = \\ &= 28\lambda^2 - 106 + 78 = 28\lambda^2 - 28 \\ &= 28(\lambda^2 - 1) = 0 \quad (\lambda \in \mathbb{Z}) \end{aligned}$$

$$\begin{aligned} \left| \begin{bmatrix} 1 & 5 & 1 \\ 1+\lambda & 5 & 3 \\ 3 & 4 & 6-\lambda^2 \end{bmatrix} \right| &= 5(6-\lambda^2) + 54 \cancel{12} (1+\lambda) \\ &\quad - 15 - 12 - 6(6-\lambda^2)(1+\lambda) = \\ &= 6\lambda^3 + \lambda^2 - 32\lambda + 25 \\ &= (\lambda-1)(6\lambda^2 + 7\lambda - 25) = \\ &= (\lambda-1)(6\lambda^2 - 25) \\ &= (\lambda-1)(-\lambda^2 + 3) \end{aligned}$$