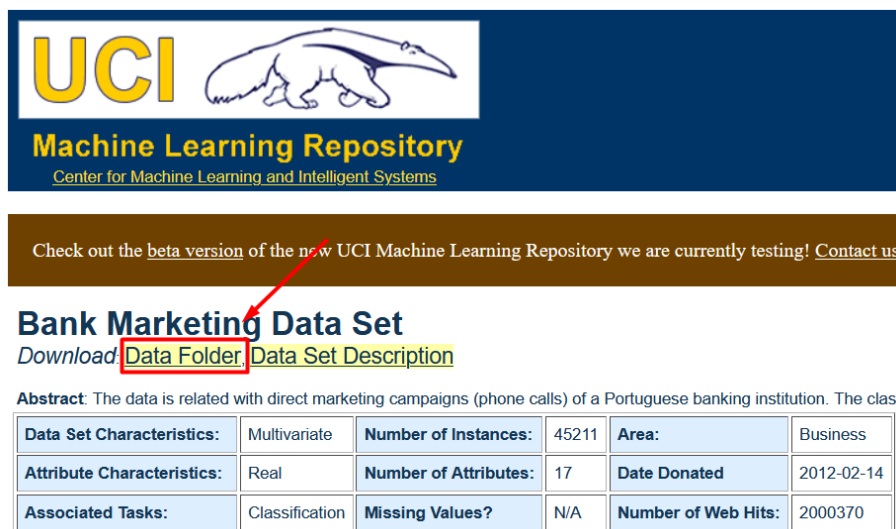


Chapter Project (Regression Model)

Previously in M1-FA1, we installed R and R studio to get started with R programming. Using R studio, we were tasked to run an R script using a provided dataset and observe the number of data, and percentage of train and test datasets, list all variables and identify qualitative and quantitative attributes. For this assessment, we are tasked with creating a simple multiple regression model using R Studio.

I. Downloading the bank.zip file

To get started, we had to download our dataset from the provided link, <https://archive.ics.uci.edu/ml/datasets/Bank+Marketing>. First, we had to click on *Data Folder*, then it directed us to another webpage listing two zipped files and a link to the parent directory.



UCI Machine Learning Repository
Center for Machine Learning and Intelligent Systems

Check out the [beta version](#) of the new UCI Machine Learning Repository we are currently testing! [Contact us](#)

Bank Marketing Data Set

Download: [Data Folder](#) [Data Set Description](#)

Abstract: The data is related with direct marketing campaigns (phone calls) of a Portuguese banking institution. The class

Data Set Characteristics:	Multivariate	Number of Instances:	45211	Area:	Business
Attribute Characteristics:	Real	Number of Attributes:	17	Date Donated	2012-02-14
Associated Tasks:	Classification	Missing Values?	N/A	Number of Web Hits:	2000370

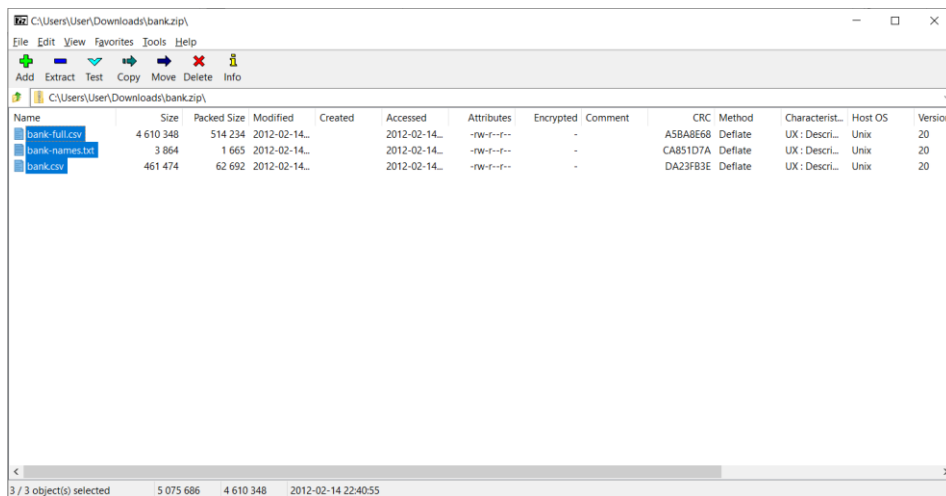
Our dataset should be inside the *bank.zip* file, so we clicked on it to start downloading.

Index of /ml/machine-learning-databases/00222

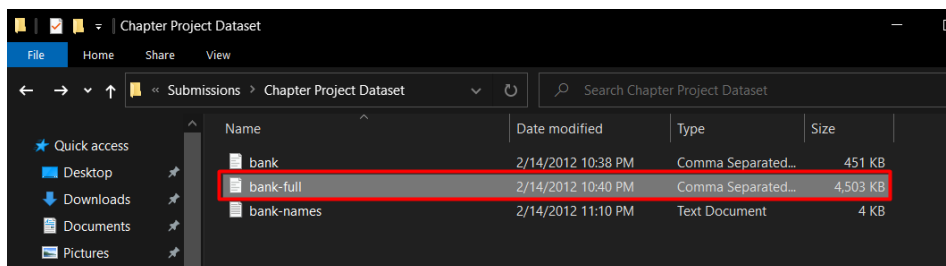
- [Parent Directory](#)
- [bank-additional.zip](#)
- [bank.zip](#) ←

Apache/2.4.6 (CentOS) OpenSSL/1.0.2k-fips SVN/1.7.14 Phusion_Passenger/4.0.53 mod_perl/2.0.11

After it finished downloading, we extracted the zipped file using a file archiver, such as 7-zip, to extract the contents to a folder of our choosing.

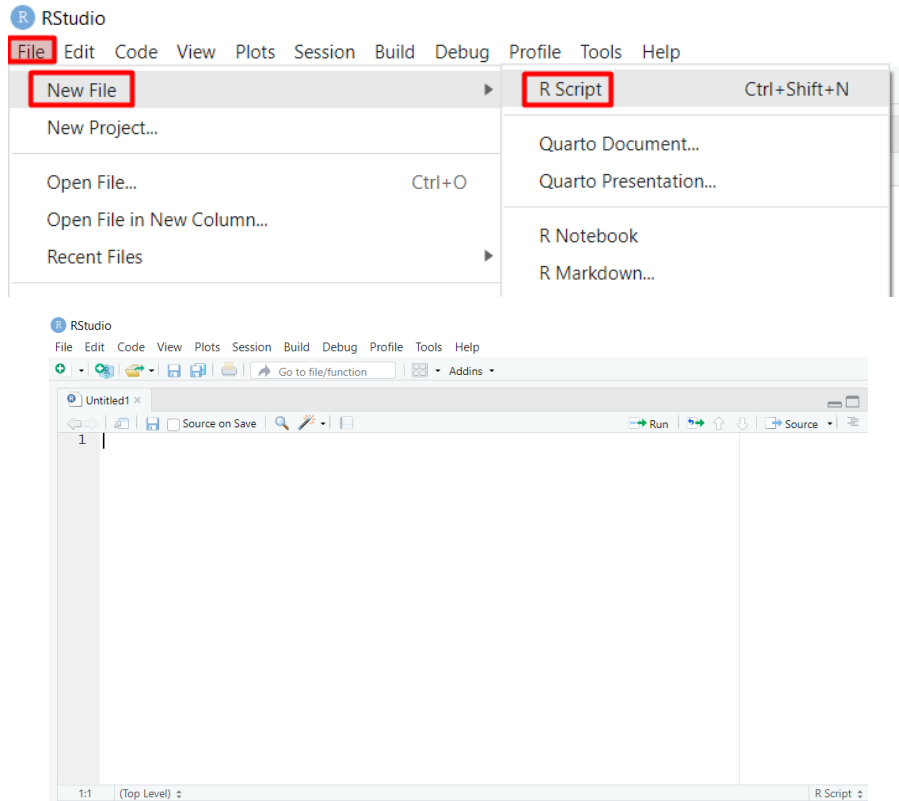


In this assessment, we would be using the *bank-full* csv file as our dataset in creating the multiple regression model using R Studio.



II. Preparing the bank-full dataset

To begin, we first opened R Studio and clicked on File > New File > R Script or simply enter the shortcut Ctrl + Shift + N to open a blank new R Script.



Inside our Rscript, we will first install the necessary libraries. These libraries will be useful in mapping variables, plotting, and creating our linear regression model.

```
install.packages("ggplot2")
install.packages("dplyr")
install.packages("caTools")    # For Linear regression

library(caTools)
library(ggplot2)
library(dplyr)
```

Then, we will read the bank-full.csv data set and print the first six rows of the data frame to confirm if the data was properly attached in R Studio. After, we use the *summary* function to summarize the values in the data frame.

```
# Read the bank-full.csv data set
data <- read.csv("C:/Users/User/Documents/Mapua/Third Year - 3rd Term/CS174 BM2 DATA SCIENCE 4/Submissions/Chapter Project Dataset/bank-full.csv", sep=";")

print(head(data))

# ask for a summary of the data
summary(data)
```

```
> print(head(data))
  age      job marital education default balance housing loan contact day month duration campaign
1  58 management married tertiary      no    2143      yes no unknown  5  may      261         1
2  44 technician single secondary      no     29      yes no unknown  5  may      151         1
3  33 entrepreneur married secondary      no     2      yes yes unknown  5  may       76         1
4  47 blue-collar married unknown      no   1506      yes no unknown  5  may       92         1
5  33 unknown single unknown      no     1      no no unknown  5  may      198         1
6  35 management married tertiary      no    231      yes no unknown  5  may      139         1
 pdays previous poutcome y
1    -1         0 unknown no
2    -1         0 unknown no
3    -1         0 unknown no
4    -1         0 unknown no
5    -1         0 unknown no
6    -1         0 unknown no
```

```
> # ask for a summary of the data
> summary(data)
   age      job      marital      education      default
Min.   :18.00   Length:45211   Length:45211   Length:45211   Length:45211
1st Qu.:33.00   Class :character   Class :character   Class :character   Class :character
Median :39.00   Mode  :character   Mode  :character   Mode  :character   Mode  :character
Mean   :40.94
3rd Qu.:48.00
Max.   :95.00
 balance      housing      loan      contact      day
Min.   : -8019   Length:45211   Length:45211   Length:45211   Min.   : 1.00
1st Qu.:   72   Class :character   Class :character   Class :character   1st Qu.: 8.00
Median :  448   Mode  :character   Mode  :character   Mode  :character   Median :16.00
Mean   : 1362
3rd Qu.: 1428
Max.   :102127
 month      duration      campaign      pdays      previous
Length:45211   Min.   : 0.0   Min.   : 1.000   Min.   : -1.0   Min.   : 0.0000
Class :character   1st Qu.:103.0   1st Qu.: 1.000   1st Qu.: -1.0   1st Qu.: 0.0000
Mode  :character   Median :180.0   Median : 2.000   Median : -1.0   Median : 0.0000
Mean   :258.2   Mean   : 2.764   Mean   : 40.2   Mean   : 0.5803
3rd Qu.:319.0   3rd Qu.: 3.000   3rd Qu.: -1.0   3rd Qu.: 0.0000
Max.   :4918.0   Max.   :63.000   Max.   :871.0   Max.   :275.0000
 poutcome      y
Length:45211   Length:45211
Class :character   Class :character
Mode  :character   Mode  :character
```

Before creating the multiple regression model, we noted the attribute information on the site <https://archive.ics.uci.edu/ml/datasets/Bank+Marketing> and considered three input variables as our independent variable and one dependent variable for our analysis.

Our three input variables were the following:

- **Campaign** - number of contacts performed during the direct marketing campaign of a Portuguese banking institute and for this client (numeric, includes last contact)
- **Balance** - the amount of money in a bank account at a given time (numeric)
- **Previous** - number of contacts performed before this campaign and for this client (numeric)

We noticed that the supposed output/dependent variable in the dataset was $y = \text{has the client subscribed to a term deposit?}$ (binary: 'yes', 'no'). However, regression models require the dependent variable to be numerical. So, instead of y , we used **duration** as it highly affects the output target (e.g., if $\text{duration}=0$, then $y=\text{'no'}$). If the duration is more than 0, it would mean the client subscribed to a term deposit.

Moving forward with these variables, we used the `cor` function to determine the correlation between the four variables.

```
# correlation of duration, campaign, balance, and previous
print(cor(data[, c('duration', 'campaign', 'balance', 'previous')]))
```

Which gave the following table:

	duration	campaign	balance	previous
duration	1.000000000	-0.08456950	0.02156038	0.001203057
campaign	-0.084569503	1.00000000	-0.01457828	-0.032855290
balance	0.021560380	-0.01457828	1.00000000	0.016673637
previous	0.001203057	-0.03285529	0.01667364	1.00000000

First, correlation ranges from -1 to 1. It gives us an indication on two things:

1. The direction of the relationship between the 2 variables
2. The strength of the relationship between the 2 variables

Looking at the table, duration and campaign has a negative correlation implying that the two variables vary in opposite directions, that is, if a variable increases the other decreases and vice versa. However, as the correlation is closer to 0 than to 1, it may also indicate that the two variables are independent, that is, as one variable increases, there is no tendency in the other variable to either decrease or increase. The same goes for the balance and previous variables, despite having a positive correlation.

III. Creating the Multiple Regression Model

Now that we have attached our dataset, we will now be using the *split* function to split the dataset into 80% for training and 20% for testing.

```
> # splitting of data
> split <- sample.split(data, SplitRatio = 0.8)
> split
[1] TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE FALSE TRUE TRUE TRUE
TRUE TRUE TRUE FALSE FALSE
```

The train dataset gets all the data points that are 'TRUE' and similarly the test dataset gets all the data points which are 'FALSE'.

```
> train <- subset(data, split == "TRUE")
> test <- subset(data, split == "FALSE")
```

We then display the training and testing datasets using the *dim* and *print* functions.

```
> dim(train)
[1] 34574 17
> print(head(train))
  age      job marital education default balance housing loan contact day month duration campaign pdays
1  58 management married tertiary      no   2143      yes  no unknown  5  may      261        1    -1
2  44 technician single secondary      no    29      yes  no unknown  5  may     151        1    -1
3  33 entrepreneur married secondary      no     2      yes  yes unknown  5  may     76         1    -1
4  47 blue-collar married unknown      no  1506      yes  no unknown  5  may     92         1    -1
5  33 unknown single unknown      no     1      no  no unknown  5  may    198         1    -1
6  35 management married tertiary      no    231      yes  no unknown  5  may    139         1    -1
previous poutcome y
1      0 unknown no
2      0 unknown no
3      0 unknown no
4      0 unknown no
5      0 unknown no
6      0 unknown no
>
> dim(test)
[1] 10637 17
> print(head(test))
  age      job marital education default balance housing loan contact day month duration campaign pdays
7  28 management single tertiary      no   447      yes  yes unknown  5  may     217         1    -1
9  58 retired married primary      no   121      yes  no unknown  5  may     50         1    -1
16 51 retired married primary      no   229      yes  no unknown  5  may    353         1    -1
17 45 admin. single unknown      no    13      yes  no unknown  5  may     98         1    -1
24 25 services married secondary      no    50      yes  no unknown  5  may    342         1    -1
26 44 admin. married secondary      no   -372      yes  no unknown  5  may    172         1    -1
previous poutcome y
7      0 unknown no
9      0 unknown no
16     0 unknown no
17     0 unknown no
24     0 unknown no
26     0 unknown no
```

After, we used the `lm` function to fit linear models to data frames in the R Language.

```
> model <- lm(duration ~ campaign + balance + previous, data = train)
> summary(model)

Call:
lm(formula = duration ~ campaign + balance + previous, data = train)

Residuals:
    Min       1Q   Median       3Q      Max
-336.7  -153.3   -78.2    58.1  3625.2

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  2.747e+02  1.966e+00  139.729 < 2e-16 ***
campaign     -6.978e+00  4.406e-01  -15.836 < 2e-16 ***
balance       1.557e-03  4.428e-04    3.516 0.000439 ***
previous     -1.450e-01  5.693e-01   -0.255 0.798978
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 254.1 on 34570 degrees of freedom
Multiple R-squared:  0.007617, Adjusted R-squared:  0.007531
F-statistic: 88.45 on 3 and 34570 DF, p-value: < 2.2e-16
```

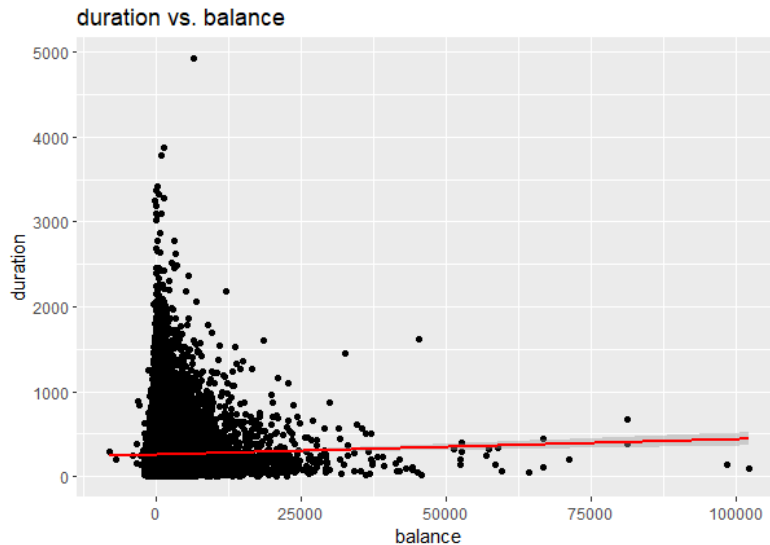
The output reveals three sections: residuals, coefficients, and performance measures. The **residuals** section summarizes the residuals, the error between the prediction of the model and the actual results. It is noted that smaller residuals are better. In the **coefficients** section, for each variable and the intercept, a weight is produced, and that weight has other attributes like the standard error, a t-test value and significance. Lastly, under the **performance** section, three sets of measurements are provided: residual standard error, multiple r-square, and f-statistic.

- For the residuals section, we can see that the multiple regression model has a range of -336.7 to 3625.2.
- Coefficients:
 - (Intercept): The intercept is the left over when you average the independent and dependent variable. The intercept of 274.7 is the estimated mean Y value when all Xs are zero. This would be the estimated duration for someone with campaign, balance, and previous of 0.
 - Campaign: This means that for every second the call lasts, you should expect to get a decrease amount of ~7 contacts performed during the marketing campaign.
 - Balance: As the call duration increases, the balance of the person increases by 0.001557.
 - Previous: For every second of the call, the number of contacts decrease by 0.145.
- Performance Measures:
 - Residual Standard Error: This gives us an idea of how far observed duration (y value) are from the predicted or fitted duration (the y-hats). A standard error of 254.1 is not that bad.
 - Multiple / Adjusted R-Square: The R-squared is bad for this model since we could only reach 0.7617%. Which means a variation of duration cannot be explained by our model using campaign, balance, and previous.

- F-Statistic: With a p value of 2.2e-16, our model does not seem to be doing anything.

IV. Making the Regression Graph for the Multiple Regression Model

This section includes the regression graph for each correlation between each independent variable (*balance*, *campaign*, and *previous*) and the dependent variable *duration*. The correlation between the variables is described by the graph through a regression line, which also represents the numerical correlation derived from the correlation table from the [section “II. Preparing the bank-full dataset”](#).



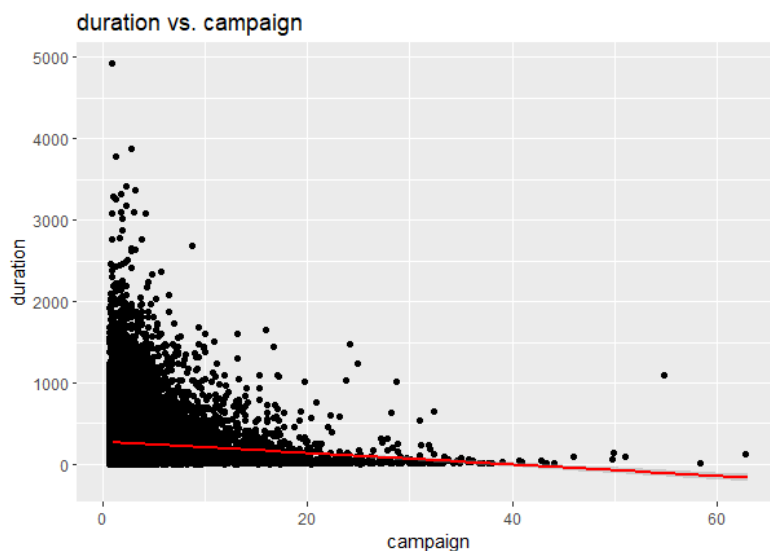
According to the correlation table, the variables *duration* and *balance* have a **correlation rate of 0.02156038**, indicating a positive relationship between the two variables.

	duration	campaign	balance	previous
duration	1.000000000	-0.08456950	0.02156038	0.001203057
campaign	-0.084569503	1.000000000	-0.01457828	-0.032855290
balance	0.021560380	-0.01457828	1.000000000	0.016673637
previous	0.001203057	-0.03285529	0.01667364	1.000000000

The values on the correlation table are further validated by the *duration vs. balance* graph as the regression line on the scatterplot indicates a **low positive correlation** between the two variables. This relationship is somewhat evident as the regression line slightly increases from its originating to its concluding point. Therefore, the observation that a weak positive correlation

Commented [KACS1]: Looking at the table, duration and campaign has a negative correlation implying that the two variables vary in opposite directions, that is, if a variable increases the other decreases and vice versa. However, as the correlation is closer to 0 than to 1, it may also indicate that the two variables are independent, that is, as one variable increases, there is no tendency in the other variable to either decrease or increase. The same goes for the balance and previous variables, despite having a positive correlation.

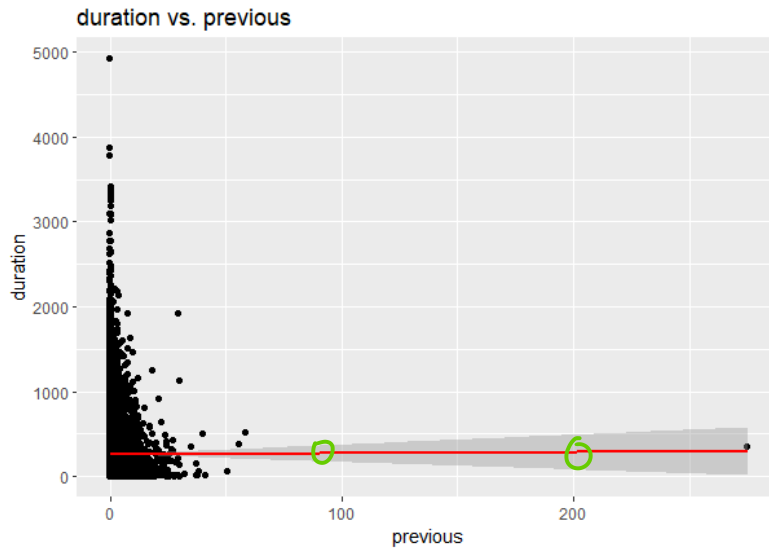
nearing 0 or 1 indicates a relationship between independent variables, where neither variable influences each other, is confirmed.



In contrast, the variables *duration* and *campaign* have a **correlation rate of -0.084569503**, indicating a negative relationship between the two variables.

	duration	campaign	balance	previous
duration	1.000000000	-0.08456950	0.02156038	0.001203057
campaign	-0.084569503	1.000000000	-0.01457828	-0.032855290
balance	0.021560380	-0.01457828	1.000000000	0.016673637
previous	0.001203057	-0.03285529	0.01667364	1.000000000

The values on the correlation table are further validated by the *duration vs. campaign* graph as the regression line on the scatterplot indicates a **low negative correlation** between the two variables. This relationship is clear as the regression line decreases from its originating to its concluding point. Furthermore, the weak negative correlation produced by the graph confirms the observation that a directly proportional relationship exists between the independent and dependent variables.



Lastly, the variables *duration* and *previous* have a **correlation rate of 0.001203057**—indicating an extremely weak positive relationship between the two variables, as evidenced by the nearing 0 correlation rate.

	duration	campaign	balance	previous
duration	1.000000000	-0.08456950	0.02156038	0.001203057
campaign	-0.084569503	1.00000000	-0.01457828	-0.032855290
balance	0.021560380	-0.01457828	1.00000000	0.016673637
previous	0.001203057	-0.03285529	0.01667364	1.000000000

The values on the correlation table are further validated by the *duration vs. previous* graph as the regression line on the scatterplot portrays an **extremely low positive correlation** between the two variables. The regression line may not indicate such a correlation given that its slope is not as evident as the first regression line. This relationship is somewhat clear as the regression line increases at the two highlighted points from its originating to its concluding point. The weak positive correlation produced by the graph confirms the observation that two independent variables have no effect on each other with regards to increasing or decreasing data. Another observation as evidenced by the horizontal regression line is that a correlation between the *duration* and *previous* variables does not exist as the data neither increases nor decreases. Furthermore, this indication also shows that no correlation exists between the *duration* and *previous* variable.

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