

## Note

In mathematics, you must be able to represent intervals and identify smaller sections of a relation or a set of numbers.

You have used the following inequality symbols:

$>$  greater than

$<$  less than

$\geq$  greater than or equal to

$\leq$  less than or equal to

Linear Inequality is an inequality that contains an algebraic expression of degree 1

For example:

$$5x + 3 \leq 6x - 2$$

We solve inequality much the same as we do equations.

### Ex. 1 - Solve an Inequality

Solve for all values of  $x$ .

$$4x + 3 \geq 15$$

$$4x \geq 15 - 3$$

$$4x \geq 12$$

$$\frac{4x}{4} \geq \frac{12}{4}$$

$$x \geq 3$$

We can also write out solution using set notation.

$$\{x \in \mathbb{R} \mid x \geq 3\}$$

$$x \in [3, \infty)$$

Solve for all values of  $x$ .

$$7 - 3x \leq -2$$

$$-3x \leq -2 - 7$$

$$-3x \leq -9$$

$$\frac{-3x}{-3} \leq \frac{-9}{-3}$$

$$x \geq 3$$

When dividing or multiplying by a negative constant, we need to reverse the inequality sign

$$\{x \in \mathbb{R} \mid x \geq 3\}$$

$$x \in [3, \infty)$$

**Ex. 3 - Solving a Double Inequality**

Solve for all values of x

$$30 \leq 3(2x + 4) - 2(x + 1) \leq 46$$

$$30 \leq 6x + 12 - 2x - 2 \leq 46$$

$$30 \leq 4x + 10 \leq 46$$

$$30 - 10 \leq 4x + 10 - 10 \leq 46 - 10$$

$$20 \leq 4x \leq 36$$

$$\frac{20}{4} \leq \frac{4x}{4} \leq \frac{36}{4}$$

$$5 \leq x \leq 9$$