F.E som I ROV (CGS)

Appliped maths - I

D: PH (April Exam) 181

Con. 6865-13.

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(REVISED COURSE)

GS-5103

(3 Hours)

[Total Marks: 80

- N.B. (1) Question No. 1 is compulsory.
 - (2) Attempt any three questions from Question Nos. 2 to Questions No. 6
 - (3) Figures to the right indicate full marks.

1. (a) If
$$\cos hx = \sec \theta$$
 prove that $x = \log (\sec \theta + \tan \theta)$.

(b) If
$$u = \log (x^2 + y^2)$$
, prove that $\frac{\partial^2 u}{\partial x \partial y} = \frac{\partial^2 u}{\partial y \partial x}$

(c) If
$$x = r \cos \theta$$
, $y = r \sin \theta$. Find $\frac{\partial(x, y)}{\partial(r, \theta)}$.

- (d) Expand $\log (1 + x + x^2 + x^3)$ in powers of x upto x^8 .
- (e) Show that every square matrix can be uniquelly expressed as sum of a symmetric and a Skew-symmetric matrix.
- (f) Find nth order derivative of $y = \cos x$. $\cos 2x$. $\cos 3x$.
- 2. (a) Solve the equation $x^6 i = 0$.
 - (b) Reduce matrix A to normal form and find its rank where :-

$$A = \begin{bmatrix} 1 & 2 & 3 & 2 \\ 2 & 3 & 5 & 1 \\ 1 & 3 & 4 & 5 \end{bmatrix}$$

(c) State and prove Euler's theorem for a homogeneous function in two variables and 8

hence find
$$x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$$
 where $u = \frac{\sqrt{x} + \sqrt{y}}{x + y}$

- 3. (a) Determine the values of λ so that the equations x + y + z = 1; $x + 2y + 4z = \lambda$; 6 $x + 4y + 10z = \lambda^2$ have a solution and solve them completely in each case.
 - (b) Find the stationary values of
 - $x^3 + y^3 3axy$, a > 0. (c) Separate into real and imagianary parts tan^{-1} (e^{i0}).

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4. (a) If
$$x = u \cos v$$
, $y = u \sin v$

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Prove that
$$\frac{\partial(x,y)}{\partial(u,v)} \cdot \frac{\partial(u,v)}{\partial(x,y)} = 1$$
.

- (b) If $\tan [\log (x + iy)] = a + ib$, prove that $\tan [\log (x^2 + y^2)] = \overline{(1 a^2 b^2)}$ where 6 $a^2 + b^2 \neq 1$.
- (c) Using Gauss-Siedel iteration method, solve

$$10x_1 + x_2 + x_3 = 12$$

$$2x_1 + 10x_2 + x_3 = 13$$

$$2x_1 + 2x_2 + 10x_3 = 14$$

upto three iterations.

(a) Expand $\sin^7 \theta$ in a series of sines of multiples of θ .

(b) Evaluate
$$\lim_{x \to 0} \frac{(x^x - x)}{(x - 1 - \log x)}$$

(c) If $y^{1/m} + y^{-1/m} = 2x$, prove that

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$$y^{1/m} + y^{-1/m} = 2x$$
, prove that

$$(x^2 - 1) y_{n+2} + (2n + 1) xy_{n+1} + (n^2 - m^2) y_n = 0.$$

(a) Examine the following vectors for linear dependence/Independence.

$$X_1 = (a, b, c), X_2 = (b, c, a), X_3 = (c, a, b)$$
 where $a + b + c \neq 0$.

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(b) If
$$z = f(x, y)$$
, $x = e^{u} + e^{-v}$, $y = e^{-u} - e^{v}$, prove that

$$\frac{\partial z}{\partial u} - \frac{\partial z}{\partial v} = x \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y}$$

(c) Fit a straight line to the following data and estimate the production in the year 1957.

Year:	1951	1961	1971	1981	1991
Production in the					
Thousand tons:	10	12	08	10	13