Erratum: Composite Spin and Quadrupole Wave in the Ordered Phase of $\operatorname{Tb}_{2+x}\operatorname{Ti}_{2-x}\operatorname{O}_{7+y}$ [SPIN 5, 1540003 (2015)]

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We have become aware of an error in Eq. (1) in the published paper. It should read

$$|\pm 1\rangle_{\rm D} = A|\mp 4\rangle \pm B|\mp 1\rangle + C|\pm 2\rangle \mp D|\pm 5\rangle$$
.

This is an exchange of the ground doublet states $|\pm 1\rangle_D$, which is needed to use the same phases $\phi_{r,r'}$ of Eq. (13) as those of Ref. [1]. It affects six signs of Eqs. (6) and (7) as follows:

$$J_x = J_y = 0, \ J_z = -(4A^2 + B^2 - 2C^2 - 5D^2)\sigma^z = -3.40\sigma^z$$

and

$$\begin{split} \frac{1}{2}[3J_z^2 - J(J+1)] &= 3A^2 - \frac{39}{2}B^2 - 15C^2 + \frac{33}{2}D^2 = 3.05 \;, \\ \frac{\sqrt{3}}{2}[J_x^2 - J_y^2] &= \left(-\frac{21\sqrt{3}}{2}B^2 + 9\sqrt{10}AC\right)\sigma^x = 3.00\sigma^x, \\ \frac{\sqrt{3}}{2}[J_xJ_y + J_yJ_x] &= -\left(-\frac{21\sqrt{3}}{2}B^2 + 9\sqrt{10}AC\right)\sigma^y = -3.00\sigma^y, \\ \frac{\sqrt{3}}{2}[J_zJ_x + J_xJ_z] &= -\left(3\sqrt{30}BC + 9\sqrt{\frac{33}{2}}AD\right)\sigma^x = -8.16\sigma^x, \\ \frac{\sqrt{3}}{2}[J_yJ_z + J_zJ_y] &= -\left(3\sqrt{30}BC + 9\sqrt{\frac{33}{2}}AD\right)\sigma^y = -8.16\sigma^y \;. \end{split}$$

These errors do not affect any other results and conclusions of the paper. The error corrected version of [SPIN 5, 1540003 (2015)] is Ref. [2].

^[1] S. Onoda and Y. Tanaka, Phys. Rev. B 83, 094411 (2011).

^[2] H. Kadowaki, H. Takatsu, T. Taniguchi, B. Fåk, and J. Ollivier, Composite Spin and Quadrupole Wave in the Ordered Phase of $Tb_{2+x}Ti_{2-x}O_{7+y}$, arXiv:1505.00503(v5), which is the error corrected version of [SPIN 5, 1540003 (2015)].