#### **OPTIMIZATION PROBLEM FORMULATION**

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#### **PROBLEM**

To produce  $100 \, kmol/h$  of n-buthyl acetate (AcBu), through the reaction:

$$BuOH + AcAc \leftrightharpoons BuAc + H_2O$$
  
 $Buthanol Acetic acid H^+ Buthyl acetate Water$ 

The kinetics is defined by the Langmuir-Hinshelwood-Hougen-Watson equation (M-LHHW). Sources (Gangadwala, Mankar, & Mahajani, 2003) (The Dow Chemical Company®)

$$r_{i} = v_{i} \, M_{cat} K_{f} K_{s,AcH} K_{s,BuOH} \frac{a_{AcH} \, a_{BuOH} - \frac{1}{K_{a}} a_{BuAc} \, a_{H2O}^{\alpha}}{\left(1 + K_{s,AcH} a_{AcH} + K_{s,BuOH} a_{BuOH} + K_{s,BuAc} a_{BuAc} + K_{s,H2O} a_{H2O}^{\alpha}\right)^{2}}$$

$K_f^0$	$14.0093\times10^6 kmol/kg/s$
$E_f$	$72.896 \times 10^3 \ kJ/kmol$
$K_a^0$	3.8207
$\boldsymbol{E_a}$	$-3.5817\times10^3\ kJ/kmol$
$K_{s,AcH}$	4.4521
$K_{s,BuOH}$	6.9211
$K_{s,BuAc}$	3.5995
$K_{s,H20}$	9.0304
α	2.00

A reactor for this process will be designed and it must accomplish with the lowest fixed costs and the lowest operating costs.

#### **REACTOR CONDITIONS**

Variable		Ranges
$F_{BuOH}$	Reactor's butanol feed flow	100 – 500 kmol/h
$F_{AcAc}$	Reactor's acetic acid feed flow	100 – 500 kmol/h
T	Operating temperature	50 − 120 °C
P	Operating pressure	$1-10 \ bar$

Inlet temperature

$$\circ$$
 25  $^{\circ}$ C

- Pressure
  - o 1-10 bar

1 – to avoid vacuum

10 - larger costs

• Optimal relationship between reactives flows (AcAc : BuOH)

1:5

## **RESTRICTIONS**

• Steam fraction = 0

• Outlet temperature bounds: 25 – 120 °C

BuAc = spec

Nombre de la restricción	Definición
Outlet temperature limit $T_{out}$ . Amberlyst 15 catalyst works up to 120 °C, keep temperature below of it avoids the formation of DBE	$T_{out} \le 120^{\circ} \text{C}$
No formation of steam inside the reactor. Outlet steam fraction $X_{vap}$ cero	$X_{vap} = 0$
Established prodution accomplishment	$F_{BuAc} = 120 \ kmol/h$

## **COSTS**

## **Fixed costs**

$$C_{fijos} = reactor cost = W \times \$_{catalyst} + C_{shell}$$

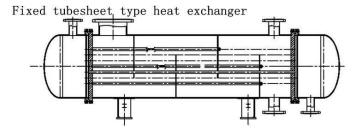
 $C_{fijos}$  Fixed costs

 $W_{cat}$  Catalyst weight

 $$_{catalizador}$$  Catalyst cost per kilogram

 $C_{shell}$  Reactor's shell costs

Reactor costs:



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$$Cp = F_P F_M F_L C_B$$

Fixed head

$$c_B = \exp(11.0545 - 0.9228 * \ln(A) + 0.09861 * \ln(A)^2)$$

$$F_M = a + \left(\frac{A}{100}\right)^b$$

$$a = 0$$

$$b = 0$$

$$F_M = 1$$

$$F_L = 1.05$$

$$F_P = 1$$

All for CE index of 394, now is 556.8

## **Operating costs**

Corresponding to the annual costs of the currents of power

$$C_{operación} = \frac{costo\ de}{las\ corrientes} = F_0 \cdot x_{BuOH}_0 \cdot \$_{BuOH} + F_0 \cdot x_{AcAc_0} \cdot \$_{AcAc}$$

$C_{operaci\'on}$	Operating costs per year
$F_0$	Reactor feed flow rate
$x_{BuOH_0}$	Inlet butanol composition
$\$_{BuOH}$	Cost of butanol per kilogram
$x_{AcAc_0}$	Inlet acetic acid composition
\$ <sub>AcAc</sub>	Cost of acetic acid per kilogra

The plant operates 330 days a year

#### **Optimization variables**

The variables chosen for optimization are the following:

 $F_{BuOH}$  Inlet butanol flow rate

 $F_{AcAc}$  Inlet acetic acid flow rate

T Reactor operating temperature

P Reactor operating pressure

 $x_{BuOH_0}$  Inlet butanol composition

 $x_{AcAc_0}$  Inlet acetic composition

# References

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