# Example of Reduction Techniques LCO

June 8, 2021

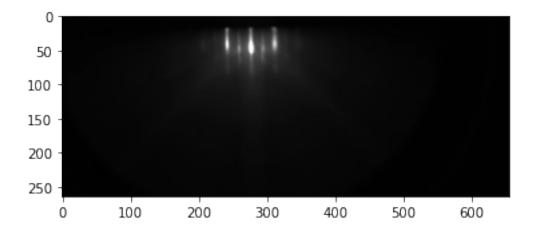
First load in the necessary packages.

```
[]: import numpy as np
import scipy
import cv2
import matplotlib
import matplotlib.pyplot
import pandas as pd
import nimfa
```

Next import one of the pictures and convert to black and white. This one was cropped in order to remove the portion of direct beam that does not go through the sample. I plotted the image below in order to make sure the cropping was appropriate before using this for the remainder of the frames.

```
[2]: photo = cv2.imread('d:/SampleVideos/Run20190816.121521_LCO/c01_0040.jpg')
    photo1 = cv2.cvtColor(photo, cv2.COLOR_BGR2GRAY)
    crop_photo = photo1[228:492, 0:656]
    matplotlib.pyplot.imshow(crop_photo, cmap = "gray")
```

[2]: <matplotlib.image.AxesImage at 0x19716f0d880>



Below I am importing all of the frames, converting them to a vector (using flatten) and then

combining them all in a pandas data frame.

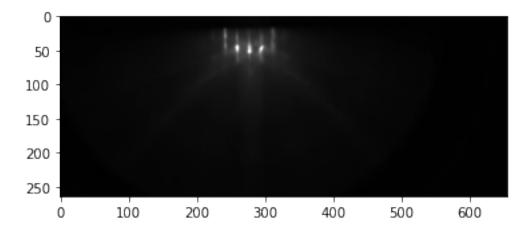
Next I can take the first frame and convert it back to the proper dimensions (272, 656) to be plotted.

```
[5]: frames.shape
  first = frames.iloc[1, ]
  a = first.values.reshape((264, 656))
  a.shape
```

[5]: (264, 656)

```
[6]: matplotlib.pyplot.imshow(a, cmap = "gray")
```

[6]: <matplotlib.image.AxesImage at 0x2214475b040>



Now I just want to take the frames that occured during the deposition (40:493) and divide by 255 to normalize.

```
[9]: #frames.shape
frames1 = frames.iloc[10:400,]
```

```
frames1.shape
frames1 = frames1.div(255)
```

[9]: (390, 173184)

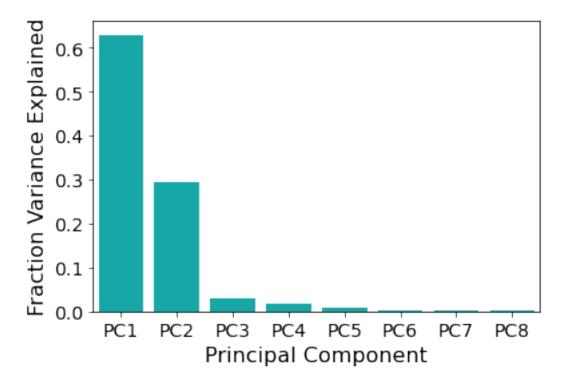
Below is how PCA is performed. The first eight principal components were examined.

```
[5]:
                       PC2
                                 PC3
                                           PC4
                                                     PC5
                                                               PC6
             PC1
                                                                         PC7
                                                                             \
    0 13.431299 4.504454 -2.088145 -0.270143 -1.184281
                                                          1.676010
                                                                   0.705404
    1 13.337527 4.438419 -1.905959 -0.389112 -1.099094 1.572648
                                                                    0.641521
    2 13.251833 4.276931 -1.847257 -0.281000 -0.974805 1.379608
                                                                   0.526152
    3 13.159721 4.164771 -1.707398 -0.350469 -0.888760 1.200875
                                                                   0.433295
    4 13.022094 3.976239 -1.641733 -0.394775 -0.779574 0.855548 0.212309
            PC8
    0 -0.160114
    1 - 0.171419
    2 -0.137706
    3 -0.145820
    4 -0.063056
```

Below is the fraction of variance explained and under that it is plotted with respect to the principal component in the form of a scree plot.

```
[7]: pca.explained_variance_ratio_
```

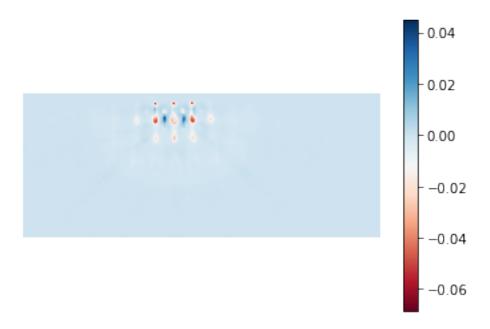
```
[7]: array([0.62954019, 0.29398366, 0.0306172, 0.01663218, 0.00810598, 0.00351248, 0.00164182, 0.00092873])
```



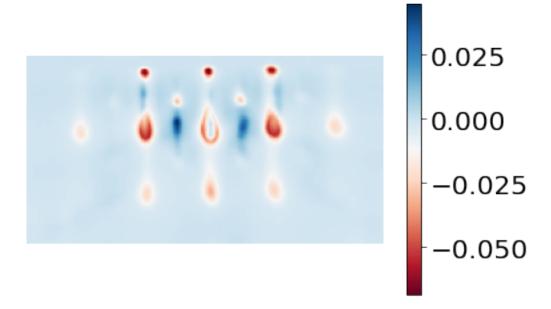
The first loading plot it shown below.

```
[8]: matplotlib.pyplot.imshow(pcnew.components_[0].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
```

[8]: (-0.5, 655.5, 263.5, -0.5)



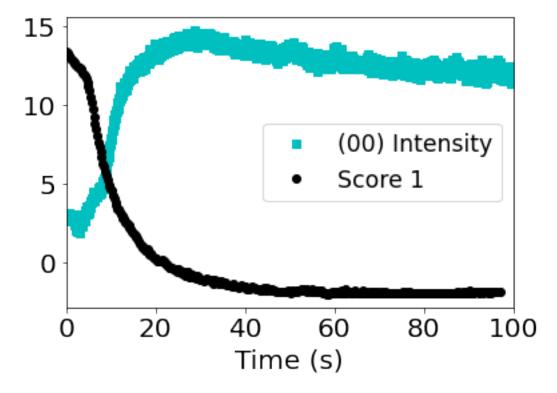
Below is a cropped version of the first loadings plot to see the detail better.



Next I define the time for each frame and add it to the dataframe so that the scores can be plotted with respect to time.

```
[9]: Time = np.arange(0.0, 97.5, .25)
    pc_df['Time'] = Time
    pc_df.head()
[9]:
                       PC2
                                 PC3
             PC1
                                            PC4
                                                      PC5
                                                                PC6
                                                                          PC7
       13.431299 4.504454 -2.088145 -0.270143 -1.184281
                                                           1.676010
                                                                     0.705404
    1 13.337527 4.438419 -1.905959 -0.389112 -1.099094 1.572648
                                                                    0.641521
    2 13.251833 4.276931 -1.847257 -0.281000 -0.974805
                                                          1.379608
                                                                     0.526152
    3 13.159721 4.164771 -1.707398 -0.350469 -0.888760 1.200875
                                                                    0.433295
    4 13.022094 3.976239 -1.641733 -0.394775 -0.779574 0.855548
                                                                    0.212309
            PC8
                Time
    0 -0.160114
                 0.00
    1 -0.171419
                 0.25
    2 -0.137706
                 0.50
    3 -0.145820
                 0.75
    4 -0.063056
                 1.00
```

The first set of scores are below. I also read in the intensity of the (00) RHEED spot to plot on top.

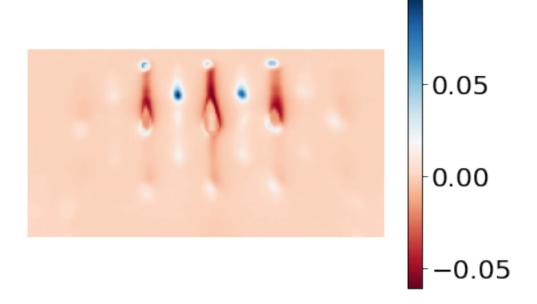


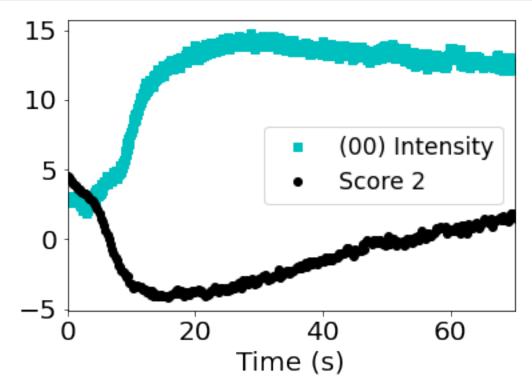
We are going to look at the other components next. PC2:

```
[14]: matplotlib.pyplot.imshow(pcnew.components_[1].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
```

```
[14]: (-0.5, 655.5, 263.5, -0.5)
```



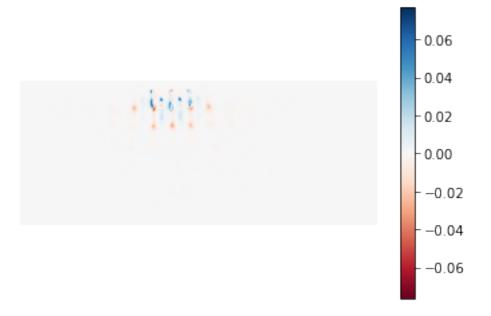




PC3

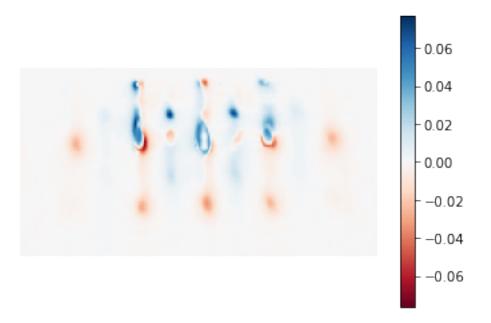
```
[14]: matplotlib.pyplot.imshow(pcnew.components_[2].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
```

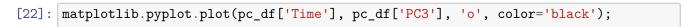
[14]: (-0.5, 655.5, 263.5, -0.5)

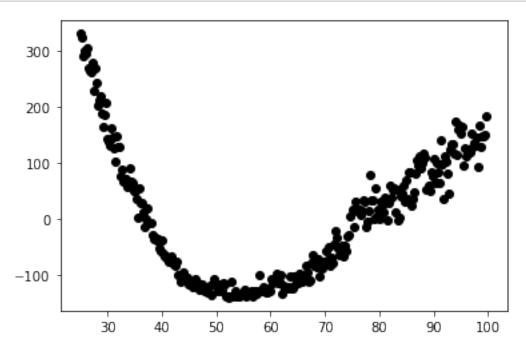


```
[15]: pc3 = pcnew.components_[2].reshape(264,656)
matplotlib.pyplot.imshow(pc3[10:110,180:370],cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
matplotlib.pyplot.savefig('d:/Research/Paper_on_RHEED_DataScience/Figures/solo/
→lco/load3.png', dpi=1200, bbox_inches='tight')
```

[15]: (-0.5, 189.5, 99.5, -0.5)



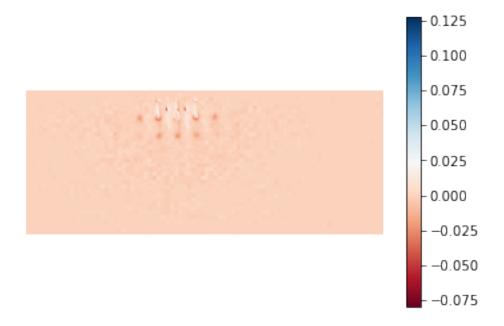




PC4

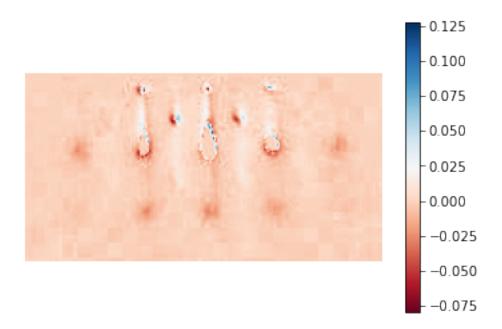
```
[23]: matplotlib.pyplot.imshow(pcnew.components_[3].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
```

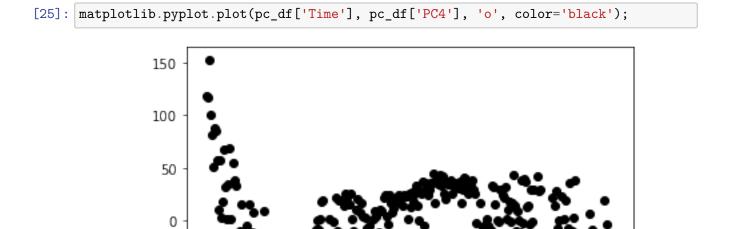
[23]: (-0.5, 655.5, 263.5, -0.5)



```
[24]: pc4 = pcnew.components_[3].reshape(264,656)
matplotlib.pyplot.imshow(pc4[10:110,180:370],cmap = "RdBu")
matplotlib.pyplot.colorbar()
matplotlib.pyplot.axis('off')
```

[24]: (-0.5, 189.5, 99.5, -0.5)





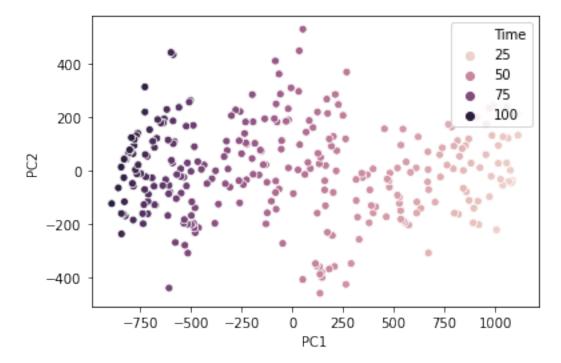
I stopped plotting the loading and score plots here, but it can be continued in the same manner as above.

The principal components can be plotted with respect to each other.

-50

-100

```
[49]: import seaborn as sns
%matplotlib inline
sns.scatterplot(x = pc_df['PC1'], y = pc_df['PC2'], hue = pc_df['Time']);
```



Below is how the Euclidian distance was determined for NMF so that a rank could be chosen.

Now let's do nmf with three components.

```
[13]: from sklearn.decomposition import NMF
model = NMF(n_components=3, init='random', random_state=0, max_iter = 100)
W = model.fit_transform(frames1)
H = model.components_
W.shape
```

C:\Users\kag99\Anaconda3\lib\site-packages\sklearn\decomposition\\_nmf.py:1076: ConvergenceWarning: Maximum number of iterations 100 reached. Increase it to improve convergence.

warnings.warn("Maximum number of iterations %d reached. Increase it to"

# [13]: (390, 3)

Below you can see the head of the basis plots.

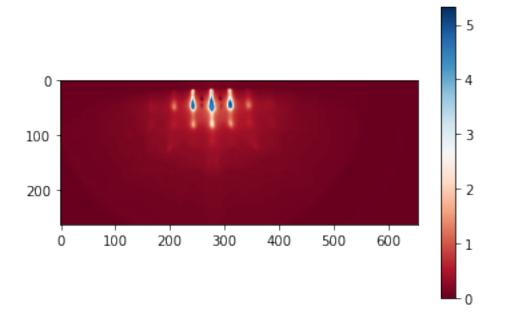
```
[14]: df = pd.DataFrame(W, columns = ['Column_A', 'Column_B', 'Column_C'])
  Time = np.arange(0,97.5,.25)
  df['Time'] = Time
  df.head()
```

```
[14]: Column_A Column_B Column_C Time
0 0.013201 0.409087 0.037607 0.00
1 0.014298 0.409843 0.037346 0.25
2 0.016704 0.408961 0.034737 0.50
3 0.018497 0.407842 0.033421 0.75
4 0.021566 0.403952 0.031059 1.00
```

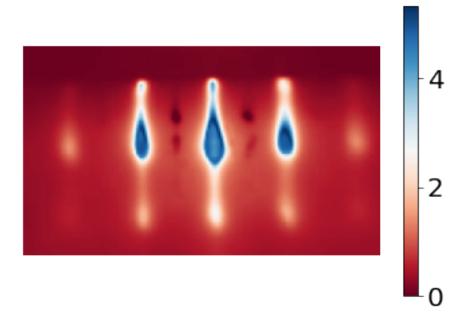
The coefficient plot for the first cluster.

```
[11]: matplotlib.pyplot.imshow(H[0,:].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
```

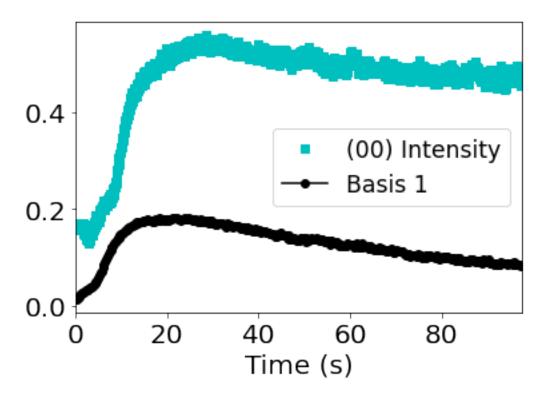
## [11]: <matplotlib.colorbar.Colorbar at 0x211cdf46e80>



```
[15]: fig, ax = matplotlib.pyplot.subplots()
  pc1 = H[0,:].reshape(264,656)
  m = matplotlib.pyplot.imshow(pc1[0:100,187:357],cmap = "RdBu")
  cbar = ax.figure.colorbar(m, ax=ax)
  cbar.ax.tick_params(labelsize=20)
```



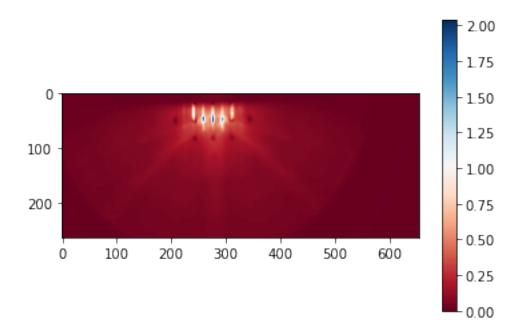
The basis plot for the first cluster with the intensity of the (00) spot plotted as well.

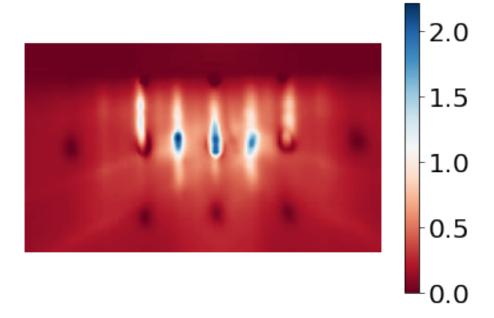


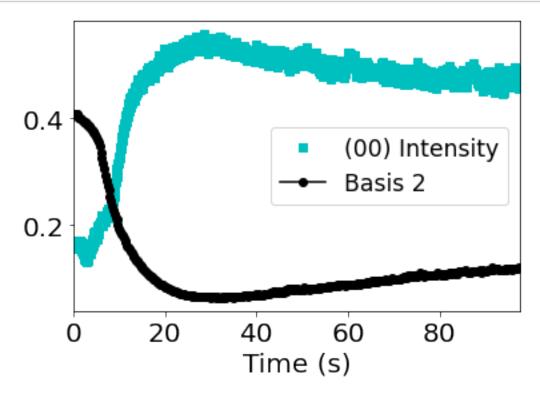
# Cluster 2

```
[11]: matplotlib.pyplot.imshow(H[1,:].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
```

[11]: <matplotlib.colorbar.Colorbar at 0x1b64462d8b0>



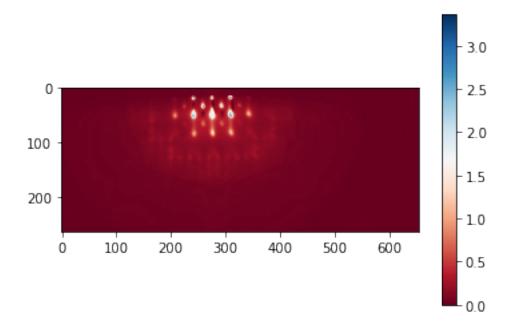


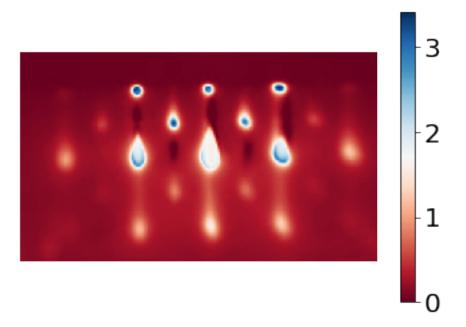


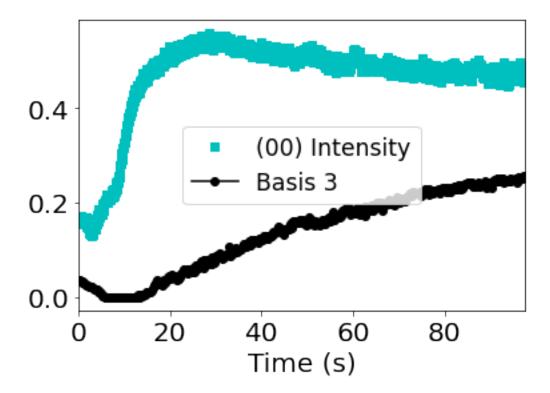
### Cluster 3

```
[14]: matplotlib.pyplot.imshow(H[2,:].reshape(264,656),cmap = "RdBu")
matplotlib.pyplot.colorbar()
```

# [14]: <matplotlib.colorbar.Colorbar at 0x1b6447b8d00>







Next kmeans will be performed, but first a silhouette plot is made for a number of clusters in order to determine the final number of clusters used in kmeans.

```
[38]: from sklearn.datasets import make_blobs
      from sklearn.cluster import KMeans
      from sklearn.metrics import silhouette_samples, silhouette_score
      import matplotlib.pyplot as plt
      import matplotlib.cm as cm
      import numpy as np
      range_n_clusters = [2, 3, 4, 5]
      X = frames1
      for n_clusters in range_n_clusters:
          # Create a subplot with 1 row and 2 columns
          fig, (ax1, ax2) = plt.subplots(1, 2)
          fig.set_size_inches(18, 7)
          # The 1st subplot is the silhouette plot
          # The silhouette coefficient can range from -1, 1 but in this example all
          # The (n_clusters+1)*10 is for inserting blank space between silhouette
          # plots of individual clusters, to demarcate them clearly.
          ax1.set_ylim([0, len(X) + (n_clusters + 1) * 10])
```

```
# Initialize the clusterer with n clusters value and a random generator
# seed of 10 for reproducibility.
clusterer = KMeans(n_clusters=n_clusters, random_state=10)
cluster_labels = clusterer.fit_predict(X)
# The silhouette_score gives the average value for all the samples.
# This gives a perspective into the density and separation of the formed
# clusters
silhouette_avg = silhouette_score(X, cluster_labels)
print("For n_clusters =", n_clusters,
      "The average silhouette_score is :", silhouette_avg)
# Compute the silhouette scores for each sample
sample_silhouette_values = silhouette_samples(X, cluster_labels)
y_lower = 10
for i in range(n_clusters):
    # Aggregate the silhouette scores for samples belonging to
    # cluster i, and sort them
   ith_cluster_silhouette_values = \
        sample_silhouette_values[cluster_labels == i]
    ith_cluster_silhouette_values.sort()
   size_cluster_i = ith_cluster_silhouette_values.shape[0]
   y_upper = y_lower + size_cluster_i
   color = cm.nipy_spectral(float(i) / n_clusters)
   ax1.fill_betweenx(np.arange(y_lower, y_upper),
                      0, ith_cluster_silhouette_values,
                      facecolor=color, edgecolor=color, alpha=0.7)
    # Label the silhouette plots with their cluster numbers at the middle
    ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))
    # Compute the new y_lower for next plot
   y_lower = y_upper + 10 # 10 for the 0 samples
ax1.set title("The silhouette plot for the various clusters.")
ax1.set_xlabel("The silhouette coefficient values")
ax1.set_ylabel("Cluster label")
# The vertical line for average silhouette score of all the values
ax1.axvline(x=silhouette_avg, color="red", linestyle="--")
ax1.set_yticks([]) # Clear the yaxis labels / ticks
ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
```

For n\_clusters = 2 The average silhouette\_score is : 0.6678388772737464

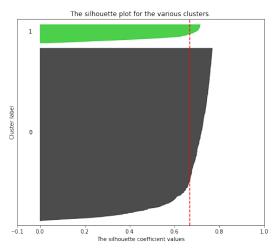
For n\_clusters = 3 The average silhouette\_score is : 0.5160394880942849

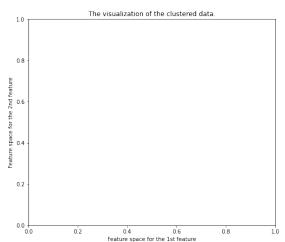
For n\_clusters = 4 The average silhouette\_score is : 0.5006246255570259

For n\_clusters = 5 The average silhouette\_score is : 0.4488560397155397

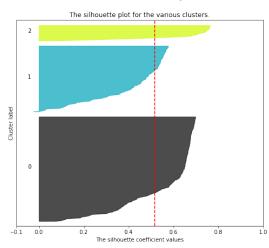
For n\_clusters = 6 The average silhouette\_score is : 0.4380582772394918

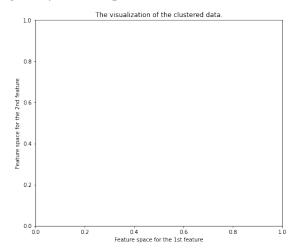
#### Silhouette analysis for KMeans clustering on sample data with n\_clusters = 2



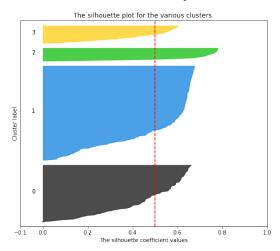


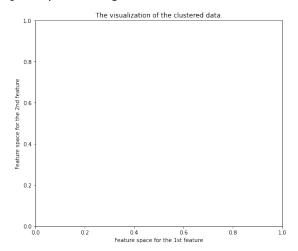
### Silhouette analysis for KMeans clustering on sample data with $n_c$ clusters = 3



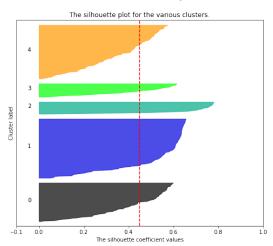


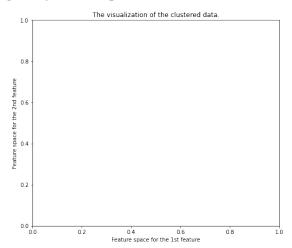
### Silhouette analysis for KMeans clustering on sample data with $n_c$ lusters = 4



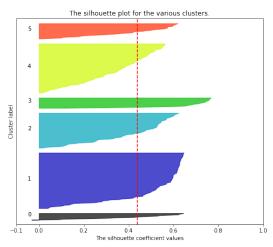


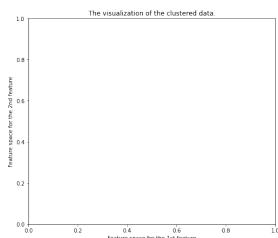
### Silhouette analysis for KMeans clustering on sample data with n\_clusters = 5





#### Silhouette analysis for KMeans clustering on sample data with $n_c$ lusters = 6





Kmeans is performed with two clusters.

Add the time of each frame to the dataframe.

```
[13]: rawKmeans.rename(columns={0: "Clusters"}, inplace = True)
  Time = np.arange(0.0,97.5,.25)
  rawKmeans['Time'] = Time
  rawKmeans.head()
```

```
[13]:
         Clusters
                    Time
                    0.00
      0
                 1
      1
                 1
                    0.25
      2
                 1
                    0.50
      3
                    0.75
                 1
      4
                    1.00
[14]:
      rawKmeans.shape
[14]: (390, 2)
     The next two code chunks are just combining the original data set with all the frames to the cluster
     numbers so that we can get images back.
[15]: Index = np.arange(0,390,1)
      frames1['Index'] = Index
      frames1.set_index('Index', inplace = True)
      frames1.head()
[15]:
               0
                          1
                                     2
                                                3
                                                          4
                                                                     5
                                                                                6
                                                                                        \
      Index
      0
              0.007843
                        0.007843
                                   0.007843
                                             0.007843
                                                        0.007843
                                                                   0.007843
                                                                              0.007843
                        0.003922
      1
              0.003922
                                   0.003922
                                                        0.003922
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                                                                   0.003922
                                                                              0.003922
      2
              0.007843
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                                                                                173183
      Index
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                                   0.003922
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                                                                   0.003922
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      2
              0.003922
                        0.003922
                                   0.003922
                                              0.003922
                                                        0.003922
                                                                   0.003922
                                                                              0.003922
      3
              0.003922
                        0.003922
                                   0.003922
                                              0.003922
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                                                                   0.003922
                                                                              0.003922
              0.003922
                        0.003922
                                   0.003922
                                             0.003922
                                                        0.003922 0.003922
                                                                              0.003922
```

[5 rows x 173184 columns]

```
[16]: clusters = pd.concat([rawKmeans, frames1], axis=1)
    clusters.head()
```

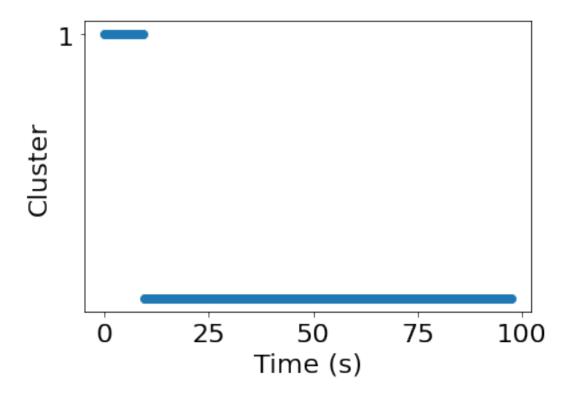
```
[16]:
        Clusters
                 Time
                                        1
     0
                  0.00 0.007843 0.007843 0.007843 0.007843 0.007843 0.007843
     1
                  0.25  0.003922  0.003922  0.003922  0.003922
                                                              0.003922
                                                                       0.003922
     2
               1 0.50 0.007843 0.007843 0.007843 0.007843
                                                              0.007843
                                                                       0.007843
     3
                  0.75  0.007843  0.007843  0.007843  0.007843
                                                              0.007843
                                                                       0.007843
                  1.00 0.007843 0.007843 0.007843 0.007843 0.007843 0.007843
               6
                         7 ...
                                173174
                                          173175
                                                   173176
                                                             173177
                                                                      173178 \
     0 0.007843 0.007843
                           ... 0.003922 0.003922 0.003922 0.003922
     1 0.003922 0.003922
                              0.003922 0.003922 0.003922
                                                           0.003922 0.003922
     2 0.007843 0.007843 ...
                              0.003922 0.003922 0.003922
                                                           0.003922 0.003922
     3 0.007843 0.007843 ... 0.003922 0.003922 0.003922
                                                           0.003922 0.003922
     4 \quad 0.007843 \quad 0.007843 \quad ... \quad 0.003922 \quad 0.003922 \quad 0.003922 \quad 0.003922 \quad 0.003922
          173179
                    173180
                             173181
                                       173182
                                                173183
     0 0.003922 0.003922 0.003922 0.003922 0.003922
     1 0.003922 0.003922 0.003922 0.003922
     2 0.003922 0.003922 0.003922
                                     0.003922 0.003922
     3 0.003922
                  0.003922 0.003922
                                     0.003922 0.003922
     4 0.003922 0.003922 0.003922 0.003922
```

[5 rows x 173186 columns]

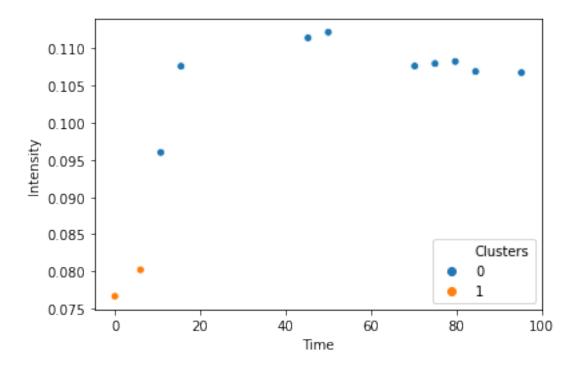
You can rename the clusters so that they don't start with 0

```
[17]: rawKmeans['Cluster'] = rawKmeans['Clusters']
rawKmeans.loc[rawKmeans['Clusters'] == 0, 'Cluster'] = 1
rawKmeans.loc[rawKmeans['Clusters'] == 1, 'Cluster'] = 2
```

Next I plot the clusters with resplect to time.

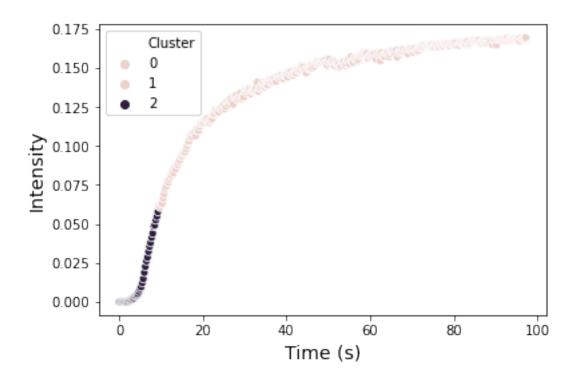


I save the clusters to a csv file so that I can compare the clusters to my intensity data. The time of the frames and the points for which the intensity was captured do not match up perfectly as seen below.



I can, however, directly compare to NMF

[67]: Text(0.5, 0, 'Time (s)')



Next I want to work on averaging the images from each cluster. I start be separating out all of cluster 0.

```
[30]: clus0 = clusters['Clusters']==0
      cluster0 = clusters[clus0]
      cluster0.head()
[30]:
          Clusters
                                   0
                                                         2
                                                                   3
                      Time
                                              1
      38
                      9.50
                            0.007843
                                      0.007843
                                                 0.007843
                                                           0.007843
                                                                      0.007843
                 0
                                                 0.007843
                                                                      0.007843
      39
                 0
                      9.75
                            0.007843
                                      0.007843
                                                            0.007843
                     10.00
                                                 0.007843
                                                            0.007843
                                                                      0.007843
      40
                 0
                            0.007843
                                      0.007843
      41
                     10.25
                            0.007843
                                       0.007843
                                                 0.007843
                                                            0.007843
                                                                      0.007843
                                                 0.007843
                     10.50
                            0.007843
                                       0.007843
                                                            0.007843
                                                                      0.007843
      42
                 5
                            6
                                       7
                                               173174
                                                          173175
                                                                    173176
                                                                               173177
      38
          0.007843
                    0.007843
                               0.007843
                                             0.003922
                                                       0.003922
                                                                  0.003922
                                                                             0.003922
          0.007843
                    0.007843
                               0.007843
                                             0.003922
                                                       0.003922
                                                                  0.003922
                                                                             0.003922
      39
      40
          0.007843
                    0.007843
                               0.007843
                                             0.003922
                                                       0.003922
                                                                  0.003922
                                                                             0.003922
          0.007843
      41
                     0.007843
                               0.007843
                                             0.003922
                                                        0.003922
                                                                  0.003922
                                                                             0.003922
      42
          0.007843
                     0.007843
                               0.007843
                                             0.003922
                                                        0.003922
                                                                  0.003922
                                                                             0.003922
            173178
                       173179
                                 173180
                                            173181
                                                      173182
                                                                 173183
      38
          0.003922
                    0.003922
                               0.003922
                                          0.003922
                                                    0.003922
                                                               0.003922
          0.003922
                    0.003922
                               0.003922
                                          0.003922
                                                    0.003922
                                                               0.003922
      39
      40
          0.003922
                    0.003922
                               0.003922
                                          0.003922
                                                    0.003922
                                                               0.003922
```

```
41 0.003922 0.003922 0.003922 0.003922 0.003922 0.003922 42 0.003922 0.003922 0.003922 0.003922 0.003922
```

[5 rows x 173186 columns]

```
[31]: mean0 = cluster0.mean()
mean0 = mean0.iloc[2:178435]
mean0.shape
```

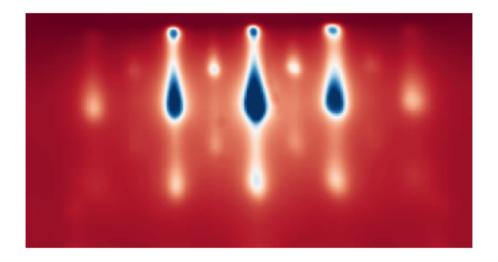
[31]: (173184,)

Below is the average of cluster 1.

```
[32]: matplotlib.pyplot.imshow(mean0.values.reshape((264, 656)), cmap = "RdBu")
    matplotlib.pyplot.colorbar()
    matplotlib.pyplot.axis('off')
```

[32]: (-0.5, 655.5, 263.5, -0.5)



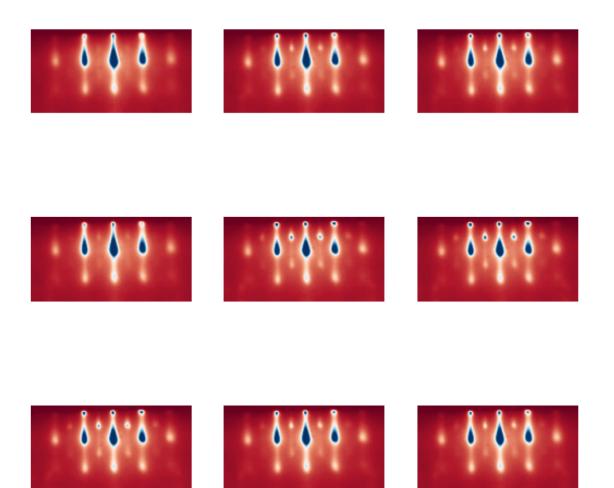


```
[50]: cluster0.shape
```

[50]: (352, 173186)

I also look at a random sample of frames from the cluster to compare to the average for any differences.

```
[51]: import random
      lis = []
      for x in range(9):
          num = random.randint(0,len(cluster0)-1)
          lis.append(num)
      X_{data} = []
      for i in lis:
          first = cluster0.iloc[i, 2:]
          a = first.values.reshape((264, 656))
          image = a[10:110,180:370]
          X_data.append(image)
          \#matplotlib.pyplot.imshow(a[0:100,180:350],cmap = "RdBu")
          #matplotlib.pyplot.colorbar()
      matplotlib.pyplot.figure(figsize=(9,9)) # specifying the overall grid size
      for i in range(9):
          matplotlib.pyplot.subplot(3,3,i+1) # the number of images in the grid is_{\sqcup}
       →5*5 (25)
          matplotlib.pyplot.imshow(X_data[i], cmap = "RdBu")
          matplotlib.pyplot.axis('off')
      matplotlib.pyplot.show()
```

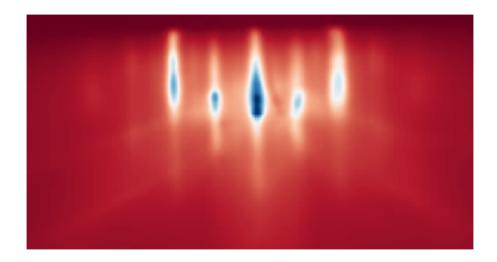


## Next look at cluster 1

```
[34]: clus1 = clusters['Clusters'] == 1
    cluster1 = clusters[clus1]
    #cluster0.head()
    mean1 = cluster1.mean()
    mean1 = mean1.iloc[2:178435]
    #mean0.shape
    matplotlib.pyplot.imshow(mean1.values.reshape((264, 656)), cmap = "RdBu")
    matplotlib.pyplot.colorbar()
    matplotlib.pyplot.axis('off')
```

[34]: (-0.5, 655.5, 263.5, -0.5)





```
[43]: import random
      lis = []
      for x in range(9):
          num = random.randint(0,len(cluster1)-1)
          lis.append(num)
      X_{data} = []
      for i in lis:
         first = cluster1.iloc[i, 2:]
          a = first.values.reshape((264, 656))
          image = a[10:110,180:370]
          X_data.append(image)
      matplotlib.pyplot.figure(figsize=(9,9)) # specifying the overall grid size
      for i in range(9):
          matplotlib.pyplot.subplot(3,3,i+1) # the number of images in the grid is_{\sqcup}
      →5*5 (25)
          matplotlib.pyplot.imshow(X_data[i], cmap = "RdBu")
          matplotlib.pyplot.axis('off')
      matplotlib.pyplot.show()
```

