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% Task: Partition  $\{1, \dots, n\}$  into  $r$  sum-free sets

% Input: positive integers  $n, r$ 

l{in(I, 1..r)}1 :- I = 1..n.
% achieved: set  $\{1, \dots, n\}$  partitioned into subsets
%  $\{I:in(I,1)\}, \dots, \{I:in(I,r)\}$ 

:- in(I,X), in(J,X), in(I+J,X).
% Achieve these subsets are sum-free

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% Task: Find independent sets of vertices of size  $n$ 

% Input: set node/1 of vertices of a graph  $G$ ;
% set edge/2 of edges of  $G$ , positive integer  $n$ .

n {in(X) : node(X)}n.
% achieved : in/1 is a set consisting of  $n$  vertices

:- in(X), in(Y), edge(X,Y).
% achieved: in/1 has no pairs of adjacent vertices

# show in/1.

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% Task: Find a clique of size  $n$ 

% Input: set node/1 of vertices of a graph  $G$ ;
% set edge/2 of edges of  $G$ , positive integer  $n$ .

n {in(X) : node(X)}n.
% achieved : in/1 is a set consisting of  $n$  vertices

:- in(X), in(Y), not edge(X,Y).
% achieved: in/1 has no pairs of non-adjacent vertices

# show in/1.

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%Task: Find the number of edges in a graph G and degrees of vertices

% Input: set of nodes/1 of vertices of a graph G; set
edge/2 of edges of G.

adjacent(X,Y) :- edge(X,Y).
adjacent(X,Y) :- edge(Y,X).
% achieved: adjacent (X,Y) iff X,Y are adjacent in the
graph.

number_of_edges(N/2) :- N = #count{X,Y : adjacent(X,Y)}.
% achieved: number_of_edges(N) if and only if N is the number of edges of
G.

degree(X,D) :- vertex(X), D = #count{Y: adjacent(X,Y)}.
% achieved: degree(X,D) if and only if D is the degree of the vertex X of
G.

#show degree/2. #show number_of_edges/1.

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% Task: Find largest independent sets of vertices

% Input: set node/1 of vertices of a graph G;
           % set edge /2 of edges of G

{in(X)} :- node(X).
% achieved: in/1 is a set consisting of n vertices of G.

:- in(X), in(Y), edge(X,Y).
% achieved: in/1 has no pairs of adjacent vertices.

#maximize{1,X : in(X)}.
% achieved: the number of elements of in/1 is maximal

#show in/1.

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% Task: Calculate the number of classes taught on each of the five  
floors.
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% Input: set where/2 of all pairs (C,I) such that  
           % class C is taught on the I-th floor.
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howmany(I,N) :- N = #count{C : where(C,I)}, I=1..5.
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% achieved: howmany(I,N) if and only if the number of classes %  
taught on the I-th floor is N.
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#show howmany/2.
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