

# Exercise

1. train a NB classifier to predict “Class” using the following training data:

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammal
python	no	no	no	no	non-mammal
salmon	no	no	yes	no	non-mammal
whale	yes	no	yes	no	mammal
frog	no	no	sometimes	yes	non-mammal
komodo	no	no	no	yes	non-mammal
bat	yes	yes	no	yes	mammal
pigeon	no	yes	no	yes	non-mammal
cat	yes	no	no	yes	mammal
leopard shark	yes	no	yes	no	non-mammal
turtle	no	no	sometimes	yes	non-mammal
penguin	no	no	sometimes	yes	non-mammal
porcupine	yes	no	no	yes	mammal
eel	no	no	yes	no	non-mammal
salamander	no	no	sometimes	yes	non-mammal
gila monster	no	no	no	yes	non-mammal
platypus	no	no	no	yes	mammal
owl	no	yes	no	yes	non-mammal
dolphin	yes	no	yes	no	mammal
eagle	no	yes	no	yes	non-mammal

2. use your classifier to predict the class of the following example:

Give Birth	Can Fly	Live in Water	Have Legs	Class
yes	no	yes	no	?

# Solution

training data

Attributes  $A_i$       Class  
B      F      W      L      C

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammal
python	no	no	no	no	non-mammal
salmon	no	no	yes	no	non-mammal
whale	yes	no	yes	no	mammal
frog	no	no	sometimes	yes	non-mammal
komodo	no	no	no	yes	non-mammal
bat	yes	yes	no	yes	mammal
pigeon	no	yes	no	yes	non-mammal
cat	yes	no	no	yes	mammal
leopard shark	yes	no	yes	no	non-mammal
turtle	no	no	sometimes	yes	non-mammal
penguin	no	no	sometimes	yes	non-mammal
porcupine	yes	no	no	yes	mammal
eel	no	no	yes	no	non-mammal
salamander	no	no	sometimes	yes	non-mammal
gila monster	no	no	no	yes	non-mammal
platypus	no	no	no	yes	mammal
owl	no	yes	no	yes	non-mammal
dolphin	yes	no	yes	no	mammal
eagle	no	yes	no	yes	non-mammal

y/n   y/n   y/s/n   y/n   m/n  
values of attributes

20 animals, of which  
7 are m(ammal) and  
13 n(on-mammal), thus

$$P(C = m) = \frac{7}{20}$$
$$P(C = n) = \frac{13}{20}$$

# Solution

training data

Attributes  $A_i$       Class  
B      F      W      L      C

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammal
					non-mammal
					non-mammal
whale	yes	no	yes	no	mammal
					non-mammal
					non-mammal
bat	yes	yes	no	yes	mammal
					non-mammal
cat	yes	no	no	yes	mammal
					non-mammal
					non-mammal
porcupine	yes	no	no	yes	mammal
					non-mammal
					non-mammal
platypus	no	no	no	yes	mammal
					non-mammal
dolphin	yes	no	yes	no	mammal
					non-mammal

y/n    y/n    y/s/n    y/n    m/n  
values of attributes

of the 7 mammals

$$P(L = y | C = m) = \frac{5}{7}$$

$$P(L = n | C = m) = \frac{2}{7}$$

$$P(W = y | C = m) = \frac{2}{7}$$

$$P(W = s | C = m) = \frac{0}{7}$$

$$P(W = n | C = m) = \frac{5}{7}$$

$$P(F = y | C = m) = \frac{1}{7}$$

$$P(F = n | C = m) = \frac{6}{7}$$

$$P(B = y | C = m) = \frac{6}{7}$$

$$P(B = n | C = m) = \frac{1}{7}$$

# Solution

training data

Attributes  $A_i$       Class  
 B      F      W      L      C

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
					mammal
python	no	no	no	no	non-mammal
salmon	no	no	yes	no	non-mammal
					mammal
frog	no	no	sometimes	yes	non-mammal
komodo	no	no	no	yes	non-mammal
					mammal
pigeon	no	yes	no	yes	non-mammal
					mammal
leopard shark	yes	no	yes	no	non-mammal
turtle	no	no	sometimes	yes	non-mammal
penguin	no	no	sometimes	yes	non-mammal
					mammal
eel	no	no	yes	no	non-mammal
salamander	no	no	sometimes	yes	non-mammal
gila monster	no	no	no	yes	non-mammal
					mammal
owl	no	yes	no	yes	non-mammal
					mammal
eagle	no	yes	no	yes	non-mammal

y/n   y/n   y/s/n   y/n   m/n

values of attributes

of the 13 non-mammals

$$P(L = y | C = n) = \frac{9}{13}$$

$$P(L = n | C = n) = \frac{4}{13}$$

$$P(W = y | C = n) = \frac{3}{13}$$

$$P(W = s | C = n) = \frac{4}{13}$$

$$P(W = n | C = n) = \frac{6}{13}$$

$$P(F = y | C = n) = \frac{3}{13}$$

$$P(F = n | C = n) = \frac{10}{13}$$

$$P(B = y | C = n) = \frac{1}{13}$$

$$P(B = n | C = n) = \frac{12}{13}$$

# Solution

Give Birth	Can Fly	Live in Water	Have Legs	Class
yes	no	yes	no	?

mammal?

$$\begin{aligned}
 &P(C = m) \\
 &\cdot P(B = y|C = m) \\
 &\cdot P(F = n|C = m) \\
 &\cdot P(W = y|C = m) \\
 &\cdot P(L = n|C = m) \\
 &= \frac{7}{20} \cdot \frac{6}{7} \cdot \frac{6}{7} \cdot \frac{2}{7} \cdot \frac{2}{7} \\
 &= 0.021
 \end{aligned}$$

>

mammal!

non-mammal?

$$\begin{aligned}
 &P(C = n) \\
 &\cdot P(B = y|C = n) \\
 &\cdot P(F = n|C = n) \\
 &\cdot P(W = y|C = n) \\
 &\cdot P(L = n|C = n) \\
 &= \frac{13}{20} \cdot \frac{1}{13} \cdot \frac{10}{13} \cdot \frac{3}{13} \cdot \frac{4}{13} \\
 &= 0.0027
 \end{aligned}$$