ECE 759

High Performance Computing for Engineering Applications Assignment 4 Due 3/17/2025 at 23:59 PM

Submit responses to all tasks which don't specify a file name to Canvas in a file called assignment4.pdf. Submit all plots (if any) on Canvas. Do not zip your Canvas submission.

All source files should be submitted in the HW04 subdirectory on the main branch of your homework git repo with no subdirectories. Your HW04 folder should contain task2.cpp and task3.cpp.

All commands or code must work on *Euler* without loading additional modules unless specified otherwise. A program may behave differently on your computer, so be sure to test on *Euler* before you submit. Note that this assignment is relevant to OpenMP, so the following line needs to be added to your slurm script:

• #SBATCH --cpus-per-task=8 (or -c 8 for short) should be added, which requests one node with 8 virtual cores (note the slight misnomer – Linux refers to virtual cores as cpus). The maximum number of threads required in this assignment is 8, so you should not ask for more than 8 cores.

Please submit clean code. Consider using a formatter like clang-format.

* Before you begin, copy the provided files from Assignments/HW04 directory of the ECE 759 Resource Repo. Do not change any of the provided files since these files will be overwritten with clean, reference copies when grading.

Specify your GitHub link here:

github.com/ragravalb/sepo759/tsec/main/HWO4

The GitHub link to your code folder should be: https://github.com/YourGitHubName/repo759/HW04

In this assignment, we will simulate a dynamical system of particles interacting gravitationally, commonly referred to as the **N-body** problem. Such simulations can model systems like the orbits of planets in the Solar System or the movement of stars in a galaxy.

First, review the N-body Python code in the file located at Assignments/HW04/nbody.py. Below is an introduction to the N-body problem:

Force Calculation:

We will assume a system of N point particles, indexed by $i=1,\ldots,N$. Every particle has the following properties:

- mass m_i
- position $\mathbf{r}_i = [x_i, y_i, z_i]$
- velocity $\mathbf{v_i} = [vx_i, vy_i, vz_i]$

Each particle experiences the gravitational force exerted by all other particles according to Newton's law of universal gravitation, which follows the inverse-square law. The acceleration a_i of particle i is given by:

$$a_i = G \sum_{i \neq j} m_i \frac{r_j - r_i}{|r_j - r_i|^3}$$

where G is the Gravitational constant.

To implement this, we have a Python function that computes the gravitational force on each particle using an input matrix of size $N \times 3$ that contains the positions of all particles:

```
def getAcc(pos, mass, G, softening):
2
       Calculate the acceleration on each particle due to Newton's Law
       pos \, is an N \, x \, 3 \, matrix of positions
       mass is an N \times 1 vector of masses
       G is Newton's Gravitational constant
       softening is the softening length
       a is N \times 3 matrix of accelerations
9
       N = pos.shape[0]
11
       a = np.zeros((N, 3))
12
13
       for i in range(N):
14
           for j in range(N):
                if i != j:
16
                     dx = pos[j, 0] - pos[i, 0]
dy = pos[j, 1] - pos[i, 1]
dz = pos[j, 2] - pos[i, 2]
17
18
19
                     inv_r3 = (dx**2 + dy**2 + dz**2 + softening**2) ** (-1.5)
20
                     a[i, 0] += G * (dx * inv_r3) * mass[j, 0]
21
22
                     a[i, 1] += G * (dy * inv_r3) * mass[j, 0]
                     a[i, 2] += G * (dz * inv_r3) * mass[j, 0]
24
       return a
```

The softening parameter in the code is a small value added to avoid numerical issues when two particles are very close to each other. In such cases, the acceleration predicted by the inverse-square law would approach infinity. In reality, masses are not perfect point particles and have a finite size, so this parameter prevents unrealistic behavior in the simulation by smoothing out the gravitational force at short distances.

Time Integration:

The positions and velocities of the particles are updated using a 'kick-drift-kick' method. For each timestep Δt , the following steps are applied to every particle:

1. Half-step 'kick': Update the velocity based on the current acceleration:

$$oldsymbol{v_i^{T+1}} = oldsymbol{v_i^T} + rac{\Delta t}{2} imes oldsymbol{a_i^T}$$

2. Full-step 'drift': Update the position using the new velocity:

$$\boldsymbol{r_i^{T+1}} = \boldsymbol{r_i^T} + \Delta t \times \boldsymbol{v_i^T}$$

3. Another half-step 'kick': Update the velocity again based on the new acceleration.

This evolution is implemented in the code using a for-loop and the acceleration function defined earlier:

```
# Simulation Main Loop
      for i in range(Nt):
           # (1/2) kick
           vel += acc * dt / 2.0
           # drift
6
           pos += vel * dt
           # ensure particles stay within the board limits
9
           pos[pos > board_size] = board_size
10
           pos[pos < -board_size] = -board_size</pre>
           # update accelerations
13
14
           acc = getAcc(pos, mass, G, softening)
15
           #(1/2) kick
16
           vel += acc * dt / 2.0
17
18
           # update time
19
           t += dt
20
```

Initial Conditions:

To run the simulation, we need to specify the initial positions and velocities of the particles at time t = 0. You can experiment with different setups in the provided code to observe how the system evolves under various initial conditions.

- **Problem 1**. Please review the introduction to the N-body problem above. Ensure that you understand both the algorithm and the Python code.
 - a) Install Python library numpy and matplotlib: python3 -m pip install numpy matplotlib
 - b) Run the nbody.py script either on your personal machine or on the Euler compute node. If you run it locally, you will see an animation of the N-body simulation. At the end of the simulation, the code will automatically save a plot. Rename this plot as task1.png and submit it to Canvas.

Problem 2. Port the N-body simulation code into C++. A skeleton code is provided in Assignments/HW04/task2.cpp.

- a) Write a program task2.cpp that accomplish the following:
 - Complete the provided skeleton code from task2.cpp.
 - Compile:

```
g++ task2.cpp -Wall -03 -std=c++17 -o task2
```

- Run the program; make sure you use Slurm:
 ./task2 number_of_particles simulation_end_time
- (Optional) For debugging and visualization, we provide a function savePositionsToCSV. This function saves the positions at each iteration to a CSV file. You can then use plot_positions.py to visualize the C++ simulation results. However, if you're measuring performance, disable this function as it introduces significant I/O overhead.

Problem 3. Parallelize the N-body C++ code using OpenMP.

- a) Write a program task3.cpp that accomplish the following:
 - Add an argument num_threads, which specifies the number of threads to launch with OpenMP.
 - Insert OpenMP directives (#pragma omp parallel for) in sections of the code that can be parallelized.
 - Compile:

```
g++ task3.cpp -Wall -03 -std=c++17 -o task3 -fopenmp
```

• Run the program; make sure you use Slurm and request multiple CPU cores: ./task3 number_of_particles simulation_end_time num_threads

Problem 4. Let's do experiments using different OpenMP scheduling policies.

- a) In task3.cpp, try the following scheduling policies: static, dynamic, and guided.
- b) On Euler, via Slurm do the following:

For each scheduling policy, run task3 with the following parameters:

- number_of_particles = 100 or larger
- simulation_end_time = 100 or larger
- $num_threads = 1, 2, \cdots, 8$

Generate plots called task4.pdf that show the time taken by the N-body simulation versus num_threads on a linear-linear scale. The task4.pdf should contain three plots, one for each scheduling policy. Feel free to share the plots on Piazza.