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STAT 206 (Applied Bayesian Statistics)

Take-Home Test 3: Part 2 (Revised 17 Mar 2022)

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Here are the *revised* ground rules: this test is open-book and open-notes, and has three parts. Part 1 consists of 7 true/false questions, each worth 10 points, for a total of 70 points; this part is *mandatory* for all STAT 206 students. Part 2 has a single calculation question in it, worth 220 points; this part is also mandatory for all STAT 206 students. Part 3 is entirely optional for all STAT 206 students and acts as a source of extra credit (up to 220 additional points): any points earned here will be added to the numerator, but not the denominator, in computing your course percentage correct

(total points achieved) / (total points assigned).

Undergraduates who wish to gain full mastery of all of the material presented this quarter are strongly encouraged to participate in office hour sessions from now through Sun 20 Mar 2022.

Some advice on style as you write up your solutions: pretend that you're sitting next to the grader, having a conversation about problem (x) part (y). You say, "The answer is z," and the grader says, "Why?" You then give your explanation, as succinctly as possible to get your idea across. The right answer with no reasoning to support it, or incorrect reasoning, will get **half credit**, so try to make a serious effort on each part of each problem (this will ensure you at least half credit). In an AMS graduate class I taught in 2012, on a take-home test like this one there were 15 true/false questions, worth a total of 150 points; one student got a score of 92 out of 150 (61%, a D-, in a graduate class where B- is the lowest passing grade) on that part of the test, for repeatedly answering just "true" or "false" with no explanation. Don't let that happen to you.

On each problem, the graders and I mentally start everybody out at -0 (i.e., with a perfect score), and then you accumulate negative points for incorrect answers and/or reasoning, or parts of problems left blank.

This test is to be entirely your own efforts; do not collaborate with anyone or get help from anyone but me or our TA (Jacob Fontana). The intent is that the course lecture notes and readings should be sufficient to provide you with all the guidance you need to solve the problems posed below, but you may use other written materials (e.g., the web, journal articles, and books other than those already mentioned in the readings), **provided that you cite your sources thoroughly and accurately**; you will lose (substantial) credit for, e.g., lifting blocks of text directly from wikipedia and inserting them into your solutions without full attribution.

If it's clear that (for example) two people have worked together on a part of a problem that's worth 20 points, and each answer would have earned 16 points if it had not arisen from a collaboration, then each person will receive 8 of the 16 points collectively earned (for a total score of 8 out of 20), and I reserve

the right to impose additional penalties at my discretion. If you solve a problem on your own and then share your solution with anyone else, you're just as guilty of illegal collaboration as the person who took your solution from you, and both of you will receive the same penalty. This sort of thing is necessary on behalf of the many people who do not cheat, to ensure that their scores are meaningfully earned. In the AMS graduate class in 2012 mentioned above, five people failed the class because of illegal collaboration; don't let that happen to you.

In class I've demonstrated numerical work in R; you can (of course) make the calculations and plots requested in the problems below in any environment you prefer (e.g., Matlab, ...). To avoid plagiarism, if you end up using any of the code I post on the course web page or generate during office hours, at the beginning of your Appendix (see below) you can say something like the following:

I used some of Prof. Draper's R code in this assignment, adapting it as needed.

Those of You who are using LaTeX or some other word-processing environment to prepare Your solutions can stick quote blocks below each question, into which You can type Your answers (I suggest that You use **bold** or *italic* font to distinguish Your solutions from the questions). If You're submitting Your answers in longhand, which is perfectly acceptable, You can just write them out on separate sheets of paper, making sure that the grader can easily figure out which chunk of text is the solution to which part of which problem.

Please collect {all of the code you used in answering the questions below} into an Appendix at the end of your document, so that (if you do something wrong) the grader can more accurately give you part credit.

Parts 2 and 3 of this test are similar to problem 2(B) in Take-Home Test 2, in that they look really long but don't actually have that much for You to do: just read the problems carefully, run my code (sometimes You'll need to modify it a bit), and figure how to interpret the output.

Part 2: Calculation

[220 total points for this problem] As I'm sure You know, if You encounter a wild mushroom in a forest there's no guarantee that it's edible; every year several people die in the U.S. from wild mushroom poisoning. Two questions come to mind, in this age of cell phone apps: (1) Can the edible/poisonous status of a wild mushroom be accurately predicted from characteristics such as its appearance and odor? and (2) If You were building an app to give people advice about whether a wild mushroom they've found is edible, (to make the app easy to use) what's the minimum number of variables necessary to get highly accurate predictions?

The U.C. Irvine Machine Learning Repository has a data set – a copy of which is now available in the Pages tab of the course Canvas page, along with a text file containing important contextual information – consisting of n=8,124

hypothetical samples corresponding to 23 species of gilled mushrooms in the *Agaricus* and *Lepiota* Family. Each species is identified as definitely edible, definitely poisonous, or of unknown edibility and not recommended. This latter class was combined with the poisonous one. The *Audubon Society Field Guide to North American Mushrooms* (1981) clearly states that there is no simple rule for determining the edibility of a mushroom; no rule like "leaflets three, let it be" for Poisonous Oak and Ivy.

As You'll see when You begin looking at the data set, there are k=22 predictor variables (x_1, \ldots, x_k) available, ranging from aspects of the mushroom's cap to its habitat, and the outcome variable y is coded 1 for poisonous and 0 for edible. The goals of this problem, corresponding to the two questions above, are (1) to build linear regression models, using these predictors, to produce estimated probabilities \hat{p} that (y=1) as a function of a given mushroom's characteristics, (2) to identify the smallest subset of the x_j (for inclusion in the app) that still produces highly accurate \hat{p} values, and (3) to decide whether the predictive modeling in step (2) is accurate enough to release the app to the general public without poisoning a lot of people in the process.

We're going to do a maximum-likelihood analysis of this data set, because (I'm assuming that) You and I know so little about 'gilled mushrooms in the *Agaricus* and *Lepiota* Family' that a Bayesian analysis here would just reproduce the likelihood story. I'm also doing something a bit unusual in having You fit *linear* regression models to a binary outcome variable, but the more usual choice of *logistic* regression models (like those in part 3 of this test) would give essentially the same results.

When You examine the set of predictor variables, You'll see that they're all categorical (R calls such variables factors), taking on a number of possible values (levels) ranging from 1 to 12.

Important: All of the levels of all of the predictors in the data set have been abbreviated to a single letter in the standard English alphabet; the context file contains a dictionary that translates those abbreviations to their actual meanings.

Obviously any predictor variable that takes on only 1 possible value is useless for predicting anything; there is such a variable, so early on in the analysis we'll drop it (veil.type) and reset k to 21. One variable – stalk.root – has a lot of missing values (2,480 out of 8,124), but one nice thing about categorical predictors is that missingness can be treated as just another level of the factor, so that no cases are lost by having to omit rows in the data set with missing values in them (that would be an undesirable action that's not needed with factor predictors). If those 2,480 values are Missing Completely At Random (MCAR; see Quiz 2), this will just make stalk.root noisier as a predictor; if they're not MCAR, we can use the fact of their missingness in the prediction process¹.

As discussed in class, the basic frequentist (multiple) linear regression model is of the form (for $i = 1, \ldots, n$)

$$y_i = \beta_0 + \sum_{j=1}^k x_{ij} \,\beta_j + e_i \,, \tag{1}$$

in which the $(e_i \mid \sigma[SM:\mathbb{N}] \mathcal{B})$ are IID $N(0, \sigma^2)$; here $[SM:\mathbb{N}]$ denotes the Normality assumption for the sampling model (SM), which is not part of problem context. In class we also saw that this model can be written in matrix form as

$$y = X \beta + e, \qquad (2)$$

where \boldsymbol{y} is the $(n \times 1)$ column vector whose transpose is (y_1, \ldots, y_n) , X is the $[n \times (k+1)]$ matrix whose first column is a vector of 1s (to account for the intercept term β_0) and whose ith row is $(1, x_{i1}, \ldots, x_{ik})$, $\boldsymbol{\beta}$ is the $[(k+1) \times 1]$ column vector whose transpose is $(\beta_0, \beta_1, \ldots, \beta_k)$ and \boldsymbol{e} is the $(n \times 1)$ column vector whose transpose is (e_1, \ldots, e_n) .

¹Ideally we should do a sensitivity analysis in which the 2,480 rows are temporarily omitted from the data set, to see if we get the same results as those that arise when those rows are included; I've decided not to ask You to do that here, because the problem is already fairly long.

In applying this model to the mushroom data, a new question immediately arises: how can You bring a categorical predictor – such as the 18th predictor in the data set ring.number, with the 3 levels "n" (none), "o" (one) and "t" (two) – into a regression model? The answer is with a set of *indicator*, also known as dummy, variables: with $x_{\{18\}} = \text{ring.number}$ as an example (here $x_{\{18\}}$ means the 18th predictor variable), having $\ell = 3$ levels, You create a new variable z_1 that's 1 if $x_{\{18\}} =$ "n" and 0 otherwise, and another new variable z_2 that's 1 if $x_{\{18\}} =$ "o" and 0 otherwise, and a third new variable z_3 that's 1 if $x_{\{18\}} =$ "t" and 0 otherwise.

If You now include all $\ell=3$ of the z_j in the set of predictors, in place of $x_{\{18\}}$, You will have created what's called a *collinearity* problem: by the nature of how the z_j were defined, for every mushroom i in the data set it's a fact that $z_{i1}+z_{i2}+z_{i3}=1$. This makes the X matrix in equation (2) non-invertible, meaning that the computation of the maximum-likelihood estimate of $\boldsymbol{\beta}$, namely $\hat{\boldsymbol{\beta}}=(X^TX)^{-1}X^T\boldsymbol{y}$, would be more difficult to carry out. The (simple) solution is to omit one of the z variables in the set of z_j You include in the modeling: after all, in the ring.number example, if You knew z_{i1} and z_{i2} , $z_{i3}=(1-z_{i1}-z_{i2})$ would be redundant (in the jargon of regression modeling, the category whose z dummy has been left out is called the *omitted group*). Letting ℓ_j be the number of levels of categorical predictor x_j and setting $L=\sum_{i=1}^k \ell_j$, the new linear regression model, expressed in terms of the dummy variables z, is

$$y_{i} = \beta_{0} + \left[\beta_{1} z_{i1} + \dots + \beta_{\ell_{1}-1} z_{i,\ell_{1}-1}\right] + \left[\beta_{\ell_{1}} z_{i2} + \dots + \beta_{\ell_{1}+\ell_{2}-2} z_{i,\ell_{1}+\ell_{2}-2}\right] + \dots + \left[\beta_{L-K-(\ell_{k}-2)} z_{i,L-K-(\ell_{k}-2)} + \dots + \beta_{L-k} z_{i,L-k}\right] + e_{i}.$$
(3)

This looks nasty but isn't: original categorical variable (factor) x_1 is replaced by $(\ell_1 - 1)$ dummy variables, original factor x_2 is replaced by $(\ell_2 - 1)$ dummies, and so on up to original factor x_k being replaced by $(\ell_k - 1)$ dummies, for a total of $k^* = (L - k)$ dummy variables replacing the original k factors. In the mushroom data set there are k = 21 non-trivial factors as predictor variables, and the total number of dummies needed to carry this information is [(6 + 4 + 10 + 2 + 9 + 2 + 2 + 2 + 12 + 2 + 5 + 4 + 4 + 9 + 9 + 4 + 3 + 5 + 9 + 6 + 7) - 21] = 95. (Where did I get the numbers $(6 + 4 + \cdots + 7)$?)

(a) [10 total points for this sub-problem] Create a new directory for this case study and download into this directory all of the files in the Pages tab of the course Canvas page that have 'mushroom' in their names. I've written some R code for You, to start You on the analysis of this data set; it's in the file you just downloaded called

stat-206-mushroom-data-analysis.txt

There's a block of code at the top of the file that begins 'the first block of code starts here' and ends 'the first block of code ends here'; run this code block and study the output. The function tab.sum in this code block provides diagnostic information on whether a factor x will turn out to be predictively useful in the modeling; briefly explain in what sense tab.sum provides such information (*Hint:* the function estimates the conditional mean (and SD, not useful here) of what variable given what other variable?). [10 points]

Solution. Well from the data output we see the first column is the different cap shapes alongside their n, mean and SD. This is to tell us the conditional expectation of the mean based on poisonous or not at each level of the given factor. That is to really say it gives us the probability that given mushroom cap shape is poisonous

(b) [20 total points for this sub-problem] Run the second code block, in which a linear regression model is fit with the dichotomous outcome poisonous regressed on the factor cap.shape, and study

Table 1: Extracts from the output of the second code block.

```
#
       cap.shape n
                       mean
                                 sd
# [1,] 1
                      0.1061947 0.308428
                  452
# [2,] 2
# [3,] 3
                  3152 0.4936548 0.5000391
                                                 output of tab.sum
# [4.] 4
                       0.7246377 0.4469667
# [5,] 5
                 32
# [6,] 6
                  3656 0.4671772 0.4989898
# Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                           0.02279
                                     4.659 3.22e-06 ***
# (Intercept)
               0.10619
# cap.shapec
               0.89381
                           0.24335
                                     3.673 0.000241 ***
                                                           output of
# cap.shapef
               0.38746
                           0.02437
                                    15.898
                                            < 2e-16 ***
                                                           linear
# cap.shapek
               0.61844
                           0.02834
                                    21.824
                                            < 2e-16 ***
                                                           regression
# cap.shapes
              -0.10619
                           0.08864
                                    -1.198 0.230926
# cap.shapex
               0.36098
                           0.02416
                                    14.942 < 2e-16 ***
```

the output. When the predictions \hat{y} from equation (3) are specialized to this regression, they looks like

$$\hat{y}_i = \hat{\beta}_0 + \hat{\beta}_1 z_{i1} + \dots + \hat{\beta}_5 z_{i5}, \tag{4}$$

in which the $\hat{\beta}_j$ are the maximum-likelihood estimates of the regression coefficients and where $\{z_{i1} = 1 \text{ if } \mathtt{cap.shape} = \text{`c'} \text{ and } 0 \text{ otherwise}\}$, $\{z_{i2} = 1 \text{ if } \mathtt{cap.shape} = \text{`f'} \text{ and } 0 \text{ otherwise}\}$, and so on down to $\{z_{i5} = 1 \text{ if } \mathtt{cap.shape} = \text{`x'} \text{ and } 0 \text{ otherwise}\}$. Now examine the extracts from the tab.sum and regression fitting in Table 1. Explicitly identify $(\hat{\beta}_0, \ldots, \hat{\beta}_5)$ in the output in the table [10 points], and – by thinking about the form of equation (4) for each of the levels of cap.shape – explicitly relate the numbers in the mean column of the tab.sum output in Table 1 to the $\hat{\beta}_j$. [10 points]

Solution. It is clear from the table that we get our $\hat{\beta}_j$ value from the "Estimate" column on the table. So,

$$(\hat{\beta}_1, \hat{\beta}_2, \dots, \hat{\beta}_5) = (0.10619, 0.89381, 0.38746, 0.61844, -0.10619, 0.36098).$$

We see that $\hat{\beta}_0$ is equal to the mean about "poisonous" when cap shape is "b". This follows from (4) by,

$$\hat{y_b} = 0.10619 + \hat{\beta_1}0 + \dots + \hat{\beta_5}0 = 0.10619$$

To see the way it relates to the rest of the mean values relate to the rest of $\hat{\beta}_j$ let's look at when cap.shape =' c',

$$\hat{y}_c = 0.10619 + 0.89381 \cdot 1 + \hat{\beta}_2 \cdot 0 + \dots + \hat{\beta}_5 \cdot 0 = 1$$

which matches the mean table for mushroom cap f. Which means the relation is,

$$E(y \mid \text{cap.shape} = i) = \bar{y}_i = \hat{y}_i.$$

More directly in terms of $\hat{\beta}_j$ the relation it is that $\hat{\beta}_0$ is equal to the mean y in the omitted category. Then for $j \geq 1$ we have $\hat{\beta}_j$ is equal to the mean y in category j minus the mean y in the omitted category.

- (c) [40 total points for this sub-problem] Toward the end of the second code block, the code computes predicted $\hat{p} = P(y = 1 | x_1 [SM : \mathbb{L}] \mathcal{B})$ values (in which $[SM : \mathbb{L}]$ signifies the linear regression modeling assumption, which is not part of \mathcal{B}), makes a diagnostic plot and computes a numerical diagnostic the Predictive Separation Index (PSI) measuring the predictive strength of the factor cap.shape.
 - (i) [20 total points for this sub-problem] The diagnostic plot is in two parts: the top panel is a histogram of the \hat{p} values for the mushrooms for which y = 0, and the bottom panel shows the same thing except for the cases in which y = 1. What would the ideal shape of these histograms be, if a factor x offers perfect information for predicting a dichotomous outcome y? Explain briefly [10 points]. Do the histograms achieve that goal with the predictor cap.shape? Explain briefly [10 points].

Solution. For the histogram of y=0, the ideal shape would be a single spike at 0, meaning all \hat{p} equalling 0 and nothing else. For when y=1, the ideal shape would be a single spike at 1, meaning all the \hat{p} equalling 1 and nothing else. This is because this would mean they are perfect predictions since our true value for the histograms is either y=0 or 1, without loss of generality, if y=1 ideally we would want to have perfect prediction, meaning all the $\hat{p}=1$ since that is the truth.

Knowing these ideal histograms and comparing, we see cap.shape is a horrible predictor. This is because we see for both graphs most the spikes are concentrated at around 0.48, far away from what we ideally want.

(ii) [20 total points for this sub-problem] The PSI, which is a numerical index that goes hand-in-hand with the diagnostic plot, is defined as follows:

$$PSI(x) = [\text{mean } (\hat{p} \text{ given } x) \text{ when } y = 1] - [\text{mean } (\hat{p} \text{ given } x) \text{ when } y = 0].$$
 (5)

What's the ideal value of the PSI, if a factor x is perfectly predictive of y? Explain briefly $[10 \ points]$. Does the PSI come close to achieving that goal with cap.shape? Explain briefly $[10 \ points]$.

Solution. Well recall what we said in the last part. If our histograms were ideal it would mean when y = 1 all our \hat{p} values would be equal to 1 and if y = 0 then all our \hat{p} values would be equal to 0. So if we were to take the mean of all the \hat{p} in the ideal case when y = 1, then the mean should also be 1. Similarly the mean of all the \hat{p} in the ideal case when y = 0 should be 0. Therefore when calculating the PSI in the ideal case we would get PSI(x) = 1 - 0 = 1. We see though after running the code provided we get,

$$PSI(x) = 0.51326496 - 0.45295970 = 0.06030526$$

Which we see is ridiculously far from ideal, meaning we don't come close to achieving our goal PSI with cap.shape.

Table 2: Predictive accuracy of each of the factors x in the mushroom data set, with PSI sorted from largest to smallest.

Factor (x)	PSI	Predictive Power
odor	0.942	extremely strong
spore.print.color	0.566	strong
gill.color	0.464	moderate
ring.type	0.363	moderate
stalk.surface.above.ring	0.346	moderate
stalk.surface.below.ring	0.3304	moderate
gill.size	0.292	moderate
stalk.color.above.ring	0.275	moderate
stalk.color.below.ring	0.265	$\operatorname{moderate}$
bruises	0.252	moderate
population	0.238	weak
habitat	0.194	weak
stalk.root	0.165	weak
gill.spacing	0.121	weak
cap.shape	0.0603	weak
cap.color	0.0477	weak
ring.number	0.0461	weak
cap.surface	0.0388	weak
veil.color	0.0235	almost none
gill.attachment	0.0167	almost none
${\tt stalk.shape}$	0.0104	almost none

(d) [30 total points for this sub-problem] Run the third code block and study the output. I've written a function called univariate.exploration that automates the process of repeating the first and second code blocks; run this function with each of the other 20 categorical predictors (save odor for last, for reasons that will become clear); in each case, pay particular attention to the table created by tab.sum, the diagnostic plot and the PSI value. Summarize Your findings by completing Table 2 (sort your entries from highest PSI down to lowest); I suggest that You use the phrases extremely strong, strong, moderate, weak, and almost none to describe the predictive power of each x variable (you can choose your own cutpoints defining those categories; there are no unique right answers; just be reasonable in your choices) [20 points]. If You were going to base the app on only one or two predictors, which ones look like the best candidates? Explain briefly [10 points].

Solution. If we were going to base the app on only one or two predictors it would have to be on odor and spore.print.color since they have the highest PSI, but it seems like odor is already an extremely strong predictor all on its own. So if we had to only pick one it would be odor.

(e) [30 total points for this sub-problem] In the output from code block 3, the PSI for cap.surface came out 0.03877928, which we could round to 0.03878. That number appears somewhere else in the regression output; where? Read pages 748–749 in DeGroot and Schervish (2012), available in the Pages tab of the course Canvas page; based on Your reading of these pages, briefly explain what the number in the regression output is trying to measure [10 points]. Does it make sense

that the PSI and this number are closely related? (This relation only holds for regressions with a dichotomous outcome; if y is continuous, the PSI doesn't make sense.) [10 points] Check several other sets of output from the univariate.exploration function with different predictors; is the relation between the PSI and the number in the regression output always the same? [10 points]

Solution. Well when we do regression we want to see how well variables x_i explain observed variation of random variable Y. Meaning we'd have a column for x, a column for y, and once we perform our regression we have a column for \hat{y} which is the predictions. If our predictions were exact and always correct the y column and \hat{y} column would match exactly. Meaning if we saw this on a scatter plot the regression line would cut through all the points, meaning all the points can be described through a linear function. That would mean though the correlation between y and \hat{y} would work out to be 1, which is what R is defined to be. In short the regression output is trying to measure the correlation between actual y values with the predicted y values.

It makes good sense here that the PSI and this number are closely related based on what is read in the book and,

$$0 \le R^2 \le 1$$
$$0 < PSI < 1$$

and as stated in the problem, this relation is only possible when y is dichotomous. Yes, we see from the outputs, the relation is always the same.

Run the fourth code block, in which a linear regression model is fit with all available predictors (let's call this the full (sampling) model [SM:F]), and study the output. You can see that R has a convenient way (poisonous \sim .) to specify all of the predictors without having to name all of them. You can further see that prediction of the poisonous status of all n=8,124 mushrooms using the full model is perfect: all of the truly poisonous mushrooms have estimated $P(y_i=1 \mid \boldsymbol{x}_i [SM:\mathbb{LF}] \mathcal{B})=1$, and all of the truly edible mushrooms have estimated $P(y_i=1 \mid \boldsymbol{x}_i [SM:\mathbb{LF}] \mathcal{B})=0$ (here \boldsymbol{x}_i is the vector of predictor variables for mushroom i).

However, this evaluation of the predictive quality of $[SM: \mathbb{LF}]$ may overstate its accuracy, because we used the same (entire) data set both to fit $[SM: \mathbb{LF}]$ and then to see how good $[SM: \mathbb{LF}]$ is. As mentioned in class, cross-validation (CV) is a good way to check on the extent of any over-fitting: You partition the data set at random into non-overlapping subsets, fit the model on one subset, and evaluate the quality of the fit on another. A well-established CV method is called s-fold cross-validation: randomly partition the entire data set into s non-overlapping exhaustive subsets $\{S_1, \ldots, S_s\}$, and loop as j (say) goes from 1 to s: set aside subset S_j , fit the model M_j on the union of all of the other subsets, and evaluate the quality of the fit on S_j , by using M_j to predict all of the y values in S_j ; when the loop is finished, average the resulting s quality estimates to get an overall evaluation of the model's predictive accuracy that avoids over-fitting.

(f) [20 total points for this sub-problem] Run the fifth code block, which implements s-fold CV with s=10 (this choice has been shown to be reliable), and study the output, which is summarized in a graph and a number: the graph plots the cross-validated predictions against the true values of the outcome variable poisonous, and the number is the CV estimate of what's called the root-mean-squared error (RMSE) $\hat{\sigma}$ of the regression predictions, namely $\hat{\sigma} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2}$ (here \hat{y}_i is the

predicted value of y_i ; what the code actually does is (a) compute the s=10 separate estimates $\hat{\sigma}_j$ of the RMSE arising from the cross-validation process and then (b) combine the $\hat{\sigma}_j$ values optimally with $\hat{\sigma} = \sqrt{\frac{1}{n} \sum_{j=1}^{s} \hat{\sigma}_j^2}$). Does the graph arising from the CV process support the idea that the predictions from the full model $[SM: \mathbb{LF}]$ are perfect, even when cross-validated? Explain briefly [10 points]. Does the cross-validated RMSE value also support this idea? Explain briefly points].

Solution. We see that in every fold every poisonous mushrooms was indeed classified as poisonous, and in every fold every mushroom that was edible was classified as edible. So yes, it does support the idea that the predictions from the model are perfect.

We see the cross-validated RMSE value worked out to be $2.06785e - 13 \approx 0$, meaning it.

We see the cross-validated RMSE value worked out to be $2.06785e-13\approx 0$, meaning it agrees with the idea of perfect prediction.

Now that we've achieved the rare feat of perfect prediction, let's think about the app we're designing: do we really want to make users supply multiple-choice answers to 21 different questions about the mushroom they're thinking of eating? The next (and nearly final) task in this problem is to see if a subset of the full set of 21 predictors can do as well, or nearly as well, in predictive accuracy as the full model $[SM: \mathbb{LF}]$.

(g) [10 total points for this sub-problem] Run the sixth code block, which implements a method called step-wise variable selection, using the Bayesian Information Criterion (BIC) we talked about in class; recall that lower BIC values correspond to better models. The output of this code block is sufficiently voluminous that I put it into another .txt file, also available on the course web page:

stat-206-mushroom-analysis-variable-selection-with-bic.txt

Study the output from this code block. This implementation of the R function step starts with the $null\ model$ consisting of just an intercept term, and then sequentially chooses the best variable not yet in the model and adds it. For the mushroom data, the algorithm goes through 11 iterations of this method, until it discovers that the model with 10 sequentially-best predictors yields perfect predictions, at which point it stops with an excellent and snarky warning message. By thinking about what the output is saying about the best subset of x variables, and in what order, answer the following three questions, as k goes from 1 to 3:

If the app were going to be based on only k variable(s), which {one is}/{ones are} best?

Explain briefly (note that 3 answers are needed here) [10 points].

Solution. Looking at the output for the first iteration it is clear that in the case k = 1 odor is the best variable to use.

Looking at the output for the second iteration we see for k = 2 we should choose variables odor and spore.print.color.

Finally for the the output of the third iteration we see for k=2 we should use variables odor, spore.print.color, and stalk.color.below.ring.

(h) [30 total points for this sub-problem] Suppose that we tentatively decide to base the app only on the mushroom's odor. We would then still have to specify a decision rule to implement in the app, as a function of the \hat{p} value it produces for a new mushroom. It's easy to show (You're not asked to show this) that the optimal decision rule is of the form

Table 3: Cross-tabulation of truth against what the app says for decision rules based on **odor** with two \hat{p} cutoffs, 0.05 (left) and 0.01 (right).

0.05 Cutoff			0.01 Cutoff						
Truth			Truth						
		Poisonous	Edible	Total			Poisonous	Edible	Total
\mathbf{App}	Poisonous	3796	0	3796	\mathbf{App}	Poisonous	3916	3408	7324
\mathbf{Says}	Edible	120	4208	4328	Says	Edible	0	800	800
	Total	3916	4208			Total	3916	4208	

If $\hat{p} \geq c$, declare the mushroom poisonous; otherwise declare it edible

for some $0 \le c \le 1$. Run the seventh code block, which summarizes the quality of two odor-based decision rules, one with c = 0.05 and the other with c = 0.01. Fill out Table 3 above by **carefully** re-arranging the output of the final two **table** commands in the code block [10 points]. Letting (as usual with classification rules) {App says poisonous} be a positive (+) finding and {App says edible} be a negative (-) result, use Your filled-out Table 3 to estimate the false-positive and false-negative rates for each of the 0.05- and 0.01-cutoff rules (You may wish to refer back to the *ELISA* case study in class and/or Take-Home Test 1) [10 points]. Considering the real-world implications of a false-positive error, and repeating for false-negative mistakes, is the 0.05-cutoff rule acceptable as a basis for our app? What about the 0.01-cutoff rule? Explain briefly in both cases [10 points].

Solution. For the 0.05 cutoff we see our false-positive (FP) rate and false-negative (FN) rate to be,

$$FP = \frac{0}{4208} = 0$$

$$FN = \frac{120}{3916} = 0.031$$

while under the 0.01 cutoff we see the FP and FN to be,

$$FP = \frac{3408}{4208} = 0.8099$$
$$FN = \frac{0}{3916} = 0$$

When considering the real world implications for the FP and FN rates, the 0.05 cutoff is not acceptable. This is because 3 percent of edible mushrooms will actually be poisonous, meaning one would eat said mushroom and face lethal effects. So while the 0.05 cut-off won't ever suggest avoiding an edible mushroom, it at times will suggest taking a poisonous mushroom.

On the other hand we see 0.01 cutoff value will be perfect. This is because even though most of the mushrooms it will label as poisonous are edible, it will label a poisonous mushroom negative. Meaning no one under this cutoff value will eat a poisonous mushroom which is the number one priority with our predictions.

(i) [10 total points for this sub-problem] Repeat part (h) (modifying code block 7 appropriately) with the app based on the best two predictor variables (instead of just odor), and exploring new

cutoff values c. Is there now, with the two best predictors instead of one, an optimal cutoff that You regard as an acceptable trade-off between false-positive and false-negative mistakes, if You were going to sell the resulting app to wild-mushroom hunters? Explain briefly [10 points].

Solution. Modifying the code to use odor and spore.print.color and choosing c values 0.05, 0.07, and 0.08, we get the following FP and FN values.

c	0.05	0.07	0.08
FP	0.148	0.137	0
FN	0	0	0.0123

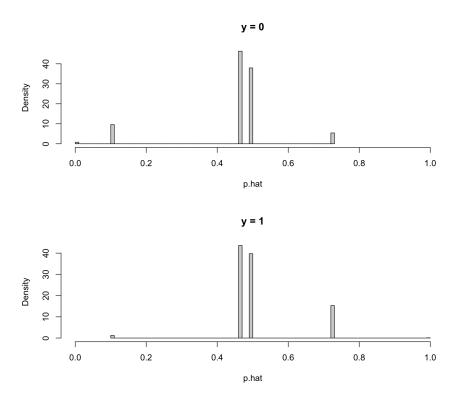
We see that for c=0.05 the FP went up when using both odor and spore.print.color, but the FN rate went down to 0 which is our first priority. When using c=0.07 the FP improves a bit by going down a little bit and we still maintain a 0 FN rate which is good. Finally for c=0.08 our FP rate improves greatly, all the way down to 0, but our FN is increased from 0 to 0.0123 which isn' good. Meaning the perfect trade off is reached with c=0.07 as our cutoff when using the two best predictors instead of one. This is because we only throw out a relatively small proportion of edible mushrooms (15%), but in return we never give a false negative to a poisonous mushroom. This FP rate under these circumstances is much better than what we saw in the last part.

(j) [20 total points for this sub-problem] A student (Burleigh Charlton) in an earlier incarnation of this course raised the following issue about our app, which is referred to in the statistical data science literature as the problem of errors-in-variables or measurement error in the predictors: Yes, odor is a great predictor, but what happens to our predictive accuracy if a non-expert user of the app cannot precisely distinguish among the odors {almond, anise, creosote, fishy, foul, musty, none, pungent, spicy}? Discuss briefly [10 points]. How do You feel now about releasing the app to the general public? Explain briefly [10 points].

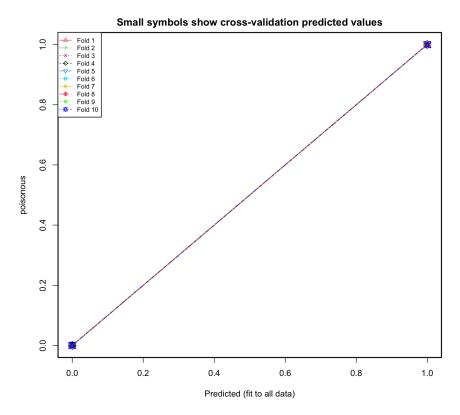
Solution. This observation definitely puts doubt on the app's capabilities under this circumstance. This is because scent can be subjective at times, meaning a fishy scent may be more musty to someone. This window of subjectivity can be dangerous when deciding on if a mushroom is edible or not based on scent descriptions of our app. I don't think releasing the app to the general public would be very wise, unless we can guarantee that non-experts have some sort of instrument that can measure the scent of something, and in which case we would need to implement that feature into the app. We could also release it to the public, but in a way that the users agree and understand that our app is more for educational purposes and not if you should eat a mushroom or not.

CODE APPENDIX

Plot referenced in part c



Plot referenced in part f



Code used which was provided by professor Draper. Most comments are deleted to save space, the only

modifications were adding comments for when noting some of the FP and FN rates. The code output for the blocks is at the very end after the code.

```
########################## the first block of code starts here
# unbuffer the output, if relevant in your R environment
\# launch a new copy of R and start with an empty R workspace
rm(list = ls(l))
raw.mushroom.data <- read.csv( 'stat-206-mushroom-data-2.txt', header = T,
                                stringsAsFactors = T)
str ( raw.mushroom.data )
print (
  n \leftarrow \dim(\text{raw.mushroom.data})[1]
raw.mushroom.data$poisonous <- ifelse( raw.mushroom.data$poisonous == 'p',
                                        1, 0)
raw.mushroom.data \leftarrow subset(raw.mushroom.data, select = -veil.type)
str ( raw.mushroom.data )
with (raw.mushroom.data, mean(poisonous))
tab.sum \leftarrow function(x.1, y)
  stopifnot( length( x.1 ) == length( y ) )
```

```
summary.function <- function(x) {
    return(list(n = length(x)), mean = mean(x, na.rm = TRUE),
                  sd = sd(x, na.rm = TRUE))
 }
  map.function <- function ( level ) {
    indices \leftarrow (x.1 = level)
   summary.function( y[ indices ] )
  }
  levels <- sort ( unique ( x.1 ) )
  out.matrix <- do.call(rbind, Map(map.function, levels))
  out.matrix <- cbind( levels, out.matrix )
  out.matrix <- rbind(out.matrix, c('Total', summary.function(y)))
  colnames( out.matrix )[ 1 ] <- as.character( substitute( x.1 ) )</pre>
  return ( out.matrix )
with (raw.mushroom.data,
      signif( table( cap.shape, useNA = 'always' ) / n, 4 ) )
with (raw.mushroom.data, tab.sum(cap.shape, poisonous))
summary (linear.model.1 <- lm (poisonous cap.shape,
                                data = raw.mushroom.data)
p.hat.linear.model.1 <- predict( linear.model.1, type = 'response')
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
hist (p. hat. linear. model. 1 raw. mushroom. data$poisonous = 0],
      nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
      xlim = \mathbf{c}(0, 1)
```

}

```
hist(p.hat.linear.model.1[raw.mushroom.data$poisonous == 1],
     nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
     xlim = \mathbf{c}(0, 1)
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(1, 1))
pdf('stat-206-take-home-test-3-part-2-solutions-figure-1.pdf')
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
hist (p. hat. linear. model. 1 raw. mushroom. data$poisonous = 0],
      nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
     xlim = \mathbf{c}(0, 1)
hist (p. hat. linear. model. 1 [raw. mushroom. data $poisonous == 1],
      nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
     xlim = \mathbf{c}(0, 1)
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(1, 1))
dev. off()
c (mean (p.hat.linear.model.1 [raw.mushroom.data$poisonous = 0]),
  mean(p.hat.linear.model.1[raw.mushroom.data$poisonous == 1]),
  mean(p.hat.linear.model.1[raw.mushroom.data$poisonous == 1]) -
    mean(p.hat.linear.model.1[raw.mushroom.data$poisonous = 0]))
univariate.exploration <- function ( new.variable ) {
 print( with( raw.mushroom.data,
              signif( table( new.variable, useNA = 'always') / n, 4 ) )
 print( with( raw.mushroom.data, tab.sum( new.variable, poisonous ) )
 print ( summary ( temp. linear. model <- lm ( poisonous ~ new. variable,
                                          data = raw.mushroom.data ) )
 p. hat.temp.linear.model <- predict (temp.linear.model, type = 'response')
 \mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
```

```
\mathbf{hist}(\mathsf{p.hat}.\mathsf{temp.linear.model}[\mathsf{raw.mushroom.data\$poisonous} = 0],
       nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
       xlim = \mathbf{c}(0, 1)
  hist (p. hat.temp.linear.model raw.mushroom.data$poisonous = 1],
       nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
       x\lim = \mathbf{c}(0, 1)
 \mathbf{par}(\mathbf{mfrow} = \mathbf{c}(1, 1))
  print(c(
   mean(p.hat.temp.linear.model[raw.mushroom.data$poisonous = 0]),
   mean(p.hat.temp.linear.model[raw.mushroom.data$poisonous = 1]),
   mean(p.hat.temp.linear.model[raw.mushroom.data$poisonous == 1]) -
   mean(p.hat.temp.linear.model[raw.mushroom.data$poisonous == 0])))
}
with (raw.mushroom.data, univariate.exploration (cap.surface))
install.packages( 'R. utils')
require (R. utils)
predictors <- colnames ( raw.mushroom.data ) [ 2:22 ]
for ( predictor in predictors) {
  printf( "\n\n======\n", predictor )
  with (raw.mushroom.data,
       univariate.exploration( eval( parse( text = predictor ) ) )
}
summary (linear.model.all.predictors < lm (poisonous ~.,
                                         data = raw.mushroom.data)
p.hat.linear.model.all.predictors <-
  predict( linear.model.all.predictors, type = 'response')
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
```

```
hist (p.hat.linear.model.all.predictors [raw.mushroom.data$poisonous = 0],
     nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
     xlim = \mathbf{c}(0, 1)
hist (p.hat.linear.model.all.predictors [raw.mushroom.data$poisonous = 1],
     nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
     xlim = \mathbf{c}(0, 1)
par(mfrow = c(1, 1))
\mathbf{c} (
mean(p.hat.linear.model.all.predictors[raw.mushroom.data$poisonous = 0]),
mean(p.hat.linear.model.all.predictors[raw.mushroom.data$poisonous == 1]),
mean(p.hat.linear.model.all.predictors[raw.mushroom.data$poisonous = 1]) -
mean(p.hat.linear.model.all.predictors[raw.mushroom.data$poisonous == 0]
)
\# [1] 2.981711e-13 1.0000000e+00 1.0000000e+00
dynamic.require <- function( package ) {</pre>
  if ( eval( parse( text = paste( 'require(', package, ')' ) ) ) {
   return( 'done')
 }
 install.packages( package )
 return( eval( parse( text = paste( 'require(', package, ')') ) )
}
dynamic.require('DAAG')
cross.validation.all.predictors.10.fold <- cv.lm(
 data = raw.mushroom.data, form.lm = formula( poisonous ~ . ),
 m = 10, printit = F)
warnings()
```

```
# Warning messages:
\# 1: In \ predict.lm(subs.lm, newdata = data[rows.out,]) :
   prediction from a rank-deficient fit may be misleading
\# 2: In predict.lm(subs.lm, newdata = data[rows.out,]) :
   prediction from a rank-deficient fit may be misleading
\# 3: In predict.lm(subs.lm, newdata = data[rows.out, ]) :
    prediction from a rank-deficient fit may be misleading
#
\# 4: In predict.lm(subs.lm, newdata = data[rows.out, ]) :
   prediction from a rank-deficient fit may be misleading
\# 5: In predict.lm(subs.lm, newdata = data[rows.out, ]) :
   prediction from a rank-deficient fit may be misleading
\# 6: In predict.lm(subs.lm, newdata = data/rows.out, )) :
   prediction from a rank-deficient fit may be misleading
\# 7: In predict.lm(subs.lm, newdata = data/rows.out, )) :
   prediction from a rank-deficient fit may be misleading
\# 8: In predict.lm(subs.lm, newdata = data[rows.out, ]) :
   prediction from a rank-deficient fit may be misleading
#
\# 9: In \ predict.lm(subs.lm, newdata = data[rows.out,]) :
   prediction from a rank-deficient fit may be misleading
\# 10: In predict.lm(subs.lm, newdata = data[rows.out, ]) :
    prediction from a rank-deficient fit may be misleading
# 11: In cv.lm(data = raw.mushroom.data, form.lm = formula(poisonous ~
  As there is >1 explanatory variable, cross-validation
#
  predicted values for a fold are not a linear function
#
#
  of corresponding overall predicted values. Lines that
   are shown for the different folds are approximate
\# the next function call computes the cross-validated
# root-mean-squared error of the regression predictions,
# which is essentially the same as the value
# from the regression with the full data set
sqrt(attr(cross.validation.all.predictors.10.fold, 'ms'))
\# [1] 2.199488e-13
# the next function call investigates which predictors can be dropped
# from the model with little or no predictive accuracy loss
null.model <- lm( poisonous ~ 1, data = raw.mushroom.data )
full.model \leftarrow lm(poisonous ~., data = raw.mushroom.data)
```

```
variable.selection.with.bic < step( null.model,
                                  scope = list ( lower = null.model,
                                  upper = full.model),
                                  direction = 'forward',
                                  trace = 1,
                                  steps = 1000, k = log(n)
# the output of this function call is in the file
    stat-206-mushroom-analysis-variable-selection-with-bic . txt
#
# open this file and study its contents
summary( linear.model.just.odor <--</pre>
          lm( poisonous ~ odor, data = raw.mushroom.data ) )
# Call:
# lm(formula = poisonous ~ odor, data = raw.mushroom.data)
\# Residuals:
    Min
            1Q Median
                              Max
                         3Q
#
\# -0.034 -0.034 0.000 0.000 0.966
\# Coefficients:
             Estimate Std. Error t value Pr(>|t|)
#
\# (Intercept) 1.37e-14
                     5.98e-03
                                  0.00
# odorc
             1.00e+00
                       1.05e-02
                                 95.30 < 2e-16 ***
\# odorf
             1.00e+00
                       6.51e-03
                                153.71 < 2e-16 ***
\# odorl
             9.37e-14
                       8.45e-03
                                 0.00
                                             1
# odorm
             1.00e+00
                       2.08e-02
                                 48.08 < 2e-16 ***
                                 5.39 7.1e-08 ***
# odorn
             3.40e-02
                       6.31e-03
                                104.54 < 2e-16 ***
# odorp
             1.00e+00
                       9.57e-03
# odors
             1.00e+00
                       7.78e-03
                                128.55 < 2e-16 ***
                       7.78e-03
                                128.55 < 2e-16 ***
# odory
             1.00e+00
# ----
# Signif. codes: 0 '*** '0.001 '** '0.01 '* '0.05 '. '0.1 ' '1
# Residual standard error: 0.12 on 8115 degrees of freedom
\# Multiple R-squared: 0.943, Adjusted R-squared: 0.943
# F-statistic: 1.67e+04 on 8 and 8115 DF, p-value: <2e-16
p.hat.linear.model.just.odor <-
  predict( linear.model.just.odor, type = 'response')
```

```
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
hist (p. hat. linear. model. just.odor [raw. mushroom. data$poisonous = 0],
      nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
      xlim = \mathbf{c}(0, 1)
hist (p. hat. linear. model. just.odor [raw. mushroom. data$ poisonous == 1],
      nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
      xlim = \mathbf{c}(0, 1)
par(mfrow = c(1, 1))
table (p.hat.linear.model.just.odor, useNA = 'always')
# p.hat.linear.model.just.odor
\# 1.36725100485403e-14 1.07412118907621e-13
                                                                   0.9999999999999
                                             0.0340136054422548
#
                   400
                                                           3528
                                       400
192
     0.99999999999851
                          1.0000000000000006
                                               1.0000000000000009
                                                                    #
#
                 2160
                                        36
                                                            576
576
      1.000000000000018
                                      < NA >
#
#
                  256
                                         0
app.says.poisonous.0.05 <- ifelse(p.hat.linear.model.just.odor > 0.05, 1, 0)
with ( raw.mushroom.data, table ( app.says.poisonous.0.05, poisonous ) )
#
                        poisonous
# app.says.poisonous.0.05
                            0
                       0 4208 120
#
#
                        1
                            0 3796
with (raw.mushroom.data, table (app.says.poisonous.0.01, poisonous))
8
#
                        poisonous
\# app.says.poisonous.0.01
#
                         800
                        1 3408 3916
#
# looking at the best decision rules based on odor and spore print color:
summary(linear.model.odor.spore.print.color <--
          lm( poisonous ~ odor + spore.print.color, data = raw.mushroom.data ) )
p.hat.linear.model.odor.spore.print.color <-
```

```
predict( linear.model.odor.spore.print.color, type = 'response')
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(2, 1))
hist (p.hat.linear.model.odor.spore.print.color[raw.mushroom.data$poisonous == 0]
      nclass = 100, main = 'y = 0', xlab = 'p.hat', prob = T,
      xlim = \mathbf{c}(0, 1)
hist (p. hat. linear. model. odor. spore. print. color [raw. mushroom. data$ poisonous = 1]
      nclass = 100, main = 'y = 1', xlab = 'p.hat', prob = T,
      xlim = \mathbf{c}(0, 1)
\mathbf{par}(\mathbf{mfrow} = \mathbf{c}(1, 1))
table (p. hat. linear. model. odor. spore. print. color, useNA = 'always')
# p.hat.linear.model.odor.spore.print.color
  -2.38704001323558e-14
                          6.99159606210441e{-15}
                                                   1.71080299696395e-14
#
                                              176
                                                                      200
#
                                                   7.00592314937111e-14
   6.71763024013884e-14
                           6.85040678851202e-14
#
                       24
                                               48
#
   7.00838615098795e-14
                           7.14192263879391e-14
                                                   8.15356602954742e-14
#
                                             1296
                                                                     1344
#
   9.80382985958486e-14
                           1.08154732503384e-13
                                                     0.0646108663730507
#
                      176
                                              200
#
     0.0719530102790713
                              0.998042094958255
                                                      0.999999999999684
#
                                             1584
#
      0.999999999999694
                                1.000000000000006
                                                        1.000000000000007
#
                       96
#
        1.0000000000000009
                                1.000000000000016
                                                        1.000000000000018
#
                                                                      128
#
        1.000000000000019
                                1.00538423886428
                                                                    < NA>
#
                      128
                                              576
                                                                        0
odor.spore.print.color.app.says.poisonous.0.05 <-
  ifelse (p.hat.linear.model.odor.spore.print.color > 0.05, 1, 0)
with (raw.mushroom.data, table (odor.spore.print.color.app.says.poisonous.0.05,
                                   poisonous ) )
#
                                                    poisonous
\# odor.spore.print.color.app.says.poisonous.0.05
#
                                                   0 3584
                                                      624 3916
#
odor.spore.print.color.app.says.poisonous.0.07 <-
  ifelse (p.hat.linear.model.odor.spore.print.color > 0.07, 1, 0)
```

```
with (raw.mushroom.data, table (odor.spore.print.color.app.says.poisonous.0.07,
                             poisonous ) )
                                            poisonous
# odor.spore.print.color.app.says.poisonous.0.07 0
#
                                           0 3632
#
                                              576 3916
# 0.05 Cutoff
     1 	 0
\# 1 - 3916 624
\# 0 - 0 3584
\# FP = 0.1483
\# FN = 0
#
\# 0.07 Cutoff
       1
             0
\# 1 - 3916
            576
\# 0 - 0
           3631
\# FP = 0.1369
\# FN = 0
#
odor.spore.print.color.app.says.poisonous.0.08 <-
  ifelse (p.hat.linear.model.odor.spore.print.color > 0.08, 1, 0)
with ( raw.mushroom.data, table ( odor.spore.print.color.app.says.poisonous.0.08,
                             poisonous ) )
                                            poisonous
# odor.spore.print.color.app.says.poisonous.0.08
#
                                           0 4208
                                                   48
                                               0 3868
#
                                           1
# 0.08 Cutoff
              0
      1
# 1 - 3868
              0
# 0 - 48
             4208
\# FP = 0
\# FN = 0.0123
'data.frame':
                      8124 obs. of 23 variables:
                        : Factor w/ 2 levels "e", "p": 2 1 1 2 1 1 1 2 1 ...
 $ poisonous
                        : Factor w/ 6 levels "b", "c", "f", "k",...: 6 6 1 6 6 6 1 1
 $ cap.shape
                        : Factor w/ 4 levels "f", "g", "s", "y": 3 3 3 4 3 4 3 4 3
 $ cap.surface
```

\$ cap.color

: Factor w/ 10 levels "b", "c", "e", "g", ...: 5 10 9 9 4 10

```
: Factor w/ 2 levels "f", "t": 2 2 2 2 1 2 2 2 2 2
  $ bruises
                                                              : Factor w/ 9 levels "a", "c", "f", "l"
  $ odor
                                                                                                                                                 , \dots : 7 \ 1 \ 4 \ 7 \ 6 \ 1 \ 1 \ 4
                                                              : Factor w/ 2 levels "a", "f": 2 2 2 2 2 2 2 2 2 2 2 \phantom{0}
  $
     gill.attachment
  $ gill.spacing
                                                              : Factor w/ 2 levels "c", "w": 1 1 1 1 2 1 1 1 1 1
  $ gill.size
                                                              : Factor w/ 2 levels "b", "n": 2 1 1 2 1 1 1 2 1 ...
                                                                  Factor w/ 12 levels "b", "e", "g", "h", ...: 5 5 6 6 5 6 3
  $ gill.color
                                                                  Factor w/ 2 levels "e", "t": 1 1 1 1 2 1 1 1 1 1 ...
  $ stalk.shape
                                                                  Factor w/ 5 levels "?", "b", "c", "e", ...: 4 3 3 4 4 3 3 3
  $ stalk.root
                                                                  Factor w/ 4 levels "f", "k"
                                                                                                                               ", "s", "y": 3 3 3 3 3 3 3 3 3 3 3
  $ stalk.surface.above.ring:
  $ stalk.surface.below.ring: Factor w/ 4 levels "f", "k",
                                                                                                                               , " s "
                                                                                                                                       : Factor w/ 9 levels "b", "c", "e", "g", ...: 8 8 8 8 8 8 8 8
  $ stalk.color.above.ring
                                                                  Factor w/ 9 levels "b", "c", "e", "g", ...: 8 8 8 8 8 8 8 8
  $ stalk.color.below.ring
  $ veil.type
                                                                  Factor w/ 1 level "p": 1 1 1 1 1 1 1 1 1 ...
                                                              : Factor w/ 4 levels "n", "o", "w", "y": 3 3 3 3 3 3 3 3 3
  $ veil.color
                                                              : Factor w/ 3 levels "n", "o", "t": 2 2 2 2 2 2 2 2 2 2 2 2 : . . . . Factor w/ 5 levels "e", "f", "l", "n", ...: 5 5 5 5 1 5 5 5
  $ ring.number
  $ ring.type
                                                              : Factor w/ 9 levels "b", "h", "k", "n", ...: 3 4 4 3 4 3 3 4
  $ spore.print.color
                                                              : Factor w/ 6 levels "a", "c", "n", "s", ...: 4 3 3 4 1 3 3 4
  $ population
                                                              : Factor w/ 7 levels "d", "g", "l", "m", ...: 6 2 4 6 2 2 4 4
  $ habitat
 [1] 8124
 'data.frame':
                                                                    22 variables:
                                    8124 obs. of
  $ poisonous
                                                              : num 1 0 0 1 0 0 0 0 1 0
                                                              : Factor w/ 6 levels "b", "c", "f", "k", ...: 6 6 1 6 6 6 1 1
  $ cap.shape
                                                              : Factor w/ 4 levels "f", "g", "s", "y": 3 3 3 4 3 4 3 4 3
  $ cap.surface
                                                              : Factor w/ 10 levels "b", "c", "e", "g", ...: 5 10 9 9 4 10
  $ cap.color
  $ bruises
                                                              : Factor w/ 2 levels "f", "t": 2 2 2 2 1 2 2 2 2 2 ...
                                                              : Factor w/ 9 levels "a", "c", "f", "l", ...: 7 1 4 7 6 1 1 4
  $ odor
                                                              : \  \, \mathbf{Factor} \  \, \mathbf{w/} \  \, \mathbf{2} \  \, \mathbf{levels} \  \, "\mathbf{a}" \, , "\mathbf{f}" \, ; \  \, \mathbf{2} \  \,
  $ gill.attachment
                                                              : Factor w/ 2 levels "c", "w": 1 1 1 1 2 1 1 1 1 1 ...
  $ gill.spacing
  $ gill.size
                                                              : Factor w/ 2 levels "b", "n": 2 1 1 2 1 1 1 2 1 ...
  $ gill.color
                                                                  Factor w/ 12 levels "b", "e", "g", "h", ...: 5 5 6 6 5 6 3
                                                                  Factor w/ 2 levels "e","t": 1 1 1 1 2 1 1 1 1 1 ...
  $ stalk.shape
                                                                 Factor w/ 5 levels "?", "b", "c", "e", ...: 4 3 3 4 4 3 3 3
  $ stalk.root
                                                                  Factor w/ 4 levels "f", "k"
                                                                                                                               , "s", "y": 3 3 3 3 3 3 3 3 3 3
  $ stalk.surface.above.ring:
                                                                                                                                "s", "y": 3 \ 3 \ 3 \ 3 \ 3 \ 3 \ 3 \ 3
  $ stalk.surface.below.ring: Factor w/ 4 levels "f","k"
                                                                                                                                , "e", "g",...: 8 8 8 8 8 8 8 8 8
  $ stalk.color.above.ring
                                                                  Factor w/ 9 levels "b", "c"
  $ stalk.color.below.ring
                                                                                                                               ,"e","g",...: 8 8 8 8 8 8 8 8 8
                                                              : Factor w/ 9 levels "b", "c"
  $ veil.color
                                                              : Factor w/ 4 levels "n", "o", "w", "y": 3 3 3 3 3 3 3 3 3
                                                              : Factor w/ 3 levels "n", "o", "t": 2 2 2 2 2 2 2 2 2 ...
  $ ring.number
                                                                 Factor w/ 5 levels "e", "f", "l", "n", ...: 5 5 5 5 1 5 5 5
  $ ring.type
                                                              : Factor w/ 9 levels "b", "h", "k", "n", ...: 3 4 4 3 4 3 3 4
  $ spore.print.color
                                                                  Factor w/ 6 levels "a", "c", "n", "s", ...: 4 3 3 4 1 3 3 4
  $ population
                                                              : Factor w/ 7 levels "d", "g", "l", "m", ...: 6 2 4 6 2 2 4 4
  $ habitat
new. variable
                                                                                                       <NA>
                  f
0.2856000 \ 0.0004924 \ 0.3146000 \ 0.3993000 \ 0.0000000
           new.variable n
                                                    mean
                                                                           \operatorname{sd}
                                         2320 \ \ 0.3275862 \ \ 0.4694342
[1,] 1
```

[2,] 2	4 1	0
$\begin{bmatrix} 2 \ , \end{bmatrix} 2 \\ \begin{bmatrix} 3 \ , \end{bmatrix} 3$	2556 0.5524257	
$\begin{bmatrix} 4 \end{bmatrix}$ 4		
[5,] "Total"	8124 0.4820286	0.4997077
Call: lm(formula = pois	onous ~ new.var	\mathbf{riable} , $\mathbf{data} = \mathbf{raw}.\mathbf{mushroom.data}$)
Residuals:		
	Median 3Q -0.3276 0.4636	
Coefficients:		
	imate Std. Erro	or \mathbf{t} value $\Pr(> \mathbf{t})$
		7 32.200 < 2e - 16 ***
9		2 2.742 0.00612 **
		5 16.001 < 2e-16 ***
new . variabley 0.	$20879 \qquad 0.0133$	2 15.671 < 2e-16 ***
Residual standard	error: 0.49 on	8120 degrees of freedom
		Adjusted R-squared: 0.03842
F-statistic: 109.	2 on 3 and 8120	DF, p-value: $< 2.2e-16$
	* 0011 * 11 0 000 *	
[1] 0.46333584 0.		
Error in instail.	packages : Opda	ating loaded packages
c	ap.shape ====	
new.variable		
b	\mathbf{c} f	k s x $< NA>$
		1019000 0.0039390 0.4500000 0.0000000
new.variable		sd
$\begin{bmatrix} 1 & 1 \end{bmatrix}$	$\begin{array}{ccc} 452 & 0.1061947 \\ 4 & 1 \end{array}$	0.308428
$\begin{bmatrix} 2 \ , \end{bmatrix} \ 2 \ \begin{bmatrix} 3 \ , \end{bmatrix} \ 3$	3152 0.4936548	
[4,] 4	828 0.7246377	
[5,] 5	32 0	0
[6,] 6	3656 0.4671772	0.4989898
[7,] "Total"	8124 0.4820286	0.4997077
Call:	~	
lm(formula = pois	onous new. var	\mathbf{riable} , $\mathbf{data} = \mathbf{raw}.\mathbf{mushroom.data}$)
Residuals:		
	Median 3Q	Max
-0.7246 -0.4672 -	<u> </u>	

Coefficients:

```
Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
                                      4.659 \ 3.22e-06 ***
(Intercept)
                0.10619
                            0.02279
new.variablec 0.89381
                            0.24335 3.673 0.000241 ***
                            0.02437 15.898 < 2e-16 ***
new.variablef 0.38746
                            0.02834
                                      21.824 < 2e-16 ***
new. variablek 0.61844
                            0.08864 \quad -1.198 \quad 0.230926
new. variables -0.10619
new. variablex 0.36098
                                     14.942 < 2e-16 ***
                            0.02416
```

Residual standard error: 0.4846 on 8118 degrees of freedom Multiple R-squared: 0.06031, Adjusted R-squared: 0.05973 F-statistic: 104.2 **on** 5 and 8118 DF, p-value: < 2.2e-16

$[1] \quad 0.45295970 \quad 0.51326496 \quad 0.06030526$

------ cap.surface

new. variable

f $0.2856000 \ 0.0004924 \ 0.3146000 \ 0.3993000 \ 0.0000000$

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					
$ \begin{bmatrix} 2 & , \\ 3 & , \\ 3 & \\ 4 & 1 & 0 \\ 2556 & 0.5524257 & 0.4973413 \\ [4 & ,] & 3244 & 0.5363748 & 0.498752 $		new.variable	n	mean	sd
[3,] 3 2556 0.5524257 0.4973413 [4,] 4 3244 0.5363748 0.498752	[1,]	1	2320	0.3275862	0.4694342
$\begin{bmatrix} 4 & 1 \end{bmatrix}$ 4 3244 0.5363748 0.498752	[2,]	2	4	1	0
L /1	[3,]	3	2556	0.5524257	0.4973413
[5,] "Total" 8124 0.4820286 0.4997077	[4,]	4	3244	0.5363748	0.498752
	[5,]	"Total"	8124	0.4820286	0.4997077

Call:

lm(formula = poisonous ~ new. variable, data = raw.mushroom.data)

Residuals:

Coefficients:

	Estimate	Std. Error	t value	$\Pr(> \mathbf{t})$	
(Intercept)	0.32759	0.01017	32.200	< 2e-16	***
new.variableg	0.67241	0.24522	2.742	0.00612	**
new.variables	0.22484	0.01405	16.001	< 2e-16	***
new. variabley	0.20879	0.01332	15.671	< 2e-16	***

Residual standard error: 0.49 on 8120 degrees of freedom Multiple R-squared: 0.03878, Adjusted R-squared: 0.03842 F-statistic: 109.2 **on** 3 and 8120 DF, p-value: < 2.2e-16

 $[1] \quad 0.46333584 \quad 0.50211511 \quad 0.03877928$

```
=== cap.color =
new.variable
                                                b
                                                                                                               \mathbf{c}
                                                                                                                                                                             е
                                                                                                                                                                                                                                           g
                                                                                                                                                                                                                                                                                                         n
                                                                                                                                                                                                                                                                                                                                                                       р
                                                                                                       <NA>
                                                              У
 0.020680 \ \ 0.005416 \ \ 0.184600 \ \ 0.226500 \ \ 0.281100 \ \ 0.017730 \ \ 0.001969 \ \ 0.001969 \ \ 0.128000 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.001969 \ \ 0.0
                                         new.variable n
                                                                                                                                                                     mean
                                                                                                                                                                                                                                           \operatorname{sd}
          [1,]
                                                                                                                                    168
                                                                                                                                                                      0.7142857 \ 0.4531045
          [2,] 2
                                                                                                                                    44
                                                                                                                                                                      0.2727273 \ 0.4505106
          [3,]3
                                                                                                                                    1500 0.584
                                                                                                                                                                                                                                          0.4930579
           [4,]
                                       4
                                                                                                                                    1840 0.4391304 0.496416
                                                                                                                                    2284 \quad 0.4465849 \quad 0.4972475
           [5,] 5
           [6,]6
                                                                                                                                    144
                                                                                                                                                                      0.61111111 \ \ 0.4891996
          [7,]
                                         7
                                                                                                                                    16
                                                                                                                                                                      0
                                                                                                                                                                                                                                           0
           [8,] 8
                                                                                                                                    16
                                                                                                                                                                      0
                                                                                                                                                                                                                                           0
```

Call:

[9,]9

[10,] 10

[11,] "Total"

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

 $1040 \quad 0.3076923 \quad 0.4617605$

 $1072 \quad 0.6268657 \quad 0.4838631$

 $8124 \quad 0.4820286 \quad 0.4997077$

Residuals:

Min 1Q Median 3Q Max
$$-0.7143$$
 -0.4466 -0.3077 0.5534 0.7273

Coefficients:

	Estimate	Std. Error	t value	$\Pr(> \mathbf{t})$	
(Intercept)	0.71429	0.03764	18.975	< 2e-16	***
new.variablec	-0.44156	0.08263	-5.344	9.34e - 08	***
new.variablee	-0.13029	0.03970	-3.282	0.00103	**
new.variableg	-0.27516	0.03932	-6.997	$2.82{\rm e}\!-\!12$	***
new.variablen	-0.26770	0.03900	-6.864	$7.21 \mathrm{e}{-12}$	***
new.variablep	-0.10317	0.05541	-1.862	0.06263	
new.variabler	-0.71429	0.12765	-5.595	2.27e - 08	***
new.variableu	-0.71429	0.12765	-5.595	2.27e - 08	***
new .variablew	-0.40659	0.04057	-10.022	< 2e-16	***
new . variabley	-0.08742	0.04049	-2.159	0.03086	*

Residual standard error: 0.4879 on 8114 degrees of freedom Multiple **R**-squared: 0.04771, Adjusted **R**-squared: 0.04665 F-statistic: 45.17 on 9 and 8114 DF, p-value: < 2.2e-16

$\begin{bmatrix} 1 \end{bmatrix}$ 0.45903087 0.50674109 0.04771021

[7,]7

[8,]8

new.variable <NA> f \mathbf{t} $0.5844 \ 0.4156 \ 0.0000$ new.variable n mean sd 4748 0.6933446 0.4611536 [1,] 1 3376 0.1848341 0.3882204 [2,]2[3,] "Total" 8124 0.4820286 0.4997077 Call: lm(formula = poisonous ~ new.variable, data = raw.mushroom.data) Residuals: Min 1Q Median $3\mathbf{Q}$ Max -0.6933 -0.1848 -0.1848 0.3067 0.8152Coefficients: Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ $0.006274 \quad 110.50$ (Intercept) 0.693345 < 2e - 16 ***new. variable t - 0.5085100.009733 -52.24<2e-16****Residual standard error: 0.4323 on 8122 degrees of freedom Multiple R-squared: 0.2515, Adjusted R-squared: 0.2514 F-statistic: 2730 on 1 and 8122 DF, p-value: < 2.2e-16[1] 0.3607826 0.6123153 0.2515327 odor ==== new. variable f l \mathbf{m} a \mathbf{c} <NA> new.variable n mean sd [1,] 1 400 0 0 [2,] 2 192 10 [3,] 3 2160 10 [4,]4400 0 [5,] 5 36 1 [6,]6 $3528 \quad 0.03401361 \quad 0.1812898$

0

256 1576

1

```
[9,]9
                     576 1
                     8124 0.4820286
[10,] "Total"
                                        0.4997077
Call:
lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)
Residuals:
     Min
                      Median
                                              Max
                 1Q
                                     3Q
-0.03401 -0.03401
                     0.00000
                                0.00000
                                          0.96599
Coefficients:
                 Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept)
                1.366e - 14
                            5.976e - 03
                                          0.000
                                                       1
new.variablec 1.000e+00
                           1.049e-02
                                        95.299
                                                 < 2e-16 ***
new. variablef 1.000\,\mathrm{e}{+00} 6.506\,\mathrm{e}{-03} 153.711
                                                 < 2e-16 ***
                                                 1
new. variablel 9.370e-14 8.451e-03
                                        0.000
new. variablem 1.000\,\mathrm{e}{+00} 2.080\,\mathrm{e}{-02} 48.085 < 2\,\mathrm{e}{-16} ***
new. variablen 3.401e-02 6.306e-03
                                          5.394 \quad 7.08e - 08 ***
new. variablep 1.000\,\mathrm{e}{+00} 9.566\,\mathrm{e}{-03} 104.536 < 2\,\mathrm{e}{-16} ***
new. variables 1.000e+00 - 7.779e-03 128.554 < 2e-16 ***
new.variabley 1.000e+00
                            7.779e-03 128.554 < 2e-16 ***
Residual standard error: 0.1195 on 8115 degrees of freedom
Multiple R-squared: 0.9429, Adjusted R-squared: 0.9428
F-statistic: 1.674e+04 on 8 and 8115 DF, p-value: < 2.2e-16
[1] 0.02754714 0.97039878 0.94285164
                  gill.attachment ==
new. variable
      a
                f
                     < NA >
0.02585 \ 0.97420 \ 0.00000
     new.variable n
                          mean
                                      \operatorname{sd}
[1,] 1
                    210
                          0.08571429 \ 0.2806106
[2,] 2
                    7914 0.4925449 0.499976
[3,] "Total"
                    8124 0.4820286
                                      0.4997077
Call:
lm(formula = poisonous ~ new. variable, data = raw.mushroom.data)
Residuals:
     Min
                 1Q
                      Median
                                     3\mathbf{Q}
                                              Max
-0.49254 -0.49254 -0.08571 0.50746
                                          0.91429
```

Coefficients:

```
Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
               0.08571
                           0.03420
                                      2.507
                                              0.0122 *
(Intercept)
new.variablef 0.40683
                           0.03465
                                     11.742
                                              <2e-16****
Residual standard error: 0.4955 on 8122 degrees of freedom
Multiple R-squared: 0.01669, Adjusted R-squared: 0.01657
F-statistic: 137.9 on 1 and 8122 DF, p-value: < 2.2e-16
[1] 0.4739822 0.4906748 0.0166926
           === gill.spacing =
new. variable
                <NA>
     \mathbf{c} w
0.8385 \ 0.1615 \ 0.0000
     new.variable n
                             \operatorname{sd}
                        mean
[1,]1
                 6812 0.5584263 0.4966111
[2,] 2
                   1312 \ 0.08536585 \ 0.2795319
              8124 \quad 0.4820286 \quad 0.4997077
[3,] "Total"
Call:
lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)
Residuals:
     Min
               1Q
                     Median
                                   3\mathbf{Q}
-0.55843 -0.55843 -0.08537 0.44157
                                       0.91463
Coefficients:
               Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept) 0.558426 0.005676
                                       98.39
                                               <2e-16 ***
new. variablew -0.473060 0.014123 -33.50
                                               <2e-16 ***
Residual standard error: 0.4684 on 8122 degrees of freedom
Multiple R-squared: 0.1214, Adjusted R-squared: 0.1213
F-statistic: 1122 on 1 and 8122 DF, p-value: < 2.2e-16
[1] 0.4235231 0.5448965 0.1213734
                 gill.size ====
new. variable
     b n
                <NA>
0.6908 \ 0.3092 \ 0.0000
     new.variable n
```

 sd

mean

```
[1,] 1
                   5612 \quad 0.3014968 \quad 0.4589488
[2,]2
                   2512 \quad 0.8853503 \quad 0.3186621
[3,] "Total"
                  8124 0.4820286 0.4997077
Call:
lm(formula = poisonous ~ ^{\sim} new. \, variable \, , \, data = raw.mushroom. \, data)
Residuals:
    Min
              1Q Median
                               3\mathbf{Q}
                                      Max
-0.8853 -0.3015 -0.3015 0.1147
                                   0.6985
Coefficients:
               Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
              0.301497
                        0.005615
                                      53.70
                                              <2e-16****
(Intercept)
new. variablen 0.583854
                          0.010097
                                      57.83
                                               <2e-16 ***
Residual standard error: 0.4206 on 8122 degrees of freedom
Multiple \mathbf{R}-squared: 0.2916, Adjusted \mathbf{R}-squared: 0.2915
F-statistic: 3344 on 1 and 8122 DF, p-value: < 2.2e-16
[1] 0.3414563 0.6330827 0.2916263
                 gill.color =
new.variable
       b
                 е
                                    h
                                            k n
                          g
                                                                 O
                                   <NA>
                   W
                            У
new.variable n
                         mean
                                     \operatorname{sd}
 [1,] 1
                    1728 1
                                     0
 [2,] 2
                    96
                                     0
 [3,]3
                    752 \quad 0.6702128
                                     0.4704486
                    732 \quad 0.7213115
 [4,]4
                                     0.4486605
 [5,] 5
                    408 \quad 0.1568627
                                     0.3641178
 [6,]
                    1048 \ 0.1068702
                                     0.3090957
      6
 [7,]
                    64 \quad 0
 [8,] 8
                    1492 0.4289544
                                     0.4950927
 [9,]9
                    24
[10,] 10
                    492 \quad 0.09756098 \quad 0.2970221
                    1202\ 0.2046589
[11,] 11
                                     0.4036201
[12,] 12
                    86
                         0.255814
                                     0.4388768
[13,] "Total"
                    8124 \quad 0.4820286
                                     0.4997077
```

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 113.50 1.000e+008.811e-03<2e-16****new. variable $e^{-1.000}$ e+00 3.841e - 02-26.04<2e-16****new. variable g - 3.298e - 011.600e-02-20.61<2e-16 *** -17.25<2e-16 *** **new**. variableh -2.787e-011.615e-02-41.82new. variablek -8.431e-012.016e-02<2e-16****new. variable -8.931e-011.434e-02-62.28<2e-16****new. variable 0.000 = -1.000 = -1.0004.662e-02-21.45<2e-16 *** -44.12new. variable -5.710e-011.294e-02<2e-16 *** 1.469e - 14new. variabler 7.528e-020.001 1.872e-02-48.22<2e-16******new**. variable -9.024e-01**new**. variablew -7.953e-011.376e-02-57.82<2e-16 *** new. variable varia4.047e - 02-18.39<2e-16 ***

Residual standard error: 0.3663 on 8112 degrees of freedom Multiple **R**-squared: 0.4635, Adjusted **R**-squared: 0.4628 F-statistic: 637.2 on 11 and 8112 DF, p-value: < 2.2e-16

$[1] \quad 0.2585941 \quad 0.7221236 \quad 0.4635296$

stalk.shape

new.variable

e $t < NA > 0.4328 \ 0.5672 \ 0.0000$

new.variable n mean sd

[1,] 1 3516 0.5403868 0.4984371 [2,] 2 4608 0.4375 0.4961322 [3,] "Total" 8124 0.4820286 0.4997077

Call:

 $lm(formula = poisonous \ \tilde{} \ new. \ variable, \ data = raw.mushroom. \ data)$

Residuals:

Coefficients:

Estimate Std. Error ${\bf t}$ value $\Pr(>|{\bf t}|)$ (Intercept) 0.540387 0.008384 64.455 <2e-16 *** new.variablet -0.102887 0.011132 -9.242 <2e-16 ***

Residual standard error: 0.4971 on 8122 degrees of freedom Multiple **R**-squared: 0.01041, Adjusted **R**-squared: 0.01029 F-statistic: 85.42 on 1 and 8122 DF, p-value: < 2.2e-16

[1] 0.47701166 0.48741954 0.01040788

```
=== stalk.root ====
new. variable
               b
                     \mathbf{c} e
                                                <NA>
0.30530 \ \ 0.46480 \ \ 0.06844 \ \ 0.13790 \ \ 0.02363 \ \ 0.00000
     new.variable n
                        mean
                                      \operatorname{sd}
[1,] 1
                    2480 0.7096774 0.4540027
[2,]2
                    3776 0.4915254 0.4999944
[3,]3
                          0.07913669 \ 0.2701951
                    556
[4,]4
                    1120 \ 0.2285714 \ 0.4201001
[5,]5
                    192 	 0
[6,] "Total"
                    8124 0.4820286 0.4997077
```

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

	Estimate	Std. Error	t value	$\Pr(> \mathbf{t})$	
(Intercept)	0.709677	0.009169	77.40	< 2e - 16	***
new.variableb	-0.218152	0.011802	-18.48	< 2e - 16	***
new.variablec	-0.630541	0.021425	-29.43	< 2e - 16	***
new.variablee	-0.481106	0.016438	-29.27	< 2e - 16	***
new.variabler	-0.709677	0.034204	-20.75	< 2e - 16	***

Residual standard error: 0.4566 on 8119 degrees of freedom Multiple **R**-squared: 0.1655, Adjusted **R**-squared: 0.1651 F-statistic: 402.5 on 4 and 8119 DF, p-value: < 2.2e-16

[1] 0.4022577 0.5677476 0.1654900

stalk.surface.above.ring

new.variable

```
f
                                              <NA>
                  k
0.067950 \ 0.292000 \ 0.637100 \ 0.002954 \ 0.000000
     new.variable n
                          mean
[1,]
                     552
                          0.2608696 \quad 0.4395072
[2,] 2
                    2372 0.9392917 0.2388448
[3,] 3
                     5176 \quad 0.2967543 \quad 0.4568714
[4,]4
                    24
                          0.33333333 \ 0.4815434
[5,] "Total"
                    8124 0.4820286 0.4997077
Call:
lm(formula = poisonous ~ new. variable, data = raw. mushroom. data)
Residuals:
     Min
                       Median
                 1Q
                                      3\mathbf{Q}
                                               Max
-0.93929 \quad -0.29675 \quad -0.26087
                                0.06071
                                           0.73913
Coefficients:
                Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept)
                 0.26087
                              0.01721
                                        15.160
                                                   <2e-16****
new. variablek
                0.67842
                              0.01911
                                        35.510
                                                   <2e-16 ***
new. variables
                 0.03588
                              0.01810
                                         1.982
                                                   0.0475 *
new. variabley
                 0.07246
                              0.08430
                                         0.860
                                                   0.3900
Residual standard error: 0.4043 on 8120 degrees of freedom
Multiple R-squared: 0.3457, Adjusted R-squared: 0.3454
F-statistic: 1430 on 3 and 8120 DF, p-value: < 2.2e-16
[1] 0.3154020 0.6610798 0.3456778
              == stalk.surface.below.ring
new. variable
       f
                k
                         \mathbf{S}
                                        < NA >
0.07386 \ 0.28360 \ 0.60760 \ 0.03496 \ 0.00000
     new.variable n
                          mean
                                      \operatorname{sd}
[1,] 1
                    600
                          0.24
                                      0.4274395
[2,] 2
                    2304 \ 0.9375
                                      0.242114
                    4936 \quad 0.3111831 \quad 0.4630244
[3,]3
[4,]4
                    284
                          0.2676056 \ 0.4434923
[5,] "Total"
                    8124 \quad 0.4820286 \quad 0.4997077
Call:
lm(formula = poisonous ~ new. variable, data = raw. mushroom. data)
Residuals:
```

Max

 $3\mathbf{Q}$

1Q Median

Min

```
-0.9375 -0.3112 -0.2400 0.0625 0.7600
```

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ 14.375 < 2e-16 ***(Intercept) 0.240000.01670new. variablek 37.211 $< 2e{-}16 ***$ 0.697500.01874 $4.026 \quad 5.73 \,\mathrm{e}{-05} \;***$ new.variables 0.07118 0.01768**new**. variabley 0.027610.029460.9370.349

Residual standard error: 0.409 on 8120 degrees of freedom Multiple **R**-squared: 0.3304, Adjusted **R**-squared: 0.3302 F-statistic: 1336 on 3 and 8120 DF, p-value: < 2.2e-16

[1] 0.3227483 0.6531857 0.3304375

stalk.color.above.ring

new.variable

b **c** e g n o p v y <NA>

	new. variable	n	mean	\mathbf{sd}
[1,]	1	432	1	0
[2,]	2	36	1	0
[3,]	3	96	0	0
[4,]	4	576	0	0
[5,]	5	448	0.9642857	0.1857843
[6,]	6	192	0	0
[7,]	7	1872	0.6923077	0.4616618
[8,]	8	4464	0.3835125	0.4862958
[9,]	9	8	1	0
[10,]	"Total"	8124	0.4820286	0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 1.000e+002.047e - 0248.841 <2e-16 *** new. variablec 9.813e - 147.382e-020.0001.000 **new**. variable -1.000e+004.802e-02 -20.826<2e-16******new**. variable g -1.000e+002.709e-02 -36.920<2e-16 *** 2.870e-02new. variable -3.571e-02-1.2450.213

```
new. variableo -1.000e+00
                          3.691e - 02 - 27.092
                                                <2e-16 ***
new. variable -3.077e-01
                          2.271e-02 -13.546
                                                <2e-16 ***
new. variablew -6.165e-01
                          2.144e-02 -28.751
                                                <2e-16 ***
new. variable y -2.260e-14
                                                 1.000
                          1.518e - 01
                                       0.000
```

Residual standard error: 0.4256 on 8115 degrees of freedom Multiple R-squared: 0.2755, Adjusted R-squared: 0.2748 F-statistic: 385.7 on 8 and 8115 DF, p-value: < 2.2e-16

==== stalk.color.below.ring ===

[1] 0.3492453 0.6247129 0.2754676

```
new. variable
  b
      \mathbf{c}
         е
            g
                n
                   O
                       р
  <NA>
```

new.variable n mean sd

[1,]	1	432	1	0
[2,]	2	36	1	0
[3,]	3	96	0	0
[4,]	4	576	0	0
[5,]	5	512	0.875	0.3310424
[6,]	6	192	0	0
[7,]	7	1872	0.6923077	0.4616618
[8,]	8	4384	0.3832117	0.4862247
[9,]	9	24	1	0
[10,]	"Total"	8124	0.4820286	0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Min 1Q Median $3\mathbf{Q}$ Max $-0.8750 \quad -0.3832$ 0.00000.30770.6168

Coefficients:

	Estimate	Std. Error	t value	$\Pr(> \mathbf{t})$	
(Intercept)	1.000e+00	$2.062\mathrm{e}\!-\!02$	48.490	< 2e-16	***
new.variablec	$4.091\mathrm{e}{-14}$	$7.436\mathrm{e}{-02}$	0.000	1	
new.variablee	$-1.000\mathrm{e}{+00}$	$4.836\mathrm{e}\!-\!02$	-20.676	< 2e-16	***
new. variableg	$-1.000\mathrm{e}{+00}$	$2.728\mathrm{e}\!-\!02$	-36.655	< 2e-16	***
new. variablen	$-1.250\mathrm{e}{-01}$	$2.800\mathrm{e}{-02}$	-4.464	$8.16\mathrm{e}{-06}$	***
new. variableo	$-1.000\mathrm{e}{+00}$	$3.718\mathrm{e}\!-\!02$	-26.897	< 2e-16	***
new. variablep	-3.077e-01	$2.288\mathrm{e}\!-\!02$	-13.449	< 2e-16	***
new variablew	-6.168e-01	2.162e-02	-28.535	< 2e-16	***

Residual standard error: 0.4286 on 8115 degrees of freedom Multiple \mathbf{R} -squared: 0.2649, Adjusted \mathbf{R} -squared: 0.2642 F-statistic: 365.6 on 8 and 8115 DF, p-value: < 2.2e-16

[1] 0.3543188 0.6192611 0.2649423

=== veil.color ==

new. variable

<NA> W $0.0118200 \ \ 0.0118200 \ \ 0.9754000 \ \ 0.0009847 \ \ 0.0000000$ new variable n mean sd

	now. variable	11	IIICCIII	
[1,]	1	96	0	0
[2,]	2	96	0	0

$$\begin{bmatrix} 3 \ , \end{bmatrix} \ 3$$
 7924 0.4931853 0.4999851

$$[4,]$$
 4 8 1 0

[5,] "Total" 8124 0.4820286 0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Min 1Q Median $3\mathbf{Q}$ Max $-0.4932 \quad -0.4932$ $0.0000 \quad 0.5068 \quad 0.5068$

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 1.568e-13 5.041e-02 0.000**new**. variableo -1.082e-13 7.129e-020.0001 **new**. variablew 4.932e-01 5.071e-029.725 < 2e-16 *****new**. variabley $1.000\,\mathrm{e}{+00}$ $1.817\,\mathrm{e}{-01}$ 5.502 $3.86\,\mathrm{e}{-08}$ ***

Residual standard error: 0.4939 on 8120 degrees of freedom Multiple R-squared: 0.02354, Adjusted R-squared: 0.02318 F-statistic: 65.25 on 3 and 8120 DF, p-value: < 2.2e-16

 $\begin{bmatrix} 1 \end{bmatrix}$ 0.47068251 0.49422063 0.02353812

ring.number ====

new. variable

 \mathbf{t} O $0.004431 \ 0.921700 \ 0.073860 \ 0.000000$

$[1\ ,]\ 1$	n mean 36 1 7488 0.508547 600 0.12 8124 0.4820286	$egin{array}{c} 0 \ 0.4999603 \ 0.3252327 \end{array}$			
Call: lm(formula = poiso	onous ~ new.va i	\mathbf{riable} , $\mathbf{data} = \mathbf{raw.mushroom.data}$)			
Residuals:	•	Max 0.8800			
(Intercept) 1.0 new . variableo -0 .	$ \begin{array}{r} 00000 & 0.0813 \\ 49145 & 0.0815 \end{array} $	or \mathbf{t} value $\Pr(> \mathbf{t})$ 5 12.292 < 2e-16 *** 5 -6.027 1.75e-09 *** 6 -10.507 < 2e-16 ***			
Residual standard error: 0.4881 on 8121 degrees of freedom Multiple R —squared: 0.04613, Adjusted R —squared: 0.04589 F—statistic: 196.4 on 2 and 8121 DF, p—value: $< 2.2e-16$ [1] 0.45979396 0.50592110 0.04612713					
new.variable	ing.type ====				
e f 0.341700 0.005908 new.variable [1,] 1 [2,] 2 [3,] 3 [4,] 4 [5,] 5 [6,] "Total"		$egin{array}{c} 0 \\ 0 \\ 0 \\ 0.4042232 \end{array}$			
Call: lm(formula = poiso	onous ~ new.va i	\mathbf{riable} , $\mathbf{data} = \mathbf{raw.mushroom.data}$)			
Residuals:	Median 3 Q -0.2056 0.3631	Max 0.7944			

Coefficients:

```
Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept)
                                         84.18 < 2e-16 ***
                 0.636888
                             0.007566
new. variable f -0.636888
                                       -10.97 < 2e-16 ***
                             0.058033
new. variablel
               0.363112
                             0.013411
                                         27.07 < 2e-16 ***
                                          5.43 \quad 5.79e - 08 ***
new. variablen
               0.363112
                             0.066868
new. variable 0.431242
                                        -43.72 < 2e-16 ***
                             0.009864
```

Residual standard error: 0.3986 on 8119 degrees of freedom Multiple **R**-squared: 0.3639, Adjusted **R**-squared: 0.3636 F-statistic: 1161 on 4 and 8119 DF, p-value: $< 2.2e{-}16$

 $[1] \quad 0.3066008 \quad 0.6705372 \quad 0.3639364$

```
new.variable

b h k n o r u w
y <NA>
0.005908 0.200900 0.230400 0.242200 0.005908 0.008863 0.005908 0.293900 0.005908
```

0.005908 0.200900 0.230400 0.242200 0.005908 0.008863 0.005908 0.293900 0.005908 0.

new variable n mean sd

	new. variable	11	mean	su
[1,]	1	48	0	0
[2,]	2	1632	0.9705882	0.1690095
[3,]	3	1872	0.1196581	0.324648
[4,]	4	1968	0.1138211	0.3176746
[5,]	5	48	0	0
[6,]	6	72	1	0
[7,]	7	48	0	0
[8,]	8	2388	0.758794	0.4279046
[9,]	9	48	0	0
10,]	"Total"	8124	0.4820286	0.4997077

spore.print.color

Call:

 $\mathbf{lm}(\mathbf{formula} = \mathtt{poisonous} \ \tilde{\ } \mathbf{new}. \ \mathbf{variable} \ , \ \mathbf{data} = \mathtt{raw}. \ \mathtt{mushroom}. \ \mathbf{data})$

Residuals:

Coefficients:

Residual standard error: 0.3292 on 8115 degrees of freedom Multiple **R**-squared: 0.5665, Adjusted **R**-squared: 0.566 F-statistic: 1325 on 8 and 8115 DF, p-value: < 2.2e-16

 $[1] \quad 0.2089720 \quad 0.7754458 \quad 0.5664738$

```
population
new. variable
            c n s v y
                                                <NA>
     a
0.04727 \ 0.04185 \ 0.04924 \ 0.15360 \ 0.49730 \ 0.21070 \ 0.00000
    new.variable n mean
                            \operatorname{sd}
[1,] 1
                384 - 0
                               0
                 340 \quad 0.1529412 \quad 0.3604613
[2,]2
[3,]3
                 400 - 0
                               0
                1248 \ 0.2948718 \ 0.4561679
[4,]4
[5,] 5
                4040 \quad 0.7049505 \quad 0.4561215
[6,]6
                1712 0.3785047 0.485156
[7,] "Total" 8124 0.4820286 0.4997077
```

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Min	$1\mathbf{Q}$	Median	$3\mathbf{Q}$	Max
-0.7049	-0.3785	0.0000	0.2950	0.8471

Coefficients:

	Estimate	Std. Error	t value	$\Pr(> \mathbf{t})$	
(Intercept)	$1.208\mathrm{e}{-13}$	$2.227\mathrm{e}{-02}$	0.000	1	
new.variablec	$1.529\mathrm{e}{-01}$	$3.250\mathrm{e}{-02}$	4.705	$2.58{\rm e}\!-\!06$	***
new.variablen	$-1.343 e\!-\!13$	3.118e - 02	0.000	1	
new.variables	$2.949\mathrm{e}{-01}$	$2.547\mathrm{e}{-02}$	11.577	< 2e-16	***
new . variablev	$7.050\mathrm{e}{-01}$	2.331e-02	30.245	< 2e-16	***
new . variabley	3.785 e - 01	$2.465\mathrm{e}\!-\!02$	15.358	< 2e-16	***

Residual standard error: 0.4365 on 8118 degrees of freedom Multiple **R**-squared: 0.2375, Adjusted **R**-squared: 0.2371 F-statistic: 505.8 on 5 and 8118 DF, p-value: $< 2.2e{-}16$

```
— habitat —
new.variable
      d
                      l
                               {
m m}
                                       р
                                                     u
0.38750 \ \ 0.26440 \ \ 0.10240 \ \ 0.03594 \ \ 0.14080 \ \ 0.04530 \ \ 0.02363 \ \ 0.00000
     new.variable n
                           mean
                                       \operatorname{sd}
[1,] 1
                     3148 \quad 0.4027954 \quad 0.4905382
[2,]
     2
                     2148 0.3445065 0.4753177
[3,]3
                     832
                           0.7115385 \ 0.4533194
[4,]4
                     292
                           0.1232877 \ 0.3293315
[5,] 5
                     1144 0.8811189 0.3237901
                     368
[6,]6
                           0.7391304 \ 0.4397067
[7,]
                     192 	 0
[8,] "Total"
                     8124 0.4820286 0.4997077
Call:
lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)
Residuals:
    Min
               1Q Median
                                  3\mathbf{Q}
                                          Max
-0.8811 -0.4028
                  0.0000 \quad 0.5972 \quad 0.8767
Coefficients:
                Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept)
                0.40280
                              0.00800 50.35 < 2e-16 ***
new. variable g - 0.05829
                              0.01256 -4.64 3.54e-06 ***
                              0.01750
new. variablel
                                          17.64 < 2e-16 ***
                0.30874
new. variable -0.27951
                              0.02746 -10.18 < 2e-16 ***
                              0.01550 30.87 < 2e-16 ***
new. variablep 0.47832
                              0.02473 13.60 < 2e-16 ***
new.variableu 0.33633
                              0.03337 -12.07 < 2e-16 ***
new. variable -0.40280
Residual standard error: 0.4489 on 8117 degrees of freedom
\label{eq:Multiple R-squared: 0.1937} \text{Multiple } \mathbf{R}\!\!-\!\!\text{squared: 0.1937}\,, \qquad \text{Adjusted } \mathbf{R}\!\!-\!\!\!\text{squared: 0.1931}
F-statistic: 325 on 6 and 8117 DF, p-value: < 2.2e-16
[1] 0.3886502 0.5823697 0.1937195
              == cap.surface =
new. variable
         f
                                                     < NA >
                     g
0.2856000 \ \ 0.0004924 \ \ 0.3146000 \ \ 0.3993000 \ \ 0.0000000
     new.variable n mean
                                       \operatorname{sd}
                     2320 0.3275862 0.4694342
[1,] 1
```

L / J	4 1 2556 0.5524257 3244 0.5363748 8124 0.4820286	0.498752		
Call: lm(formula = pe	oisonous ~ new.va ı	\mathbf{riable} , $\mathbf{data} = \mathbf{raw}.\mathbf{mushroom}.\mathbf{data}$)		
	$f{Q}$ Median $3{f Q}$ $4 - 0.3276 - 0.4636$	Max 0.6724		
Coefficients: (Intercept) new. variables new. variables new. variabley	0.32759 0.0101 0.67241 0.2452 0.22484 0.0140	or t value $Pr(> t)$ 7 32.200 < 2e-16 *** 22 2.742 0.00612 ** 25 16.001 < 2e-16 *** 26 15.671 < 2e-16 ***		
Residual standard error: 0.49 on 8120 degrees of freedom Multiple R —squared: 0.03878, Adjusted R —squared: 0.03842 F—statistic: 109.2 on 3 and 8120 DF, p—value: $< 2.2e-16$ [1] 0.46333584 0.50211511 0.03877928				
	cap.color ====			
new. variable b	c e	or n n n n		
W V	<na></na>	g n p r u		
v		$500 \ 0.281100 \ 0.017730 \ 0.001969 \ 0.001969 \ 0.128000 \ 0.$		
new. varia		sd		
[1,] 1	168 0.714285	0.4531045		
[2,]2	$44 \qquad 0.272727$	3 0.4505106		
[3,] 3	$1500 \ 0.584$	0.4930579		
[4,] 4	1840 0.439130			
$\begin{bmatrix} 5 \end{bmatrix}$	2284 0.446584			
[6,] 6		1 0.4891996		
$\begin{bmatrix} 7 & 7 \end{bmatrix}$	$\begin{array}{cc} 16 & 0 \\ 16 & 0 \end{array}$	$0 \\ 0$		
[8,] 8 $[9,]$ 9	$1040 \ 0.307692$	Ÿ		
[10,] $[10]$	1072 0.626865			
[11,] "Total"	8124 0.482028			

 $\mathbf{lm}(\mathbf{formula} = \text{poisonous} \ \tilde{\ } \mathbf{new}. \ \mathbf{variable} \ , \ \mathbf{data} = \text{raw.mushroom.} \mathbf{data})$

```
Residuals:
```

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 0.71429 $0.03764 \quad 18.975 < 2e-16 ***$ new. variable c -0.44156 $0.08263 \quad -5.344 \quad 9.34e - 08 \quad ***$ new. variable -0.13029 $-3.282 \quad 0.00103 **$ 0.039700.03932 -6.997 2.82e-12 ***new. variable -0.27516new. variable -0.267700.03900-6.864 7.21e-12 *** new. variable -0.103170.05541 $-1.862 \quad 0.06263$. $0.12765 \quad -5.595 \quad 2.27e - 08 ***$ new. variabler -0.71429new. variable u - 0.71429 $0.12765 \quad -5.595 \quad 2.27e - 08 ***$ 0.04057 -10.022 < 2e-16 *****new**. variablew -0.40659new. variabley -0.08742 $0.04049 \quad -2.159 \quad 0.03086 *$

Residual standard error: 0.4879 on 8114 degrees of freedom Multiple **R**-squared: 0.04771, Adjusted **R**-squared: 0.04665 F-statistic: 45.17 on 9 and 8114 DF, p-value: < 2.2e-16

$[1] \quad 0.45903087 \quad 0.50674109 \quad 0.04771021$

bruises

new.variable

f t <NA>

 $0.5844 \ 0.4156 \ 0.0000$

new.variable n mean sd

[1,] 1 4748 0.6933446 0.4611536 [2,] 2 3376 0.1848341 0.3882204 [3,] "Total" 8124 0.4820286 0.4997077

Call:

lm(formula = poisonous ~ "new. variable", ~ data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error ${\bf t}$ value $\Pr(>|{\bf t}|)$ (Intercept) 0.693345 0.006274 110.50 <2e-16 *** ${\bf new}$. variablet -0.508510 0.009733 -52.24 <2e-16 ***

Residual standard error: 0.4323 on 8122 degrees of freedom Multiple **R**-squared: 0.2515, Adjusted **R**-squared: 0.2514 F-statistic: 2730 on 1 and 8122 DF, p-value: $< 2.2e{-}16$

$[1] \quad 0.3607826 \quad 0.6123153 \quad 0.2515327$

	odor =								
new.variable									
a	\mathbf{c}	f	1	\mathbf{m}	n	p	S		
y < NA >									
$0.049240 \ 0.02363$	0.2659	0 0 0	.049240 0.004	431 0.	.434300	0.031510	0.070900	0.070900	0.
new.variab	ole n	mean	sd						
[1,] 1	400	0	0						
[2,] 2	192	1	0						
[3,] 3	2160	1	0						
[4,] 4	400	0	0						
[5,] 5	36	1	0						

[7,] 7 256 1 0 [8,] 8 576 1 0

[9,] 9 576 1 0 [10,] "Total" 8124 0.4820286 0.4997077

Call:

[6,]6

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

 $3528 \ 0.03401361 \ 0.1812898$

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) $1.366e{-14}$ 5.976e - 030.0001 new.variablec 1.000e+00 1.049e-0295.299< 2e-16 *****new**. variable f 1.000e+00 $6.506e - 03 \ 153.711$ < 2e-16 ***new. variablel 9.370e-14 8.451e - 030.0001 48.085< 2e-16 *****new**. variablem 1.000e+002.080e-02new.variablen 3.401e-02 6.306e-03 $5.394 \quad 7.08e - 08 ***$ new.variablep 1.000e+00 9.566e-03 104.536 < 2e-16 *** new.variables 1.000e+00 7.779e-03 128.554 < 2e-16 *** new.variabley 1.000e+00 7.779e-03 128.554 < 2e-16 ***

Residual standard error: 0.1195 on 8115 degrees of freedom

```
Multiple R-squared: 0.9429, Adjusted R-squared: 0.9428
F-statistic: 1.674e+04 on 8 and 8115 DF, p-value: < 2.2e-16
\begin{bmatrix} 1 \end{bmatrix} 0.02754714 0.97039878 0.94285164
  gill.attachment
new.variable
              f
                    <NA>
      a
0.02585 \ 0.97420 \ 0.00000
     new.variable n mean
                                     \operatorname{sd}
[1,]1
                   210 \quad 0.08571429 \ 0.2806106
[2,]2
                  7914 0.4925449 0.499976
[3,] "Total" 8124 0.4820286 0.4997077
Call:
lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)
Residuals:
     Min
                1\mathbf{Q}
                      Median
                                    3\mathbf{Q}
                                            Max
-0.49254 -0.49254 -0.08571 0.50746
Coefficients:
               Estimate Std. Error \mathbf{t} value Pr(>|\mathbf{t}|)
(Intercept)
                0.08571
                            0.03420
                                       2.507
                                                0.0122 *
new.variablef 0.40683
                            0.03465
                                      11.742
                                                <2e-16 ***
Residual standard error: 0.4955 on 8122 degrees of freedom
Multiple R-squared: 0.01669, Adjusted R-squared: 0.01657
F-statistic: 137.9 on 1 and 8122 DF, p-value: < 2.2e-16
\begin{bmatrix} 1 \end{bmatrix} 0.4739822 0.4906748 0.0166926
           === gill.spacing ======
new. variable
     \mathbf{c}
            W
                 <NA>
0.8385 \ 0.1615 \ 0.0000
     new.variable n mean
                                     \operatorname{sd}
[1,]1
                  6812 0.5584263 0.4966111
\begin{bmatrix} 2 \end{bmatrix}
                  1312 \ 0.08536585 \ 0.2795319
[3,] "Total" 8124 0.4820286 0.4997077
```

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Residual standard error: 0.4684 on 8122 degrees of freedom Multiple **R**-squared: 0.1214, Adjusted **R**-squared: 0.1213 F-statistic: 1122 on 1 and 8122 DF, p-value: < 2.2e-16

[1] 0.4235231 0.5448965 0.1213734

gill.size ====

new.variable

b n <NA>
0.6908 0.3092 0.0000

new.variable n mean sd

[1,] 1 5612 0.3014968 0.4589488 [2,] 2 2512 0.8853503 0.3186621 [3,] "Total" 8124 0.4820286 0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Residual standard error: 0.4206 on 8122 degrees of freedom Multiple **R**-squared: 0.2916, Adjusted **R**-squared: 0.2915 F-statistic: 3344 on 1 and 8122 DF, p-value: < 2.2e-16

[1] 0.3414563 0.6330827 0.2916263

gill.color new. variable b h k g n р <NA> W u У new.variable n mean 1728 1 [1,]1 0 2 [2,]96 0 0 [3,]752 0.67021283 0.4704486[4,]4 732 0.72131150.4486605[5,]5 408 0.15686270.36411786 $1048\ \ 0.1068702$ 0.3090957[6,][7,]7 64 0 0 [8,]8 $1492\ \ 0.4289544$ 0.4950927[9,]9 241

0.2970221

0.4036201

0.4388768

0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

0.09756098

0.255814

 $1202 \ 0.2046589$

8124 0.4820286

Residuals:

[10,] 10

[11,] 11

[12,] 12

[13,] "Total"

492

86

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 113.50 1.000e+008.811e-03<2e-16 *** new. variablee -1.000e+003.841e - 02-26.04<2e-16 *** new. variableg -20.61-3.298e-011.600e-02<2e-16 *** new. variableh -2.787e-011.615e-02-17.25<2e-16******new**. variablek -8.431e-012.016e-02-41.82<2e-16 *** new. variablen -8.931e-01-62.28<2e-16 *** 1.434e-02-21.45new. variableo $-1.000\,\mathrm{e}{+00}$ 4.662e-02<2e-16 *** -44.12new. variablep -5.710e-011.294e-02<2e-16 ***new. variabler 1.469e - 147.528e-020.001 new. variableu -9.024e-011.872e-02-48.22<2e-16 *** new. variable -7.953e-011.376e-02-57.82<2e-16****new. variable y - 7.442e - 01 $4.047\,\mathrm{e}\!-\!02$ -18.39<2e-16 ***

Residual standard error: 0.3663 on 8112 degrees of freedom Multiple **R**-squared: 0.4635, Adjusted **R**-squared: 0.4628 F-statistic: 637.2 on 11 and 8112 DF, p-value: $< 2.2e{-}16$

$[1] \quad 0.2585941 \quad 0.7221236 \quad 0.4635296$

==== stalk.shape = new.variable е \mathbf{t} <NA> $0.4328 \ 0.5672 \ 0.0000$ new.variable n mean \mathbf{sd} [1,] 1 3516 0.5403868 0.4984371 [2,] 2 $4608 \quad 0.4375$ 0.4961322[3,] "Total" 8124 0.4820286 0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Residual standard error: 0.4971 on 8122 degrees of freedom Multiple **R**-squared: 0.01041, Adjusted **R**-squared: 0.01029 F-statistic: 85.42 on 1 and 8122 DF, p-value: < 2.2e-16

[1] 0.47701166 0.48741954 0.01040788

==== stalk.root ===== new. variable b <NA> \mathbf{c} е $0.30530 \quad 0.46480 \quad 0.06844 \quad 0.13790 \quad 0.02363 \quad 0.00000$ new.variable n mean [1,] 1 2480 0.7096774 0.4540027[2,] 2 3776 0.4915254 0.4999944[3,] 3 $556 \quad 0.07913669 \quad 0.2701951$ [4,]4 $1120 \ 0.2285714 \ 0.4201001$ [5,]5192 00 [6,] "Total" 8124 0.4820286 0.4997077

Call:

 $\mathbf{lm}(\mathbf{formula} = \mathtt{poisonous} \ \tilde{\ } \mathbf{new}. \ \mathbf{variable} \ , \ \mathbf{data} = \mathtt{raw}. \ \mathtt{mushroom}. \ \mathbf{data})$

```
Residuals:
```

Min Median 1**Q** $3\mathbf{Q}$ Max 0.0000-0.7097 -0.49150.50850.9209

Coefficients:

Estimate Std. Error t value Pr(>|t|)(Intercept) 77.400.7096770.009169<2e-16 *** new. variableb -0.2181520.011802-18.48<2e-16****new. variable c -0.6305410.021425 -29.43 < 2e-16 ***-29.27 <2e-16 *** new. variablee -0.4811060.016438new. variabler -0.709677-20.75 <2e-16 *** 0.034204

Residual standard error: 0.4566 on 8119 degrees of freedom Multiple R-squared: 0.1655, Adjusted R-squared: 0.1651 F-statistic: 402.5 on 4 and 8119 DF, p-value: < 2.2e-16

[1] 0.4022577 0.5677476 0.1654900

==== stalk.surface.above.ring ====

new. variable

f k \mathbf{S} $0.067950 \ \ 0.292000 \ \ 0.637100 \ \ 0.002954 \ \ 0.000000$

	new. variable	n	mean	sa
[1,]	1	552	0.2608696	0.4395072
[2,]	2	2372	0.9392917	0.2388448
[3,]	3	5176	0.2967543	0.4568714
[4,]	4	24	0.3333333	0.4815434
[5,]	"Total"	8124	0.4820286	0.4997077

Call:

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Min 1**Q** Median $3\mathbf{Q}$ Max $-0.93929 \quad -0.29675 \quad -0.26087$ 0.060710.73913

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 15.160 0.260870.01721<2e-16 ***new. variablek 0.678420.0191135.510 <2e-16****new. variables 0.035880.01810 1.982 0.0475 *new. variablev 0.8600.39000.072460.08430

48

Residual standard error: 0.4043 on 8120 degrees of freedom Multiple \mathbf{R} -squared: 0.3457, Adjusted \mathbf{R} -squared: 0.3454 F-statistic: 1430 on 3 and 8120 DF, p-value: < 2.2e-16[1] 0.3154020 0.6610798 0.3456778 === stalk.surface.below.ring new.variable f k <NA> \mathbf{S} $0.07386 \ 0.28360 \ 0.60760 \ 0.03496 \ 0.00000$ new.variable n mean 600[1,] 1 0.240.4274395[2,] 2 2304 0.9375 0.242114[3,]34936 0.3111831 0.4630244 $284 \quad 0.2676056 \quad 0.4434923$ [4,]4[5,] "Total" $8124 \ 0.4820286 \ 0.4997077$ Call: lm(formula = poisonous ~ new.variable, data = raw.mushroom.data) Residuals: 1Q Median $3\mathbf{Q}$ Max $-0.9375 \quad -0.3112 \quad -0.2400$ 0.76000.0625Coefficients: Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) $0.01670 \quad 14.375 < 2e-16 ***$ 0.2400037.211 < 2e-16 ***new. variablek 0.69750 0.01874new. variables 0.07118 $4.026 \ 5.73e-05 ***$ 0.01768new. variabley 0.02761 0.029460.9370.349Residual standard error: 0.409 on 8120 degrees of freedom Multiple R-squared: 0.3304, Adjusted R-squared: 0.3302 F-statistic: 1336 on 3 and 8120 DF, p-value: < 2.2e-16[1] 0.3227483 0.6531857 0.3304375 ==== stalk.color.above.ring = new. variable \mathbf{c} eg n O р <NA> W new.variable n mean sd

0

432

1

[1,] 1

[2,]	2	36	1	0
[3,]	3	96	0	0
[4,]	4	576	0	0
[5,]	5	448	0.9642857	0.1857843
[6,]	6	192	0	0
[7,]	7	1872	0.6923077	0.4616618
[8,]	8	4464	0.3835125	0.4862958
[9,]	9	8	1	0
[10,]	"Total"	8124	0.4820286	0.4997077

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) 1.000e+002.047e - 0248.841 <2e-16 *** 1.000 9.813e - 147.382e-020.000**new**. variablec new. variable $-1.000\,\mathrm{e}{+00}$ 4.802e-02 -20.826<2e-16 *** new. variable g -1.000e+002.709e-02 -36.920<2e-16 *** new. variable -3.571e-022.870e-02-1.2450.213new. variable 0.000e+0.00e+03.691e-02 -27.092<2e-16 *** new. variable -3.077e-012.271e-02 -13.546<2e-16 *** **new**. variablew -6.165e-012.144e - 02 - 28.751<2e-16****new. variable y - 2.260e - 141.518e - 010.0001.000

Residual standard error: 0.4256 on 8115 degrees of freedom Multiple **R**-squared: 0.2755, Adjusted **R**-squared: 0.2748 F-statistic: 385.7 on 8 and 8115 DF, p-value: < 2.2e-16

[1] 0.3492453 0.6247129 0.2754676

new.variable

b c e g n o p w

y <NA>
0.053180 0.004431 0.011820 0.070900 0.063020 0.023630 0.230400 0.539600 0.002954 0.

new.variable n mean sd [1,]1 432 1 0 [2,] 2 36 1 0 [3,]3 96 0 0 576 [4,]40 0

[5,]	5	512	0.875	0.3310424
[6,]	6	192	0	0
[7,]	7	1872	0.6923077	0.4616618
[8,]	8	4384	0.3832117	0.4862247
[9,]	9	24	1	0
[10,]	"Total"	8124	0.4820286	0.4997077

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ < 2e-16 ***(Intercept) 1.000e+002.062e-0248.4901 new.variablec 4.091e-14 7.436e-020.000new. variable -1.000e+004.836e-02 -20.676< 2e-16 ***new.variableg -1.000e+002.728e - 02 - 36.655< 2e-16 ***2.800e-02 -4.464 8.16e-06 *** **new**. variable -1.250e-01new. variableo -1.000e+003.718e - 02 - 26.897< 2e-16 ***new. variable p - 3.077e - 012.288e-02 -13.449 < 2e-16 *****new**. variablew -6.168e-012.162e-02 -28.535< 2e-16 ***new. variable y -1.192e-148.989e-020.0001

Residual standard error: 0.4286 on 8115 degrees of freedom Multiple **R**-squared: 0.2649, Adjusted **R**-squared: 0.2642 F-statistic: 365.6 on 8 and 8115 DF, p-value: < 2.2e-16

[1] 0.3543188 0.6192611 0.2649423

veil.color

new. variable

	new.variable	n	mean	sd
[1,]	1	96	0	0
[2,]	2	96	0	0
[3,]	3	7924	0.4931853	0.4999851
[4,]	4	8	1	0
[5]	"Total"	8124	0.4820286	0.4997077

Call:

 $\mathbf{lm}(\mathbf{formula} = \text{poisonous} \ \tilde{\ } \mathbf{new}. \ \mathbf{variable} \ , \ \mathbf{data} = \text{raw.mushroom.} \mathbf{data})$

Residuals:

Coefficients:

Residual standard error: 0.4939 on 8120 degrees of freedom Multiple **R**-squared: 0.02354, Adjusted **R**-squared: 0.02318 F-statistic: 65.25 on 3 and 8120 DF, p-value: < 2.2e-16

 $[1] \quad 0.47068251 \quad 0.49422063 \quad 0.02353812$

ring.number

new.variable

[2,] 2 7488 0.508547 0.4999003 [3,] 3 600 0.12 0.3252327 [4,] "Total" 8124 0.4820286 0.4997077

Call:

 $lm(formula = poisonous ~ ^r new. variable, data = raw.mushroom.data)$

Residuals:

Coefficients:

Residual standard error: 0.4881 on 8121 degrees of freedom Multiple **R**-squared: 0.04613, Adjusted **R**-squared: 0.04589

 $[1] \quad 0.45979396 \quad 0.50592110 \quad 0.04612713$ === ring.type ==== new.variable 1 n $0.341700 \ \ 0.005908 \ \ 0.159500 \ \ 0.004431 \ \ 0.488400 \ \ 0.000000$ new.variable n mean 2776 0.6368876 0.4809835 [1,] 1 [2,]2 48 0 0 [3,]31296 10 [4,]40 36 [5,] 5 $3968 \quad 0.2056452 \quad 0.4042232$ [6,] "Total" 8124 0.4820286 0.4997077 Call: lm(formula = poisonous ~ new.variable, data = raw.mushroom.data) Residuals: Min 1Q Median Max $3\mathbf{Q}$ -0.6369 -0.2056 -0.2056 0.36310.7944Coefficients: Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ 0.007566 84.18 < 2e-16 ***(Intercept) 0.636888new. variable f -0.636888 -10.97 < 2e-16 ***0.05803327.07 < 2e-16 ***new. variablel 0.363112 0.013411 $5.43 \ 5.79e-08 ***$ new. variablen 0.363112 0.066868-43.72 < 2e-16 *****new**. variable p - 0.4312420.009864Residual standard error: 0.3986 on 8119 degrees of freedom Multiple R-squared: 0.3639, Adjusted R-squared: 0.3636 F-statistic: 1161 on 4 and 8119 DF, p-value: < 2.2e-16[1] 0.3066008 0.6705372 0.3639364 spore.print.color new. variable b h k n O r <NA> $0.005908 \ \ 0.200900 \ \ 0.230400 \ \ 0.242200 \ \ 0.005908 \ \ 0.008863 \ \ 0.005908 \ \ 0.293900 \ \ 0.005908 \ \ 0.$ new.variable n mean sd 48 0 0 [1,] 1

F-statistic: 196.4 **on** 2 and 8121 DF, p-value: < 2.2e-16

```
[2,]
      2
                      1632 \ 0.9705882 \ 0.1690095
 [3,]
                      1872 \quad 0.1196581 \quad 0.324648
      3
 [4,]
      4
                      1968 0.1138211 0.3176746
 [5,]
      5
                      48
                            0
                                        0
 [6,]6
                      72
                            1
                                        0
 [7,] 7
                      48
                            0
                                        0
                      2388 \quad 0.758794
                                        0.4279046
 [8,]
      8
 [9,]9
                            0
[10,] "Total"
                      8124 0.4820286 0.4997077
```

lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)

Residuals:

Coefficients:

Estimate Std. Error \mathbf{t} value $\Pr(>|\mathbf{t}|)$ (Intercept) -3.683e-14 4.751e-020.0001.0000 <2e-16 *** new. variableh 9.706e-014.821e-0220.134 new.variablek 1.197e-01 4.812e-022.4870.0129 *new. variable 1.138e-014.809e-022.3670.0180 * **new**. variableo -2.675e-14 6.719e-020.0001.0000 **new**. variabler 1.000e+006.134e-02 16.303<2e-16 *** **new**. variable u - 1.163e - 13 6.719e - 020.0001.0000 7.588e - 01**new**. variablew 4.799e-0215.812 <2e-16 *****new**. variable v = -1.632e - 146.719e-020.0001.0000

Residual standard error: 0.3292 on 8115 degrees of freedom Multiple **R**-squared: 0.5665, Adjusted **R**-squared: 0.566 F-statistic: 1325 on 8 and 8115 DF, p-value: $< 2.2e{-}16$

$[1] \quad 0.2089720 \quad 0.7754458 \quad 0.5664738$

population new. variable \mathbf{c} \mathbf{n} $0.04727 \ 0.04185 \ 0.04924 \ 0.15360 \ 0.49730 \ 0.21070 \ 0.00000$ new.variable n mean sd [1,]0 384 [2,] 2 $0.1529412 \ 0.3604613$ 340[3,]34000 0 [4,]4 $1248 \quad 0.2948718 \quad 0.4561679$ [5,] 5 4040 0.7049505 0.4561215

```
[6,]6
                   1712 0.3785047 0.485156
                   8124 0.4820286 0.4997077
[7,] "Total"
Call:
lm(formula = poisonous ~ new.variable, data = raw.mushroom.data)
Residuals:
    Min
              1Q Median
                                       Max
                               3Q
-0.7049 -0.3785
                  0.0000
                           0.2950
                                    0.8471
Coefficients:
                 Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
(Intercept)
               1.208e-13 2.227e-02
                                         0.000
                                                       1
                                         4.705
new. variablec
               1.529e-01
                           3.250e-02
                                                2.58e - 06 ***
new. variable -1.343e-13 3.118e-02
                                         0.000
                                                       1
              2.949e-01 2.547e-02 11.577 < 2e-16 ***
new. variables
                                        30.245 < 2e-16 ***
new. variablev 7.050e-01 2.331e-02
new. variabley 3.785e-01 2.465e-02
                                        15.358 < 2e-16 ***
Residual standard error: 0.4365 on 8118 degrees of freedom
Multiple R-squared: 0.2375, Adjusted R-squared: 0.2371
F-statistic: 505.8 on 5 and 8118 DF, p-value: < 2.2e-16
[1] 0.3675295 0.6050653 0.2375358
       ------ habitat =
new. variable
      d
                      l
                                                                <NA>
                               \mathbf{m}
                                       p
                                                u
0.38750 \ \ 0.26440 \ \ 0.10240 \ \ 0.03594 \ \ 0.14080 \ \ 0.04530 \ \ 0.02363 \ \ 0.00000
     new.variable n
                        mean
                                    \operatorname{sd}
[1,] 1
                   3148 \quad 0.4027954 \quad 0.4905382
 [2, ]
                   2148 0.3445065 0.4753177
[3,]3
                   832
                         0.7115385 \ 0.4533194
[4,]4
                         0.1232877 \ 0.3293315
                   292
[5,] 5
                   1144 0.8811189 0.3237901
[6,]6
                   368
                         0.7391304 \ 0.4397067
[7,]7
                   192
                         0
                                    0
[8,] "Total"
                   8124 0.4820286 0.4997077
Call:
lm(formula = poisonous ~ new. variable, data = raw.mushroom.data)
Residuals:
    Min
              1Q Median
                               3\mathbf{Q}
                                       Max
-0.8811 -0.4028
                  0.0000
                           0.5972
                                    0.8767
```

Coefficients:

```
Estimate Std. Error \mathbf{t} value \Pr(>|\mathbf{t}|)
                                      50.35 < 2e-16 ***
(Intercept)
                0.40280
                           0.00800
new. variable -0.05829
                           0.01256
                                      -4.64 \ 3.54e-06 ***
new. variablel
                                    17.64 < 2e-16 ***
               0.30874
                           0.01750
new. variable -0.27951
                           0.02746 -10.18 < 2e-16 ***
                                     30.87 < 2e-16 ***
new. variablep
              0.47832
                           0.01550
new.variableu
              0.33633
                           0.02473
                                      13.60 < 2e-16 ***
new. variable -0.40280
                                     -12.07 < 2e-16 ***
                           0.03337
```

Residual standard error: 0.4489 on 8117 degrees of freedom Multiple **R**-squared: 0.1937, Adjusted **R**-squared: 0.1931 F-statistic: 325 on 6 and 8117 DF, p-value: < 2.2e-16

[1] 0.3886502 0.5823697 0.1937195

Start: AIC=-11263.75 poisonous $\tilde{1}$

	Df	Sum of Sq	RSS AIC
+ odor	8	1912.46	115.92 -34443
+ spore. print .color	8	1149.02	879.35 -17982
+ gill.color	11	940.21	1088.16 -16224
+ ring.type	4	738.20	1290.18 -14904
+ stalk.surface.above.ring	3	701.16	1327.21 -14683
+ stalk.surface.below.ring	3	670.25	1358.12 -14496
+ gill.size	1	591.53	1436.85 -14056
+ stalk.color.above.ring	8	558.75	1469.62 -13810
+ stalk.color.below.ring	8	537.40	1490.97 -13692
+ bruises	1	510.20	1518.17 -13609
+ population	5	481.81	1546.56 -13422
+ habitat	6	392.94	1635.44 -12959
+ stalk.root	4	335.68	1692.70 -12697
+ gill.spacing	1	246.19	1782.19 -12306
+ cap.shape	5	122.32	1906.05 -11724
+ ring.number	2	93.56	1934.81 -11629
+ cap.color	9	96.77	1931.60 -11580
+ cap.surface	3	78.66	1949.72 -11558
+ veil.color	3	47.74	1980.63 -11430
+ gill.attachment	1	33.86	1994.52 -11392
+ stalk.shape	1	21.11	2007.27 -11340
<none></none>			2028.38 -11264

Step: AIC = -34443.47 poisonous odor

	Df	Sum of Sq	RSS AIC
+ spore. print .color	8	71.372	44.546 - 42141
+ gill.color	11	26.216	89.702 -36427
+ stalk.color.below.ring	7	24.034	91.884 -36268
+ stalk.color.above.ring	7	9.216	106.702 -35053
+ cap.color	9	9.257	106.661 -35039
+ cap.shape	5	8.770	107.149 -35038
+ veil.color	3	7.688	108.231 -34974
+ stalk.surface.below.ring	3	7.669	108.249 -34973
+ habitat	6	6.460	109.459 -34855
+ stalk.shape	1	5.407	110.511 -34823
+ ring.number	1	5.345	110.573 -34818
+ cap.surface	3	4.614	111.304 -34746
+ stalk.surface.above.ring	3	3.137	112.781 -34639
+ population	5	3.168	112.751 -34624
+ gill.size	1	2.172	113.746 -34588
+ stalk.root	4	1.984	113.935 -34548
+ gill.spacing	1	0.544	115.374 -34473
+ gill.attachment	1	0.224	115.695 -34450
<none></none>			115.918 -34443
+ bruises	1	0.107	115.812 -34442
+ ring.type	3	0.072	115.846 -34422

Step: AIC=-42140.9 poisonous $\tilde{}$ odor + spore.**print**.color

	Df	Sum of Sq	RSS AIC
+ stalk.color.below.ring	7	22.1338	22.412 -47658
+ ring.number	1	13.1096	31.437 - 44964
+ stalk.color.above.ring	7	7.3900	37.156 -43552
+ veil.color	3	6.9738	37.572 -43497
+ stalk.surface.below.ring	3	6.7788	37.767 - 43455
+ cap.surface	3	3.6934	40.853 - 42817
+ gill.size	1	3.4232	41.123 - 42781
+ cap.shape	5	3.5458	41.000 - 42770
+ stalk.surface.above.ring	3	2.3045	42.242 - 42545
+ habitat	6	2.2297	42.317 - 42504
+ stalk.root	4	1.6007	42.946 - 42402
+ gill.color	11	1.5537	42.993 - 42330
+ cap.color	9	1.4087	43.138 - 42321
+ population	5	0.8309	43.715 - 42249
+ ring.type	3	0.7262	43.820 - 42247
+ gill.spacing	1	0.1083	44.438 - 42152
+ bruises	1	0.0667	44.480 - 42144
<none></none>			44.546 - 42141
+ stalk.shape	1	0.0145	44.532 - 42135
+ gill.attachment	1	0.0000	44.546 - 42132

Step: AIC=-47658.37 poisonous $\tilde{}$ odor + spore.**print**.color + stalk.color.below.ring

	D.C	a ca	Dag Ala
		Sum of Sq	
+ cap.surface	3	3.7256	18.687 - 49108
+ ring.number	1	3.5446	18.868 - 49048
+ stalk.surface.below.ring	3	1.1767	21.236 -48069
+ cap.shape	5	0.9824	21.430 - 47977
+ gill.size	1	0.8334	21.579 -47957
+ ring.type	3	0.3166	22.096 -47747
+ habitat	6	0.3529	22.059 - 47733
+ population	5	0.2850	22.127 -47717
+ cap.color	9	0.2637	22.149 - 47674
+ gill.spacing	1	0.0574	22.355 -47670
+ bruises	1	0.0551	22.357 - 47669
+ stalk.surface.above.ring	3	0.1045	22.308 -47669
+ stalk.shape	1	0.0528	22.360 -47669
<none></none>			22.412 -47658
+ gill.color	11	0.2545	22.158 -47652
+ stalk.color.above.ring	6	0.1312	22.281 -47652
+ gill.attachment	1	0.0000	22.412 -47649
+ veil.color	2	0.0000	22.412 -47640
+ stalk.root	4	0.0482	22.364 -47640

Step: AIC=-49108.27
poisonous ~ odor + spore.print.color + stalk.color.below.ring + cap.surface

	Df	Sum of Sq	RSS AIC
+ ring.number	1	2.48176	16.205 -50257
+ stalk.surface.below.ring	3	1.18705	17.500 - 49614
+ gill.size	1	0.58157	18.105 - 49356
+ ring.type	3	0.43850	18.248 - 49274
+ cap.shape	5	0.27206	18.415 - 49182
+ habitat	6	0.24536	18.442 -49162
+ gill.spacing	1	0.08246	18.604 - 49135
+ stalk.shape	1	0.07158	18.615 - 49130
+ stalk.surface.above.ring	3	0.10967	18.577 - 49129
+ population	5	0.14576	18.541 - 49127
+ cap.color	9	0.20523	18.482 - 49117
+ stalk.color.above.ring	6	0.12786	18.559 - 49110
<none></none>			18.687 - 49108
+ bruises	1	0.01566	18.671 - 49106
+ gill.attachment	1	0.00000	18.687 - 49099
+ veil.color	2	0.00000	18.687 - 49090
+ gill.color	11	0.17461	18.512 -49086
+ stalk.root	4	0.01822	18.669 -49080

Step: AIC=-50256.9
poisonous ~ odor + spore.print.color + stalk.color.below.ring + cap.surface + ring.number

	Df	Sum of Sq	RSS AIC
+ ring.type	3	-	14.048 -51390
+ cap.color	9	2.18298	14.022 -51351
+ gill.color	11	2.12107	14.084 -51298
+ stalk.surface.below.ring	3	1.21190	14.993 -50861
+ gill.size	1	0.31583	15.889 -50408
+ cap.shape	5	0.24978	15.955 -50338
+ stalk.surface.above.ring	3	0.21374	15.991 -50338
+ habitat	6	0.24635	15.959 -50327
+ bruises	1	0.08304	16.122 -50290
+ gill.spacing	1	0.05550	16.150 -50276
+ population	5	0.12384	16.081 -50274
+ stalk.shape	1	0.02242	16.183 -50259
<none></none>			16.205 -50257
+ gill.attachment	1	0.00000	16.205 -50248
+ veil.color	2	0.00001	16.205 -50239
+ stalk.root	4	0.00285	16.202 -50222
+ stalk.color.above.ring	6	0.00814	16.197 -50207

 $Step: \quad AIC {=} {-} 51390.23$

poisonous ~ odor + spore.print.color + stalk.color.below.ring +
 cap.surface + ring.number + ring.type

	Df	Sum of Sq	RSS AIC
+ stalk.root	4	2.26840	11.780 -52785
+ cap.color	9	1.67725	12.371 -52342
+ stalk.surface.below.ring	3	0.92739	13.121 -51918
+ stalk.surface.above.ring	3	0.35856	13.690 -51573
+ habitat	6	0.36429	13.684 -51550
+ gill.spacing	1	0.25755	13.791 -51532
+ cap.shape	5	0.17140	13.877 -51445
+ population	5	0.14555	13.903 -51430
<none></none>			14.048 -51390
+ bruises	1	0.00420	14.044 -51384
+ stalk.shape	1	0.00096	14.047 -51382
+ gill.size	1	0.00070	14.047 -51382
+ gill.attachment	1	0.00000	14.048 -51381
+ veil.color	2	0.00000	14.048 -51372
+ stalk.color.above.ring	6	0.00299	14.045 -51338
+ gill.color	10	0.00313	14.045 -51302

Step: AIC = -52784.92

poisonous ~ odor + spore.print.color + stalk.color.below.ring +

```
Df Sum of Sq
                                                  RSS
                                                          AIC
+ stalk.surface.below.ring
                                3
                                      5.1624
                                               6.6174 -57443
+ bruises
                                1
                                      1.2064 \ 10.5734 \ -53654
+ stalk.surface.above.ring
                                3
                                      1.0573 \ 10.7226 \ -53522
+ cap.color
                                9
                                      0.7838 \ 10.9960 \ -53263
+ gill.spacing
                                1
                                      0.6222 \ 11.1577 \ -53217
+ habitat
                                      0.4559\ 11.3239\ -53052
                                6
+ stalk.shape
                                      0.2982\ 11.4816\ -52984
                                1
+ cap.shape
                                      0.3044 \ 11.4754 \ -52953
                                5
+ population
                                5
                                      0.2914 \ 11.4884 \ -52943
                                2
+ veil.color
                                      0.2018 \ 11.5780 \ -52907
+ stalk.color.above.ring
                                6
                                      0.2493 \ 11.5305 \ -52905
+ gill.size
                                1
                                      0.0650 \ 11.7148 \ -52821
<none>
                                             11.7798 -52785
+ gill.attachment
                                1
                                      0.0000 \ 11.7798 \ -52776
+ gill.color
                                      0.0681 \ 11.7117 \ -52742
                               10
```

Step: AIC = -57442.89

poisonous odor + spore.print.color + stalk.color.below.ring + cap.surface + ring.number + ring.type + stalk.root + stalk.surface.below.ring

	Df	Sum of Sq	RSS AIC
+ bruises	1	1.82544	4.7920 -60056
+ stalk.surface.above.ring	3	1.02744	5.5900 -58787
+ cap.shape	5	0.33635	6.2811 -57822
+ population	5	0.29867	6.3187 -57773
+ stalk.shape	1	0.25363	6.3638 -57751
+ stalk.color.above.ring	6	0.27408	6.3433 -57733
+ veil.color	2	0.20997	6.4074 -57687
+ cap.color	9	0.19822	6.4192 -57609
+ habitat	6	0.14618	6.4712 -57570
+ gill.size	1	0.04047	6.5769 -57484
+ gill.spacing	1	0.03067	6.5867 -57472
<none></none>			6.6174 -57443
+ gill.attachment	1	0.00000	6.6174 -57434
+ gill.color	10	0.02099	6.5964 -57379

Step: AIC = -60056.01

poisonous ~ odor + spore.print.color + stalk.color.below.ring + cap.surface + ring.number + ring.type + stalk.root + stalk.surface.below.ring + bruises

	Df	Sum of Sq	RSS	AIC
+ stalk.shape	1	4.7920	0.0000	-483670
+ habitat	6	2.9216	1.8704	-67645
+ gill.spacing	1	1.9616	2.8304	-64325

```
+ gill.size
                                 1
                                       1.8787 \ \ 2.9133
                                                       -64090
+ stalk.color.above.ring
                                       0.6268 \ 4.1651
                                                         -61141
                                 6
+ population
                                 5
                                       0.6061 \ 4.1859
                                                         -61110
+ cap.shape
                                 5
                                       0.5631 \ 4.2289
                                                         -61027
+ veil.color
                                 2
                                       0.4006 \ 4.3914
                                                       -60747
+ stalk.surface.above.ring
                                       0.2652 \ 4.5267
                                 3
                                                         -60492
+ cap.color
                                 9
                                       0.2734 \ 4.5186
                                                       -60452
+ gill.color
                                10
                                       0.2095 \ 4.5825
                                                         -60329
<none>
                                                4.7920
                                                         -60056
+ gill.attachment
                                       0.0000 \ 4.7920
                                                         -60047
                                 1
Step: AIC=-483670.1
poisonous ~ odor + spore.print.color + stalk.color.below.ring +
     cap.surface + ring.number + ring.type + stalk.root + stalk.surface.below.ring +
     bruises + stalk.shape
                                Df
                                     Sum of Sq
                                                         RSS
                                                                   AIC
                                                 1.0824e - 22 - 483670
<none>
+ gill.size
                                 1 0.0000e+00 1.0824e-22 -483661
+ gill.spacing
                                 1 0.0000e+00 1.0824e-22 -483661
+ gill.attachment
                                 1 \quad 0.0000 \,\mathrm{e} + 00 \quad 1.0824 \,\mathrm{e} - 22 \quad -483661
+ veil.color
                                 2 \quad 0.0000 \,\mathrm{e} + 00 \quad 1.0824 \,\mathrm{e} - 22 \quad -483652
+ stalk.surface.above.ring
                                 3 \ 1.0560e - 26 \ 1.0823e - 22 \ -483644
                                 5 \ 1.6375e-25 \ 1.0807e-22 \ -483637
+ population
                                 5\ 1.3757e-25\ 1.0810e-22\ -483635
+ cap.shape
+ habitat
                                 6\ 2.4886e-25\ 1.0799e-22\ -483635
+ gill.color
                                10 \ 4.9050e - 25 \ 1.0775e - 22 \ -483617
                                 6\ 0.0000\,\mathrm{e}{+00}\ 1.0824\,\mathrm{e}{-22}\ -483616
+ stalk.color.above.ring
                                 9 \ 1.2811e - 25 \ 1.0811e - 22 \ -483599
+ cap.color
p. hat. linear. model. odor. spore. print. color
-2.32853438184597e-14
                          7.23553945963381e-15
                                                     1.73500502059269e-14
                                                                                 6.7559392891808
6.88284893569256e{-14}
                       24
                                                176
                                                                          200
24
                          48
 7.02793786039266\,\mathrm{e}{-14} \quad 7.02803655307894\,\mathrm{e}{-14}
                                                     7.15530233878984e-14 8.16675341341915
9.80802761699014e-14
                       48
                                                 48
                                                                         1296
1344
                            176
 1.08194786916194e{-13}
                              0.0646108663730508
                                                        0.0719530102790714
                                                                                    0.99804209495
0.99999999999684
                                                                          624
                      200
                                                 48
```

36

1.00000000000007

1.00538423886428

72

1.00000000000

1.000000000000006

1.00000000000019

96

576

96

1584

576

0.999999999999694

1.00000000000018

1.00000000000016

<NA>

128

576

0

poisonous

app.says.poisonous.0.05 0 1 0 4208 120 1 0 3796

poisonous

app.says.poisonous.0.01 0 1 0 800 0 1 3408 3916

poisonous

128

odor.spore.**print**.color.app.says.poisonous.0.05 0 1 0 3584 0 1 624 3916

poisonous

odor.spore.**print**.color.app.says.poisonous.0.07 0 1 0 3632 0 1 576 3916

poisonous