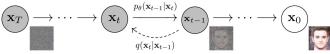


Denoising Diffusion Probabilistic Models for Synthetic Histopathologic Image Generation





Diffusion process as described in Ho et. al



Cosine beta schedule (above)



Linear beta schedule (above)

Algorithm 1 Training

- 1: repeat
- $\mathbf{x}_0 \sim q(\mathbf{x}_0)$
- $t \sim \text{Uniform}(\{1, ..., T\})$
- $\epsilon \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- Take gradient descent step on
- $\nabla_{\theta} || \epsilon \epsilon_{\theta} \left(\sqrt{\bar{\alpha}} \mathbf{x}_0 + \sqrt{1 \bar{\alpha}_t} \epsilon, t \right) ||^2$
- 7: until converged

Algorithm 2 Sampling

- 1: $\mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$
- 2: **for** t = T, ..., 1 **do**
- $\mathbf{z} \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$ if t > 1, else $\mathbf{z} = \mathbf{0}$
- $\mathbf{x}_{t-1} = \frac{1}{\sqrt{\alpha_t}} \left(\mathbf{x}_t \frac{1 \alpha_t}{\sqrt{1 \bar{\alpha}_t}} \epsilon_{\theta}(\mathbf{x}_t, t) \right) + \sigma_t \mathbf{z}$
- 5: end for
- 6: return x₀

$$\mathcal{L}_{\text{simple}} = \mathbb{E}_{t, \mathbf{x}_0, \epsilon} \left[\left| \left| \epsilon - \epsilon_{\theta}(\mathbf{x}_t, t) \right| \right|^2 \right]$$
$$= \mathbb{E}_{t, \mathbf{x}_0, \epsilon} \left[\left| \left| \epsilon - \epsilon_{\theta}(\sqrt{\bar{\alpha}} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon, t) \right| \right|^2 \right]$$

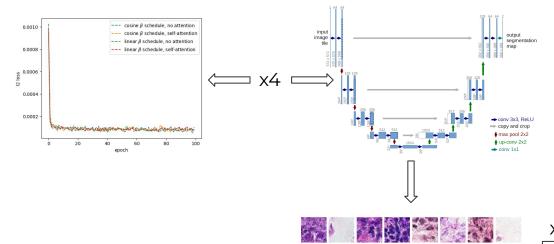


Table 2. Average SSIM & Maximum Likelihood Results

Sched.	Attn.	SSIM (†)	Log. Likelihood (\psi)
linear	none	0.00013885	0.01569078
linear	self	0.00010798	0.01568433
cosine	none	0.00026722	0.01448672
cosine	self	0.00015712	0.01710702



$$BCE = -\sum_{s,b} \left[y \times \log(p) + (1 - y) \times \log(1 - p) \right]$$

$$SSIM(\mathbf{x}, \mathbf{y}) = [l(\mathbf{x}, \mathbf{y})]^{\alpha} \cdot [c(\mathbf{x}, \mathbf{y})]^{\beta} \cdot [s(\mathbf{x}, \mathbf{y})]^{\gamma}$$







x2 Models Cancerous/ Non-Cancerous

Generate 512 images of each class using selected architecture (cosine schedule, no attention)

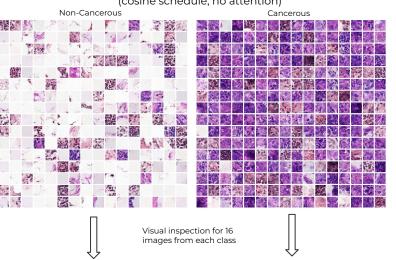


Table 3. Four Questions of +/- Class Matching

Correct (%)	Incorrect (%)
25 (69.4%)	11 (30.6%)

Table 4. Four Questions of +/- Class Identification

Class	Correct (%)	Incorrect (%)
+	15 (83.3%)	3 (16.7%)
_	11 (61.1%)	7 (38.9%)

Table 5. Four Questions of Generated/Ground-Truth Matching

 Class
 Correct (%)
 Incorrect (%)

 +
 8 (44.4%)
 10 (55.6%)

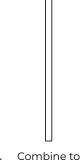
 8 (44.4%)
 10 (55.6%)

Table 6. Four Questions of Generated/Ground-Truth Identification

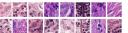
Class	Correct (%)	Incorrect (%)
GT +	4 (44.4%)	5 (55.6%)
GT -	2 (22.2%)	7 (77.8%)
Gen +	2 (22.2%)	7 (77.8%)
Gen -	3 (33.3%)	6 (66.7%)

Table 7. Two Questions of Overall Quality (Scores range from 1 to 5)

Class	Cellularity	Atypia	Color	Overall
+	3.89	4.22	3.67	4.33
-	4.33	4.00	3.67	4.11



Cancerous





Non-Cancerous



