

# Axioms

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## 1 Introduction

**Definition 1.1.** For all  $a, b, c$  in  $S$ , one has  $(a \cdot b) \cdot c = a \cdot (b \cdot c)$ .

**Definition 1.2.** There exists an element  $e$  in  $S$  such that, for every  $a$  in  $S$ , one has  $e \cdot a = a$  and  $a \cdot e = a$ . Such an element is unique and is called the **identity element**.

**Definition 1.3.**

**Definition 1.4.** For each  $a$  in  $S$ , there exists an element  $b$  in  $S$  such that  $a \cdot b = e$  and  $b \cdot a = e$ , where  $e$  is the identity element.

For each  $a$ , the element  $b$  is unique and is called the **inverse** of  $b$  and is denoted  $a^{-1}$ .

## 2 More Information

You can learn more about controlling the appearance of HTML output here:  
<https://quarto.org/docs/output-formats/html-basics.html>