## Brainspan glm interaction analysis

## ZHAO Kai

```
suppressPackageStartupMessages({
  require(ggplot2)
  require(formatR)
  require(knitr)
  require(cluster)
  require(factoextra)
  require(dplyr)
  require(RColorBrewer)
  require(clusterProfiler)
  require(org.Hs.eg.db)
  require(enrichplot)
  require(stringr)
  require(forcats)
  require(DOSE)
  require(ggplot2)
  require(hrbrthemes)
  require(viridis)
  require(reshape2)
  require(gridExtra)
  require(extrafont)
truncated_var <- function(x){</pre>
    remove_idx <- c(which.max(x), which.min(x))</pre>
    var(x[-remove_idx])
}
wrap_labal <- function(x, width = 60){</pre>
    str_wrap(x, width=60)
glm_interaction <- function(object, inc_cfd){</pre>
  residual <- object[['data']]</pre>
  confounder_num <- ncol(object[['confounder']])</pre>
  for(i in 1:confounder_num){
    sub_predictions <- object[['cfd_matrices']][[i]] %*% object[['column_factor']]</pre>
    residual <- residual - sub_predictions[object[['confounder']][,i], ]</pre>
  }
  column_factor <- object[['column_factor']]</pre>
  train_indicator <- object[['train_indicator']]</pre>
  confounder <- object[['confounder']][, inc_cfd]</pre>
```

```
unique_cfd <- unique(confounder)</pre>
  interaction_indicator <- rep(0, nrow(confounder))</pre>
  for(k in 1:nrow(unique_cfd)){
    selected <- apply(confounder, 1, function(x) all(x == unique_cfd[k,]))</pre>
    interaction_indicator[selected] <- k</pre>
  }
  unique_ita <- unique(interaction_indicator)</pre>
  coeff_matrix <- matrix(0, nrow = length(unique_ita), ncol = nrow(column_factor))</pre>
  pval_matrix <- matrix(0, nrow = length(unique_ita), ncol = nrow(column_factor))</pre>
  for(i in unique_ita) {
    ids <- which(interaction_indicator == i);</pre>
    st_idx <- 1; ed_idx <- 1
    nonzero_num <- length(ids) * ncol(column_factor);</pre>
    outcomes = rep(0,nonzero_num);
    features = matrix(0, nrow = nonzero_num, ncol = nrow(column_factor))
    for(k in ids){
      ed_idx = st_idx + ncol(column_factor) - 1;
      features[st_idx:ed_idx, ] = t(column_factor);
      outcomes[st idx:ed idx] = residual[k,];
      st_idx = ed_idx + 1
    data <- data.frame(response = outcomes, features)</pre>
    fit <- glm(response ~ . - 1, family = gaussian(), data = data)</pre>
    coeff_matrix[i,] <- unname(coefficients(fit))</pre>
    pval_matrix[i,] <- coef(summary(fit))[,4]</pre>
 return(list(unique_cfd, coeff_matrix, pval_matrix))
opts_chunk$set(tidy.opts=list(width.cutoff=80),tidy=TRUE)
setwd("~/data/multidimensional_datasets/brainspan_genes_matrix_csv/")
# load results for brain span
load("~/data/Results/brainspan/insider_brainspan_fitted_object.RData")
# load("~/data/Results/brainspan/insider_brainspan_R23_fitted_object.RData")
attach(object) # attach it for easy syntax
str(object) # show the structure of our result
## List of 9
                      : num [1:524, 1:43411] 5.23 4.66 4.35 4.84 4.39 ...
## $ data
   ..- attr(*, "dimnames")=List of 2
   ....$ : chr [1:524] "V2" "V3" "V4" "V5" ...
     ....$ : chr [1:43411] "ENSG00000000003" "ENSG0000000005" "ENSG00000000419" "ENSG00000000457" ...
## $ confounder
                  : num [1:524, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
   ..- attr(*, "dimnames")=List of 2
##
   ....$ : chr [1:524] "V2" "V3" "V4" "V5" ...
     .. ..$ : chr [1:2] "preriod_id" "sid"
```

```
: num [1:524, 1:43411] 5.23 0 0 0 4.39 ...
##
    ..- attr(*, "dimnames")=List of 2
     ....$ : chr [1:524] "V2" "V3" "V4" "V5" ...
##
     ....$: chr [1:43411] "ENSG00000000003" "ENSG0000000005" "ENSG00000000419" "ENSG00000000457" ...
##
                     : num [1:524, 1:43411] 0 4.66 4.35 4.84 0 ...
##
    $ testset
## $ train indicator: int [1:524, 1:43411] 1 0 0 0 1 1 1 1 1 1 1 ...
## $ params
                     :List of 4
     ..$ global_tol : num 1e-10
##
##
     ..$ sub tol
                    : num 1e-05
##
     ..$ tuning_iter: num 100
     ..$ max_iter : num 50000
## $ cfd_matrices :List of 2
    ..$ factor0: num [1:13, 1:19] -0.6989 0.347 0.0491 0.2013 0.1966 ...
     ..$ factor1: num [1:26, 1:19] -1.18 -1.06 0.79 2.98 -1.2 ...
## $ column_factor : num [1:19, 1:43411] -0.00716 0.02072 0 0.00857 0.00791 ...
## $ test_rmse
                     : num 4.66e-310
## - attr(*, "class")= chr "insider"
stage_factor <- cfd_matrices[[1]]</pre>
tissue_factor <- cfd_matrices[[2]]</pre>
# interactions <- cfd_matrices[[3]]</pre>
# read meta information
dic <- read.csv("~/data/Results/brainspan/dictionary.csv", stringsAsFactors = F)</pre>
# obtain ensemble genes included in our study
load("brainspan dataset annotated fitered.RData")
gene_id <- data.frame(ensembl_gene_id = colnames(data), stringsAsFactors =F)</pre>
# match the included genes with meta information
row_meta <- read.csv('rows_metadata.csv', stringsAsFactors = F)</pre>
meta <- inner_join(gene_id, row_meta, by = "ensembl_gene_id")</pre>
# prepare struture and stage names for naming corresponding latent factors
structure <- unique(dic[,c(6, 9)])
structure <- structure[order(structure[,2]),]</pre>
stage <- unique(dic[,c(11, 12)])</pre>
r_names <- apply(stage, 1, function(x) paste0(x[2], "_", trimws(x[1])))
# name tissue_factor and stage_factor
rownames(tissue_factor) <- structure[,1]</pre>
rownames(stage_factor) <- r_names</pre>
```

## Explore the interaction between development stages and brain regions

\textcolor{red}{Exploring the interaction is an important feature of our approach, so if possible we may carry out analysis on all possible combinations between brain regions and development stages and select reasonable results for interpretation.

```
summary <- table(dic[, c(9, 11)])
colnames(summary) <- r_names
rownames(summary) <- structure[, 1]
print(summary)

## Period
## sid Early fetal_2 Early fetal_3 Early mid-fetal_4 Early mid-fetal_5</pre>
```

##	Ocx	2	0	0	
##	M1C-S1C	2	0	0	
##	AMY	2	3	3	
##	MGE	2	0	0	
##	STC	1	2	2	
##	URL	2	0	0	
##	CGE	2	0	0	
##	DTH	2	3	0	
## ##	MFC DFC	2 2	2 3	3 3	
##	OFC	2	3	3	
##	LGE	2	0	0	
##	ITC	1	3	3	
##	HIP	2	3	3	
##	VFC	1	3	3	
##	PCx	2	0	0	
##	TCx	1	0	0	
##	A1C	0	3	3	
##	V1C	0	3	3	
##	STR	0	3	3	
##	M1C	0	3	3	
##	IPC	0	3	3	
##	S1C	0	3	3	
##	CB	0	1	2	
##	CBC	0	1	0	
##	MD	0	0	1	
##	F	Period			
##			fetal_7 Neo	natal and early infancy_8	
##	Ocx	0	0	0	
## ##	Ocx M1C-S1C	0 1	0 0	0	
## ## ##	Ocx M1C-S1C AMY	0 1 1	0 0 2	0 0 3	
## ## ## ##	Ocx M1C-S1C AMY MGE	0 1 1 0	0 0 2 0	0 0 3 0	
## ## ## ##	Ocx M1C-S1C AMY MGE STC	0 1 1 0 2	0 0 2 0 3	0 0 3 0 3	
## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL	0 1 1 0 2	0 0 2 0 3 0	0 0 3 0 3 0	
## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE	0 1 1 0 2 0	0 0 2 0 3 0	0 0 3 0 3 0	
## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH	0 1 1 0 2 0 0	0 0 2 0 3 0 0	0 0 3 0 3 0 0	
## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC	0 1 1 0 2 0 0 0	0 0 2 0 3 0 0 0	0 0 3 0 3 0 0 0	
## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC	0 1 1 0 2 0 0 0 0 2 2	0 0 2 0 3 0 0 0 2 3	0 0 3 0 3 0 0 0 0 2 2	
## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC	0 1 1 0 2 0 0 0 0 2 2 2	0 0 2 0 3 0 0 0 2 3 2	0 0 3 0 3 0 0 0 0 2 2 2	
## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE	0 1 1 0 2 0 0 0 0 2 2 2 2 1	0 0 2 0 3 0 0 0 2 3 2	0 0 3 0 3 0 0 0 0 2 2 2 2	
## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC	0 1 1 0 2 0 0 0 0 2 2 2 1 0	0 0 2 0 3 0 0 0 2 3 2 0	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3	
## ## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP	0 1 1 0 2 0 0 0 0 2 2 2 1 0 2 2	0 0 2 0 3 0 0 0 2 3 2 0	0 0 3 0 3 0 0 0 0 2 2 2 2 2 0 3	
## ## ## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC	0 1 1 0 2 0 0 0 0 2 2 2 1 0 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3	
######################################	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3	
## ## ## ## ## ## ## ## ##	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC UFC LGE ITC HIP VFC PCx TCx	0 1 1 0 2 0 0 0 0 2 2 2 1 0 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0	0 0 3 0 3 0 0 0 0 2 2 2 2 2 0 3 3	
## # # # # # # # # # # # # # # # # # #	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 1 0 0	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3	
######################################	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC OFC LGE ITC HIP VFC PCx TCx A1C	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 1 0 0	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3 2	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3 2 2 2 0 0	
######################################	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC OFC LGE ITC HIP VFC PCx TCx A1C V1C	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3 0 2 2 2 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3 2 2 0	
######################################	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 0 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3 2 2 2 0 0	
# # # # # # # # # # # # # # # # # # #	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C IPC S1C	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 0 0 0 1 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3 0 0 3 3 0 0 3 3 0 0 3 3 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3 2 2 2 2	
#############################	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C IPC S1C CB	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 0 0 0 1 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3 0 0 3 3 0 0 3 3 0 0 3 3 3 0 0 0 3 3 2 2 2 2	0 0 0 3 0 0 0 0 0 2 2 2 2 0 0 3 3 2 2 2 2	
# # # # # # # # # # # # # # # # # # #	Ocx M1C-S1C AMY MGE STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C IPC S1C	0 1 1 0 2 0 0 0 0 2 2 2 1 0 0 2 2 2 2 0 0 0 1 2 2 2 2	0 0 2 0 3 0 0 0 2 3 2 0 2 2 3 0 0 3 3 0 0 3 3 0 0 3 3 0 0 3 3 3	0 0 3 0 3 0 0 0 0 2 2 2 2 0 3 3 2 2 2 2	

##	1	Period		
	sid		Early childhood 10	Middle and late childhood_11
##	Ocx	0	0	0
##	M1C-S1C	0	0	0
##	AMY	0	4	3
##	MGE	0	0	0
##	STC	1	5	3
##	URL	0	0	0
##	CGE	0	0	0
##	DTH	0	0	0
##	MFC	1	3	3
##	DFC	1	4	3
##	OFC	1	3	2
##	LGE	0	0	0
##	ITC	1	4	3
##	HIP	0	3	3
##	VFC	0	5	3
##	PCx	0	0	0
##	TCx	0	0	0
##	A1C	0	3	3
##	V1C	1	4	3
##	STR	0	3	1
##	M1C	0	3	2
##	IPC	1	4	3
##	S1C	1	3	2
##	CB	0	0	0
##	CBC	1	5	3
##	MD	1	4	1
##	]	Period		
##	sid	Adolescence_12	_	Middle adulthood_14
##	Ocx	0	0	0
##	M1C-S1C	0	0	0
##	AMY	2	5	1
##		3		
##	MGE	0	0	0
	STC	0 4	5	1
##	STC URL	0 4 0	5 0	1 0
##	STC URL CGE	0 4 0 0	5 0 0	1 0 0
## ##	STC URL CGE DTH	0 4 0 0	5 0 0 0	1 0 0 0
## ## ##	STC URL CGE DTH MFC	0 4 0 0 0 3	5 0 0 0 5	1 0 0 0
## ## ## ##	STC URL CGE DTH MFC DFC	0 4 0 0 0 3 3	5 0 0 0 5 4	1 0 0 0 0 0
## ## ## ##	STC URL CGE DTH MFC DFC OFC	0 4 0 0 0 3 3 3	5 0 0 0 5 4 5	1 0 0 0 0 0 1 1
## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE	0 4 0 0 0 3 3 3 0	5 0 0 0 5 4 5	1 0 0 0 0 0 1 1 1
## ## ## ## ##	STC URL CGE DTH MFC DFC LGE LGE	0 4 0 0 0 3 3 3 0 4	5 0 0 5 4 5 0	1 0 0 0 0 1 1 1 0
## ## ## ## ## ##	STC URL CGE DTH MFC DFC UFC UFC LGE ITC HIP	0 4 0 0 0 3 3 3 0 4 3	5 0 0 5 4 5 0 5 5	1 0 0 0 0 1 1 1 0
## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC	0 4 0 0 0 3 3 3 3 0 4 3	5 0 0 5 4 5 0 5 5 5	1 0 0 0 0 1 1 1 0
## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx	0 4 0 0 0 3 3 3 0 4 3 3	5 0 0 5 4 5 0 5 5 5	1 0 0 0 0 1 1 1 1 1 1
## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx	0 4 0 0 0 3 3 3 0 4 3 3 0	5 0 0 5 4 5 0 5 5 5	1 0 0 0 0 1 1 1 0 1 1 1 0
## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C	0 4 0 0 0 3 3 3 0 4 3 3 0	5 0 0 5 4 5 0 5 5 5 0 0	1 0 0 0 0 1 1 1 0 1 1 1 0 0
## ## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C	0 4 0 0 3 3 3 0 4 3 3 0 0	5 0 0 5 4 5 0 5 5 5 0 0	1 0 0 0 0 1 1 1 1 1 0 0 1 1 1 0
## ## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR	0 4 0 0 3 3 3 0 4 3 3 0 0 0 3 3 3 3 3 0 0	5 0 0 5 4 5 0 5 5 5 0 0 0 5 4 5 5	1 0 0 0 0 1 1 1 1 0 0 0 1 1 1 1 0
## ## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C	0 4 0 0 0 3 3 3 0 4 3 3 0 0 0 3 3 3 3 2 3 3 2 3 3 3 3 3 3 3	5 0 0 5 4 5 0 5 5 5 0 0 0 5 5 5 5 5 5 5	1 0 0 0 0 1 1 1 1 0 0 0 1 1 1 1 1 1
## ## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C IPC	0 4 0 0 0 3 3 3 0 4 3 3 0 0 0 3 3 3 3 3	5 0 0 0 5 4 5 0 5 5 0 0 0 0 5 5 5 5 5 5	1 0 0 0 0 1 1 1 1 0 0 0 1 1 1 1 1 1 1
## ## ## ## ## ## ## ##	STC URL CGE DTH MFC DFC OFC LGE ITC HIP VFC PCx TCx A1C V1C STR M1C	0 4 0 0 0 3 3 3 0 4 3 3 0 0 0 3 3 3 3 2 3 3 2 3 3 3 3 3 3 3	5 0 0 5 4 5 0 5 5 5 0 0 0 5 5 5 5 5 5 5	1 0 0 0 0 1 1 1 1 0 0 0 1 1 1 1 1 0

```
##
     CBC
                                               5
                                                                     1
##
     MD
                                                                     1
# interactions <- glm_interaction(object, c(1, 2))</pre>
load("~/data/multidimensional_datasets/brainspan_genes_matrix_csv/glm_interaction.RData")
unique_cfd <- interactions[[1]]</pre>
colnames(unique_cfd) <- c("period", "structure_id")</pre>
definations <- data.frame(stage_names = r_names[unique_cfd[, 1]], structure_names = structure[,
    1] [unique_cfd[, 2]])
coeff_matrix <- interactions[[2]]</pre>
pval_matrix <- interactions[[3]]</pre>
significant_pvals <- apply(pval_matrix, 1, function(x) {</pre>
    sum(x <= 0.05)
})
cat("number of significant pvalues for each combination: ", significant_pvals, "\n")
## number of significant pvalues for each combination: 14 16 19 18 19 17 17 17 16 16 19 16 19 17 18 15
# interaction_indicator <- rep(0, nrow(object[['confounder']])) for(k in
# 1:rrow(unique\_cfd)){ selected <- apply(confounder, 1, function(x) all(x ==
# unique_cfd[k,])) interaction_indicator[selected] <- k }</pre>
\# intersted_idx <- which(apply(pval_matrix, 1, function(x) sum(x < 1e-8)) ==
# 19)
# confound_values <- (confounder[which(interaction_indicator ==</pre>
# intersted idx[3]), ])
# stage_id <- r_names[confound_values[1]] tissue_id <-</pre>
# structure[confound_values[2], 1]
# metagene_id <- which.max(coeff_matrix[intersted_idx[3],])</pre>
# which.min(coeff_matrix[intersted_idx[3],])
```