## Reinforcement Learning Exercise 3

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## 1 Proofs (5P)

a) Show that the Bellman optimality operator  $\mathcal{T}$  is a  $\gamma$ -contraction. Be able to explain all the steps! (2P)

$$(\Im v)(s) = \max_{a} \sum_{s',r} p(s',r|s,a)[r + \gamma v(s')] \tag{1}$$

b) Assuming a general finite MDP  $(S, A, R, p, \gamma)$  where rewards are bounded:  $r \in [r_{\min}, r_{\max}]$  for all  $r \in R$ . Prove the following equations. (3P)

$$\frac{r_{\min}}{1 - \gamma} \le v(s) \le \frac{r_{\max}}{1 - \gamma} \tag{2}$$

$$|v(s) - v(s')| \le \frac{r_{\text{max}} - r_{\text{min}}}{1 - \gamma} \tag{3}$$

## 2 Value Iteration (5P)

As in the previous exercise sheet, we will use the FrozenLake environment from gym (https://gym.openai.com/envs/FrozenLake-v0/). The code template can be found on github (https://github.com/humans-to-robots-motion/rl-course) in ex03-dynp/ex03-dynp.py.

- a) Implement the value iteration algorithm (see lecture 3 slide 27) in the function value\_iteration. Use the values for  $\gamma$  and  $\theta$  that are given in the code. Initialize the value function V(s) to 0 for all states. How many steps does it need to converge? What is the optimal value function? (3P)
- b) Compute the optimal policy from the value function. (2P)