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Groops.
Def: A set G with a multiplication & is a group if
r" multiplication is a bimap (binary operation))
          4: G x G - G
                (a,b) maxb
(1), at (bt c) = (axb) xc accordance lan.
    3 e E G St axe=exa=a identity.
(3). For any a6G, = 1666 sx axb=b*a=e
denove by (6, x), If axb=bxa, Gis called abelian.
                    commutation law
Ref: A set t with 't' and 'x' is called a field if
    (F,+) is abelian group with addition Identity "o"
 (2) (F1909, x) is abelian group with multiplication identity"1"
 (3) "x" and "t" are compitable, i.e.
          ax(b+1)= axb+ax(
         (a+b) x c = axc+bx c distribution law.
                           [] think since "x" is commutative
                            ax(b+1)=axb+ax(is enough)
 Kings
(lef: A set R with "+" and "x" is ralled a ring if
 (1). (k,+) form a abelian group with addition identity "D"
 (2). (R,x) form a "semigroup", that is
         0x(px()=(axp)x(
 (3). "+" and "x" are compitable. that is:
                                     ( need two equation sime
            \alpha_{x}(b+c) = \alpha^{x}b + \alpha_{x}c
                                      "x" may not commutative
          (a+b) \times C = a \times C + b \times C
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Dresewation:

() A field is a ring () A ring is not necessary a field.

Moreover (i) if ab=ba, $\forall a,b\in R$. R is called commutative ring (ii). if $e\in R$ s.t ae=ea=a, $\forall a\in R$. the e is called the identity of R.

Q: 1 How to construct gp. G?

(G, X) Whose do no ask about a gp. 6?

Loe (H, x) le groups

Pef: $X = G \times H = f(g,h) [g \in G, h \in H \setminus Mulei." - "$ $(g,h,) \cdot (g_2,h) = (g(x \cdot g_2,h,* h \times h v)$

claim (GxH,.) is a group. Check it!

Pireve Produce_ of (G.x)

(H,*)