



MA333 Introduction to Big Data Science Deep Learning

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Outlines

Introduction

What is Deep Learning ?

Why Deep Learning is Growing ?

History

The structural building block of Deep Learning

Forward Propagation

Back Propagation

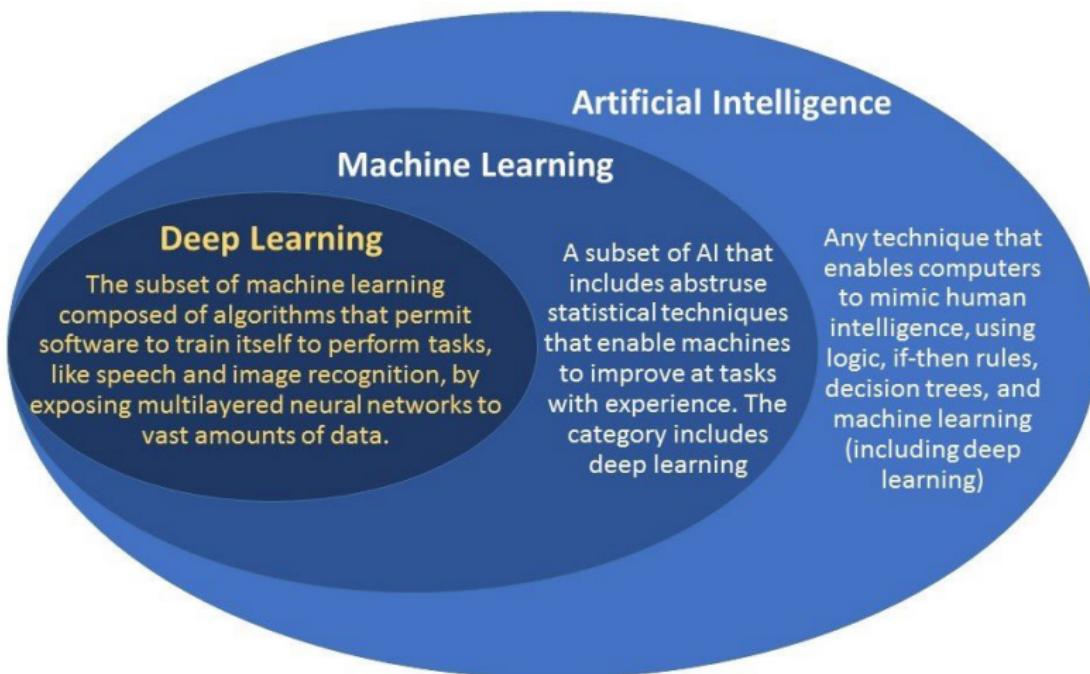
Architectures

Recurrent Neural Network (RNN)

Convolutional Neural Network (CNN)

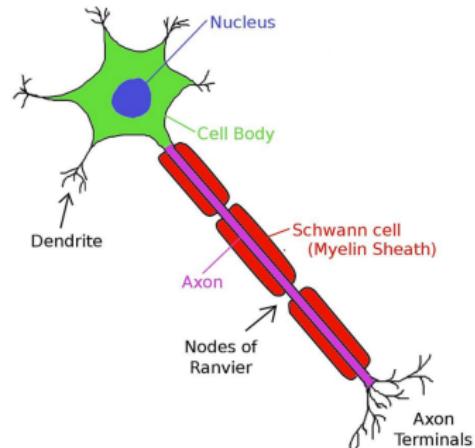
Generative model

What is Deep Learning ?



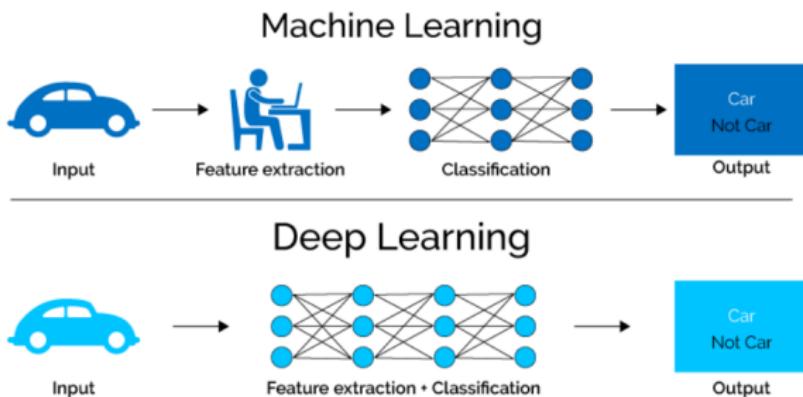
Deep Learning

- Deep learning is a sub field of Machine Learning that very closely tries to mimic human brain's working using neurons.
- These techniques focus on building Artificial Neural Networks (ANN) using several hidden layers.
- There are a variety of deep learning networks such as Multilayer Perceptron (MLP), Autoencoders (AE), Convolution Neural Network (CNN), Recurrent Neural Network (RNN).



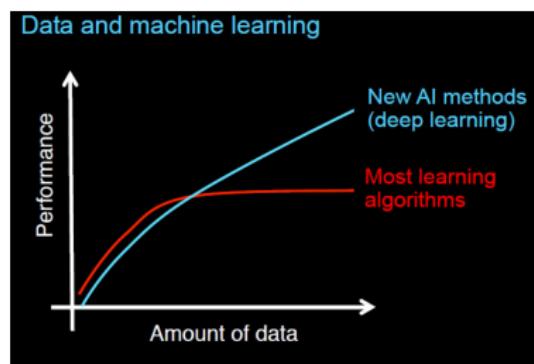
ML vs DL

- In Machine Learning, the features need to be identified by an domain expert.
- In Deep Learning, the features are learned by the neural network.



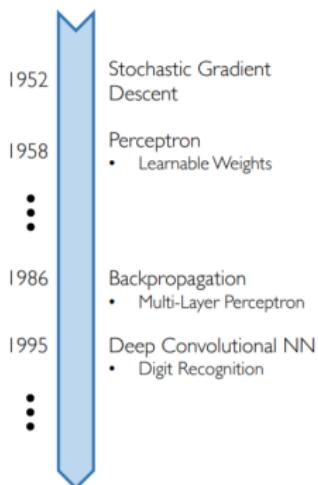
Why Deep Learning is Growing ?

- Processing power needed for Deep learning is readily becoming available using GPUs, Distributed Computing and powerful CPUs.
- Moreover, as the data amount grows, Deep Learning models seem to outperform Machine Learning models.
- Explosion of features and datasets.
- Focus on customization and real time decisioning.





Why Now?



Neural Networks date back decades, so why the resurgence?

1. Big Data

- Larger Datasets
- Easier Collection & Storage



2. Hardware

- Graphics Processing Units (GPUs)
- Massively Parallelizable



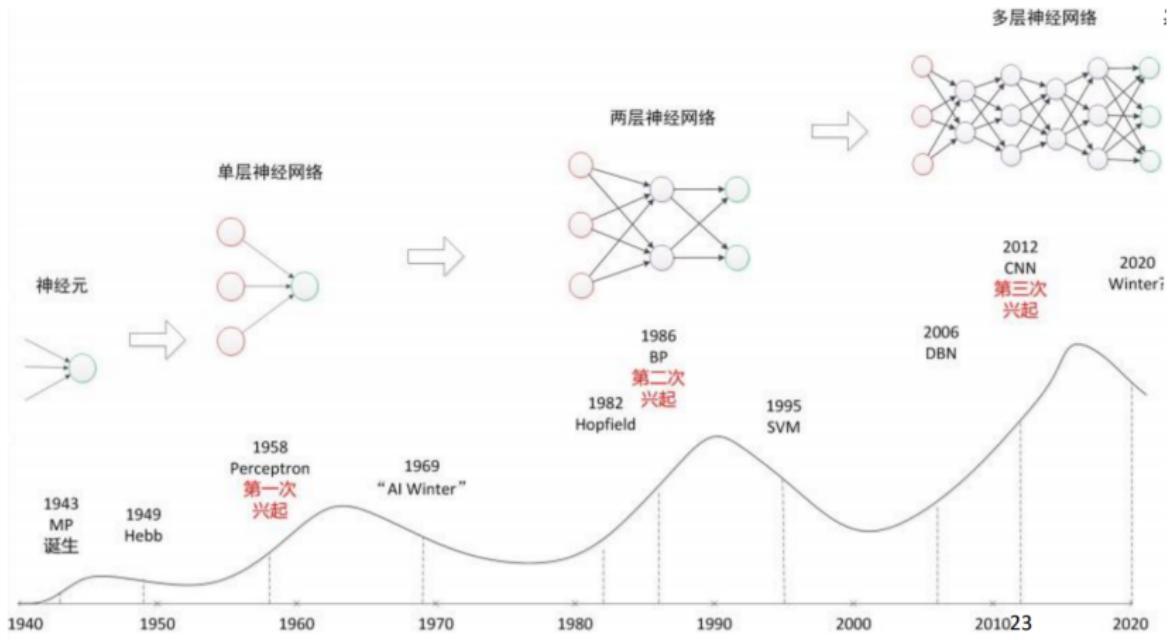
3. Software

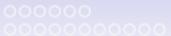
- Improved Techniques
- New Models
- Toolboxes





History





Big Guys

COMPANIES & PEOPLE



Taken in NIPS2014, from left: Yann LeCun (Facebook, NYU),
Geoffrey Hinton (Google, U of Toronto), Yoshua Bengio (U of
Montreal), Andrew Ng (Baidu)



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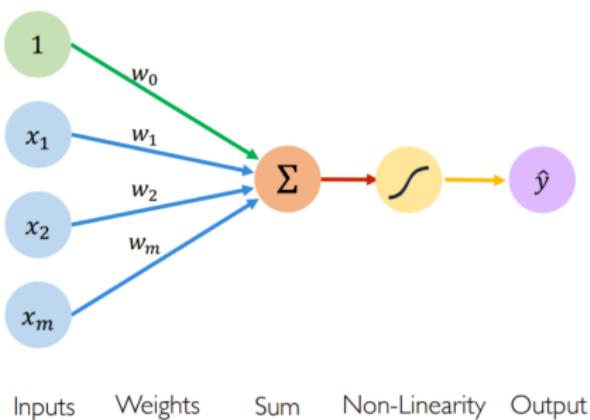
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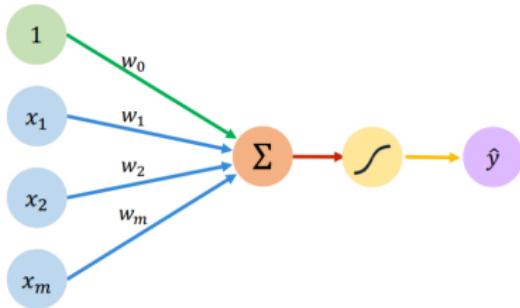
The Perceptron : Forward Propagation



$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right),$$

- \hat{y} is the Output,
- g is a Non-linear activation function,
- w_0 is the Bias.

The Perceptron : Forward Propagation



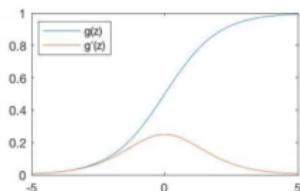
$$\hat{y} = g(w_0 + \mathbf{x}^T \mathbf{w}), \text{ where}$$

$$\mathbf{x} = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix} \text{ and } \mathbf{w} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}.$$



Common Activation Functions

Sigmoid Function

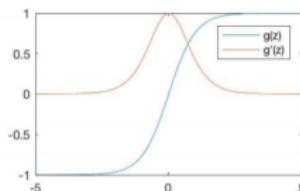


$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$

`tf.nn.sigmoid(z)`

Hyperbolic Tangent

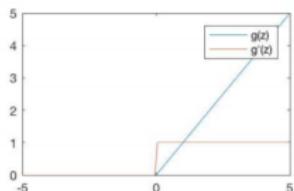


$$g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$

`tf.nn.tanh(z)`

Rectified Linear Unit (ReLU)



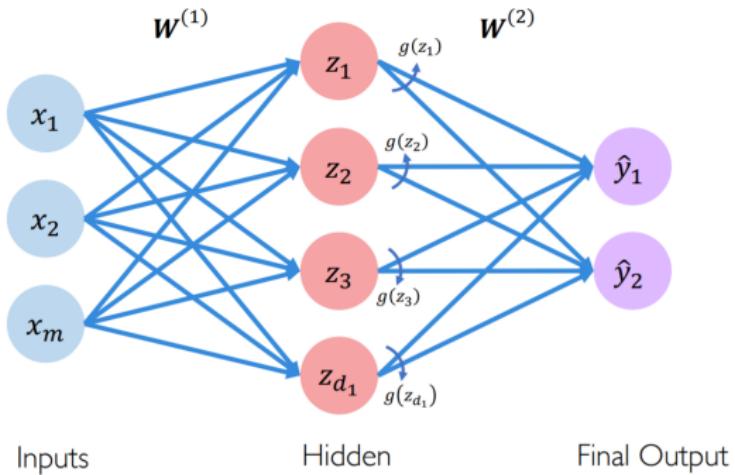
$$g(z) = \max(0, z)$$

$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & \text{otherwise} \end{cases}$$

`tf.nn.relu(z)`

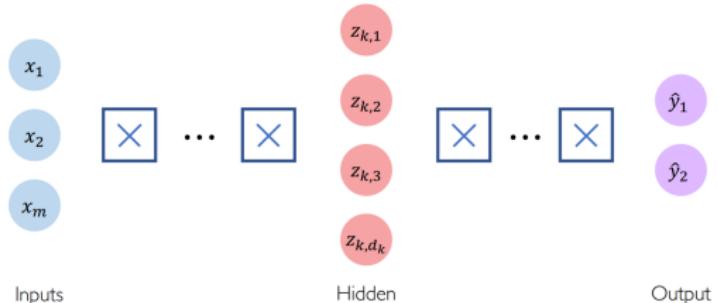
Note all activation functions are nonlinear.

Single Layer Neural Network



$$z_i = w_{0,i}^{(1)} + \sum_{j=1}^m x_j w_{j,i}^{(1)}, \quad \hat{y}_i = g \left(w_{0,i}^{(2)} + \sum_{j=1}^{d_1} z_j w_{j,i}^{(2)} \right).$$

Deep Neural Network



$$z_{k,i} = w_{0,i}^{(k)} + \sum_{j=1}^{d_{k-1}} g(z_{k-1,j}) w_{j,i}^{(k)}.$$

Theorem (Universal approximation theorem (Cybenko 1980, 1989))

1. Any function can be approximated by a three-layer neural network within sufficiently high accuracy.
2. Any bounded continuous function can be approximated by a two-layer neural network within sufficiently high accuracy.

Loss Optimization

We want to find the network weights that achieve the lowest loss

$$\mathbf{W}^* = \operatorname{argmin}_{\mathbf{W}} \frac{1}{n} \sum_{i=1}^n \mathcal{L}\left(f\left(x^{(i)}; \mathbf{W}\right), y^{(i)}\right),$$

where $\mathcal{L}\left(f\left(x^{(i)}; \mathbf{W}\right), y^{(i)}\right)$ is the loss function we defined according to the specific problem to measure the differences between output state $f\left(x^{(i)}; \mathbf{W}\right)$ and reference state $y^{(i)}$. It also can be written as

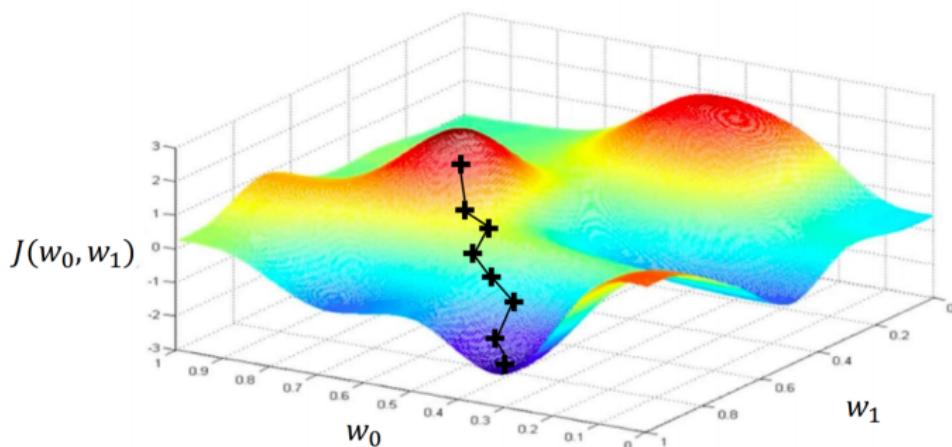
$$\mathbf{W}^* = \operatorname{argmin}_{\mathbf{W}} C(\mathbf{W}).$$

Remember

$$\mathbf{W} = \left\{ \mathbf{W}^{(0)}, \mathbf{W}^{(1)}, \dots \right\}.$$

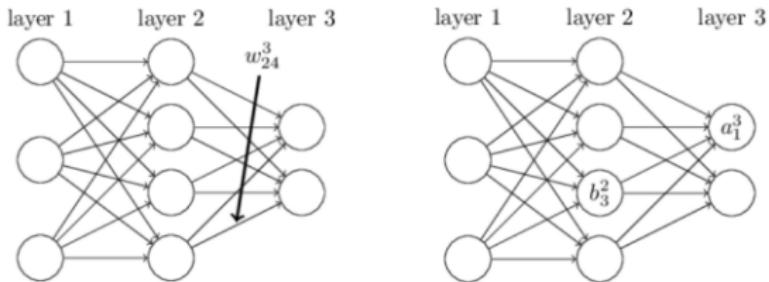
Gradient Decent

We can use Gradient Decent algorithm to find the optimal parameter \mathbf{W} .



Note that we should calculate $\frac{\partial C}{\partial \mathbf{W}}$ to update \mathbf{W} .

Notations



- w_{jk}^l is the weight for the connection from the k^{th} neuron in the $(l-1)^{th}$ layer to the j^{th} neuron in the l^{th} layer.
 - for brevity $b_j^l = w_{j0}^l$ is the bias of the j^{th} neuron in the l^{th} layer.
 - a_j^l for the activation of the j^{th} neuron in the l^{th} layer z_j^l .

$$a_j^l = g(z_j^l) = g\left(\sum_k w_{jk}^l a_k^{l-1} + b_j^l\right)$$

Four fundamental equations

We first define the error δ_j^l of neuron j in layer by

$$\delta_j^l \equiv \frac{\partial C}{\partial z_j^l},$$

and we give the four fundamental equations of back propagation :

$$\delta^L = \nabla_a C \odot \sigma'(z^L) \quad (BP1)$$

$$\delta^l = \left(\left(w^{l+1} \right)^T \delta^{l+1} \right) \odot \sigma'(z^l) \quad (BP2)$$

$$\frac{\partial C}{\partial b_j^L} = \delta_j^l \quad (BP3)$$

$$\frac{\partial C}{\partial w_{jk}^l} = a_k^{l-1} \delta_j^l \quad (BP4)$$

An equation for the error in the output layer (BP1)

The components of δ^L are given by

$$\delta^L = \nabla_a C \odot \sigma' (z^L) \quad (BP1)$$

Démonstration.

$$\begin{aligned}\delta_j^L &= \frac{\partial C}{\partial z_j^L} \\ &= \sum_k \frac{\partial C}{\partial a_k^L} \frac{\partial a_k^L}{\partial z_j^L} \\ &= \frac{\partial C}{\partial a_j^L} \frac{\partial a_j^L}{\partial z_j^L} = \frac{\partial C}{\partial a_j^L} \frac{\partial \sigma(z_j^L)}{\partial z_j^L} \\ &= \frac{\partial C}{\partial a_j^L} \sigma'(z_j^L)\end{aligned}$$



An equation for the error in the hidden layer (BP2)

$$\delta^l = \left(\left(w^{l+1} \right)^T \delta^{l+1} \right) \odot \sigma' \left(z^l \right) \quad (BP2)$$

Démonstration.

$$\begin{cases} \delta_j^l = \frac{\partial C}{\partial z_j^l} = \sum_k \frac{\partial C}{\partial z_k^{l+1}} \frac{\partial z_k^{l+1}}{\partial z_j^l} = \sum_k \delta_k^{l+1} \frac{\partial z_k^{l+1}}{\partial z_j^l} \\ z_k^{l+1} = \left(\sum_i w_{ki}^{l+1} a_i^l \right) + b_k^{l+1} = \left(\sum_i w_{ki}^{l+1} \sigma(z_i^l) \right) + b_k^{l+1} \end{cases}$$

$$\Rightarrow \begin{cases} \delta_j^l = \sum_k \delta_k^{l+1} \frac{\partial z_k^{l+1}}{\partial z_j^l} \\ \frac{\partial z_k^{l+1}}{\partial z_j^l} = w_{kj}^{l+1} \sigma'(z_j^l) \end{cases} \Rightarrow \delta_j^l = \sum_k \delta_k^{l+1} w_{kj}^{l+1} \sigma'(z_j^l) \quad \square$$

The change of the cost with respect to any bias (BP3)

$$\frac{\partial C}{\partial b_j^l} = \delta_j^l \quad (BP3)$$

Démonstration.

$$\begin{cases} \frac{\partial C}{\partial b_j^l} = \sum_k \frac{\partial C}{\partial z_k^l} \frac{\partial z_k^l}{\partial b_j^l} = \frac{\partial C}{\partial z_j^l} \frac{\partial z_j^l}{\partial b_j^l} \\ z_j^l = \left(\sum_k w_{jk}^l d_k^{l-1} \right) + b_j^l \Rightarrow \frac{\partial z_k^l}{\partial b_j^l} = 1 \end{cases} \Rightarrow \frac{\partial C}{\partial b_j^l} = \frac{\partial C}{\partial z_j^l} \cdot 1 = \delta_j^l. \quad \square$$

The change of the cost with respect to any weight (BP4)

$$\frac{\partial C}{\partial w_{jk}^l} = a_k^{l-1} \delta_j^l \quad (BP4)$$

Démonstration.

$$\begin{cases} \frac{\partial C}{\partial w_{jk}^l} = \sum_i \frac{\partial C}{\partial z_i^l} \frac{\partial z_i^l}{\partial w_{jk}^l} = \frac{\partial C}{\partial z_j^l} \frac{\partial z_j^l}{\partial w_{jk}^l} \\ z_j^l = \left(\sum_m w_{jm}^l a_m^{l-1} \right) + b_j^l \Rightarrow \frac{\partial z_j^l}{\partial w_{jk}^l} = a_k^{l-1} \end{cases}$$

$$\Rightarrow \frac{\partial C}{\partial w_{jk}^l} = \frac{\partial C}{\partial z_j^l} \frac{\partial z_j^l}{\partial w_{jk}^l} = \delta_j^l a_k^{l-1}$$





Back Propagation procedure

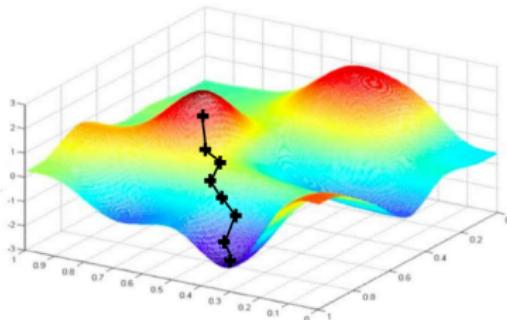
- 1. Input x : Set the corresponding activation a^1 for the input layer.
- 2. Feedforward : For each $l = 2, 3, \dots, L$ compute $z^l = w^l a^{l-1} + b^l$ and $a^l = \sigma(z^l)$.
- 3. Output error δ^L : Compute the vector $\delta^L = \nabla_a C \odot \sigma'(z^L)$.
- 4. Backpropagate the error : For each $l = L-1, L-2, \dots, 2$ compute $\delta^l = ((w^{l+1})^T \delta^{l+1}) \odot \sigma'(z^l)$.
- 5. Output : The gradient of the cost function is given by $\frac{\partial C}{\partial w_{jk}^l} = a_k^{l-1} \delta_j^l$ and $\frac{\partial C}{\partial b_j^l} = \delta_j^l$.



Gradient Descent

Algorithm

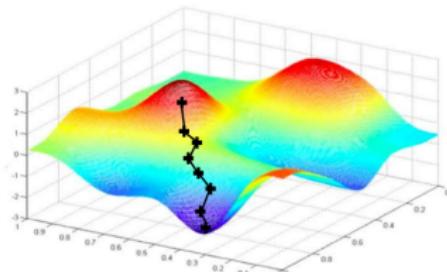
1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Compute gradient, $\frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
4. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
5. Return weights



Stochastic Gradient Descent

Algorithm

1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
2. Loop until convergence:
3. Pick single data point i
4. Compute gradient, $\frac{\partial J_i(\mathbf{W})}{\partial \mathbf{W}}$
5. Update weights, $\mathbf{W} \leftarrow \mathbf{W} - \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
6. Return weights



- Mini-batches lead to fast training !
- Can parallelize computation + achieve significant speed increases on GPUs.

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Convolutional Neural Network (CNN)

Generative model

A sequence modeling problem : predict the next word

- **France** is where I grew up, but I now live in Boston. I speak fluent ???.
- The food was good, not bad at all.
vs. The food was bad, not good at all.

Sequence modeling : design criteria

To model sequences, we need to :

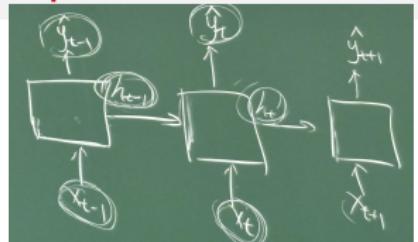
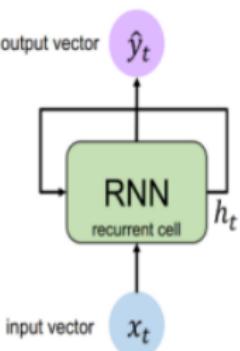
- 1. Handle variable-length sequences
- 2. Track long-term dependencies
- 3. Maintain information about order
- 4. Share parameters across the sequence

Today : Recurrent Neural Networks (RNNs) as an approach to sequence modeling problems

RNN state update and output

Apply a recurrence relation at every time step to process a sequence :

Note : the same function and set of parameters are used at every time step



Output Vector

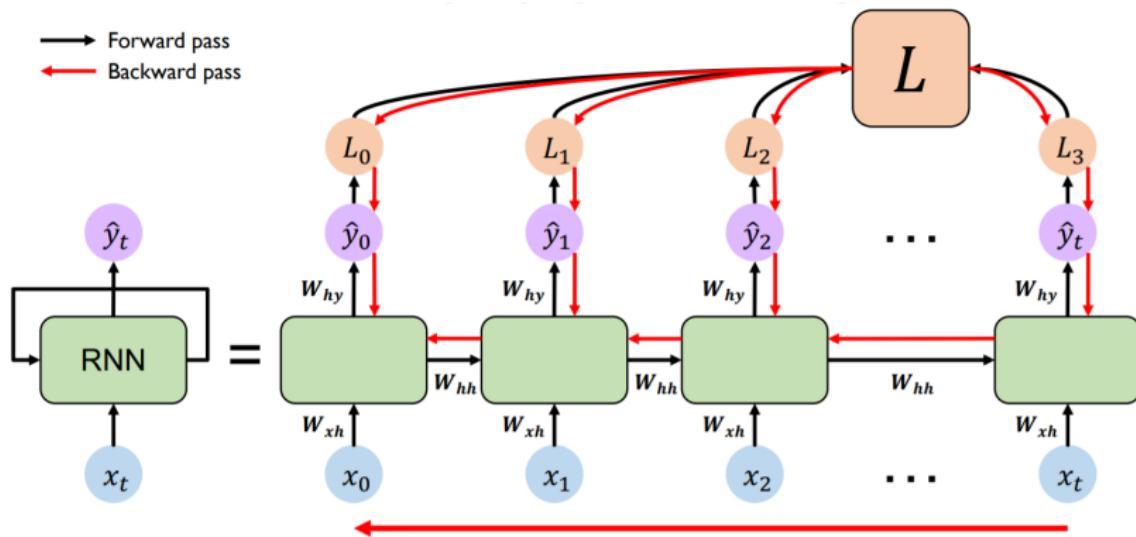
$$\hat{y}_t = \mathbf{W}_{hy} h_t$$

Update Hidden State

$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

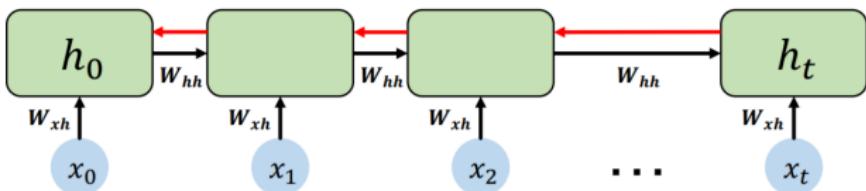
Input Vector

RNNs : backpropagation through time



Note that it reuse the same weight matrices at every time step

Standard RNN gradient flow : exploding gradients



Computing the gradient wrt h_0 involves **many factors of W_{hh}** (and repeated f' !)

Many values > 1:
exploding gradients

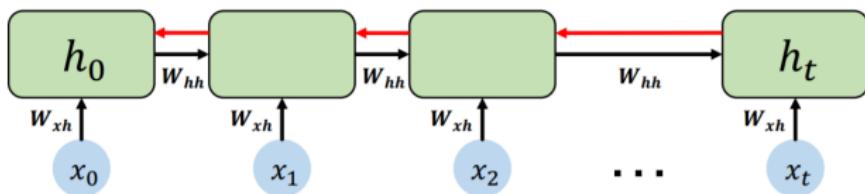
Gradient clipping to
scale big gradients

$$\sum_{t=0}^T L(f(x_t; \underline{w}), y_t) = L(\underline{w})$$

$\min_w L(w) \quad w_{k+1} = w_k - \alpha \nabla L(w)$

f_0, f_t, f_t'

Standard RNN gradient flow : vanishing gradients



Computing the gradient wrt h_0 involves **many factors of W_{hh}** (and repeated f' !)

Largest singular value > 1 :
exploding gradients

Gradient clipping to
scale big gradients

Largest singular value < 1 :
vanishing gradients

1. Activation function
2. Weight initialization
3. Network architecture

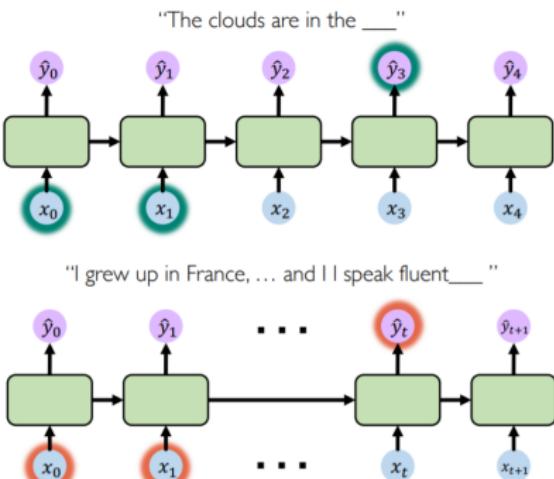
The problem of long-term dependencies

Why are vanishing gradients a problem?

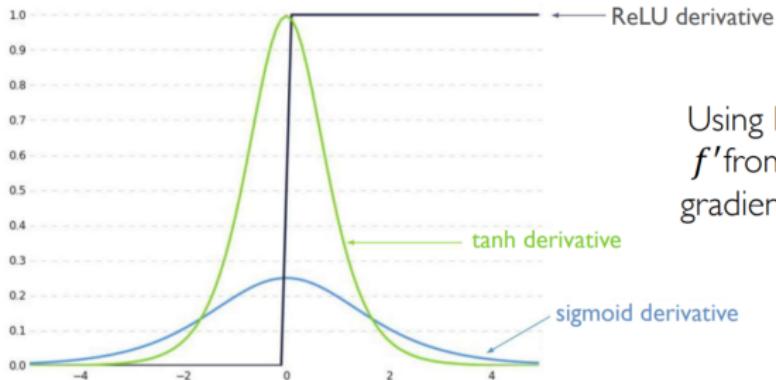
Multiply many **small numbers** together

Errors due to further back time steps
have smaller and smaller gradients

Bias parameters to capture short-term
dependencies



Trick 1 : activation functions



Using ReLU prevents f' from shrinking the gradients when $x > 0$

Trick 2 : parameter initialization

- Initialize weights to identity matrix .
- Initialize biases to zero.

$$I_n = \begin{pmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 1 \end{pmatrix}$$

This helps prevent the weights from shrinking to zero.

Trick 3 : gated cells

Idea : use a more complex recurrent unit with gates to control what information is passed through

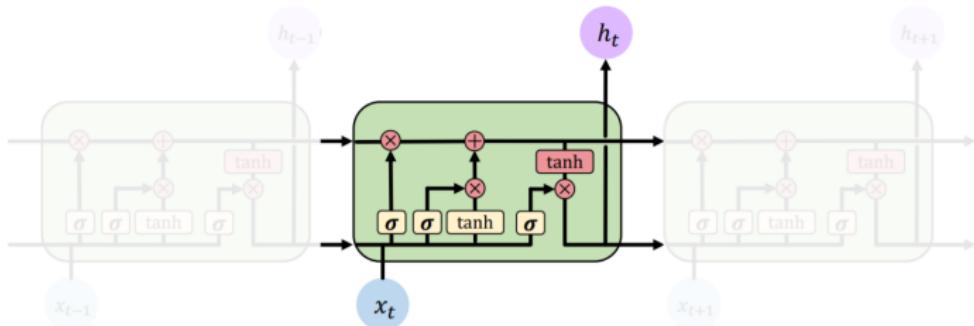
gated cell

LSTM, GRU, etc.

Long Short Term Memory (LSTMs) networks rely on a gated cell to track information throughout many time steps.

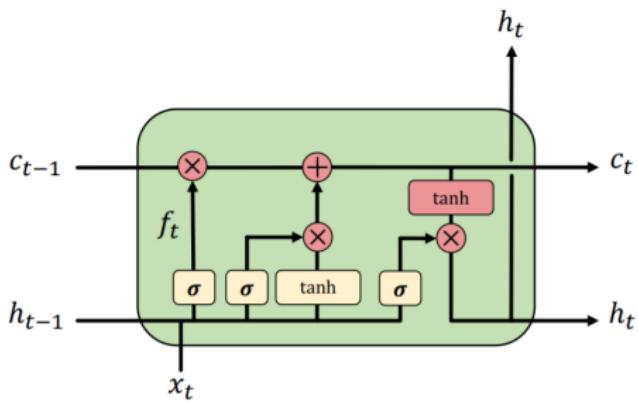
Long Short Term Memory (LSTMs)

LSTM repeating modules contain interacting layers that control information flow.



LSTM cells are able to track information throughout many time steps.

Long Short Term Memory (LSTMs)

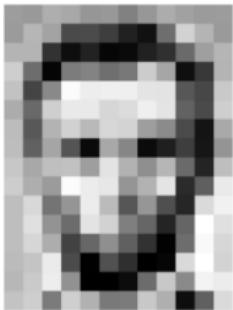


- What information to throw away ?
- What to store ?
- What to output ?

Recurrent neural networks (RNNs)

- 1. RNNs are well suited for sequence modeling tasks.
- 2. Model sequences via a recurrence relation.
- 3. Training RNNs with backpropagation through time.
- 4. Gated cells like LSTMs let us model long-term dependencies.
- 5. Models for music generation, classification, machine translation.

Tasks in Computer Vision



Input Image



187	183	174	168	160	162	159	151	172	141	186	166
185	182	162	74	76	62	38	17	112	210	180	154
180	180	89	14	24	6	10	33	48	196	189	181
206	199	6	122	131	171	120	204	164	16	66	160
156	68	137	231	237	236	239	228	227	87	71	231
173	195	97	217	230	230	234	239	239	234	97	74
188	88	179	209	185	210	211	198	130	75	20	169
188	97	165	84	10	160	134	11	31	62	32	148
159	148	191	118	106	227	178	142	182	196	36	150
205	174	186	230	236	231	149	178	220	43	96	234
160	216	116	149	236	187	86	180	79	36	218	241
186	224	147	114	227	210	137	102	36	101	295	224
180	214	179	56	103	143	96	80	3	109	249	215
187	196	230	76	1	84	47	0	8	217	280	211
181	202	237	145	0	0	13	108	205	136	243	236
186	206	123	207	177	121	133	200	175	13	96	218

Pixel Representation



Lincoln

$$\begin{bmatrix} 0.8 \\ 0.1 \\ 0.05 \\ 0.05 \end{bmatrix}$$

Washington

$$\begin{bmatrix} 0.1 \\ 0.8 \\ 0.05 \\ 0.05 \end{bmatrix}$$

Jefferson

$$\begin{bmatrix} 0.05 \\ 0.8 \\ 0.1 \\ 0.05 \end{bmatrix}$$

Obama

$$\begin{bmatrix} 0.05 \\ 0.05 \\ 0.8 \\ 0.1 \end{bmatrix}$$

- Regression : output variable takes continuous value.
- Classification : output variable takes class label. Can produce probability of belonging to a particular class.

Problems in Manual Feature Extraction

Domain knowledge

Define features

Detect features
to classify

Viewpoint variation



Scale variation



Deformation



Occlusion



Illumination conditions



Background clutter



Intra-class variation

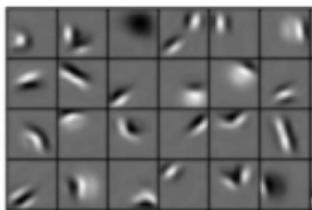




Learning Feature Representations

Can we learn a hierarchy of features directly from the data instead of hand engineering?

Low level features



Edges, dark spots

Mid level features



Eyes, ears, nose

High level features

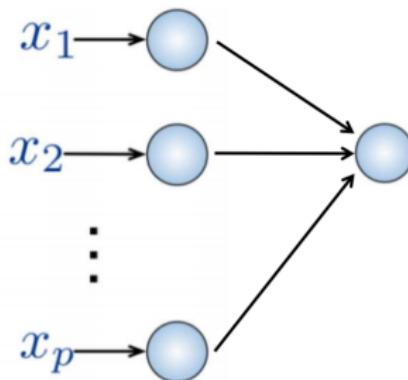


Facial structure

Fully Connected Neural Network

Input :

- 2D image.
- Vector of pixel values.



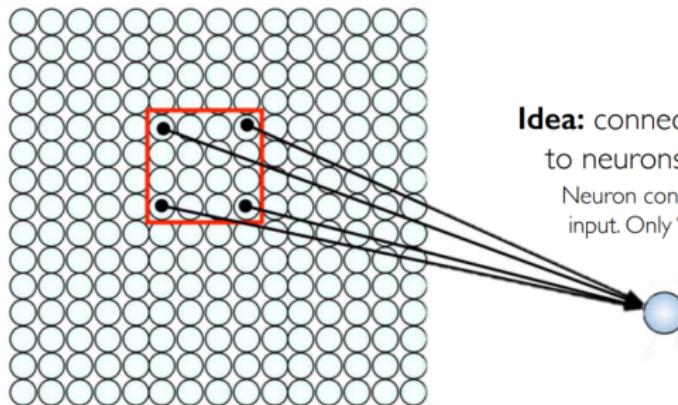
Fully Connected :

- Connect neuron in hidden layer to all neurons in input layer.
- No spatial information !
- And many, many parameters !

How can we use spatial structure in the input to inform the architecture of the network ?

Using Spatial Structure

Input: 2D image.
Array of pixel values



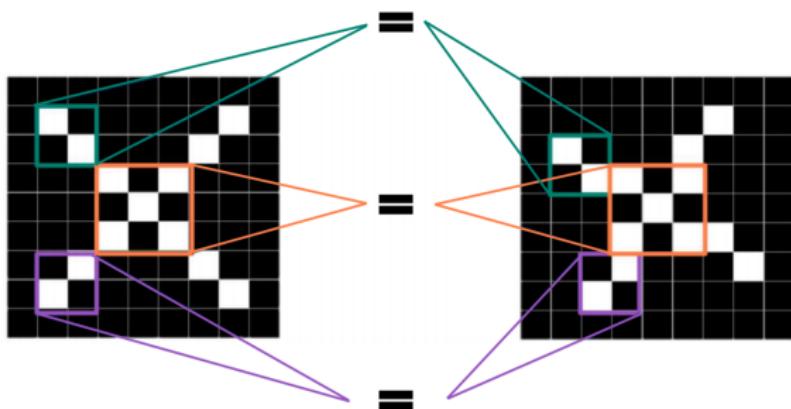
Idea: connect patches of input
to neurons in hidden layer.
Neuron connected to region of
input. Only "sees" these values.

- Connect patch in input layer to a single neuron in subsequent layer.
- Use a sliding window to define connections.
- How can we weight the patch to detect particular features ?

Applying Filters to Extract Features

- 1 Apply a set of weights (a filter) to extract local features.
- 2 Use multiple filters to extract different features.
- 3 Spatially share parameters of each filter. (features that matter in one part of the input should matter elsewhere.)

Features of X



- Image is represented as matrix of pixel values and computers are literal !
- We want to be able to classify an X as an X even if it is shifted, shrunk, rotated, deformed.

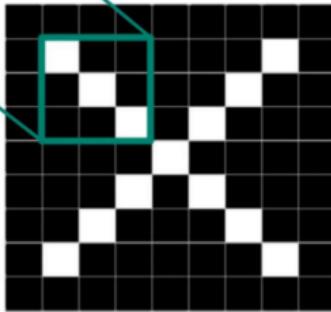
Filters to Detect X Features

filters

$$\begin{bmatrix} 1 & -1 & -1 \\ -1 & 1 & -1 \\ -1 & -1 & 1 \end{bmatrix}$$

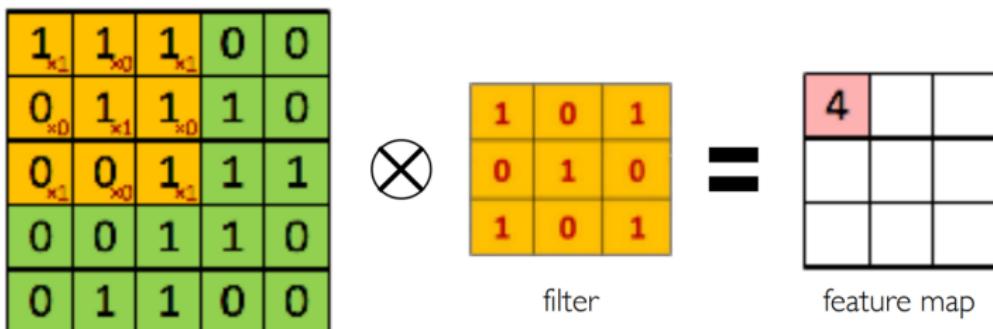
$$\begin{bmatrix} 1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & -1 \end{bmatrix}$$



The Convolution Operation

- Suppose we want to compute the convolution of a 5x5 image and a 3x3 filter.
- We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs :



The Convolution Operation

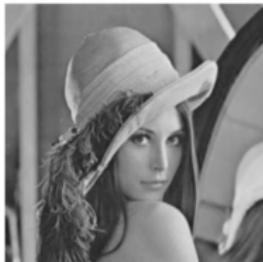
- Suppose we want to compute the convolution of a 5x5 image and a 3x3 filter.
- We slide the 3x3 filter over the input image, element-wise multiply, and add the outputs :

The diagram illustrates the convolution operation. On the left is a green input image (5x5) with values: 1, 1, 1, 0, 0; 0, 1, 1, 1, 0; 0, 0, 1_{x1}, 1_{x0}, 1_{x1}; 0, 0, 1_{x0}, 1_{x2}, 0_{x0}; 0, 1, 1_{x1}, 0_{x0}, 0_{x1}. In the center is a yellow filter (3x3) with values: 1, 0, 1; 0, 1, 0; 1, 0, 1. To the right is a pink feature map (3x3) with values: 4, 3, 4; 2, 4, 3; 2, 3, 4. Between the input image and the filter is a large black circle with a white cross inside, representing element-wise multiplication. To the right of the filter is a double equals sign (=), and below the feature map is the label "feature map".

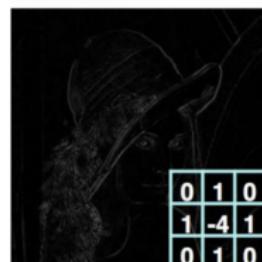


Producing Feature Maps

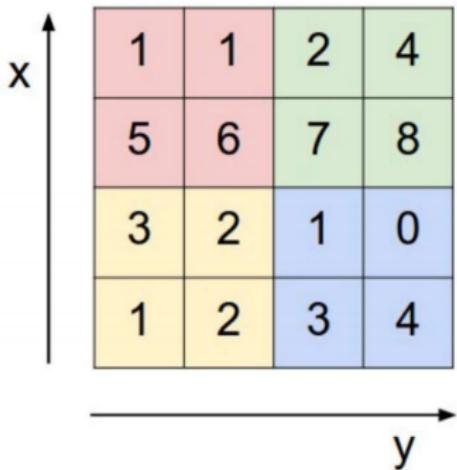
Different filters have different effects !



Original



Pooling

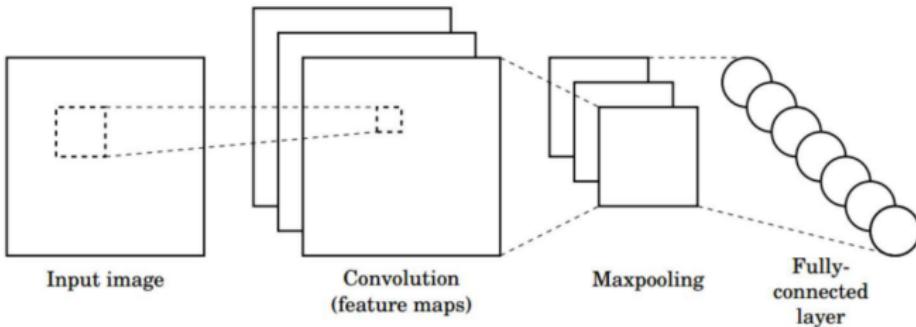


max pool with 2x2 filters
and stride 2

6	8
3	4

- 1) Reduced dimensionality
- 2) Spatial invariance

CNNs for Classification

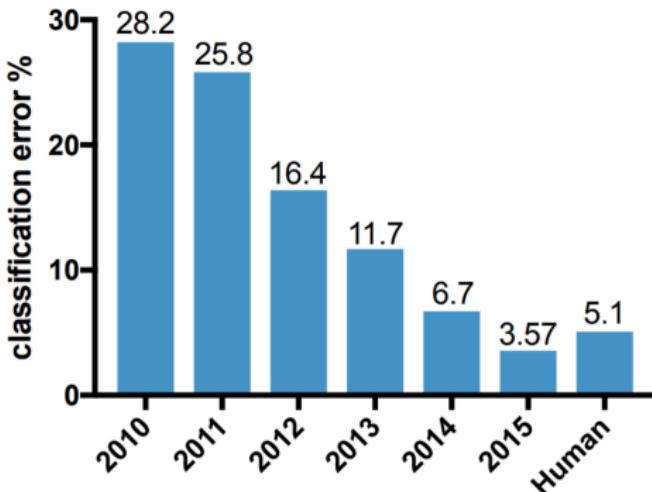


- 1. Convolution : Apply filters with learned weights to generate feature maps.
- 2. Non-linearity : Often ReLU.
- 3. Pooling : Downsampling operation on each feature map.

Train model with image data.

Learn weights of filters in convolutional layers.

ImageNet Challenge : Classification Task



2012: AlexNet. First CNN to win.

- 8 layers, 61 million parameters

2013: ZFNet

- 8 layers, more filters

2014: VGG

- 19 layers

2014: GoogLeNet

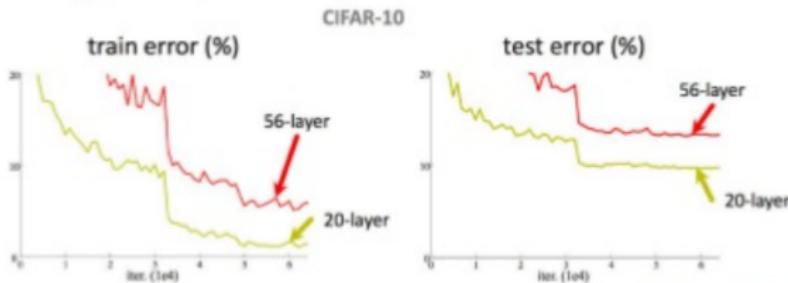
- "Inception" modules
- 22 layers, 5 million parameters

2015: ResNet

- 152 layers

The problem when go deeper

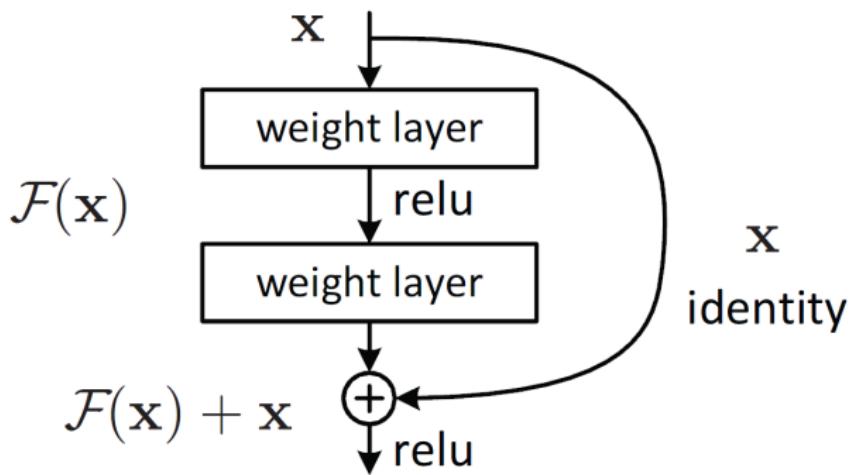
- Simply stack layers after layers



- Plain nets: stacking of 3x3 conv layers
 - 56-layers got higher training and test error

Problem of going deeper?

- **Vanishing Gradient**
 - Most neurons will die during back propagating the weights.

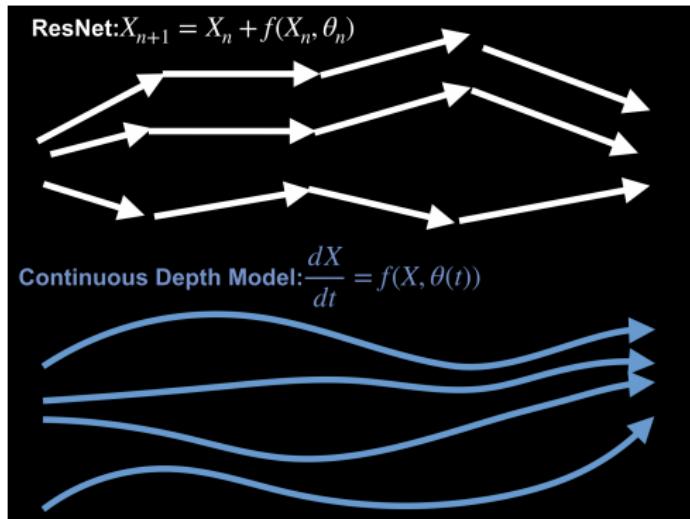


- Introduce shortcut connections (exists in prior literature in various forms).
 - Key invention is to skip 2 layers.
Skipping single layer do not give much improvement for some reason.

前面可能丢失了信息
如果不加上 x ，这些信息就永久丢失

ResNet vs ODENet

- **ResNet :** $\mathbf{h}_{t+1} = \mathbf{h}_t + f(\mathbf{h}_t, \theta_t),$
- **ODENet :** $\frac{d\mathbf{h}(t)}{dt} = f(\mathbf{h}(t), t, \theta).$





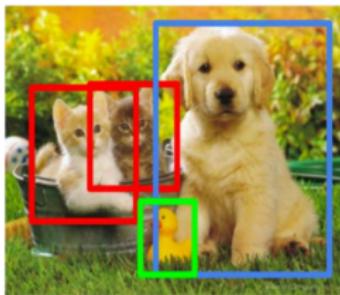
Beyond Classification

Semantic Segmentation



CAT

Object Detection



CAT, DOG, DUCK

Image Captioning



The cat is in the grass.

Supervised vs unsupervised learning

Supervised Learning

- Data : (x, y)
 x is data, y is label.
- Goal : Learn function to map $x \Rightarrow y$.
- Examples : Classification, regression, object detection, semantic segmentation, etc.

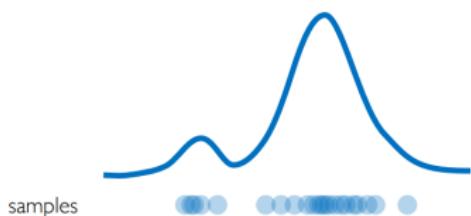
Unsupervised Learning

- Data : x
 x is data, no labels !
- Goal : Learn some hidden or underlying structure of the data.
- Examples : Clustering, feature or dimensionality reduction, etc.

Generative modeling

Goal : Take as input training samples from some distribution and learn a model that represents that distribution

Density Estimation



Sample Generation



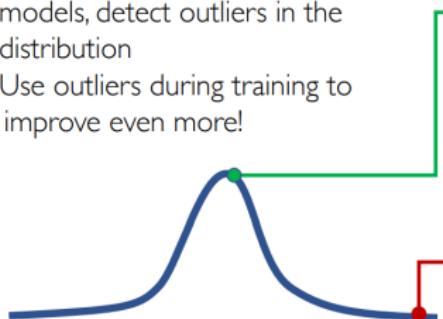
Training data $\sim P_{data}(x)$

Generated $\sim P_{model}(x)$

How can we learn $p_{model}(x)$ similar to $p_{data}(x)$?

Why generative models? Outlier detection

- **Problem:** How can we detect when we encounter something new or rare?
- **Strategy:** Leverage generative models, detect outliers in the distribution
- Use outliers during training to improve even more!



95% of Driving Data:

- (1) sunny, (2) highway, (3) straight road



Detect outliers to avoid unpredictable behavior when training



Edge Cases



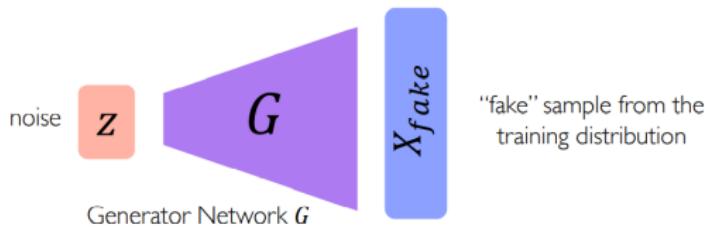
Harsh Weather



Pedestrians

What if we just want to sample

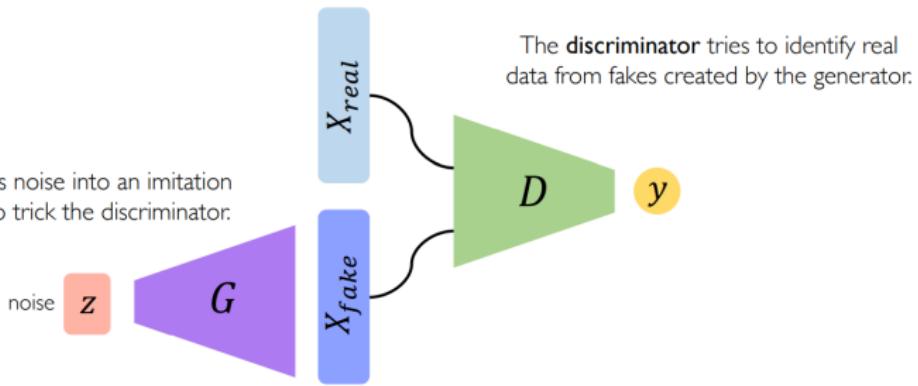
- Idea : do not explicitly model density, and instead just sample to generate new instances.
 - Problem : want to sample from complex distribution can not do this directly !
 - Solution : sample from something simple (noise), learn a transformation to the training distribution.



Generative Adversarial Networks (GANs)

- Generative Adversarial Networks (GANs) are a way to make a generative model by having two neural networks compete with each other.

The **generator** turns noise into an imitation of the data to try to trick the discriminator.

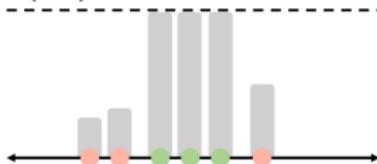


Training GANs

- Neural Network Discriminator tries to identify real data from fakes created by the generator.
 - Neural Network Generator tries to create imitations of data to trick the discriminator.

Discriminator

$$P(\text{real}) = 1$$



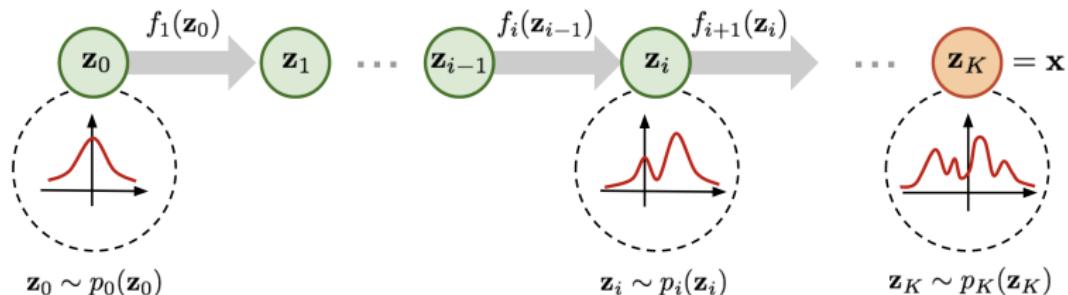
Generator



$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

What if we want the model density

Flow based model



- f is bijective and differentiable functions.
 - We have the explicitly model density $p_{z_k}(z_k)$.

CVF

Theorem

(Change of Variable Theorem) Given any $z_0 \sim p_{z_0}(z_0)$, if the transformation $f : \mathbb{R}^d \rightarrow \mathbb{R}^d$ is differentiable and bijective, then the distribution of $x = f(z_0)$ is $p_x(x) = \frac{p_{z_0}(z_0)}{\left| \det \frac{\partial f}{\partial z_0} \right|}$.

- The density probability follows

$$\log p_{z_k}(z_k) = \log p_{z_0}(z_0) - \sum_{i=1}^k \left| \det \frac{\partial f_i}{\partial z_{i-1}} \right|.$$

- we want to find parameter λ of neural network f_i satisfies :

$$\arg \min_{\lambda} D_{KL}(p_{data} || p_{z_k}^{\lambda}) \approx \arg \max_{\lambda} \sum_{i=1}^m \log p_{z_k}^{\lambda}(x^{(i)}),$$

FUTURE : LONG WAY TO GO

- Theory : why deep learning works ? How ? Interpretability.
- Capacity : how deep is enough ? / Network structure selection.
- Manipulate network.
- Geometry of loss function.
- Deep learning with less data ?
- Interdisciplinary fields : statistics, physics, geometry, game theory...
- More exciting applications ! Healthcare, industrial process, finance, AI game play, animation...