Libraries

```
import numpy as np
import h5py
import matplotlib.pyplot as plt
from math import sqrt, pi
from sklearn.cluster import KMeans
```

```
C:\ProgramData\Anaconda3\lib\site-packages\h5py\__init__.py:36:
FutureWarning: Conversion of the second argument of issubdtype from
`float` to `np.floating` is deprecated. In future, it will be treated
as `np.float64 == np.dtype(float).type`.
from ._conv import register_converters as _register_converters
```

Read

```
f = h5py.File('../data/assignmentSegmentBrainGmmEmMrf.mat','r')
list(f.keys())
imageData = f.get('imageData')
imageMask = f.get('imageMask')
imageData = np.array(imageData)
imageData = imageData.T
imageMask = np.array(imageMask)
imageMask = imageMask.T
```

GMM With EM

```
def label priors (input label, old labels, beta, map left,
        map_right, map_top, map_bottom, mask):
         img = input_label
         if len(input_label) ==1:
                 img = input label*np.ones((old labels.shape))
         top = ((img-np.roll(old labels,[1,1], [0,1]))*map top)!=0
         bottom = ((img-np.roll(old_labels,[-1,1], [0,1])) *map_bottom)!=0
         left = ((img-np.roll(old_labels,[1,2], [0,1]))*map_left)!=0
         right = ((img-np.roll(old labels, [-1,2], [0,1]))*map right)!=0
         return np.exp(-((top+bottom+left+right)*beta))*mask
def memberships( y, means, sigmas, old_labels, mask, prior_val):
         K = means.shape[0]
         likelihood = np.zeros((y.shape[0], y.shape[1], 3))
         prior = np.zeros((y.shape[0], y.shape[1], 3))
         for i in range(K):
                  likelihood[:,:,i] = ((1/(sigmas[i,0]*sqrt(2*pi)))*np.exp(-(y-means[i,0])**2/(2*sigmas[i,0]**2)))*mask* + (1/(sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/(2*sigmas[i,0])**2/
                 prior[:,:,i] = prior_val(np.array([i]),old_labels)
         norm = np.sum(prior,2)
         for i in range(K):
                  prior[:,:,i] /=norm
         membership = likelihood*prior
         norm = np.sum(membership,2)
         for i in range(K):
                  membership[:,:,i] /= norm
         temp = np.zeros((old_labels.shape))
         for i in range(K):
                   temp = membership[:,:,i]
                   temp[mask==0] = 0
                  membership[:,:,i] = temp
         return membership
def gaussian_paprameters(y, mem, maps):
         means = np.zeros((mem.shape[2],1))
         sigmas = np.zeros((mem.shape[2],1))
         for i in range(mem.shape[2]):
                  den = np.sum(mem[:, :, i])
                  means[i,0] = np.sum(mem[:, :, i]*y)/den
                  sigmas[i,0] = np.sqrt(np.sum(mem[:,:,i]*((y-means[i,0])**2)*maps)/den)
         return means, sigmas
```

```
def posterior_val(old_labels, y, means, sigmas, maps, prior_val):
          likelihood = np.zeros((old labels.shape))
           for i in range(len(means)):
                     indeold labels = np.where(old labels==i)
                     likelihood[indeold\_labels] = (1/(sigmas[i,0]*sqrt(2*pi)))*np.exp(-(y[indeold\_labels]-means[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(2*(sigmas[i,0])**2/(sigmas[i,0])**2/(sigmas[i,0])**2/(sigmas[i,0])**2/(sigmas[i,0])
mas[i,0]**2)))
          prior = prior_val(old_labels,old_labels)
           return likelihood*prior*maps
def segmentation( old labels, y, means, sigmas, iters, mask, prior_val):
           for i in range(iters):
                     oldLogPosterior = np.sum(np.log(posterior val(old labels,y,means,sigmas,mask,prior val)[mask!=0]))
                     print('%d : Initial log posterior = %f\n'%(i,oldLogPosterior))
                     membership = memberships(y,means,sigmas,old_labels,mask,prior_val)
                    new_labels = np.argmax(membership,2)
                     new labels = new labels*mask
                     posterior = posterior val(new labels,y,means,sigmas,mask,prior val)
                     newLogPosterior = np.sum(np.log(posterior[mask!=0]))
                    print('%d : Final log posterior = %f\n'%(i,newLogPosterior))
                     if newLogPosterior<oldLogPosterior:</pre>
                    means, sigmas = gaussian_paprameters(y, membership, mask)
                     equal = np.array_equal(old_labels, new labels)
                     if equal:
                                break
                     old labels = new labels
           return old labels, means, sigmas, iters
```

Label initialization

```
s = imageData.shape
K = 3
map_left = np.roll(imageMask, [1,2], [0,1])
map_right = np.roll(imageMask, [-1,2], [0,1])
map top = np.roll(imageMask, [1,1], [0,1])
map_bottom = np.roll(imageMask, [-1,1], [0,1])
beta1 = 2
beta2 = 0
prior1 = lambda input_label, old_labels: label priors(
    input_label,old_labels,beta1,map_left,map_right,
    map top,map bottom,imageMask)
prior2 = lambda input label, old labels: label priors(
    input_label,old_labels,beta2,map_left,map_right,
    map top,map bottom,imageMask)
masked img = imageData[imageMask>0]
masked_img = np.reshape(masked_img, (masked_img.shape[0], 1))
kmeans = KMeans(n_clusters = K).fit(masked_img)
initial_labels = kmeans.labels
means_init = kmeans.cluster_centers_
label_map = np.zeros((imageData.shape))
label map[imageMask>0] = initial labels
```

Variance

```
sigmas_init = np.zeros((K,1))
for i in range(K):
    clusterVals = masked_img[initial_labels==i]
    sigmas_init[i] = np.linalg.norm(clusterVals - means_init[i])/sqrt(len(clusterVals))
```

Segmentation

```
initial_labels = label_map
print('Modified ICM with beta = %f \n'%(betal))
labels1, means1, sigmas1, iters1 = segmentation(initial_labels, imageData, means_init,
```

```
sigmas_init,20,imageMask,prior1)

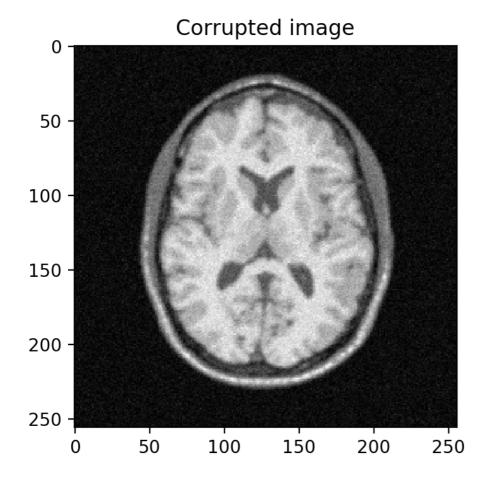
print('Modified ICM with beta = %f \n'%(beta2))
labels2,means2,sigmas2,iters2 = segmentation(initial_labels,imageData,means_init,
    sigmas_init,20,imageMask,prior2)
```

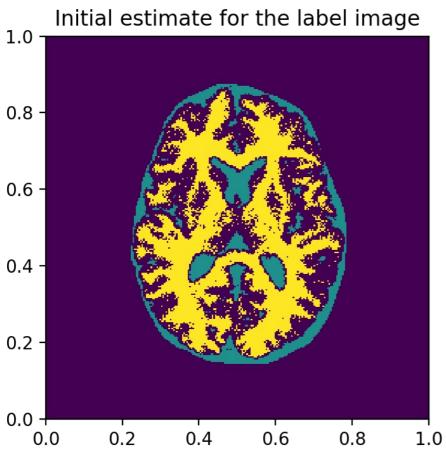
```
Modified ICM with beta = 2.000000
0 : Initial log posterior = 15919.907377
0 : Final log posterior = 18086.013949
1 : Initial log posterior = 18198.711865
1 : Final log posterior = 18697.549658
2 : Initial log posterior = 18714.199795
2 : Final log posterior = 18726.980467
3 : Initial log posterior = 18736.833042
3 : Final log posterior = 18746.036075
4 : Initial log posterior = 18756.510109
C:\ProgramData\Anaconda3\Scripts\pypublish:21: RuntimeWarning: invalid
value encountered in true_divide
4 : Final log posterior = 18630.244260
Modified ICM with beta = 0.000000
0 : Initial log posterior = 35901.907377
0 : Final log posterior = 36296.718625
1 : Initial log posterior = 36396.162509
1 : Final log posterior = 36546.829310
2 : Initial log posterior = 36503.007250
2 : Final log posterior = 36594.082126
3 : Initial log posterior = 36528.833496
3 : Final log posterior = 36585.329633
4 : Initial log posterior = 36497.443716
4 : Final log posterior = 36530.268448
5 : Initial log posterior = 36432.320468
5 : Final log posterior = 36455.949582
6 : Initial log posterior = 36360.936811
6 : Final log posterior = 36372.850988
7 : Initial log posterior = 36288.664975
7 : Final log posterior = 36295.230723
8 : Initial log posterior = 36229.516286
8 : Final log posterior = 36232.930293
9 : Initial log posterior = 36185.176518
9 : Final log posterior = 36186.652464
10 : Initial log posterior = 36153.920895
10 : Final log posterior = 36154.975846
11 : Initial log posterior = 36133.963296
```

```
11 : Final log posterior = 36134.595021
12 : Initial log posterior = 36121.520462
12 : Final log posterior = 36121.891785
13 : Initial log posterior = 36113.994770
13 : Final log posterior = 36114.276436
14 : Initial log posterior = 36109.663961
14 : Final log posterior = 36109.796252
15 : Initial log posterior = 36107.073517
15 : Final log posterior = 36107.148979
16 : Initial log posterior = 36105.570802
16 : Final log posterior = 36105.618037
17 : Initial log posterior = 36104.693355
17 : Final log posterior = 36104.707351
18 : Initial log posterior = 36104.151019
18 : Final log posterior = 36104.177058
19 : Initial log posterior = 36103.856528
19 : Final log posterior = 36103.858490
```

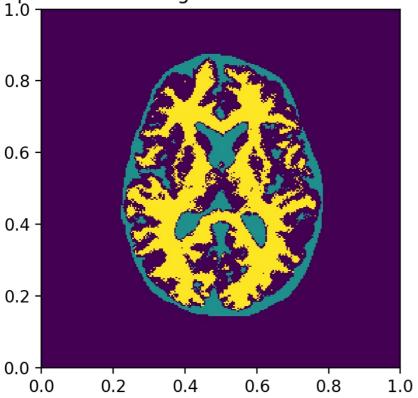
Images

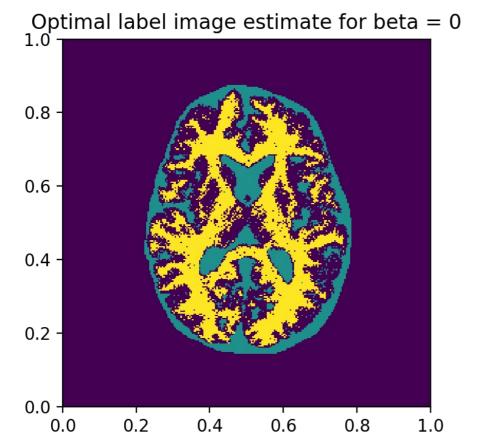
```
plt.figure()
plt.imshow(imageData, cmap=plt.cm.gray)
plt.title('Corrupted image')
plt.figure()
plt.imshow(initial_labels, extent=[0, 1, 0, 1])
plt.title('Initial estimate for the label image')
plt.figure()
plt.imshow(labels1, extent=[0, 1, 0, 1])
plt.title('Optimal label image estimate for beta = 2.0')
plt.figure()
plt.imshow(labels2, extent=[0, 1, 0, 1])
plt.title('Optimal label image estimate for beta = 0')
#Beta = 2.0
for i in range(K):
    seg = np.zeros((imageData.shape))
    seg[labels1==i] = imageData[labels1==i]
   plt.figure()
    plt.imshow(seg, cmap=plt.cm.gray)
    plt.title('Optimal class membership image estimate d for beta = 2.0'd(i+1))
\#Beta = 0
for i in range(K):
   seg = np.zeros((imageData.shape))
    seg[labels2==i] = imageData[labels2==i]
   plt.figure()
    plt.imshow(seg, cmap=plt.cm.gray)
    plt.title('Optimal class membership image estimate %d for beta = 0'%(i+1))
```





Optimal label image estimate for beta = 2.0





0.4

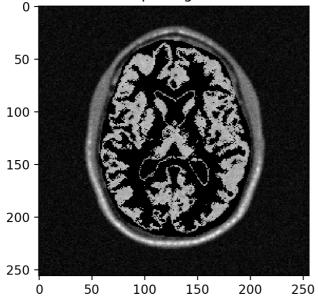
0.8

1.0

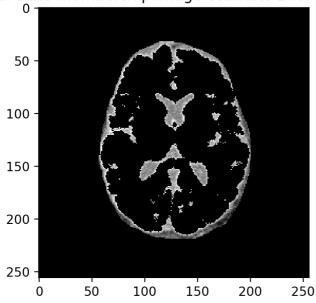
0.6

0.2

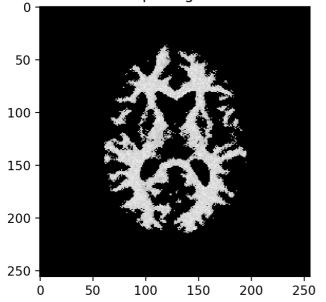
Optimal class membership image estimate 1 for beta = 2.0



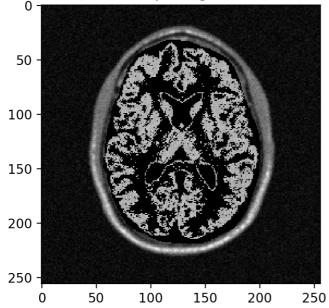
Optimal class membership image estimate 2 for beta = 2.0



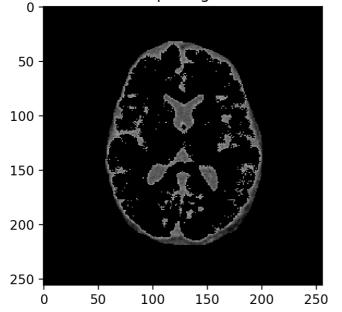
Optimal class membership image estimate 3 for beta = 2.0



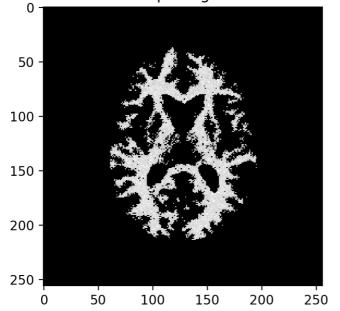
Optimal class membership image estimate 1 for beta = 0



Optimal class membership image estimate 2 for beta = 0



Optimal class membership image estimate 3 for beta = 0



Optimal Estimates

```
print('Initial class means are (%f, %f, %f)'%(means_init[0,0],means_init[1,0],means_init[2,0]))
print('For beta = 2.0, optimal class means are (%f, %f, %f)'%(means1[0,0],means1[1,0],means1[2,0]))
print('For beta = 0, optimal class means are (%f, %f, %f)'%(means2[0,0],means2[1,0],means2[2,0]))
```

```
Initial class means are (0.504863, 0.269874, 0.628400)

For beta = 2.0, optimal class means are (0.522365, 0.312841, 0.629673)

For beta = 0, optimal class means are (0.534559, 0.379461, 0.635745)
```

Published from g2.py using Pweave 0.30.3 on 23-03-2019.

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