## KNN Workbook for CS145 Homework 3

#### \*\*PRINT YOUR NAME AND UID HERE!\*\*

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Please follow the notebook linearly to implement k-nearest neighbors.

Please print out the workbook entirely when completed.

The goal of this workbook is to give you experience with the data, training and evaluating a simple classifier, k-fold cross validation, and as a Python refresher.

# Import the appropriate libraries

```
In [1]: import numpy as np # for doing most of our calculations
    import matplotlib.pyplot as plt# for plotting
    from cs145.data_utils import load_CIFAR10 # function to load the CIFAR-10 data
    set.

# Load matplotlib images inline
    %matplotlib inline

# These are important for reloading any code you write in external .py files.
    # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipyt
    hon
    %load_ext autoreload
    %autoreload 2
```

```
In [2]: # Set the path to the CIFAR-10 data
    cifar10_dir = './cs145/datasets/cifar-10-batches-py'
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test data.
    print('Training data shape: ', X_train.shape)
    print('Training labels shape: ', y_train.shape)
    print('Test data shape: ', X_test.shape)
    print('Test labels shape: ', y_test.shape)
Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
```

Test data shape: (10000, 32, 32, 3)

Test labels shape: (10000,)

```
In [3]: # Visualize some examples from the dataset.
        # We show a few examples of training images from each class.
        classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'shi
        p', 'truck']
        num_classes = len(classes)
        samples_per_class = 7
        for y, cls in enumerate(classes):
            idxs = np.flatnonzero(y train == y)
            idxs = np.random.choice(idxs, samples_per_class, replace=False)
            for i, idx in enumerate(idxs):
                plt_idx = i * num_classes + y + 1
                 plt.subplot(samples_per_class, num_classes, plt_idx)
                 plt.imshow(X_train[idx].astype('uint8'))
                 plt.axis('off')
                if i == 0:
                    plt.title(cls)
        plt.show()
```



```
In [4]: # Subsample the data for more efficient code execution in this exercise
    num_training = 5000
    mask = list(range(num_training))
    X_train = X_train[mask]
    y_train = y_train[mask]

    num_test = 500
    mask = list(range(num_test))
    X_test = X_test[mask]
    y_test = y_test[mask]

# Reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
    X_test = np.reshape(X_test, (X_test.shape[0], -1))
    print(X_train.shape, X_test.shape)
```

(5000, 3072) (500, 3072)

# K-nearest neighbors

In the following cells, you will build a KNN classifier and choose hyperparameters via k-fold cross-validation.

```
In [5]: # Import the KNN class
    from lib import KNN

In [6]: # Declare an instance of the knn class.
    knn = KNN()

# Train the classifier.
    # We have implemented the training of the KNN classifier.
    # Look at the train function in the KNN class to see what this does.
    knn.train(X=X_train, y=y_train)
```

#### **Questions**

- (1) Describe what is going on in the function knn.train().
- (2) What are the pros and cons of this training step of KNN?

#### **Answers**

- (1) Lazy Learning (instance-based learning): Simply stores training data and waits until given a test tuple.
- (2) Pros: Lazy Learning effectively uses a richer hypthesis space since it uses many local linear functions to form an implicit global approximation to the target function. On the other hand, Eager Learning must commit to a single hypothesis that covers the entire instance space and may therefore result in a less accurate classifier.

Cons: Lazy Learning takes up less time in training but more time in predicting/inference compared to Eager Learning.

# **KNN** prediction

In the following sections, you will implement the functions to calculate the distances of test points to training points, and from this information, predict the class of the KNN.

```
In [7]: # Implement the function compute_distances() in the KNN class.
# Do not worry about the input 'norm' for now; use the default definition of t
he norm
# in the code, which is the 2-norm.
# You should only have to fill out the clearly marked sections.

import time
time_start =time.time()

dists_L2 = knn.compute_distances(X=X_test)

print('Time to run code: {}'.format(time.time()-time_start))
print('Frobenius norm of L2 distances: {}'.format(np.linalg.norm(dists_L2, 'fro')))
```

Time to run code: 21.693020582199097 Frobenius norm of L2 distances: 7906696.077040902

### Really slow code

Note: This probably took a while. This is because we use two for loops. We could increase the speed via vectorization, removing the for loops. Normally it may takes 20-40 seconds.

If you implemented this correctly, evaluating np.linalg.norm(dists L2, 'fro') should return: ~7906696

#### KNN vectorization

The above code took far too long to run. If we wanted to optimize hyperparameters, it would be time-expensive. Thus, we will speed up the code by vectorizing it, removing the for loops.

```
In [9]: # Implement the function compute_L2_distances_vectorized() in the KNN class.
# In this function, you ought to achieve the same L2 distance but WITHOUT any
for Loops.
# Note, this is SPECIFIC for the L2 norm.

time_start =time.time()
dists_L2_vectorized = knn.compute_L2_distances_vectorized(X=X_test)
print('Time to run code: {}'.format(time.time()-time_start))
print('Difference in L2 distances between your KNN implementations (should be
0): {}'.format(np.linalg.norm(dists_L2 - dists_L2_vectorized, 'fro')))
Time to run code: 0.22140717506408691
Difference in L2 distances between your KNN implementations (should be 0): 0.
```

0

### **Speedup**

Depending on your computer speed, you should see a 20-100x speed up from vectorization and no difference in L2 distances between two implementations.

On our computer, the vectorized form took 0.20 seconds while the naive implementation took 26.88 seconds.

# Implementing the prediction

Now that we have functions to calculate the distances from a test point to given training points, we now implement the function that will predict the test point labels.

```
In [19]: # Implement the function predict labels in the KNN class.
      # Calculate the training error (num_incorrect / total_samples)
      # from running knn.predict labels with k=1
      error = 1
      # YOUR CODE HERE:
         Calculate the error rate by calling predict labels on the test
         data with k = 1. Store the error rate in the variable error.
      predictions = knn.predict_labels(dists_L2_vectorized, k=1)
      total_samples = len(predictions)
      num correct = np.count nonzero(predictions==y test)
      error = (total_samples - num_correct) / total_samples
      # ----- #
      # END YOUR CODE HERE
      print(error)
```

0.726

If you implemented this correctly, the error should be: 0.726. This means that the k-nearest neighbors classifier is right 27.4% of the time, which is not great.

# **Optimizing KNN hyperparameters**

In this section, we'll take the KNN classifier that you have constructed and perform cross-validation to choose a best value of k, as well as a best choice of norm.

### Create training and validation folds

First, we will create the training and validation folds for use in k-fold cross validation.

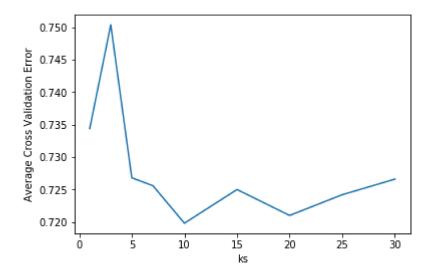
```
In [20]:
      # Create the dataset folds for cross-valdiation.
      num folds = 5
      X_train_folds = []
      y_train_folds = []
      # YOUR CODE HERE:
         Split the training data into num folds (i.e., 5) folds.
         X_train_folds is a list, where X_train_folds[i] contains the
      #
           data points in fold i.
         y train folds is also a list, where y train folds[i] contains
           the corresponding labels for the data in X_train_folds[i]
      X_train_folds = np.array_split(X_train, num_folds)
      y_train_folds = np.array_split(y_train, num_folds)
      # END YOUR CODE HERE
      X train folds = np.asarray(X train folds)
      y_train_folds = np.asarray(y_train_folds)
```

## Optimizing the number of nearest neighbors hyperparameter.

In this section, we select different numbers of nearest neighbors and assess which one has the lowest k-fold cross validation error.

```
In [28]: | time start = time.time()
        ks = [1, 3, 5, 7, 10, 15, 20, 25, 30]
        # YOUR CODE HERE:
           Calculate the cross-validation error for each k in ks, testing
           the trained model on each of the 5 folds. Average these errors
           together and make a plot of k vs. cross-validation error. Since
           we are assuming L2 distance here, please use the vectorized code!
           Otherwise, you might be waiting a long time.
        results = np.zeros(len(ks))
        # Your implementation
        for i,k in enumerate(ks):
           temp_results = []
           for fold_i in range(num_folds):
               # Partition data for cross-validation
              test_X = X_train_folds[fold_i]
              test_y = y_train_folds[fold_i]
               train X = np.concatenate(np.delete(X train folds, fold i, 0))
               train_y = np.concatenate(np.delete(y_train_folds, fold_i, 0))
               # Compute new L2 matrix and predictions
               new knn = KNN()
               new_knn.train(X=train_X, y=train_y)
               new dists = new knn.compute L2 distances vectorized(X=test X)
               new_preds = new_knn.predict_labels(new_dists, k=k)
               # Compute accuracy
               samples = len(new preds)
               corrects = np.count nonzero(new preds==test y)
               new error = (samples - corrects) / samples
               temp results.append(new error)
           results[i] = np.average(temp results)
        ks min = ks[np.argsort(results)[0]]
        results_min = min(results)
        print('Set k = {0} and get minimum error as {1}'.format(ks_min,results_min))
        # Plot of k vs. cross-validation error
        plt.plot(ks,results)
        plt.xlabel('ks')
        plt.ylabel('Average Cross Validation Error')
        plt.show()
        # END YOUR CODE HERE
        print('Computation time: %.2f'%(time.time()-time_start))
```

Set k = 10 and get minimum error as 0.7198



Computation time: 22.57

## **Questions:**

- (1) What value of k is best amongst the tested k's?
- (2) What is the cross-validation error for this value of k?

#### **Answers:**

- (1) k = 10 gave the best accuracy among the tested k's.
- (2) The cross-validation error for k = 10 is 0.7198.

# Evaluating the model on the testing dataset.

Now, given the optimal k and norm you found in earlier parts, evaluate the testing error of the k-nearest neighbors model.

```
In [29]:
      error = 1
      # YOUR CODE HERE:
        Evaluate the testing error of the k-nearest neighbors classifier
         for your optimal hyperparameters found by 5-fold cross-validation.
      opt knn = KNN()
      opt knn.train(X=X_train, y=y_train)
      opt_dists = opt_knn.compute_L2_distances_vectorized(X=X_test)
      opt_preds = opt_knn.predict_labels(opt_dists, k=ks_min)
      # Compute new accuracy
      opt_samples = len(opt_preds)
      opt_corrects = np.count_nonzero(opt_preds==y_test)
      error = (opt_samples - opt_corrects) / opt_samples
      # END YOUR CODE HERE
      print('Error rate achieved: {}'.format(error))
```

Error rate achieved: 0.718

### **Question:**

How much did your error improve by cross-validation over naively choosing k=1 and using the L2-norm?

### **Answer:**

Naive (k = 1, L2-norm): Error was 0.726.

Optimal (k = 10, L2-norm): Error is 0.718. There is an improvement of 0.008.

# The End of KNN Workbook

Please export this workbook as PDF file (see instructions) after completion.