Python 3 O

## **Optional Lab: Logistic Regression**

In this ungraded lab, you will

- explore the sigmoid function (also known as the logistic function)
- explore logistic regression; which uses the sigmoid function

# In [1]: import numpy as np %matplotlib widget import matplotlib.pyplot as plt from plt\_one\_addpt\_onclick import plt\_one\_addpt\_onclick from lab\_utils\_common import draw\_vthresh plt.style.use('./deeplearning.mplstyle')

#### **Sigmoid or Logistic Function**

As discussed in the lecture videos, for a classification task, we can start by using our linear regression model,  $f_{\mathbf{w},b}(\mathbf{x}^{(i)}) = \mathbf{w} \cdot \mathbf{x}^{(i)} + b$ , to predict y given x.

Want outputs between 0 and 1

1

0.5

3 sigmoid function logistic function

 However, we would like the predictions of our classification model to be between 0 and 1 since our output variable v is either 0 or 1.

This can be accomplished by using a "sigmoid function" which maps all input values to values between 0 and
 1.

Let's implement the sigmoid function and see this for ourselves.

#### Formula for Sigmoid function

The formula for a sigmoid function is as follows -

$$g(z) = \frac{1}{1 + e^{-z}} \tag{1}$$

 $g(z) = \frac{1}{1 + e^{-z}} \quad 0 < g(z) < 1$ © DeepLearning.Al

outputs between 0 and 1

In the case of logistic regression, z (the input to the sigmoid function), is the output of a linear regression model.

- In the case of a single example, z is scalar.
- ullet in the case of multiple examples, z may be a vector consisting of  ${\it m}$  values, one for each example.
- The implementation of the sigmoid function should cover both of these potential input formats. Let's implement this in Python.

NumPy has a function called exp(), which offers a convenient way to calculate the exponential (  $e^z$ ) of all elements in the input array ( z ).

It also works with a single number as an input, as shown below.

The sigmoid function is implemented in python as shown in the cell below.

Let's see what the output of this function is for various value of  $\ z$ 

In [4]: # Generate an array of evenly spaced values between -10 and 10
z\_tmp = np.arange(-10,11)

```
# Use the function implemented above to get the sigmoid values
y = sigmoid(z_tmp)

# Code for pretty printing the two arrays next to each other
np.set_printoptions(precision=3)
print("Input (z), Output (sigmoid(z))")
print(np.c_[z_tmp, y])

Input (z), Output (sigmoid(z))
[[-1.000e+01 4.540e-05]
```

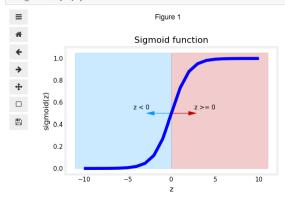
```
[[-1.000e+01 4.540e-05]
[-9.000e+00 1.234e-04]
 [-8.000e+00
              3.354e-04
 [-7.000e+00 9.111e-04]
 [-6.000e+00
              2.473e-03]
  -5.000e+00
              6.693e-03]
 [-4.000e+00 1.799e-02]
  -3.000e+00
  -2.000e+00
              1.192e-01
  -1.000e+00
              2.689e-01]
   0.000e+00
              5.000e-01]
   1.000e+00
              7.311e-01]
   2.000e+00
              8.808e-01]
   3.000e+00
              9.526e-01]
   4.000e+00
              9.820e-011
   5.000e+00
              9.933e-01]
   6.000e+00
              9.975e-01]
   7.000e+00
              9.991e-011
   8.000e+00
              9.997e-01]
   9.000e+00
              9.999e-01
 [ 1.000e+01 1.000e+00]]
```

The values in the left column are z, and the values in the right column are sigmoid(z). As you can see, the input values to the sigmoid range from -10 to 10, and the output values range from 0 to 1.

Now, let's try to plot this function using the matplotlib library.

```
In [5]: # Plot z vs sigmoid(z)
fig,ax = plt.subplots(1,1,figsize=(5,3))
ax.plot(z_tmp, y, c="b")

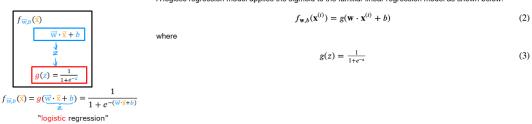
ax.set_title("Sigmoid function")
ax.set_ylabel('sigmoid(z)')
ax.set_xlabel('z')
draw_vthresh(ax,0)
```



As you can see, the sigmoid function approaches 0 as z goes to large negative values and approaches 1 as z goes to large positive values.

#### Logistic Regression

A logistic regression model applies the sigmoid to the familiar linear regression model as shown below:



Let's apply logistic regression to the categorical data example of tumor classification. First, load the examples and initial values for the parameters.

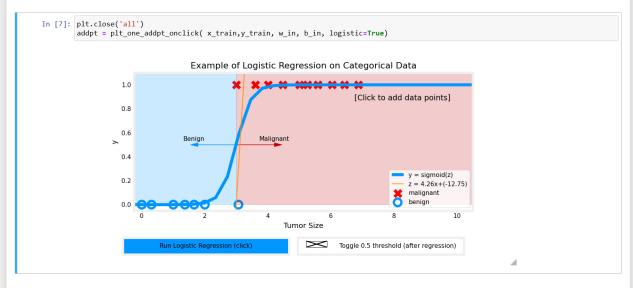
```
In [6]: x_train = np.array([0., 1, 2, 3, 4, 5])
y_train = np.array([0, 0, 0, 1, 1, 1])

w_in = np.zeros((1))
b_in = 0
```

Try the following steps:

Click on 'Run Logistic Regression' to find the best logistic regression model for the given training data

- Note the resulting model lits the data quite wei
- Note, the orange line is 'z' or w · x<sup>(i)</sup> + b above. It does not match the line in a linear regression model. Further improve these results by applying a
  threshold
- Tick the box on the 'Toggle 0.5 threshold' to show the predictions if a threshold is applied.
  - These predictions look good. The predictions match the data
  - Now, add further data points in the large tumor size range (near 10), and re-run logistic regression.
  - unlike the linear regression model, this model continues to make correct predictions



### Congratulations!

You have explored the use of the sigmoid function in logistic regression.

In [ ]: