

Cell Kernel Widgets





# **Optional Lab: Cost Function for Logistic Regression**

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#### Goals

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In this lab, you will:

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· examine the implementation and utilize the cost function for logistic regression.

```
In [1]: import numpy as np
%matplotlib widget
             import matplotlib.pyplot as plt
            from lab_utils_common import plot_data, sigmoid, dlc
plt.style.use('./deeplearning.mplstyle')
```

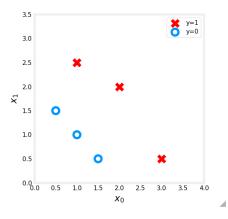
## **Dataset**

Let's start with the same dataset as was used in the decision boundary lab.

```
In [2]: X_train = np.array([[0.5, 1.5], [1,1], [1.5, 0.5], [3, 0.5], [2, 2], [1, 2.5]]) #(m,n)
y_train = np.array([0, 0, 0, 1, 1, 1]) #(m,)
```

We will use a helper function to plot this data. The data points with label y=1 are shown as red crosses, while the data points with label y=0 are shown as

```
In [3]: fig,ax = plt.subplots(1,1,figsize=(4,4))
              plot_data(X_train, y_train, ax)
             # Set both axes to be from 0-4
ax.axis([0, 4, 0, 3.5])
ax.set_ylabel('$x_1$', fontsize=12)
ax.set_xlabel('$x_0$', fontsize=12)
              plt.show()
```



### **Cost function**

In a previous lab, you developed the logistic loss function. Recall, loss is defined to apply to one example. Here you combine the losses to form the cost, which includes all the examples.

Recall that for logistic regression, the cost function is of the form

$$J(\mathbf{w}, b) = \frac{1}{m} \sum_{i=0}^{m-1} \left[ loss(f_{\mathbf{w}, b}(\mathbf{x}^{(i)}), \mathbf{y}^{(i)}) \right]$$
 (1)

•  $loss(f_{\mathbf{w},b}(\mathbf{x}^{(i)}), y^{(i)})$  is the cost for a single data point, which is:

$$loss(f_{\mathbf{w},b}(\mathbf{x}^{(i)}), y^{(i)}) = -y^{(i)} \log(f_{\mathbf{w},b}(\mathbf{x}^{(i)})) - (1 - y^{(i)}) \log(1 - f_{\mathbf{w},b}(\mathbf{x}^{(i)}))$$
(2)

• where m is the number of training examples in the data set and:

$$f_{\mathbf{w},b}(\mathbf{x}^{(\mathbf{i})}) = g(z^{(i)}) \tag{3}$$

$$z^{(i)} = \mathbf{w} \cdot \mathbf{x}^{(i)} + b \tag{4}$$

$$z^{(i)} = \mathbf{w} \cdot \mathbf{x}^{(i)} + b \tag{4}$$

$$g(z^{(i)}) = \frac{1}{1 + e^{-z^{(i)}}} \tag{5}$$

#### **Code Description**

The algorithm for <code>compute\_cost\_logistic</code> loops over all the examples calculating the loss for each example and accumulating the total.

Note that the variables X and y are not scalar values but matrices of shape (m, n) and (m, n) respectively, where n is the number of features and m is the number of training examples.

```
In [4]: def compute_cost_logistic(X, y, w, b):
    """
    Computes cost

Args:
    X (ndarray (m,n)): Data, m examples with n features
    y (ndarray (m,)): target values
    w (ndarray (n,)): model parameters
    b (scalar): model parameter

Returns:
    cost (scalar): cost
"""

m = X.shape[0]
    cost = 0.0
    for i in range(m):
        z_i = np.dot(X[i],w) + b
        f_wb_i = sigmoid(z_i)
        cost + = -y[i]*np.log(f_wb_i) - (1-y[i])*np.log(1-f_wb_i)

cost = cost / m
    return cost
```

Check the implementation of the cost function using the cell below.

```
In [5]: w_tmp = np.array([1,1])
b_tmp = -3
print(compute_cost_logistic(X_train, y_train, w_tmp, b_tmp))

0.36686678640551745
```

**Expected output**: 0.3668667864055175

#### **Example**

Now, let's see what the cost function output is for a different value of w.

- In a previous lab, you plotted the decision boundary for b=-3,  $w_0=1$ ,  $w_1=1$ . That is, you had b=-3, w=np.array([1,1]).
- Let's say you want to see if b=-4,  $w_0=1$ ,  $w_1=1$ , or b=-4, w=np.array([1,1]) provides a better model.

Let's first plot the decision boundary for these two different b values to see which one fits the data better

```
 \bullet \  \, \text{For} \, b=-3, w_0=1, w_1=1, \text{we'll plot} \, -3+x_0+x_1=0 \, \text{(shown in blue)} \\ \bullet \  \, \text{For} \, b=-4, w_0=1, w_1=1, \text{we'll plot} \, -4+x_0+x_1=0 \, \text{(shown in magenta)}
```

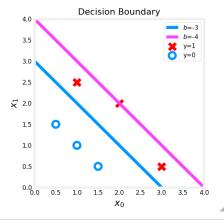
```
In [6]: import matplotlib.pyplot as plt

# Choose values between 0 and 6
x0 = np.arange(0,6)

# Plot the two decision boundaries
x1 = 3 - x0
x1_other = 4 - x0

fig,ax = plt.subplots(1, 1, figsize=(4,4))
# Plot the decision boundary
ax.plot(x0,x1, c=dlc["dlblue"], label="$b$=-3")
ax.plot(x0,x1, c=dlc["dlmagenta"], label="$b$=-4")
ax.axis([0, 4, 0, 4])

# Plot the original data
plot_data(X train,y_train,ax)
ax.axis([0, 4, 0, 4])
ax.set_ylabel('$x_0$', fontsize=12)
ax.set_ylabel('$x_0$', fontsize=12)
plt.legend(loc="upper right")
plt.title("Decision Boundary")
plt.show()
```



You can see from this plot that b = -4, w = np.array([1,1]) is a worse model for the training data. Let's see if the cost function implementation reflects this.