

```

%=====
%   Name:                hw5_2.m
%
%   Author:              Kairi Kozuma
%
%=====

% Points in the world
pwpts = [13.18000000000000,24.75000000000000,14.47000000000000,15.83000000000000,22.51000000000000,12.55000000000000;-3.36200000000000,-11.79000000000000,-9.1
sz = size(pwpts);
qwpts = [pwpts ; ones(1,sz(2))];

% Points in the image
rpts = [157,92,416,3,91,167;376,139,97,26,387,238;1,1,1,1,1,1];

% Get M matrix
M = calibrateM(qwpts, rpts);
fprintf('M matrix:\n');
disp(M);

% Test M matrix to see if original results obtained
test = (M * qwpts);
test = test./test(3,:);
fprintf('M * qwpts:\n');
disp(round(test(1:2,:)));

% F matrix
F = fliplr(eye(3));

% QR factorization
[Q U] = qr(F * (M(1:3,1:3))' * F);

% Obtain S matrix
S = diag(sign(diag(U)));

% Obtain R and K matrices
R_CW = (F * Q * S * F)';
K = (F * S * U * F)';

%trueK = K / K(3,3);

R_WC = R_CW';
N0 = M(1:3,end);
T_WC = -inv(M(1:3,1:3))* N0;
G_WC = [R_WC, T_WC; 0,0,0,1];
G_CW = inv(G_WC);
T_CW = G_CW(1:3,end);
psi = K;

disp('Psi matrix:');
disp(psi);

disp('D matrix R:');
disp(R_CW);

disp('D matrix T:');
disp(T_CW);

disp('Reconstruct M matrixM:');
M_new = [psi * R_CW, psi * T_CW];
disp(M_new);
disp(M);

%===== calibrateM =====
%
%   function [M] = calibrateM(qPts, rPts)
%
%
%   INPUT:
%       qPts - The points in world coordinates.
%       rPts - The image points (in ray form).
%
%===== calibrateM =====
function [M] = calibrateM(qPts, rPts)

%--(1) For each world point and image point pair, create the 2-row matrix,
%       and use them to create a master matrix.

sz = size(qPts);
masterMatrix = zeros(2*sz(2),2*sz(2));

for index = 1:sz(2)
    rmat = makeRMat(rPts(:,index));
    Qmat = makeQMat(qPts(:,index));
    mat = rmat * Qmat;
    index2 = 2*index;
    masterMatrix(index2:index2 + 1,:) = mat(1:2,:);
end

```

```

%--(2) Perform SVD using the master matrix and extract the projection
%      matrix. Be careful about rows versus columns ...

[UU SS VV] = svd(masterMatrix);
szvv = size(VV);

M = VV(:,szvv(2));

M = (reshape(M, 4, 3))';

end

%===== makeRMat =====
%
% function mat = makeRMat(vector)
%
%
% INPUT:
%   vector - 3 x 1 vector
%
%===== makeRMat =====
function mat = makeRMat(vector)
mat = [0, vector(3), -vector(2); -vector(3), 0, vector(1); vector(2), -vector(1), 0];
end

%===== makeQMat =====
%
% function mat = makeQMat(vector)
%
%
% INPUT:
%   vector - 4 x 1 vector
%
%===== makeQMat =====
function mat = makeQMat(qPts)
mat = [qPts',zeros(1,8); zeros(1,4), qPts', zeros(1,4);zeros(1,8), qPts'];
end

```

```

M matrix:
    -0.0331    0.0003    0.0937   -0.9567
    -0.0519   -0.0730    0.0127   -0.2581
    -0.0002    0.0000    0.0001    0.0002

```

```

M * qwpts:
    157    92    416     3    91    167
    376   139    97    26   387    238

```

```

Psi matrix:
    0.0776    0.0000    0.0621
         0    0.0776    0.0466
         0         0    0.0002

```

```

D matrix R:
    0.3255   -0.0669    0.9432
   -0.1056   -0.9938   -0.0340
   -0.9396    0.0886    0.3306

```

```

D matrix T:
  -13.2727
   -4.0327
    1.1779

```

```

Reconstruct M matrixM:
    -0.0331    0.0003    0.0937   -0.9567
    -0.0519   -0.0730    0.0127   -0.2581
    -0.0002    0.0000    0.0001    0.0002

    -0.0331    0.0003    0.0937   -0.9567
    -0.0519   -0.0730    0.0127   -0.2581
    -0.0002    0.0000    0.0001    0.0002

```