# Code Transformation for Distributed Python ML Code

## 1 Python Abstract Syntax

```
stmt^* type\_ignore
                                                                                 (ModuleDef)
module
         ::=
              (@expr)^* def id (args) (-> expr)? : (#type:s)? stmt^*
                                                                                 (FunDef)
stmt
              (@expr)^* async def id (args) (\rightarrow expr)? : (\#type:s)? stmt^*
                                                                                 (AsyncFunDef)
              (@expr)^* class id (expr^* keyword^*) : stmt^*
                                                                                 (ClassDef)
             return expr?
                                                                                 (Return)
             delete expr^*
                                                                                 (Delete)
             expr^* = expr (\#type:s)?
                                                                                 (Assign)
              expr \ binop = \ expr
                                                                                 (Augassign)
             expr : expr (= expr)?
                                                                                 (AnnAssign)
              (#type:s)? for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (FORLOOP)
              (#type:s)? async for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (AsyncForLoop)
             while (expr) : stmt^* (else : stmt^*)?
                                                                                 (WHILELOOP)
              if (expr) : stmt^* (else : stmt^*)?
                                                                                 (IF)
              (#type:s)? with with\_item^* : stmt^*
                                                                                 (WITH)
             (#type:s)? async with with_{-}item^* : stmt^*
                                                                                 (AsyncWith)
             match expr : match\_case^*
                                                                                 (Match)
             raise expr? (from expr)?
                                                                                 (Raise)
             try : stmt^* exc\_handler^* (else : stmt^*)? (finally : stmt^*)?
                                                                                 (TRY)
              assert expr expr?
                                                                                 (Assert)
              import alias^*
                                                                                 (Import)
             from i\ id? import alias^*
                                                                                 (IMPORTFROM)
              global id^*
                                                                                 (GLOBAL)
             nonlocal id^*
                                                                                 (NonLocal)
                                                                                 (EXPRSTMT)
              expr
             pass
                                                                                 (Pass)
                                                                                 (Break)
             break
                                                                                 (CONTINUE)
              continue
```

```
(BOOLOP)
                     expr boolop expr
expr
                ::=
                     expr :=
                              expr
                                                                                         (NAMEDEXPR)
                     expr binop expr
                                                                                         (BINARYOP)
                                                                                         (UNARYOP)
                     unop expr
                     lambda args : expr
                                                                                         (LAMBDA)
                                                                                         (IFEXPR)
                     expr if expr else expr
                     \{(expr : expr)^* (**expr)^*\}
                                                                                         (DICTIONARY)
                     \{expr^*\}
                                                                                         (Set)
                      [expr^*]
                                                                                         (List)
                      (expr^*)
                                                                                         (Tuple)
                     \{expr: expr comprehension^*\}
                                                                                         (DICTIONARY COMP)
                      \{expr \ comprehension^*\}
                                                                                         (SetComp)
                      [expr comprehension^*]
                                                                                         (LISTCOMP)
                      (expr \ comprehension^*)
                                                                                         (GENERATORCOMP)
                     await expr
                                                                                         (AWAIT)
                     yield expr?
                                                                                         (Yield)
                                                                                         (YIELDFROM)
                     yield from expr
                     expr (compop \ expr)^*
                                                                                         (COMPOP)
                     expr (expr^* keyword^*)
                                                                                         (Call)
                     \{expr (!i)? (:expr)?\}
                                                                                         (FORMATTED VALUE
                     expr^*
                                                                                         (JoinedStr)
                     constant
                                                                                         (Constant)
                     expr.id
                                                                                         (Attribute)
                     expr[expr]
                                                                                         (Subscript)
                     *expr
                                                                                         (Starred)
                     **expr
                                                                                         (DoubleStarred)
                                                                                         (NAME)
                     expr? (:expr)? (:expr)?
                                                                                         (SLICE)
                     and | or
                                                                                         (BOOLOPERATOR)
boolop
                ::=
binop
                     + | - | * | @ | / | ** | << | >> | | | ^ | & | // | %
                                                                                         (BINOPERATOR)
                ::=
unop
                ::=
                     \sim | not | + | -
                                                                                         (Unoperator)
                     == | != | < | <= | > | >= | is | is not | in | not in
compop
                ::=
                                                                                         (COMPOPERATOR)
comprehension
                     for expr in expr (if expr)*
                                                                                         (Comprehension)
                ::=
                     async for expr in expr (if expr)*
                                                                                         (ASYNCCOMPREHEN
                     except expr? (as id)? : stmt*
exc\_handler
                                                                                         (EXCHANDLER)
                ::=
args
                     (arg (= expr)?)^*, (arg (= expr)?)^*, arg?, (arg (= expr)?)^*, arg?
                                                                                         (Arguments)
                ::=
arg
                ::=
                     id expr? s?
                                                                                         (Argument)
keyword
                     id? = expr
                                                                                         (Keyword)
                ::=
                     id (.id)^* (as id)?
alias
                                                                                         (ALIAS)
                ::=
with\_item
                     expr (as expr)?
                                                                                         (WITHITEM)
                ::=
```

```
case pattern (if expr)? : stmt^*
                                                       (MATCHCASE)
match\_case
             ::=
pattern
             ::=
                  expr
                                                       (MATCHVALUE)
                  constant
                                                       (MATCHSINGLETON)
                                                       (MATCHSEQUENCE)
                  [pattern*]
                  *(id)?
                                                       (MATCHSTAR)
                  \{(expr: pattern)^* id?\}
                                                       (MATCHMAPPING)
                  expr (pattern^* (id = pattern)*)
                                                       (MATCHCLASS)
                  (pattern as)? id
                                                       (MatchAs)
                  pattern | pattern
                                                       (MATCHOR)
                                                       (MATCHWILDCARD)
                                                       (NoneLiteral)
constant
             ::=
                  None
                                                       (IntLiteral)
                  i
                                                       (FLOATLITERAL)
                  c
                                                       (ComplexLiteral)
                                                       (STRINGLITERAL)
                                                       (BOOLEANLITERAL)
                  (constant^*)
                                                       (TupleLiteral)
                                                       (Ellipsis)
                  i^*
                                                       (TypeIgnore)
type\_ignore
             ::=
                  Id
id
              \in
              \in
                  Str
s
                  {True, False}
              \in
i
              \in
                  \mathbb{Z}
f
              \in \mathbb{R}
                  \mathbb{C}
c
              \in
```

Note: there may be more constant terms such as an immutable container containing only constant elements. Please update the constant rule if you know such terms.

## 2 Transformation Rule for TensorFlow ML Training Code

#### 2.1 Restrictions

- 1. All import statements must be placed at the top of a module.
- 2. The tensorflow module must be assigned to a variable only using an import statement.
- 3. Members of the tensorflow module must not be aliased.
- 4. print function call expressions must not introduce side-effects.
- 5. A dataset and an optimizer object must only be created once via an assignment statement with a function call expression and must not be aliased.
- 6. Variables storing a dataset or a optimizer object must not be reassigned to store another value that is not a dataset or an optimizer object.
- 7. A dataset and an optimizer object must not be created conditionally.
- 8. optimizer.apply\_gradients function call expressions must be expression statements or a direct RHS of an assignment statement.
- 9. Global variables storing an optimizer object and referred in functions must be defined before the functions' definitions and must not be changed after their initializations.
- 10. A checkpoint object must only be created once via an assignment statement with a function call expression and must not be aliased.

## 2.2 Rules

#### 2.2.1 Types and Auxiliary Functions

```
\tau ::=
        Module
                         (Modules)
        Stmt
                         (STATEMENTS)
        Expr
                         (Expressions)
        Comprehension
                         (Comprehensions)
        ExcHandler
                         (EXCEPTION HANDLERS)
        Alias
                         (ALIASES)
        With Item
                         (WITHITEMS)
        Pattern
                         (Patterns)
        Id
                         (IDENTIFIERS)
        Str
                         (STRINGS)
        \tau list
                         (List of elements typed \tau)
```

 $\sigma \in \Sigma = Str^{\text{fin}} Id$  Environment storing mappings from strings to identifiers

```
._1 : \tau \times \tau \to \tau Get the first element of the given pair
```

 $au : au o au ext{ list } o au ext{ list } ext{Append an element to a list (right-associative)}$ 

<:  $Expr \times Expr \rightarrow \mathbb{B}$  Whether classes specified by the expressions are subclasses

#### 2.3 Rule: TensorFlow 2.x Keras API Pattern

#### 2.3.1 Transformation Rules

```
trans_M: Module \rightarrow Module
 trans_{M}[stmt^{*} type\_ignore] = trans_{\overline{S}}[stmt^{*}](\sigma)._{1} type\_ignore
  trans_{\overline{S}}: Stmt list \rightarrow \Sigma \rightarrow (Stmt list \times \Sigma)
 trans_{\overline{S}}[\![\![stmt_1 \quad stmt_2 \dots stmt_n \ ]\!](\sigma) = \mathbf{LET} \quad stmt_1^{*\prime}, \sigma_1 = trans_S[\![\![stmt_1 \ ]\!](\sigma) \mathbf{IN}
                                                          LET stmt_2^{*\prime}, \sigma_2 = trans_S[stmt_2](\sigma_1) IN
                                                          LET stmt_n^{*\prime}, \sigma_n = trans_S[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                          (stmt_1^{*\prime} \otimes stmt_2^{*\prime} \otimes ... \otimes stmt_n^{*\prime}, \sigma_n)
  trans_S: Stmt \rightarrow \Sigma \rightarrow (Stmt \ \textbf{list} \times \Sigma)
 trans_S \llbracket (@expr_1)^* \text{ def } id \text{ (args)} \pmod{-} expr_2 : (\#type:s)? stmt^* \llbracket (\sigma) = expr_2 :
      ([(@expr_1)^* def id (args) (-> expr_2)? : (\#type:s)? trans_{\overline{s}}[[stmt^*]](\sigma)._1], \sigma)
 trans_S[(@expr_1)^*] async def id (args) (-> expr_2)? : (#type:s)? stmt^*[(\sigma) =
      ([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1], \sigma)
 trans_S[(@expr_1)^* \ class \ id \ (expr_2^* \ keyword^*) : stmt^*](\sigma) =
      ([(@expr_1)^* \text{ class } id \text{ } (expr_2^* \text{ } keyword^*) \text{ } : \text{ } trans_{\overline{S}}[[stmt^*]](\sigma).\_1], \sigma) =
 trans_S[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_E[\![ expr \ ]\!](\sigma))?], \sigma)
 trans_S[\![ delete expr^* \![](\sigma) = ([delete expr^*\!], \sigma)
A strict form of assignment statements
 trans_S \llbracket id_r = expr_1 \text{ (}expr_{11} \dots expr_{1n} \text{ (}id_1 = \text{)? }expr_{21} \dots \text{ (}id_k = \text{)? }expr_{2k} \text{) (#type:s)? } \rrbracket(\sigma) =
      # Learning rate scheduler scaling
      IF expr<sub>1</sub> <: "tensorflow.keras.optimizers.schedules.PiecewiseConstantDecay" THEN
          ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
               \sigma["lr_scheduler" \mapsto id_r])
      {f ELIF} expr_1<: tensorflow.keras.optimizers.schedules.LearningRateSchedule {f THEN}
          IF id_i = initial_learning_rate WHEN 1 \le i \le k THEN
               ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
                   ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
          ELSE
               ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                   \sigma[\text{"lr\_scheduler"} \mapsto id_r])
      ELIF expr1 <: tensorflow.compat.v1.train.exponential_decay THEN
          IF id_i = learning_rate WHEN 1 \le i \le k THEN
               ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
                   ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler" \mapsto id_r])
```

```
ELSE
              ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                  \sigma["lr_scheduler" \mapsto id_r])
      # Optimizer learning rate scaling and wrapping
     ELIF expr<sub>1</sub> <: tensorflow.keras.optimizers.Optimizer THEN
          IF id_i = learning_rate WHEN 1 \le i \le k THEN
              ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
                  ... (id_k = )? expr_{2k}) (#type:s)?
              id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
          ELSE
              ([id_r = expr_1 (expr_{11} * hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (#type:s)?,
              id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
      # Model related
     ELIF expr_1 <: tensorflow.keras.Model THEN
          ([id_r = expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_2 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k})], \ \sigma[\text{``model''} \mapsto id_r])
      ELIF id_m = "model" AND expr_1 = id_t.evaluate THEN
          IF id_i = verbose WHEN 1 \le i \le k THEN
              ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = 1 if hvd.rank() == 0 else 0
                  ... (id_k = )? expr_{2k}) (#type:s)?], \sigma)
          ELSE
              ([id_r = expr_1 (expr_{11} \ expr_{12} \ 1 \ if \ hvd.rank() == 0 \ else \ 0 \dots \ expr_{1n})
                  (id_1 = )? \ expr_{21} \dots (id_k = )? \ expr_{2k}) \ (\#type:s)?], \ \sigma)
      # Checkpoint
      ELIF \sigma("tensor_flow") = id_t AND expr_1 = id_t.train.Checkpoint THEN
          ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma["checkpoint"\mapsto id_r])
      # Default
      ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
              \sigma)
 trans_{S} \llbracket expr_{0} = expr_{1} \text{ (#type:s)? } \rrbracket(\sigma) =
     IF \sigma(\text{``os''}) = id_{os} AND expr_0 = id_{os}.\text{environ [`CUDA_VISIBLE_DEVICES']}
     THEN ([], \sigma)
A general form of assignment statements except for the strict form
 trans_S \llbracket expr_1^* = expr_2 \text{ (#type:}s)? \rrbracket (\sigma) = ([expr_1^* = trans_E \llbracket expr_2 \rrbracket (\sigma) \text{ (#type:}s)?], \sigma)
 trans_S \llbracket expr_1 \ binop = expr_2 \ \rrbracket(\sigma) = ([expr_1 \ binop = trans_E \llbracket \ expr_2 \ \rrbracket(\sigma)], \ \sigma)
 trans_S \llbracket expr_1 : expr_2 (= expr_3)? \rrbracket (\sigma) = ([expr_1 : expr_2 (= trans_E \llbracket expr_3 \rrbracket (\sigma))?], \sigma)
 trans_S[\![ (\#type:s)? for \ expr_1 \ in \ expr_2 \ : \ stmt_1^* \ (else : \ stmt_2^*)? ]\!](\sigma) =
     ([(#type:s)? for expr_1 in trans_E[\![ expr_2 ]\!](\sigma) :
          trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
```

```
trans_S[ (#type:s)? async for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
    ([(#type:s)? async for expr_1 in trans_E[\![expr_2]\!](\sigma) :
        trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_{S}[ while (expr) : stmt_{1}^{*} (else : stmt_{2}^{*})? [(\sigma) =
    ([while (trans_{\overline{S}}[\![expr]\!](\sigma)) : trans_{\overline{S}}[\![stmt_1^*]\!](\sigma)._1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)._1)?], \sigma)
trans_{S}[\![ if (expr) : stmt^* (else : stmt^*)? ]\!](\sigma) =
    ([\texttt{if} \ (trans_E[\![ \ expr \ ]\!](\sigma).\_1 \ (\texttt{else} \ : \ trans_{\overline{S}}[\![ \ stmt^* \ ]\!](\sigma).\_1)?], \ \sigma)
trans_S[\![ (#type:s)? with with\_item^* : stmt^*[\!](\sigma) = ([(#type:<math>s)? with with\_item^{*\prime} : stmt^{*\prime}[\!], \sigma_2)
trans_{S}[ (\#type:s)?  async with with\_item^* : stmt^* ](\sigma) =
    ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
    ([match trans_E[\![expr]\!](\sigma) : (trans_C[\![match\_case]\!](\sigma))^*], \sigma)
trans_S[ raise expr_1? (from expr_2)? [(\sigma) = ([raise expr_1? (from <math>expr_2)?], \sigma)
trans_S[[ try : stmt_1^* | exc\_handler^* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
    ([try : trans_{\overline{S}} [stmt_1^*] (\sigma)._1 (trans_H [exc\_handler] (\sigma))^*
    (else : trans_{\overline{S}}[\![stmt_3^*]\!](\sigma)._1)? (finally : trans_{\overline{S}}[\![stmt_3^*]\!](\sigma)._1)?], \sigma)
trans_S[\![ assert expr_1 expr_2? [\![](\sigma) = ([assert trans_E[\![ expr_1 ]\![](\sigma) expr_2?], \sigma)
trans_S[\![\!] import \ alias^* ]\![\![\!](\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
        ([import alias*,
        import horovod.tensorflow as hvd,
        hvd.init(),
        gpus = id.config.experimental.list_physical_devices('GPU'),
        for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
        if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
trans_S[\![from \ i \ id? \ import \ alias^*]\!](\sigma) = ([from \ i \ id? \ import \ alias^*], \sigma_1)
trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
trans_S[\![ nonlocal id^*]\![(\sigma) = ([nonlocal id^*], \sigma)]
```

#### A strict form of expr statements

```
trans_{S}[expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})](\sigma) =
    # Config
    IF id_t = \sigma(\text{"tensor\_flow"}) AND
        expr_1 = id_t.config.experimental.set_visible_devices THEN ([], <math>\sigma)
     # model.compile
    ELIF id_m = \sigma(\text{``model''}) AND expr_1 = id_m.compile THEN
        # string "adam" case
        IF id_i = optimizer WHEN 2 \le i \le k AND expr_{2i} = "adam" THEN
            ([optim = tf.optimizers.Adam(learning_rate=0.001 * hvd.size),
             optim = hvd.DistributedOptimizer(optim),
             expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i =  optim ... (id_k = )? expr_{2k}), \sigma)
        ELIF expr_{11} = "adam" THEN
            ([optim = tf.optimizers.Adam(learning_rate=0.001 * hvd.size),
             optim = hvd.DistributedOptimizer(optim),
             expr_1 (optim ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}), \sigma)
        ELSE
             [expr_1 \ (expr_{11} \ \dots \ expr_{1n} \ (id_1 = )? \ expr_{21} \ \dots \ (id_k = )? \ expr_{2k})], \sigma)
    # model.fit
    ELIF id_m = \sigma(\text{``model''}) AND expr_1 = id_m.\text{fit THEN}
        IF id_i = callbacks WHEN 2 \le i \le k THEN
           ([callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)],
             if hvd.rank() == 0: callbacks.append(expr_{2i}),
             expr_1 (optim ... expr_{1n} (id_1 = )? expr_{21} ... callbacks = callbacks ... (id_k = )? expr_{2k})], \sigma)
        ELSE
            ([callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)],
             expr_1 (optim ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}... callbacks = callbacks )], \sigma)
     # Root Rank Blocking
    ELIF id_m = \sigma(\text{``model''}) AND (expr_1 = id_m.\text{write OR})
        expr_1 = id_m.summary OR expr_1 = id_m.save\_weights OR
        expr_1 = expr.load_weights OR expr_1 = id_m.save) OR
        id_c = \sigma(\text{"checkpoint"}) \text{ AND } expr_1 = id_c.\text{save OR}
        id_t = \sigma(\text{"tensor\_flow"}) \text{ AND } expr_1 = id_t.\text{print OR}
        expr_1 = print THEN
           ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
    ELSE
        [trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma)], \sigma)
A general form of expr statements except for the strict form
 trans_{S}[\![expr]\!](\sigma) = ([trans_{E}[\![expr]\!](\sigma)], \sigma)
 trans_S[\![ pass \!]\!](\sigma)=([pass]\!],\sigma)
 trans_S[\![ break ]\!](\sigma) = ([break], \sigma)
```

```
trans_S[\![ continue ]\!](\sigma) = ([continue], \sigma)
   trans_E : Expr \rightarrow \Sigma \rightarrow Expr
trans_{E}[\![expr_{1} \ boolop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ boolop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E}[\![expr_{1} := expr_{2}]\!](\sigma) = expr_{1} := trans_{E}[\![expr_{2}]\!](\sigma)
trans_{E}[\![expr_{1} \ binop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ binop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_E \llbracket unop \ expr \ \rrbracket(\sigma) = unop \ trans_E \llbracket \ expr \ \rrbracket(\sigma)
trans_{\mathbb{F}}[\![ ] lambda args: expr[\![ ](\sigma) = ] lambda args: trans_{\mathbb{F}}[\![ ] expr[\![ ](\sigma) ]
trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
             trans_{E}[\![expr_{1}]\!](\sigma) if trans_{E}[\![expr_{2}]\!](\sigma) else trans_{E}[\![expr_{3}]\!](\sigma)
trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
             trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
trans_{E} \llbracket \{(expr_{1} : expr_{2})^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma) \} \| (expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \| (expr_{2} : trans_{E} : trans_{E} \rrbracket (\sigma))^{*}
trans_E[\![\{expr^*\}]\!](\sigma) = \{(trans_E[\![expr]\!](\sigma))^*\}
trans_E \llbracket [expr^*] \rrbracket (\sigma) = \llbracket (trans_E \llbracket expr \rrbracket (\sigma))^* \rrbracket
trans_E \llbracket (expr^*) \rrbracket (\sigma) = ((trans_E \llbracket expr \rrbracket (\sigma))^*)
trans_{E}[\![\{expr_1: expr_2: comprehension^*\}]\!](\sigma) = \{expr_1: trans_{E}[\![expr_2:]\!](\sigma) \mid (trans_{O}[\![comprehension]\!](\sigma))^*\}
trans_E[\![\{expr\ comprehension^*\}\]](\sigma) = \{trans_E[\![\ expr\]](\sigma)\ (trans_O[\![\ comprehension]\!](\sigma))^*\}
trans_E[\![expr\ comprehension^*]\!](\sigma) = [trans_E[\![expr\ ]\!](\sigma)\ (trans_C[\![comprehension]\!](\sigma))^*]
trans_{E}[\![ (expr\ comprehension^*)\ ]\!](\sigma) = (trans_{E}[\![ expr\ ]\!](\sigma)\ (trans_{O}[\![ comprehension\ ]\!](\sigma))^*)
trans_E \llbracket await expr \rrbracket(\sigma) = await <math>trans_E \llbracket expr \rrbracket(\sigma)
trans_E yield expr? \ \|(\sigma) = \text{yield } (trans_E \ expr \ \|(\sigma))?
```

```
trans_E yield from expr \ \|(\sigma) =  yield from trans_E \ expr \ \|(\sigma) = 
trans_{E}[\![expr_{1}\ (compop\ expr_{2})^{*}\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)\ (compop\ trans_{E}[\![expr_{2}\ ]\!](\sigma))^{*}
trans_{E}[\![expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})]\!](\sigma) =
      trans_{E}[\![expr_{1}]\!](\sigma) (trans_{E}[\![expr_{11}]\!](\sigma) ... trans_{E}[\![expr_{1n}]\!](\sigma)
           (id_1 = )? trans_E \llbracket expr_{21} \rrbracket (\sigma) \dots (id_k = )? trans_E \llbracket expr_{2k} \rrbracket (\sigma))
trans_{E}[\![ \{expr_1
                             (!i)? (:expr_2)?} ](\sigma) = \{expr_1 \quad (!i)? (:expr_2)?}
trans_E \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_E \llbracket expr.id \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma)).id
trans_{E}[\![expr_{1}[expr_{2}]]\!](\sigma) = trans_{E}[\![expr_{1}]\!](\sigma)[trans_{E}[\![expr_{2}]]\!](\sigma)]
trans_E[\![ *expr ]\!](\sigma) = *expr
trans_E[\![ **expr ]\!](\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_E \llbracket expr_1? (:expr_2)? (:expr_3)? \rrbracket(\sigma) = trans_E \llbracket expr_1 \rrbracket(\sigma)? (:trans_E \llbracket expr_2 \rrbracket(\sigma))? (:trans_E \llbracket expr_3 \rrbracket(\sigma))?
                 : Comprehension \rightarrow \Sigma \rightarrow Comprehension
trans_O \llbracket for expr_1 in expr_2 (if expr_3)* \rrbracket (\sigma) = for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) (if trans_E \llbracket expr_3 \rrbracket (\sigma))*
                       ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma)._1
 trans_{\overline{A}}: Alias list \rightarrow \Sigma \rightarrow \Sigma
trans_{\overline{A}} \llbracket \ alias_1 \ \dots \ alias_{n-1} \ alias_n \ \rrbracket (\sigma) = trans_A \llbracket \ alias_n \ \rrbracket (trans_A \llbracket \ alias_{n-1} \ \rrbracket (\dots \ trans_A \llbracket \ alias_1 \ \rrbracket (\sigma)))
 trans_A
              : Alias \rightarrow
                                           \Sigma \rightarrow
```

```
trans_A \llbracket id \rrbracket (\sigma) =
      LET id = \text{tensorflow THEN } \sigma[\text{"tensor\_flow"} \mapsto id]
      LET id = os THEN \sigma["os" \mapsto id]
      ELSE \sigma
trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
     LET id_1 = \text{tensorflow THEN } \sigma[\text{"tensor\_flow"} \mapsto id_2]
      LET id_1 = \text{os THEN } \sigma[\text{"os"} \mapsto id_2]
     ELSE \sigma
trans_A \llbracket id_1 . id_2 (.id_3)^* \text{ (as } id_2)? \rrbracket (\sigma) = \sigma
 trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow
                                                                          (WithItem list \times \Sigma)
trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
      LET with\_item_1', \sigma_1 = trans_W \llbracket with\_item_1 \rrbracket (\sigma) IN
     LET with\_item_2', \sigma_2 = trans_W \llbracket with\_item_2 \rrbracket (\sigma_1) IN
      LET with\_item_n', \sigma_n = trans_W[with\_item_n](\sigma_{n-1}) IN
      (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
 trans_W : WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
trans_W \llbracket expr \rrbracket(\sigma) = (trans_E \llbracket expr \rrbracket(\sigma), \sigma)
trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (smodenv) =
      (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
              : MatchCase \rightarrow \Sigma \rightarrow MatchCase
trans_{C}[\![ case pattern (if expr)? : stmt^* ]\!](\sigma) =
      case trans_{P}[\![pattern\ ]\!](\sigma) (if trans_{E}[\![expr\ ]\!](\sigma))? : trans_{\overline{S}}[\![stmt^*\ ]\!](\sigma)._1
 trans_P: Pattern \rightarrow \Sigma \rightarrow
                                                           Pattern
trans_P \llbracket expr \rrbracket (\sigma) = trans_E \llbracket expr \rrbracket (\sigma)
trans_P \llbracket constant \rrbracket (\sigma) = constant
trans_P \llbracket [pattern^*] \rrbracket (\sigma) = \llbracket trans_P \llbracket pattern \rrbracket (\sigma)^* \rrbracket
trans_P \llbracket *(id)? \rrbracket (\sigma) = *(id)?
trans_P \llbracket \{(expr : pattern)^* \ id?\} \rrbracket (\sigma) = \{(expr : trans_P \llbracket pattern \rrbracket (\sigma))^* \ id?\} \rrbracket
trans_P \llbracket expr \ (pattern_1^* \ (id = pattern_2)^*) \ \rrbracket (\sigma) = expr \ (trans_P \llbracket pattern_1 \rrbracket (\sigma)^* \ (id = trans_P \llbracket pattern_2 \rrbracket (\sigma))^*)
```

```
trans_{P} \llbracket \ (pattern \ as)? \ id \ \rrbracket (\sigma) = (trans_{P} \llbracket \ pattern \ \rrbracket (\sigma) \ as)? \ id trans_{P} \llbracket \ pattern_{1} \ \lVert \ pattern_{2} \ \rrbracket (\sigma) = trans_{P} \llbracket \ pattern_{1} \ \rrbracket (\sigma) \ | \ trans_{P} \llbracket \ pattern_{2} \ \rrbracket (\sigma) trans_{P} \llbracket \ \_ \ \rrbracket (\sigma) = \_
```

## 2.4 Rule: TensorFlow 2.x GradientTape API Pattern

### 2.4.1 Transformation Rules

```
: Module \rightarrow Module
trans_{M} \llbracket stmt^{*} type\_ignore \rrbracket = trans_{\overline{S}} \llbracket stmt^{*} \rrbracket (\sigma).\_1 type\_ignore
 trans_{\overline{S}}: Stmt list \rightarrow \Sigma \rightarrow (Stmt list \times \Sigma)
trans_{\overline{S}}[\![\!] stmt_1 \quad stmt_2 \dots stmt_n ]\![\![\!] (\sigma) = \mathbf{LET} \quad stmt_1^{*\prime}, \sigma_1 = trans_S[\![\!] stmt_1 ]\![\![\!] (\sigma) \mathbf{IN}
                                                                    LET stmt_2^{*\prime}, \sigma_2 = trans_S[stmt_2](\sigma_1) IN
                                                                    LET stmt_n^{*\prime}, \sigma_n = trans_S[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                                    (stmt_1^{*\prime} \otimes stmt_2^{*\prime} \otimes ... \otimes stmt_n^{*\prime}, \sigma_n)
 trans_S
              : Stmt \rightarrow
                                       \Sigma \rightarrow (Stmt \ \mathbf{list} \ \times )
                                                                                 \Sigma)
trans_S[\![ (@expr_1)^* \ def \ id \ (args) \ (-> expr_2)? \ : \ (\#type:s)? \ stmt^* ]\![ (\sigma) = (-> expr_2)? \ ]
     ([(@expr_1)^* \ def \ id \ (args) \ (-> expr_2)? \ : (\#type:s)? \ trans_{\overline{S}}[[stmt^*]](\sigma).1], \sigma)
trans_S \llbracket (@expr_1)^*  async def id (args) (-> expr_2)? : (#type:s)? <math>stmt^* \llbracket (\sigma) =
     ([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[stmt^*](\sigma).1], \sigma)
trans_{S}[(@expr_{1})^{*} class id (expr_{2}^{*} keyword^{*}) : stmt^{*}](\sigma) =
     ([(@expr_1)^* \text{ class } id \text{ } (expr_2^* \text{ } keyword^*) \text{ } : \text{ } trans_{\overline{S}}[[stmt^*]](\sigma).\_1], \sigma) =
trans_S[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_E[\![ expr \ ]\!](\sigma))?], \sigma)
trans_S[\![ delete \ expr^* \ ]\!](\sigma) = ([delete \ expr^*], \sigma)
```

## A strict form of assignment statements

```
trans_{S} \llbracket id_{r} = expr_{1} \ (expr_{11} \dots expr_{1n} \quad (id_{1} = )? \ expr_{21} \dots (id_{k} = )? \ expr_{2k}) \ (\#\text{type}:s)? \ \rrbracket(\sigma) = \# \ Dataset
\textbf{IF} \ \sigma(\text{``tensor\_flow''}) = id_{t} \ \textbf{AND} \ expr_{1} = id_{t}. \texttt{data.Dataset}. expr_{3} \ \textbf{THEN}
([id_{r} = expr_{1} \ (expr_{11} \dots expr_{1n} \quad (id_{1} = )? \ expr_{21} \dots (id_{k} = )? \ expr_{2k}) \ (\#\text{type}:s)?],
\sigma[\text{``dataset''} \mapsto id_{r}])
\# \ Variable \ Broadcasting
```

```
ELIF \sigma("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
   IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
       LET id_z = \text{NewID}() IN
       ([id_z = expr_{2i},
       id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = id_z \dots (id_k = )? expr_{2k}) (#type:s)?,
       global hvd_broadcast_done,
       if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in <math>id_z], root\_rank=0),
           hvd.broadcast_variables(id_t.variables(), root_rank=0),
           hvd\_broadcast\_done = True ]], \sigma)
   ELSE
       LET id_z = \text{NewID}() IN
       ([id_z = expr_{11},
       id_r = expr_1 (id_z expr_{12} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k}) (#type:s)?,
       global hvd_broadcast_done,
       if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in <math>id_z], root\_rank=0),
           hvd.broadcast_variables(id_t.variables(), root_rank=0),
           hvd\_broadcast\_done = True | ], \sigma)
# Learning rate scheduler scaling
IF expr<sub>1</sub> <: "tensorflow.keras.optimizers.schedules.PiecewiseConstantDecay" THEN
    ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
       \sigma["lr_scheduler"\mapsto id_r])
{f ELIF} expr_1<: tensorflow.keras.optimizers.schedules.LearningRateSchedule {f THEN}
   IF id_i = initial_learning_rate WHEN 1 \le i \le k THEN
       ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
           ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
   ELSE
       ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
           \sigma["lr_scheduler" \mapsto id_r])
ELIF expr_1 <: tensorflow.compat.v1.train.exponential_decay THEN
   \mathbf{IF} \ \mathit{id}_i \ = \ \mathtt{learning\_rate} \ \ \mathbf{WHEN} \ 1 \leq i \leq k \ \ \mathbf{THEN}
       ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
           ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
   ELSE
       ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
           \sigma["lr_scheduler" \mapsto id_r])
# Optimizer learning rate scaling and wrapping
IF expr_1 <: tensorflow.keras.optimizers.Optimizer THEN
    ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
       \sigma["optimizer" \mapsto id_r])
# Model related
ELIF expr_1 <: tensorflow.keras.Model THEN
    ([id_r = expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_2 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k})], \ \sigma[\text{``model''} \mapsto id_r])
ELIF id_m = "model" AND expr_1 = id_t.evaluate THEN
   IF id_i = verbose WHEN 1 \le i \le k THEN
```

```
(id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = 1 \text{ if hvd.rank}) == 0 \text{ else } 0
                 ... (id_k = )? expr_{2k}) (#type:s)?], \sigma)
          ELSE
              ([id_r = expr_1 (expr_{11} \ expr_{12} \ 1 \ if \ hvd.rank() == 0 \ else \ 0 \dots \ expr_{1n})
                  (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) (\#type:s)?], \sigma)
      # Checkpoint
     ELIF \sigma("tensor_flow") = id_t AND expr_1 = id_t.train.Checkpoint THEN
          ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma["checkpoint"\mapsto id_r])
      # Default
     ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
              \sigma)
A general form of assignment statements except for the strict form
 trans_S[\![expr_1^* = expr_2 (\#type:s)?]\!](\sigma) =
     # CUDA Visible Devices
     IF \sigma(\text{"os"}) = id_{os} AND expr_0 = id_{os}.\text{environ} [\text{"CUDA_VISIBLE_DEVICES"}] THEN
         ([], \sigma)
     ELSE ([expr_1^* = trans_E \| expr_2 \| (\sigma) \text{ (#type:} s)?], \sigma)
 trans_S[\![expr_1\ binop = expr_2\ ]\!](\sigma) = ([expr_1\ binop = trans_E[\![expr_2\ ]\!](\sigma)], \sigma)
 trans_S \llbracket expr_1 : expr_2 (= expr_3)? \rrbracket (\sigma) =
     # Dataset
     IF expr_1 = id_1 AND \sigma("tensor_flow") = id_2
         AND expr_3 = id_2.data.Dataset.expr_4 (expr_5^* keyword^*) THEN
             ([expr_1: expr_2 = expr_3 (\#type:s)?], \sigma["dataset" \mapsto id_1])
     ELSE ([expr_1 : expr_2 (= trans_E [expr_3 ](\sigma))?], \sigma)
 trans_{S} (#type:s)? for expr_1 in expr_2: stmt_1^* (else: stmt_2^*)? ](\sigma) =
     # Adjust Steps
     IF \sigma(\text{"config"}) = id_c AND (expr_2 = \text{range}(id_c.\text{iterations\_per\_epoch}) OR
         expr_2 = tqdm(range(id_c.iterations\_per\_epoch))) THEN
             ([(#type:s)? for expr_1 in range(id_c.iterations_per_epoch // hvd.size()) :
                 trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
     ELSE ([(#type:s)? for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
```

```
trans_S[ (#type:s)? async for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
     # Adjust Steps
     IF \sigma(\text{"config"}) = id_c AND (expr_2 = \text{range}(id_c.\text{iterations\_per\_epoch}) OR
         expr_2 = tqdm(range(id_c.iterations\_per\_epoch))) THEN
              ([(#type:s)? async for expr_1 in range(id_c.iterations_per_epoch // hvd.size()) :
                   trans_{\overline{S}}[\![stmt_1^*]\!](\sigma)...1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)...1)?], \sigma)
    ELSE ([(#type:s)? async for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_{S} while (expr) : stmt_{1}^{*} (else : stmt_{2}^{*})? (\sigma) =
     (\llbracket \text{while } (trans_{\overline{E}} \llbracket \ expr \ \rrbracket(\sigma)) : trans_{\overline{S}} \llbracket \ stmt_1^* \ \rrbracket(\sigma).\_1 \ (\text{else} : trans_{\overline{S}} \llbracket \ stmt_2^* \ \rrbracket(\sigma).\_1)? \rrbracket, \sigma)
trans_S[\![ if (expr) : stmt^* (else : stmt^*)? [\![ [\![}(\sigma) ]
     ([\text{if } (trans_E[\![ expr ]\!](\sigma)) : trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1 (\text{else} : trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1)?], \sigma)
trans_S[ (\#type:s)? \text{ with } with\_item^* : stmt^* ][(\sigma) =
     LET with_item*', \sigma_1 = trans_{\overline{W}} [\![\![ with_item^* ]\!]](\sigma) IN
     LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}} [stmt^*](\sigma_1) IN
     # Wrapping Gradient Tape
     IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
         ([(\#type:s)? with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
     ELSE ([(#type:s)? with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[ (\#type:s)?  async with with\_item^* : stmt^* ](\sigma) =
     LET with\_item^{*\prime}, \sigma_1 = trans_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) IN
     LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}} [stmt^*](\sigma_1) IN
     # Wrapping Gradient Tape
     IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
         ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
     ELSE ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
     ([\mathtt{match}\ \mathit{trans}_E[\![\ \mathit{expr}\ ]\!](\sigma)\ :\ (\mathit{trans}_C[\![\mathit{match\_case}]\!](\sigma))^*],\,\sigma)
trans_S[ raise expr_1? (from expr_2)? [(\sigma) = ([raise expr_1? (from <math>expr_2)?], \sigma)
trans_S[ try : stmt_1^* exc_handler* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
     ([try : trans_{\overline{S}}[stmt_1^*](\sigma)._1 (trans_H[exc\_handler](\sigma))*
     (\texttt{else} \ : \ trans_{\overline{S}}[\![\ stmt_2^*\ ]\!](\sigma).\_1)? \quad (\texttt{finally} \ : \ trans_{\overline{S}}[\![\ stmt_3^*\ ]\!](\sigma).\_1)?], \ \sigma)
trans_{S} assert expr_{1} expr_{2}? \|(\sigma) = ([assert \ trans_{E} \| \ expr_{1} \ \|(\sigma) - expr_{2}?], \sigma)
```

```
trans_S import alias^* (\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    # import
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
       ([import alias*,
       import horovod.tensorflow as hvd,
       hvd_broadcast_done = False,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
 trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
 trans_S[\![ nonlocal id^*]\![(\sigma) = ([nonlocal <math>id^*], \sigma)
A strict form of expr statements
 trans_S[\![expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k})]\!](\sigma) =
     # Variable Broadcasting
    IF \sigma("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
        IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{2i},
            expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = id_z ... (id_k = )? expr_{2k}),
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
               hvd.broadcast_variables(id_t.variables(), root_rank=0),
               hvd\_broadcast\_done = True ]], \sigma)
        ELSE
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{11},
            expr_1 (id_z expr_{12} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}),
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
               hvd.broadcast_variables(id_t.variables(), root_rank=0),
               hvd\_broadcast\_done = True ]], \sigma)
     # Config
    IF id_t = \sigma(\text{"tensor\_flow"}) AND
        expr_1 = id_t.config.experimental.set_visible_devices THEN ([], \sigma)
     # Root Rank Blocking
     ELIF id_m = \sigma(\text{``model''}) AND (expr_1 = id_m.\text{write OR})
        expr_1 = id_m.summary OR expr_1 = id_m.save_weights OR
```

```
expr_1 = expr.load_weights OR expr_1 = id_m.save) OR
            id_c = \sigma(\text{"checkpoint"}) AND expr_1 = id_c.save OR
            id_t = \sigma(\text{"tensor\_flow"}) \text{ AND } expr_1 = id_t.\text{print OR}
            expr_1 = print THEN
                  ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
       ELSE
            [trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) \mid, \sigma)
A general form of expr statements except for the strict form
 trans_{S} \llbracket expr \rrbracket (\sigma) = ([trans_{E} \llbracket expr \rrbracket (\sigma)], \sigma)
 trans_S[\![ pass ]\!](\sigma) = ([pass], \sigma)
 trans_S[\![ break ]\!](\sigma) = ([break], \sigma)
 trans_S[\![ continue \![](\sigma) = ([continue], \sigma)
  trans_E : Expr \rightarrow \Sigma \rightarrow Expr
 trans_{E}[\![expr_{1} \ boolop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ boolop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
 trans_{E}[\![expr_{1} := expr_{2}]\!](\sigma) = expr_{1} := trans_{E}[\![expr_{2}]\!](\sigma)
 trans_{E}[\![expr_{1} \ binop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ binop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
 trans_{E} \llbracket unop \ expr \ \rrbracket(\sigma) = unop \ trans_{E} \llbracket \ expr \ \rrbracket(\sigma)
 trans_{E} \llbracket \text{ lambda } args : expr \ \rrbracket(\sigma) = \text{ lambda } args : trans_{E} \llbracket expr \ \rrbracket(\sigma)
 trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
       trans_{E}[\![ expr_{1} ]\!](\sigma) if trans_{E}[\![ expr_{2} ]\!](\sigma) else trans_{E}[\![ expr_{3} ]\!](\sigma)
 trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
       trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
 trans_{E}[\![\{(expr_{1}: expr_{2})^{*} \ (**expr_{3})^{*}\} ]\!](\sigma) = \{(expr_{1}: trans_{E}[\![expr_{2}]\!](\sigma))^{*} \ (**expr_{3})^{*}\}\}
 trans_E \llbracket \{expr^*\} \rrbracket (\sigma) = \{(trans_E \llbracket expr \rrbracket (\sigma))^*\}
 trans_E \llbracket [expr^*] \rrbracket (\sigma) = \llbracket (trans_E \llbracket expr \rrbracket (\sigma))^* \rrbracket
```

```
trans_E[\![ (expr^*) \ ]\!](\sigma) = ((trans_E[\![ expr \ ]\!](\sigma))^*)
trans_{\mathbb{E}}[\![expr_1:expr_2:comprehension^*]\!](\sigma) = \{expr_1:trans_{\mathbb{E}}[\![expr_2:]\!](\sigma) \ (trans_{\mathbb{E}}[\![comprehension]\!](\sigma))^*\}
trans_{E}[\![\{expr\ comprehension^*\}]\!](\sigma) = \{trans_{E}[\![\ expr\ ]\!](\sigma)\ (trans_{O}[\![comprehension]\!](\sigma))^*\}
trans_E[[expr \ comprehension^*]](\sigma) = [trans_E[\ expr \ ](\sigma) \ (trans_O[[comprehension]](\sigma))^*]
trans_{E} \llbracket (expr \ comprehension^*) \ \rrbracket (\sigma) = (trans_{E} \llbracket \ expr \ \rrbracket (\sigma) \ (trans_{O} \llbracket comprehension \rrbracket (\sigma))^*)
trans_{E}[\![ await \ expr \ ]\!](\sigma) = await \ trans_{E}[\![ \ expr \ ]\!](\sigma)
trans_E yield expr? \ \|(\sigma) = \text{yield } (trans_E \ expr \ \|(\sigma))?
trans_{E}[\![\!]] yield from expr[\![\!]](\sigma) = yield from trans_{E}[\![\!]] expr[\![\!]](\sigma)
trans_{E}[\![expr_{1}\ (compop\ expr_{2})^{*}\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)\ (compop\ trans_{E}[\![expr_{2}\ ]\!](\sigma))^{*}
trans_{E}[\![expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})]\!](\sigma) =
     # Adjust Steps
     IF \sigma("dataset") = id_t AND expr_1 = id_t.take THEN
          IF id_i = count WHEN 1 \le i \le k THEN
               expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} // hvd.size() ... (id_k = )? expr_{2k})
          ELSE
               expr_1 (expr_{11} // hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
     ELSE
          trans_{E}[\![expr_{1}]\!](\sigma) (trans_{E}[\![expr_{11}]\!](\sigma) ... trans_{E}[\![expr_{1n}]\!](\sigma)
               (id_1 = )? trans_E \llbracket expr_{21} \rrbracket (\sigma) \dots (id_k = )? trans_E \llbracket expr_{2k} \rrbracket (\sigma))
trans_{E}[\{expr_{1} \ (!i)? \ (:expr_{2})?\}][\sigma] = \{expr_{1} \ (!i)? \ (:expr_{2})?\}
trans_E \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_E \llbracket expr.id \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma)).id
trans_{E}[\![expr_{1}[expr_{2}]]\!](\sigma) = trans_{E}[\![expr_{1}]\!](\sigma)[trans_{E}[\![expr_{2}]]\!](\sigma)]
trans_E \llbracket *expr \rrbracket (\sigma) = *expr
```

```
trans_E[\![ **expr ]\!](\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_{E}[\![expr_{1}?\ (:expr_{2})?\ (:expr_{3})?\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)?\ (:trans_{E}[\![expr_{2}\ ]\!](\sigma))?\ (:trans_{E}[\![expr_{3}\ ]\!](\sigma))?
 trans_O: Comprehension \rightarrow \Sigma \rightarrow Comprehension
trans_O[\![\![ for \ expr_1 \ in \ expr_2 \ (if \ expr_3)^* \ ]\!](\sigma) = for \ expr_1 \ in \ trans_E[\![\![ \ expr_2 \ ]\!](\sigma) \ (if \ trans_E[\![\![ expr_3 \ ]\!](\sigma))^*
 trans_H : ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\_1
 trans_{\overline{A}} : Alias list \rightarrow \Sigma \rightarrow \overline{\Sigma}
trans_{\overline{A}} \llbracket \ alias_1 \ \dots \ alias_{n-1} \ alias_n \ \rrbracket(\sigma) = trans_A \llbracket \ alias_n \ \rrbracket(trans_A \llbracket \ alias_{n-1} \ \rrbracket(\dots \ trans_A \llbracket \ alias_1 \ \rrbracket(\sigma)))
 trans_A: Alias \rightarrow \Sigma \rightarrow
trans_A \llbracket id \rrbracket (\sigma) =
     LET id = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id]
     LET id = os THEN \sigma["os"\mapsto id]
     LET id = config THEN \sigma["config" \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
     LET id_1 = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id_2]
     LET id_1 = os THEN \sigma["os" \mapsto id_2]
     LET id = \text{config} THEN \sigma[\text{"config"} \mapsto id_2]
     ELSE \sigma
trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow (WithItem list \times \Sigma)
trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
     LET with_item<sub>1</sub>', \sigma_1 = trans_W \llbracket with_item_1 \rrbracket (\sigma) IN
     LET with\_item_2', \sigma_2 = trans_W \llbracket with\_item_2 \rrbracket (\sigma_1) IN
     LET with_item<sub>n</sub>', \sigma_n = trans_W \llbracket with_item_n \rrbracket (\sigma_{n-1}) IN
     (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
 trans_W
               : WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
```

 $trans_W \llbracket expr \rrbracket(\sigma) = (trans_E \llbracket expr \rrbracket(\sigma), \sigma)$ 

```
trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (smodenv) =
      IF \sigma("tensor_flow") = id_1 AND expr_1 = id_1.GradientTape() AND expr_2 = id_2 THEN
           (expr_1 \text{ as } expr_2, \sigma[\text{"gradient\_tape"} \mapsto id_2])
      ELSE (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
 trans_C : MatchCase \rightarrow \Sigma \rightarrow MatchCase
trans_{C}[\![ case pattern (if expr)? : stmt^{*}[\!](\sigma) =
      case trans_P \llbracket pattern \rrbracket (\sigma) (if trans_E \llbracket expr \rrbracket (\sigma))? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma)._1
 trans_P : Pattern \rightarrow \Sigma \rightarrow Pattern
trans_P \llbracket expr \rrbracket (\sigma) = trans_E \llbracket expr \rrbracket (\sigma)
trans_P \llbracket constant \rrbracket (\sigma) = constant
trans_P \llbracket [pattern^*] \rrbracket (\sigma) = \llbracket trans_P \llbracket pattern \rrbracket (\sigma)^* \rrbracket
trans_P \llbracket *(id)? \rrbracket (\sigma) = *(id)?
trans_P \llbracket \{(expr : pattern)^* \ id?\} \rrbracket (\sigma) = \{(expr : trans_P \llbracket pattern \rrbracket (\sigma))^* \ id?\} 
trans_P \llbracket expr \ (pattern_1^* \ (id = pattern_2)^*) \ \rrbracket(\sigma) = expr \ (trans_P \llbracket pattern_1 \rrbracket(\sigma)^* \ (id = trans_P \llbracket pattern_2 \rrbracket(\sigma))^*)
trans_P \llbracket (pattern \ as)? \ id \ \rrbracket(\sigma) = (trans_P \llbracket pattern \ \rrbracket(\sigma) \ as)? \ id
trans_P \llbracket pattern_1 \mid pattern_2 \rrbracket (\sigma) = trans_P \llbracket pattern_1 \rrbracket (\sigma) \mid trans_P \llbracket pattern_2 \rrbracket (\sigma)
trans_P[\![ \ \_ \ ]\!](\sigma) = \_
```

## 2.5 Rule: TensorFlow 1.x Mainscript API Pattern

#### 2.5.1 Transformation Rules

```
trans_{\overline{S}} \llbracket stmt_1 \quad stmt_2 \dots stmt_n \ \rrbracket(\sigma) = \mathbf{LET} \quad stmt_1^{*\prime}, \ \sigma_1 = trans_{\overline{S}} \llbracket stmt_1 \ \rrbracket(\sigma) \quad \mathbf{IN}
                                                            LET stmt_2^{*\prime}, \sigma_2 = trans_S[stmt_2](\sigma_1) IN
                                                            LET stmt_n^{*\prime}, \sigma_n = trans_S[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                            (stmt_1^{*\prime} \otimes stmt_2^{*\prime} \otimes ... \otimes stmt_n^{*\prime}, \sigma_n)
  trans_S: Stmt \rightarrow \Sigma \rightarrow (Stmt \ \textbf{list} \times \Sigma)
 trans_S \llbracket (@expr_1)^* \text{ def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } stmt^* \rrbracket (\sigma) =
      ([(@expr_1)^* \text{ def } id \text{ } (args) \text{ } (\rightarrow expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[[stmt^*]](\sigma).1], \sigma)
 trans_S \llbracket (@expr_1)^* \text{ async def } id (args) (-> expr_2)? : (\#type:s)? stmt^* \rrbracket (\sigma) =
      ([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[stmt^*](\sigma).1], \sigma)
 trans_{S}[(@expr_{1})^{*} class id (expr_{2}^{*} keyword^{*}) : stmt^{*}](\sigma) =
      ([(@expr_1)^* \ class \ id \ (expr_2^* \ keyword^*) : trans_{\overline{S}}[[stmt^*]](\sigma).1], \sigma) =
 trans_{S}[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_{E}[\![ expr \ ]\!](\sigma))?], \sigma)
 trans_S[\![ delete expr^* \![](\sigma) = ([delete expr^*\![], \sigma)
A strict form of assignment statements
 trans_{S}[id_{r} = expr_{1} (expr_{11} ... expr_{1j} (id_{11} = )? expr_{21} ... (id_{1k} = )? expr_{2k})]
      # Minimized Optimizer
      .id_m (expr_{31} ... expr_{3l} (id_{41} = )? expr_{41} ... (id_{4n} = )? expr_{4n}) (\#type:s)? ]](\sigma) =
          {f IF}\ expr_1 <: tensorflow.compat.v1.train.Optimizer AND id_m = minimize {f THEN}
               ([id_r = expr_1 (expr_{11} ... expr_{1j} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
                   ... (id_k = )? \ expr_{2k}).id_m \ (expr_{31} \ ... \ expr_{3l} \ (id_{41} = )? \ expr_{41} \ ... \ (id_{4n} = )? \ expr_{4n}) \ (\#type:s)?,
               id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
          ELSE
               ([id_r = expr_1 (expr_{11} * hvd.size() ... expr_{1j} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
                   .id_m (expr_{31} ... expr_{3l} (id_{41} = )? expr_{41} ... (id_{4n} = )? expr_{4n}) (#type:s)?,
               id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
 trans_S \llbracket id_r = expr_1 \text{ (}expr_{11} \dots expr_{1n} \text{ (}id_1 = \text{)? }expr_{21} \dots \text{ (}id_k = \text{)? }expr_{2k} \text{) (#type:s)? } \rrbracket(\sigma) =
      # Config Proto
      IF id_t = "tensor_flow" AND expr_1 = id_t.ConfigProto THEN
           (id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?,
               \sigma[id_r \mapsto \text{"config\_proto"}])
      # Learning rate scheduler scaling
      {f IF}\ expr_1<: "tensorflow.keras.optimizers.schedules.PiecewiseConstantDecay" {f THEN}
          ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
               \sigma["lr_scheduler"\mapsto id_r])
      {f ELIF} expr_1<: tensorflow.keras.optimizers.schedules.LearningRateSchedule {f THEN}
          IF id_i = initial_learning_rate WHEN 1 \le i \le k THEN
               ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
```

```
... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
         ELSE
             ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                 \sigma["lr_scheduler"\mapsto id_r])
     ELIF expr_1 <: tensorflow.compat.v1.train.exponential_decay THEN
         IF id_i = learning_rate WHEN 1 \le i \le k THEN
             ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
                 ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
         ELSE
             ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                 \sigma["lr_scheduler"\mapsto id_r])
      # Optimizer learning rate scaling and wrapping
     ELIF expr_1 <: tensorflow.keras.optimizers.Optimizer THEN
         IF id_i = learning_rate WHEN 1 \le i \le k THEN
             ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
                 ... (id_k = )? expr_{2k}) (#type:s)?
             id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
         ELSE
             ([id_r = expr_1 (expr_{11} * hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (#type:s)?,
             id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
     # Model related
     ELIF expr<sub>1</sub> <: tensorflow.keras.Model THEN
         ([id_r = expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_2 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k})], \ \sigma[\text{``model''} \mapsto id_r])
     ELIF id_m = "model" AND expr_1 = id_t.evaluate THEN
         IF id_i = verbose WHEN 1 \le i \le k THEN
             (id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = 1 \text{ if hvd.rank()} == 0 \text{ else } 0
                 ... (id_k = )? expr_{2k}) (#type:s)?], \sigma)
         ELSE
             ([id_r = expr_1 (expr_{11} expr_{12} 1 if hvd.rank() == 0 else 0 ... expr_{1n})
                 (id_1 = )? \ expr_{21} \dots (id_k = )? \ expr_{2k}) \ (\#type:s)?], \ \sigma)
      # Checkpoint
     ELIF \sigma("tensor_flow") = id_t AND expr_1 = id_t.train.Checkpoint THEN
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
             \sigma["checkpoint"\mapsto id_r])
     # Default
     ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
             \sigma)
 trans_S \llbracket expr_0 = expr_1 \text{ (#type:}s)? \rrbracket (\sigma) =
     IF \sigma(\text{``os''}) = id_{os} AND expr_0 = id_{os}.\text{environ [`CUDA_VISIBLE_DEVICES']}
     THEN ([], \sigma)
A general form of assignment statements except for the strict form
```

 $trans_S[\![expr_1^*]\!] = expr_2$  (#type:s)?  $[\![\sigma]\!] (\sigma) = ([expr_1^*]\!] = trans_E[\![expr_2]\!] (\sigma)$  (#type:s)?],  $\sigma$ )

```
trans_{S} \llbracket \ expr_{1} \ binop = \ expr_{2} \ \rrbracket(\sigma) = ([expr_{1} \ binop = \ trans_{E} \llbracket \ expr_{2} \ \rrbracket(\sigma)], \ \sigma)
trans_S \llbracket expr_1 : expr_2 (= expr_3)? \rrbracket (\sigma) = ([expr_1 : expr_2 (= trans_E \llbracket expr_3 \rrbracket (\sigma))?], \sigma)
trans_{S} \llbracket (\texttt{#type}:s)? \text{ for } expr_{1} \text{ in } expr_{2} : stmt_{1}^{*} \text{ (else } : stmt_{2}^{*})? \rrbracket (\sigma) =
    ([(#type:s)? for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_S[ (#type:s)? async for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
    ([(#type:s)? async for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_{S} while (expr) : stmt_{1}^{*} (else : stmt_{2}^{*})? (\sigma) =
    ([while (trans_{\overline{S}}[\![expr]\!](\sigma)) : trans_{\overline{S}}[\![stmt_1^*]\!](\sigma)._1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)._1)?], \sigma)
trans_{S}[\![ if (expr) : stmt^* (else : stmt^*)? ]\!](\sigma) =
    ([\text{if } (trans_E[\![ expr ]\!](\sigma)) : trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1 (\text{else} : trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1)?], \sigma)
trans_{S}[ (\#type:s)? with with_item^* : stmt^* ](\sigma) =
    IF "config_proto" \notin \sigma AND \sigma("tensor_flow_compat") = id_t THEN
         LET with_item*', \sigma_1 = trans_{\overline{W}} \llbracket with_item^* \rrbracket (\sigma) IN
         LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}}[stmt^*](\sigma_1) IN
         # Config
         IF \sigma_1 \setminus \sigma = [\text{"session"} \mapsto id] THEN
              ([config = id_t.ConfigProto()
              config.gpu_options.allow_growth = True
              config.gpu_options.visible_device_list = str(hvd.local_rank())
              (#type:s)? with with_item^{*\prime} : stmt^{*\prime}], \sigma_2),
    ELSE ([(#type:s)? with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![ (\#type:s)?  async with with\_item^* : stmt^* ]\!](\sigma) =
    ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
    ([match trans_E[\![expr]\!](\sigma) : (trans_C[\![match\_case]\!](\sigma))^*], \sigma)
trans_S[ raise expr_1? (from expr_2)? ](\sigma) = ([raise <math>expr_1? (from expr_2)?], \sigma)
trans_S[ try : stmt_1^* exc_handler* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
    ([try : trans_{\overline{S}}[stmt_1^*](\sigma)._1 (trans_H[exc\_handler](\sigma))*
    (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)? (finally : trans_{\overline{S}}[\![stmt_3^*]\!](\sigma).\_1)?], \sigma)
trans_S[\![ assert expr_1 expr_2? [\![(\sigma) = ([assert trans_E[\![ expr_1 ]\![(\sigma) expr_2?], \sigma)
```

```
trans_S[\![ import \ alias^* ]\!](\sigma) =
     IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow\_compat"} \mapsto id] THEN
        ([import alias*,
        import horovod.tensorflow as hvd,
        hvd.init(), \sigma_1
     ELSE ([import alias^*], \sigma_1)
 trans_S \llbracket \text{ from } i \text{ } id? \text{ import } alias^* \rrbracket (\sigma) = ([\text{from } i \text{ } id? \text{ import } alias^*], \sigma_1)
 trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
 trans_S[\![ nonlocal \ id^* \ ]\!](\sigma) = ([nonlocal \ id^*], \sigma)
A strict form of expr statements
 trans_S[\![expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k})]\!](\sigma) =
     # Config
    IF id_t = \sigma(\text{"tensor\_flow"}) AND
        expr_1 = id_t.config.experimental.set_visible_devices THEN ([], \sigma)
     # Root Rank Blocking
     ELIF id_m = \sigma(\text{``model''}) AND (expr_1 = id_m.\text{write OR})
        expr_1 = id_m.summary OR expr_1 = id_m.save_weights OR
        expr_1 = expr.load_weights OR expr_1 = id_m.save) OR
        id_c = \sigma ("checkpoint") AND expr_1 = id_c.save OR
        id_t = \sigma(\text{"tensor\_flow"}) AND expr_1 = id_t.print OR
        expr_1 = print THEN
            ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
     ELSE
         [trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) \mid, \sigma)
A general form of expr statements except for the strict form
 trans_S[\![expr]\!](\sigma) =
     # Variable Broadcasting
     IF \sigma("session") = id_s AND \sigma("tensor_flow_compat") = id_t AND
        expr = id_s.run(id_t.global\_variables\_initializer()) THEN
            ([expr,
            id_s.run(hvd.broadcast_global_variables(root_rank=0))], \sigma)
     ELIF \sigma("tensor_flow_compat") = id_t AND
        expr = id_t.global_variables_initializer().run() THEN
            ([expr,
            hvd.broadcast_global_variables(root_rank=0).run()], \sigma)
     ELSE ([trans_E \| expr \| (\sigma)], \sigma)
 trans_S[\![ pass \![](\sigma)=([pass],\sigma)
 trans_S[\![ break ]\!](\sigma) = ([break], \sigma)
```

```
trans_S[\![ continue ]\!](\sigma) = ([continue], \sigma)
trans_{\overline{E}}\llbracket \ expr_1 \quad expr_2 \ \dots \ expr_n \ \rrbracket(\sigma) = trans_E\llbracket \ expr_1 \ \rrbracket(\sigma) \quad trans_E\llbracket \ expr_2 \ \rrbracket(\sigma) \ \dots \ trans_E\llbracket \ expr_n \ \rrbracket(\sigma)
                 : Expr \rightarrow \Sigma \rightarrow Expr
trans_{E}[\![expr_{1} \ boolop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ boolop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E}[\![expr_{1} := expr_{2}]\!](\sigma) = expr_{1} := trans_{E}[\![expr_{2}]\!](\sigma)
trans_{E}[\![expr_{1} \ binop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ binop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E} \llbracket unop \ expr \ \rrbracket(\sigma) = unop \ trans_{E} \llbracket \ expr \ \rrbracket(\sigma)
trans_{\mathbb{F}}[\![ ] lambda args: expr[\![ ](\sigma) = ] lambda args: trans_{\mathbb{F}}[\![ ] expr[\![ ](\sigma) ]
trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
      trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
trans_{E}[\![ expr_{1} ]\!] if expr_{2}  else expr_{3}[\!] (\sigma) =
      trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
trans_{E} \llbracket \{(expr_{1} : expr_{2})^{*} \ (**expr_{3})^{*}\} \ \rrbracket(\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket(\sigma))^{*} \ (**expr_{3})^{*}\} \}
trans_E \llbracket \{expr^*\} \rrbracket (\sigma) = \{(trans_E \llbracket expr \rrbracket (\sigma))^*\}
trans_E \llbracket [expr^*] \rrbracket (\sigma) = \llbracket (trans_E \llbracket expr \rrbracket (\sigma))^* \rrbracket
trans_E \llbracket (expr^*) \rrbracket (\sigma) = ((trans_E \llbracket expr \rrbracket (\sigma))^*)
trans_{E}[\![\{expr_{1}: expr_{2} : comprehension^{*}\}]\!](\sigma) = \{expr_{1}: trans_{E}[\![\ expr_{2}]\!](\sigma) \mid (trans_{O}[\![\ comprehension]\!](\sigma))^{*}\}
trans_{E}[\![\{expr \ comprehension^*\}]\!](\sigma) = \{trans_{E}[\![\ expr \ ]\!](\sigma) \ (trans_{O}[\![comprehension]\!](\sigma))^*\}
trans_E[\![expr\ comprehension^*]\!](\sigma) = [trans_E[\![expr\ ]\!](\sigma)\ (trans_O[\![comprehension]\!](\sigma))^*]
trans_{E} \llbracket (expr \ comprehension^*) \ \rrbracket (\sigma) = (trans_{E} \llbracket \ expr \ \rrbracket (\sigma) \ (trans_{O} \llbracket comprehension \rrbracket (\sigma))^*)
trans_E \llbracket await expr \rrbracket(\sigma) = await <math>trans_E \llbracket expr \rrbracket(\sigma)
```

```
trans_E yield expr? \ \|(\sigma) = \text{yield } (trans_E \ expr \ \|(\sigma))?
trans_{E}[\![\!] yield from expr[\![\!](\sigma) = \text{yield from } trans_{E}[\![\!]\!] expr[\![\!](\sigma)
trans_{E}[\![expr_{1}\ (compop\ expr_{2})^{*}\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)\ (compop\ trans_{E}[\![expr_{2}\ ]\!](\sigma))^{*}
trans_{E}[\![expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})]\!](\sigma) =
      trans_{E}[\![expr_{1}]\!](\sigma) (trans_{E}[\![expr_{11}]\!](\sigma) ... trans_{E}[\![expr_{1n}]\!](\sigma)
           (id_1 = )? trans_E[\![expr_{21}]\!](\sigma) \dots (id_k = )? trans_E[\![expr_{2k}]\!](\sigma))
                            (!i)? (:expr_2)? ](\sigma) = \{expr_1 (!i)? (:expr_2)?
trans_{E}[\![ \{expr_1
trans_E \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_E \llbracket expr.id \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma)).id
trans_{E}[\![expr_{1}[expr_{2}]]\!](\sigma) = trans_{E}[\![expr_{1}]\!](\sigma)[trans_{E}[\![expr_{2}]]\!](\sigma)]
trans_E \llbracket *expr \rrbracket (\sigma) = *expr
trans_E[\![ **expr ]\!](\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_{E}[\![expr_{1}?\ (:expr_{2})?\ (:expr_{3})?\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)?\ (:trans_{E}[\![expr_{2}\ ]\!](\sigma))?\ (:trans_{E}[\![expr_{3}\ ]\!](\sigma))?
 trans_{O}: Comprehension \rightarrow \Sigma \rightarrow Comprehension
trans_O \llbracket for expr_1 in expr_2 (if expr_3)* \rrbracket(\sigma) = for expr_1 in trans_E \llbracket expr_2 \rrbracket(\sigma) (if trans_E \llbracket expr_3 \rrbracket(\sigma))*
                       ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{a}} \llbracket stmt^* \rrbracket (\sigma)._1
 trans_{\overline{A}} : Alias list \rightarrow \Sigma \rightarrow \Sigma
trans_{\overline{A}} \llbracket alias_1 \dots alias_{n-1} \ alias_n \ \rrbracket(\sigma) = trans_A \llbracket alias_n \ \rrbracket(trans_A \llbracket alias_{n-1} \ \rrbracket(\dots \ trans_A \llbracket \ alias_1 \ \rrbracket(\sigma)))
```

```
trans_A: Alias \rightarrow \Sigma \rightarrow
 trans_A \llbracket id \rrbracket (\sigma) =
     LET id = \text{tensorflow.compat.v1} THEN \sigma[\text{"tensor\_flow\_compat"} \mapsto id]
      LET id = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id]
     LET id = os THEN \sigma["os" \mapsto id]
      ELSE \sigma
 trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
      LET id_1 = tensorflow.compat.v1 THEN \sigma["tensor_flow_compat" \mapsto id_2]
      LET id_1 = tensorflow THEN \sigma["tensor_flow" \mapsto id_2]
      LET id_1 = os THEN \sigma["os" \mapsto id_2]
      ELSE \sigma
 trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow (WithItem \ \text{list} \times \Sigma)
 trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
      LET with_item<sub>1</sub>', \sigma_1 = trans_W \llbracket with_item_1 \rrbracket (\sigma) IN
     LET with_item<sub>2</sub>', \sigma_2 = trans_W \llbracket with_item_2 \rrbracket (\sigma_1) IN
      LET with\_item_n', \sigma_n = trans_W \llbracket with\_item_n \rrbracket (\sigma_{n-1}) IN
      (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
  trans_W: WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
A strict form of with item
 trans_W \llbracket expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \rrbracket (\sigma) =
     IF "config_proto" \notin \sigma AND \sigma("tensor_flow_compat") = id_t AND
           expr_1 = id_t. Session THEN
               (expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k} config = config), \sigma)
      ELSE (trans_E \llbracket expr \rrbracket (\sigma), \sigma)
A general form of with item except for the strict form
 trans_W \llbracket expr \rrbracket(\sigma) = (trans_E \llbracket expr \rrbracket(\sigma), \sigma)
 trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (\sigma) =
      (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
  trans_C: MatchCase \rightarrow \Sigma \rightarrow MatchCase
 trans_C[\![ case pattern (if expr)? : stmt^*[\![](\sigma) =
      case trans_P[\![pattern\ ]\!](\sigma) (if trans_E[\![expr\ ]\!](\sigma))? : trans_{\overline{S}}[\![stmt^*\ ]\!](\sigma)._1
  trans_P: Pattern \rightarrow \Sigma \rightarrow Pattern
 trans_P \llbracket expr \rrbracket (\sigma) = trans_E \llbracket expr \rrbracket (\sigma)
```

```
trans_{P}[\![ constant \ ]\!](\sigma) = constant
trans_{P}[\![ [pattern^*] \ ]\!](\sigma) = [trans_{P}[\![ pattern \ ]\!](\sigma)^*]
trans_{P}[\![ *(id)? \ ]\!](\sigma) = *(id)?
trans_{P}[\![ \{(expr : pattern)^* \ id?\} \ ]\!](\sigma) = \{(expr : trans_{P}[\![ pattern \ ]\!](\sigma))^* \ id?\}
trans_{P}[\![ expr \ (pattern_1^* \ (id = pattern_2)^*) \ ]\!](\sigma) = expr \ (trans_{P}[\![ pattern_1 \ ]\!](\sigma)^* \ (id = trans_{P}[\![ pattern_2 \ ]\!](\sigma))^*)
trans_{P}[\![ (pattern \ as)? \ id \ ]\!](\sigma) = (trans_{P}[\![ pattern \ ]\!](\sigma) \ as)? \ id
trans_{P}[\![ pattern_1 \ | \ pattern_2 \ ]\!](\sigma) = trans_{P}[\![ pattern_1 \ ]\!](\sigma) \ | \ trans_{P}[\![ pattern_2 \ ]\!](\sigma)
trans_{P}[\![ -]\!](\sigma) = -
```

# 3 Identifying trainig loop

## 3.1 Restrictions

- 1. Training loop must be defined in only one file.
- 2. Training loop type is either distributed gradient tape or distributed optimizer.
- 3. Each model must have only one type of training loop.
- 4. Function must not be assigned to the variables or passed as an argument.
- 5. Training loop must not be defined conditionally.

### 3.2 Rules

## 3.2.1 Summary

```
(ModuleSummary)
Summary ::=
                   ModuleSummary id \sigma_{\top} tl
                    FuncSummary tl
                                                   (FUNCSUMMARY)
                    {\tt ClassSummary}\ arg
                                                   (ClassSummary)
                    {\tt ValueSummary}\ s
                                                   (ValueSummary)
                   Model \mid \bot
                                                   (ARG)
arg
tl
                  GradTape \mid Optimizer \mid \bot \quad (TrainingLoop)
                   \sigma \cup T
\sigma \in \Sigma = Id \xrightarrow{\text{fin}} Summary
                                 ENVIRONMENT STORING MAPPINGS FROM IDS TO SUMMARIES
```

#### 3.2.2 Training Loop

```
summary_M: Module \rightarrow \Sigma \rightarrow ModuleSummary
   summary_M \llbracket id \ stmt^* \ type\_ignore \rrbracket =
               LET \sigma, tl = summary_{\overline{S}} [stmt^*](\sigma) IN
               ModuleSummary id \sigma tl
      summary_{\overline{S}}: Stmt list \rightarrow \Sigma \rightarrow (\Sigma \times tl)
    summary_{\overline{S}} \llbracket stmt_1 \quad stmt_2 \dots stmt_n \rrbracket (\sigma) = \mathbf{LET} \quad \sigma_1, tl_1 = summary_S \llbracket stmt_1 \rrbracket (\sigma) \quad \mathbf{IN}
                                                                                                                                                                 LET \sigma_2, tl_2 = summary_{\overline{S}} [\![ stmt_2 ]\!] (\sigma_1) IN
                                                                                                                                                                  LET \sigma_n, tl_n = summary_{\overline{S}}[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                                                                                                                                  (\sigma_n, tl_1 \sqcup tl_2 \sqcup \ldots tl_n)
       summary_S: Stmt \rightarrow \Sigma \rightarrow (\Sigma \times tl)
    summary_S \llbracket (@expr_1)^* \text{ def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } stmt^* \rrbracket (\sigma) =
               LET \sigma', tl = summary_{\overline{S}}[stmt^*] IN
               (\sigma[id \mapsto \text{FuncSummary } tl], \perp)
   summary_S \llbracket (@expr_1)^*  async def id (args) (-> expr_2)? : (\#type:s)? stmt^* \rrbracket (\sigma) =
               LET \sigma', tl = summary_{\overline{S}} [stmt^*] IN
               (\sigma[id \mapsto \text{FuncSummary } tl], \perp)
   summary_S \llbracket (@expr)^* \text{ class } id \text{ } (expr_{11} \dots expr_{1n} \text{ } (id_1 = )? \text{ } expr_{21} \dots (id_k = )? \text{ } expr_{2k}) \text{ } : \text{ } stmt^* \rrbracket (\sigma) = summary_S \llbracket (@expr)^* \text{ } class \text{ } id \text{ } (expr_{11} \dots expr_{1n} \text{ } (id_1 = )? \text{ } expr_{21} \dots (id_k = )? \text{ } expr_{2k}) \text{ } : \text{ } stmt^* \rrbracket (\sigma) = summary_S \llbracket (@expr)^* \text{ } class \text{ } id \text{ } (expr_{11} \dots expr_{1n} \text{ } (id_1 = )? \text{ } expr_{21} \dots (id_k = )? \text{ } expr_{2k}) \text{ } : \text{ } stmt^* \rrbracket (\sigma) = summary_S \llbracket (@expr_{11} \dots expr_{1n} \text{ } (id_1 = )? \text{ } expr_{2n} \text{ } ) \text{ } : \text{ } stmt^* \rrbracket (\sigma) = sum_S \rrbracket (\sigma
               IF expr_{1i} = id_c.keras.Model WHEN 1 \le i \le n AND
                          \sigma(id_c) = \texttt{ModuleSummary Id}("tensorflow") \ [] \perp \textbf{THEN} \ (\sigma[id \mapsto \texttt{ClassSummary} \ Model], \perp)
               ELIF expr_{2i} = id_c.keras.Model WHEN 1 \le i \le k AND
                          \sigma(id_c) = \text{ModuleSummary Id}("tensorflow") \quad [] \perp \textbf{THEN} \quad (\sigma[id \mapsto \text{ClassSummary } Model], \perp)
               ELSE (\sigma[id \mapsto \text{ClassSummary } \bot], \bot)
A strict form of assignment statements
   summary_S \llbracket id_r = id_c \text{ () (#type:s)? } \rrbracket(\sigma) =
               IF \sigma(id_r) = \text{ClassSummary } Model \text{ THEN } (\sigma[id_r \mapsto \text{ValueSummary "model_instance"}], \bot)
               ELSE (\sigma, \perp)
   summary_S[\![ (\#type:s)? \text{ for } expr_1 \text{ in } expr_2 : stmt_1^* \text{ (else : } stmt_2^*)? ]\!](\sigma) =
               LET __, tl = summary_{\overline{S}} [\![ stmt_1^* ]\!](\sigma) IN
               (\sigma, tl)
   summary_S \llbracket \text{ (#type:} s)? \text{ async for } expr_1 \text{ in } expr_2 : stmt_1^* \text{ (else : } stmt_2^*)? \rrbracket (\sigma) =
               LET __, tl = summary_{\overline{S}} [\![ stmt_1^* ]\!](\sigma) IN
               (\sigma, tl)
   summary_S[\![ while (expr): stmt_1^* \ (else: stmt_2^*)? \ ]\!](\sigma) =
               LET __, tl = summary_{\overline{S}} [stmt_1^*](\sigma) IN
               (\sigma, tl)
```

```
summary_S \llbracket \text{ (#type:}s)? \text{ with } with\_item^* : stmt^* \rrbracket (\sigma) =
     LET _-, tl = summary_{\overline{S}}[stmt^*](\sigma) IN
     (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
summary_S[\![ (\#type:s)?  async with with\_item^* : stmt^* ]\!](\sigma) =
     LET __, tl = summary_{\overline{S}}[\![ stmt^* ]\!](\sigma) IN
     (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
summary_S[\![try : stmt_1^*   exc\_handler^*   (else : stmt_2^*)?   (finally : stmt_3^*)? [\![](\sigma) =
     (\sigma, summary_{\overline{S}} \llbracket stmt_1^* \rrbracket (\sigma))
summary_S[\![\!] import \ alias^* ]\!](\sigma) = (summary_A[\![\!]\!] alias^* ]\!](\sigma), \perp)
summary_S[\![from \ 0 \ id^* \ import \ alias^*]\!](\sigma) =
     LET \sigma' = summary_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
     LET [id_2 \mapsto ModuleSummary id_2 \sigma_2 \perp, id_2 \mapsto ModuleSummary id_2 \sigma_2 \perp,
          ... id_n \mapsto \text{ModuleSummary } id_n \sigma_n \perp ] = \sigma' \setminus \sigma \text{ IN}
     \sigma \ ++ \ [id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot, \quad id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot,
          ... id_n \mapsto \text{ModuleSummary} (id^* + id_n) \sigma_n \perp
summary_S \llbracket expr \rrbracket(\sigma) = (\sigma, summary_E \llbracket expr \rrbracket(\sigma))
summary_S \llbracket stmt \rrbracket (\sigma) = (\sigma, \bot)
 summary_{\overline{A}}: Alias list \rightarrow \Sigma \rightarrow \Sigma
summary_{\overline{A}} \llbracket alias_1 \dots alias_{n-1} alias_n \rrbracket (\sigma) =
     summary_A \llbracket alias_n \rrbracket (summary_A \llbracket alias_{n-1} \rrbracket (... summary_A \llbracket alias_1 \rrbracket (\sigma) ...))
trans_A : Alias \rightarrow \Sigma \rightarrow \Sigma
trans_A \llbracket id_1 id_2 \dots id_n \rrbracket (\sigma) =
     LET \sigma_n = [id_n \mapsto \text{ModuleSummary } id_n \top \bot]
     LET \sigma_{n-1} = [id_{n-1} \mapsto \text{ModuleSummary } id_{n-1} \quad \sigma_n \quad \bot]
     LET \sigma_2 = [id_2 \mapsto ModuleSummary id_2 \sigma_3 \perp]
     LET \sigma_1 = [id_1 \mapsto ModuleSummary id_1 \sigma_2 \perp]
     \sigma ++ \sigma_1
 summary_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow tl
summary_{\overline{W}}[with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ ](\sigma) =
     summary_{W} \llbracket with\_item_{1} \rrbracket(\sigma) \sqcup summary_{W} \llbracket with\_item_{2} \rrbracket(\sigma) \sqcup ... \quad summary_{W} \llbracket with\_item_{n} \rrbracket(\sigma)
 \overline{summary_W}: WithItem \rightarrow \Sigma \rightarrow tl
summary_W \llbracket expr_1 \text{ as } expr_2? \rrbracket (\sigma) = summary_E \llbracket expr_1 \rrbracket (\sigma)
```