Code Transformation for Distributed Python ML Code

1 Python Abstract Syntax

```
stmt^* type\_ignore
                                                                                 (ModuleDef)
module
         ::=
              (@expr)^* def id (args) (-> expr)? : (#type:s)? stmt^*
                                                                                 (FunDef)
stmt
              (@expr)^* async def id (args) (\rightarrow expr)? : (\#type:s)? stmt^*
                                                                                 (AsyncFunDef)
              (@expr)^* class id (expr^* keyword^*) : stmt^*
                                                                                 (ClassDef)
             return expr?
                                                                                 (Return)
             delete expr^*
                                                                                 (Delete)
             expr^* = expr (\#type:s)?
                                                                                 (Assign)
              expr \ binop = \ expr
                                                                                 (Augassign)
             expr : expr (= expr)?
                                                                                 (AnnAssign)
              (#type:s)? for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (FORLOOP)
              (#type:s)? async for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (AsyncForLoop)
             while (expr) : stmt^* (else : stmt^*)?
                                                                                 (WHILELOOP)
              if (expr) : stmt^* (else : stmt^*)?
                                                                                 (IF)
              (#type:s)? with with\_item^* : stmt^*
                                                                                 (WITH)
             (#type:s)? async with with_{-}item^* : stmt^*
                                                                                 (AsyncWith)
             match expr : match\_case^*
                                                                                 (Match)
             raise expr? (from expr)?
                                                                                 (Raise)
             try : stmt^* exc\_handler^* (else : stmt^*)? (finally : stmt^*)?
                                                                                 (TRY)
              assert expr expr?
                                                                                 (Assert)
              import alias^*
                                                                                 (Import)
             from i\ id? import alias^*
                                                                                 (IMPORTFROM)
              global id^*
                                                                                 (GLOBAL)
             nonlocal id^*
                                                                                 (NonLocal)
                                                                                 (EXPRSTMT)
              expr
             pass
                                                                                 (Pass)
                                                                                 (Break)
             break
                                                                                 (CONTINUE)
              continue
```

```
(BOOLOP)
                     expr boolop expr
expr
                ::=
                     expr :=
                              expr
                                                                                          (NAMEDEXPR)
                     expr binop expr
                                                                                          (BINARYOP)
                                                                                          (UNARYOP)
                     unop expr
                     lambda args : expr
                                                                                          (LAMBDA)
                                                                                          (IFEXPR)
                     expr if expr else expr
                     \{(expr : expr)^* (**expr)^*\}
                                                                                          (DICTIONARY)
                     \{expr^*\}
                                                                                          (Set)
                      [expr^*]
                                                                                          (List)
                      (expr^*)
                                                                                          (Tuple)
                     \{expr: expr comprehension^*\}
                                                                                          (DICTIONARY COMP)
                      \{expr \ comprehension^*\}
                                                                                          (SetComp)
                      [expr comprehension^*]
                                                                                          (LISTCOMP)
                      (expr \ comprehension^*)
                                                                                          (GENERATOR COMP)
                     await expr
                                                                                          (AWAIT)
                     yield expr?
                                                                                          (Yield)
                                                                                          (YIELDFROM)
                     yield from expr
                     expr (compop \ expr)^*
                                                                                          (COMPOP)
                     expr (expr^* keyword^*)
                                                                                          (Call)
                     \{expr (!i)? (:expr)?\}
                                                                                          (FORMATTED VALUE
                     expr^*
                                                                                          (JoinedStr)
                     constant
                                                                                          (Constant)
                     expr.id
                                                                                          (Attribute)
                     expr[expr]
                                                                                          (Subscript)
                     *expr
                                                                                          (Starred)
                     **expr
                                                                                          (DoubleStarred)
                                                                                          (Name)
                     expr? (:expr)? (:expr)?
                                                                                          (SLICE)
                     and | or
                                                                                          (BOOLOPERATOR)
boolop
                ::=
binop
                     + | - | * | @ | / | ** | << | >> | | | ^ | & | // | %
                                                                                          (BINOPERATOR)
                ::=
unop
                ::=
                     \sim | not | + | -
                                                                                          (Unoperator)
                     == | != | < | <= | > | >= | is | is not | in | not in
compop
                ::=
                                                                                          (COMPOPERATOR)
comprehension
                     for expr in expr (if expr)*
                                                                                          (Comprehension)
                ::=
                     async for expr in expr (if expr)*
                                                                                          (ASYNCCOMPREHEN
                     except expr? (as id)? : stmt*
exc\_handler
                                                                                          (EXCHANDLER)
                ::=
args
                     (arg (= expr)?)^*, (arg (= expr)?)^*, arg?, (arg (= expr)?)^*, arg?
                                                                                          (Arguments)
                ::=
arg
                ::=
                     id expr? s?
                                                                                          (Argument)
keyword
                     id? = expr
                                                                                          (Keyword)
                ::=
                     id (.id)^* (as id)?
alias
                                                                                          (ALIAS)
                ::=
with\_item
                     expr (as expr)?
                                                                                          (WITHITEM)
                ::=
```

```
case pattern (if expr)? : stmt^*
                                                       (MATCHCASE)
match\_case
             ::=
pattern
             ::=
                  expr
                                                       (MATCHVALUE)
                  constant
                                                       (MATCHSINGLETON)
                                                       (MATCHSEQUENCE)
                  [pattern*]
                  *(id)?
                                                       (MATCHSTAR)
                  \{(expr: pattern)^* id?\}
                                                       (MATCHMAPPING)
                  expr (pattern^* (id = pattern)*)
                                                       (MATCHCLASS)
                  (pattern as)? id
                                                       (MatchAs)
                  pattern | pattern
                                                       (MATCHOR)
                                                       (MATCHWILDCARD)
                                                       (NoneLiteral)
constant
             ::=
                  None
                                                       (IntLiteral)
                  i
                                                       (FLOATLITERAL)
                  c
                                                       (ComplexLiteral)
                                                       (STRINGLITERAL)
                                                       (BOOLEANLITERAL)
                  (constant^*)
                                                       (TupleLiteral)
                                                       (Ellipsis)
                  i^*
                                                       (TypeIgnore)
type\_ignore
             ::=
                  Id
id
              \in
              \in
                  Str
s
                  {True, False}
              \in
i
              \in
                  \mathbb{Z}
f
              \in \mathbb{R}
                  \mathbb{C}
c
              \in
```

Note: there may be more constant terms such as an immutable container containing only constant elements. Please update the constant rule if you know such terms.

2 Transformation for TF2 Python Code

2.1 Restrictions

- 1. All import statements must be placed at the top of a module.
- 2. The tensorflow module must be assigned to a variable only using an import statement.
- 3. Members of the tensorflow module must not be aliased.
- 4. print function call expressions must not introduce side-effects.
- 5. A dataset and an optimizer object must only be created once via an assignment statement with a function call expression and must not be aliased.
- 6. Variables storing a dataset or a optimizer object must not be reassigned to store another value that is not a dataset or an optimizer object.
- 7. A dataset and an optimizer object must not be created conditionally.
- 8. optimizer.apply_gradients function call expressions must be expression statements or a direct RHS of an assignment statement.
- 9. Global variables storing an optimizer object and referred in functions must be defined before the functions' definitions and must not be changed after their initializations.
- 10. A checkpoint object must only be created once via an assignment statement with a function call expression and must not be aliased.

2.2 Rules

2.2.1 Types and Auxiliary Functions

```
\tau ::=
        Module
                         (Modules)
        Stmt
                         (STATEMENTS)
                         (Expressions)
        Expr
        Comprehension
                         (Comprehensions)
        ExcHandler
                         (EXCEPTION HANDLERS)
        Alias
                         (ALIASES)
        With Item
                         (WITHITEMS)
        Pattern
                         (Patterns)
        Id
                         (IDENTIFIERS)
        Str
                         (STRINGS)
        \tau list
                         (List of elements typed \tau)
```

 $\sigma \in \Sigma = Str^{\text{fin}} Id$ Environment storing mappings from strings to identifiers

```
._1 : \tau \times \tau \to \tau Get the first element of the given pair

@ : \tau list \to \tau list \to \tau list Concatenate two lists

:: \tau \to \tau list \to \tau list Append an element to a list (right-associative)
```

2.2.2 Transformation Rules

```
trans_M: Module \rightarrow Module
trans_{M}[\![stmt^{*}\ type\_ignore]\!] = trans_{\overline{S}}[\![stmt^{*}\ ]\!](\sigma).\_1 type\_ignore]
   trans_{\overline{S}}: Stmt list \rightarrow \Sigma \rightarrow (Stmt list \times \Sigma)
                                                                                                                                                             LET stmt_1^{*\prime}, \sigma_1 = trans_S[stmt_1](\sigma) IN
trans_{\overline{S}}[\![stmt_1 \quad stmt_2 \dots stmt_n ]\!](\sigma) =
                                                                                                                                                               LET stmt_2^{*\prime}, \sigma_2 = trans_S[stmt_2](\sigma_1) IN
                                                                                                                                                               LET stmt_n^{*\prime}, \sigma_n = trans_S[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                                                                                                                               (stmt_1^{*\prime} \ @ \ stmt_2^{*\prime} \ @ \ \dots \ @ \ stmt_n^{*\prime}, \ \sigma_n)
   trans_S: Stmt \rightarrow \Sigma \rightarrow (Stmt \ \textbf{list} \times \Sigma)
trans_S \llbracket (@expr_1)^* \text{ def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } stmt^* \rrbracket (\sigma) = (-> expr_2)? \text{ } (-> expr_2)
             ([(@expr_1)^* \quad \mathsf{def} \quad id \quad (args) \quad ( \rightarrow \ expr_2)? \quad : \quad (\mathtt{\#type} : s)? \quad trans_{\overline{S}}[\![ \ stmt^* \ ]\!](\sigma).\_1], \ \sigma)
([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[\![ stmt^* ]\!](\sigma).\_1], \sigma)
trans_{S}[(@expr_{1})^{*} class id (expr_{2}^{*} keyword^{*}) : stmt^{*}](\sigma) =
             ([(@expr_1)^* \ class \ id \ (expr_2^* \ keyword^*) : trans_{\overline{S}}[[stmt^*]](\sigma).1], \sigma) =
trans_S[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_E[\![ expr \ ]\!](\sigma))?], \sigma)
trans_S[\![ delete \ expr^* \ ]\!](\sigma) = ([delete \ expr^*], \sigma)
```

A strict form of assignment statements

```
trans_S \parallel id_r = expr_1 (expr_{11} \dots expr_{1n} \quad (id_1 = )? \ expr_{21} \dots (id_k = )? \ expr_{2k}) (\#type:s)? \parallel (\sigma) = (id_1 = )? expr_{2k})
     IF \sigma("tensor_flow") = id_t AND expr_1 = id_t.data.Dataset.expr_3 THEN
        ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
            \sigma["dataset"\mapsto id_r])
     ELIF \sigma ("tensor_flow") = id_t AND expr_1 = id_t.train.Checkpoint THEN
        ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
            \sigma["checkpoint"\mapsto id_r])
     ELIF \sigma(\text{"tensor_flow"}) = id_t \text{ AND } expr_1 = id_t.\text{optimizers.Adam THEN}
        IF id_i = learning_rate WHEN 1 \le i \le k THEN
            ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
                ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["optimizer" \mapsto id_r])
        ELSE
            ([id_r = expr_1 \ (expr_{11} * hvd.size() \ ... \ expr_{1n} \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                \sigma["optimizer" \mapsto id_r])
     ELIF \sigma ("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
        IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{2i},
            id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... id_i = id_z ... (id_k =)? expr_{2k}) (#type:s)?,
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
                hvd.broadcast_variables(id_t.variables(), root_rank=0),
                hvd\_broadcast\_done = True ]], \sigma)
        ELSE
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{11},
            id_r = expr_1 \ (id_z \ expr_{12} \ ... \ expr_{1n} \ \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?,
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in <math>id_z], root\_rank=0),
                hvd.broadcast_variables(id_t.variables(), root_rank=0),
                hvd\_broadcast\_done = True ]], \sigma)
     ELIF \sigma ("checkpoint") = id_t AND expr_1 = id_t.save THEN
        ([if hvd.rank() == 0: [id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k}) (#type:s)?]],
            \sigma)
     ELIF \sigma(\text{``keras''}) = id_k \text{ AND } expr_1 = id_k.\text{models.Sequential THEN}
         ([id_r = expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_2 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k})], \sigma["model"\mapsto id_r])
     ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
            \sigma)
 trans_S[\![expr_0 = expr_1 (\#type:s)?]\!](\sigma) =
     IF \sigma(\text{``os''}) = id_{os} AND expr_0 = id_{os}.\text{environ [`CUDA_VISIBLE_DEVICES']}
     THEN ([], \sigma)
A general form of assignment statements except for the strict form
```

 $trans_S[\![expr_1^*]\!] = expr_2$ (#type:s)? $[\![\sigma]\!] = ([expr_1^*]\!] = trans_E[\![expr_2]\!] = (\sigma)$ (#type:s)?], σ)

```
trans_{S}[\![expr_1 \ binop = expr_2 \ ]\!](\sigma) = ([expr_1 \ binop = trans_{E}[\![expr_2 \ ]\!](\sigma)], \sigma)
trans_S[\![expr_1:expr_2:expr_3:]\!](\sigma) = ([expr_1:expr_2:expr_2:expr_3:]\!](\sigma))?], \sigma)
    IF expr_1 = id_1 AND \sigma(\text{"tensor\_flow"}) = id_2
    AND expr_3 = id_2.data.Dataset.expr_4 (expr_5^* keyword^*) THEN
         ([expr_1: expr_2 = expr_3 (\#type:s)?], \sigma["dataset" \mapsto id_1])
    ELSE ([expr_1 : expr_2 (= trans_E[[expr_3 ]](\sigma))?], \sigma)
trans_S[\![ (\#type:s)? for \ expr_1 \ in \ expr_2 \ : \ stmt_1^* \ (else : \ stmt_2^*)? ]\!](\sigma) =
    ([(#type:s)? for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_S[ (#type:s)? async for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
    ([(#type:s)? async for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_{S} while (expr) : stmt_{1}^{*} (else : stmt_{2}^{*})? (\sigma) =
    ([while (trans_{\overline{S}}[\![expr]\!](\sigma)) : trans_{\overline{S}}[\![stmt_1^*]\!](\sigma)._1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)._1)?], \sigma)
trans_{S}[\![ if (expr) : stmt^{*} (else : stmt^{*})? [\![}(\sigma) =
    ([\text{if } (trans_E \| expr \| (\sigma)) : trans_{\overline{S}} \| stmt^* \| (\sigma).\_1 \text{ (else } : trans_{\overline{S}} \| stmt^* \| (\sigma).\_1)?], \sigma)
trans_S[ (\#type:s)? \text{ with } with\_item^* : stmt^* ][(\sigma) =
    LET with\_item^{*\prime}, \sigma_1 = trans_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}} [stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = [\text{"gradient\_tape"} \mapsto id] THEN
         ([(\#type:s)? with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![ (\#type:s)?  async with with\_item^* : stmt^* ]\!](\sigma) =
    LET with_item*', \sigma_1 = trans_{\overline{W}} \llbracket with_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}}[stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
         ([(\# type:s)? async with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
    ([match trans_E[\![expr]\!](\sigma) : (trans_C[\![match\_case]\!](\sigma))^*], \sigma)
trans_S[ raise expr_1? (from expr_2)? ](\sigma) = ([raise <math>expr_1? (from expr_2)?], \sigma)
```

```
trans_S \llbracket try : stmt_1^* = exc\_handler^* \text{ (else : } stmt_2^*)? \text{ (finally : } stmt_3^*)? \rrbracket (\sigma) =
    ([try : trans_{\overline{S}}[stmt_1^*](\sigma)._1 (trans_H[exc\_handler](\sigma))*
    (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)? (finally : trans_{\overline{S}}[\![stmt_3^*]\!](\sigma).\_1)?], \sigma)
trans_{S} assert expr_{1} expr_{2}? \|(\sigma) = ([assert \ trans_{E} \| \ expr_{1} \ \|(\sigma) - expr_{2}?], \sigma)
trans_S[\![\!] import alias^*[\![\!](\sigma)=
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
       ([import alias*,
       import horovod.tensorflow as hvd,
       hvd_broadcast_done = False,
       hvd.init().
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
trans_{S}[\![ from \ i \ id? import \ alias^* ]\!](\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF id = \text{tensorflow AND } \sigma_1 \setminus \sigma = [\text{"keras"} \mapsto id] THEN
       ([from i id? import alias^*,
       import horovod.tensorflow.keras as hvd,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([from i id? import alias^*], \sigma)
trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
trans_S[\![ nonlocal id^*]\![(\sigma) = ([nonlocal <math>id^*], \sigma)
```

A strict form of expr statements

```
trans_{S}[expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})](\sigma) =
     IF \sigma("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
        IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{2i},
            expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = id_z \dots (id_k = )? expr_{2k}),
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in <math>id_z], root\_rank=0),
                hvd.broadcast_variables(id_t.variables(), root_rank=0),
                hvd\_broadcast\_done = True ]], \sigma)
        ELSE
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{11},
            expr_1 (id_z expr_{12} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}),
            global hvd_broadcast_done,
            if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in <math>id_z], root_rank=0),
                hvd.broadcast_variables(id_t.variables(), root_rank=0),
                hvd\_broadcast\_done = True ]], \sigma)
     ELIF expr_1 = print THEN
        ([if hvd.rank() == 0:,
            [expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k})]], \sigma)
     ELIF \sigma("checkpoint") = id_t AND expr_1 = id_t.save THEN
        ([if hvd.rank() == 0: [expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k})]], \sigma)
     ELIF \sigma(\text{``model''}) = id_t \text{ AND } expr_1 = id_t.\text{fit THEN}
        IF id_i = callbacks WHEN 1 \le i \le k THEN
            ([expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ...
                id_i = expr_{2i} + [hvd.callbacks.BroadcastGlobalVariablesCallback(0)]
            ... (id_k = )? expr_{2k}), \sigma)
        ELSE
            ([expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k})
                callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(0)])], \sigma)
     ELSE
        [trans_E[\![expr_1\ (expr_{11}\ ...\ expr_{1n}\ (id_1=)?\ expr_{21}\ ...\ (id_k=)?\ expr_{2k})\ ]\!](\sigma)],\ \sigma)
A general form of expr statements except for the strict form
 trans_{S} \llbracket expr \rrbracket (\sigma) = ([trans_{E} \llbracket expr \rrbracket (\sigma)], \sigma)
trans_S[\![ pass ]\!](\sigma) = ([pass], \sigma)
 trans_S[\![ break ]\!](\sigma) = ([break], \sigma)
 trans_S[\![ continue ]\!](\sigma) = ([continue], \sigma)
```

```
trans_E : Expr \rightarrow \Sigma \rightarrow Expr
trans_{E}[\![expr_{1} \quad boolop \quad expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \quad boolop \quad trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E}[\![expr_{1} := expr_{2}]\!](\sigma) = expr_{1} := trans_{E}[\![expr_{2}]\!](\sigma)
trans_{E}[\![expr_{1} \ binop \ expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \ binop \ trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E}[\![unop\ expr\ ]\!](\sigma) = unop\ trans_{E}[\![expr\ ]\!](\sigma)
trans_{E} \llbracket \text{ lambda } args : expr \ \rrbracket(\sigma) = \text{ lambda } args : trans_{E} \llbracket expr \ \rrbracket(\sigma)
trans_{E}[\![expr_{1}]\!](\sigma) if trans_{E}[\![expr_{2}]\!](\sigma) else trans_{E}[\![expr_{3}]\!](\sigma)
trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
            trans_{E}[\![expr_{1}]\!](\sigma) if trans_{E}[\![expr_{2}]\!](\sigma) else trans_{E}[\![expr_{3}]\!](\sigma)
trans_{E} \llbracket \{(expr_{1} : expr_{2})^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \rrbracket (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \ (**expr_{3})^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \llbracket expr_{2} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \} \Vert (\sigma) = \{(expr_{1} : trans_{E} \rrbracket (\sigma))^{*} \Vert (\sigma) = \{(expr_{1} : trans_{E}
trans_E[\![\{expr^*\}]\!](\sigma) = \{(trans_E[\![expr]\!](\sigma))^*\}
trans_E \llbracket [expr^*] \rrbracket (\sigma) = \llbracket (trans_E \llbracket expr \rrbracket (\sigma))^* \rrbracket
trans_E \llbracket (expr^*) \rrbracket (\sigma) = ((trans_E \llbracket expr \rrbracket (\sigma))^*)
trans_{E}[\![\{expr_1: expr_2 \ comprehension^*\}]\!](\sigma) = \{expr_1: trans_{E}[\![\ expr_2\ ]\!](\sigma) \ (trans_{O}[\![\ comprehension]\!](\sigma))^*\}
trans_E[\![\{expr\ comprehension^*\}\]](\sigma) = \{trans_E[\![\ expr\]](\sigma)\ (trans_O[\![\ comprehension]\!](\sigma))^*\}
trans_E[\![expr\ comprehension^*]\!](\sigma) = [trans_E[\![expr\ ]\!](\sigma)\ (trans_C[\![comprehension]\!](\sigma))^*]
trans_{E} \llbracket (expr \ comprehension^*) \ \rrbracket (\sigma) = (trans_{E} \llbracket \ expr \ \rrbracket (\sigma) \ (trans_{O} \llbracket comprehension \rrbracket (\sigma))^*)
trans_{E}[\![ await \ expr \ ]\!](\sigma) = await \ trans_{E}[\![ \ expr \ ]\!](\sigma)
trans_{E}[\![\ yield\ expr?\ ]\!](\sigma) = yield\ (trans_{E}[\![\ expr\ ]\!](\sigma))?
trans_E[\![\!] yield from expr[\![\!](\sigma) = yield from trans_E[\![\!]\!] expr[\![\!](\sigma)
```

```
trans_E \llbracket expr_1 \ (compop \ expr_2)^* \ \rrbracket(\sigma) = trans_E \llbracket expr_1 \ \rrbracket(\sigma) \ (compop \ trans_E \llbracket expr_2 \rrbracket(\sigma))^*
trans_{E} \llbracket expr_{1} (expr_{11} \dots expr_{1n} (id_{1} = )? expr_{21} \dots (id_{k} = )? expr_{2k}) \rrbracket (\sigma) =
     IF \sigma("dataset") = id_t AND expr_1 = id_t.take THEN
           IF id_i = \text{count} WHEN 1 \le i \le k THEN
                 expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} // hvd.size() ... (id_k = )? expr_{2k})
           ELSE
                 expr_1 (expr_{11} // hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
      ELSE
           trans_{E}[\![expr_{1}]\!](\sigma) (trans_{E}[\![expr_{11}]\!](\sigma) ... trans_{E}[\![expr_{1n}]\!](\sigma)
                 (id_1 = )? trans_E \llbracket expr_{21} \rrbracket (\sigma) \dots (id_k = )? trans_E \llbracket expr_{2k} \rrbracket (\sigma))
trans_{E}[\{expr_{1} \ (!i)? \ (:expr_{2})?\}] | (\sigma) = \{expr_{1} \ (!i)? \ (:expr_{2})?\}\}
trans_E \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_E \llbracket expr.id \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma)).id
trans_{E} \llbracket \ expr_{1} \ \llbracket expr_{2} \rrbracket \ \llbracket (\sigma) = trans_{E} \llbracket \ expr_{1} \ \rrbracket (\sigma) \llbracket trans_{E} \llbracket \ expr_{2} \ \rrbracket (\sigma) \rrbracket
trans_E \llbracket *expr \rrbracket (\sigma) = *expr
trans_E[\![ **expr ]\!](\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_{E}[\![expr_{1}?\ (:expr_{2})?\ (:expr_{3})?\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)?\ (:trans_{E}[\![expr_{2}\ ]\!](\sigma))?\ (:trans_{E}[\![expr_{3}\ ]\!](\sigma))?
 trans_O: Comprehension \rightarrow \Sigma \rightarrow Comprehension
trans_O[\![\![ for expr_1 in expr_2 (if expr_3)^* ]\![\![\![\!]\!](\sigma) = for expr_1 in trans_E[\![\![\![\!]\!]\!](\sigma) (if trans_E[\![\![\![\!]\!]\!](\sigma)))*
 trans_H : ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\_1
 trans_{\overline{A}} : Alias list \rightarrow \Sigma \rightarrow \Sigma
trans_{\overline{A}} \llbracket \ alias_1 \ \dots \ alias_{n-1} \ alias_n \ \rrbracket(\sigma) = trans_A \llbracket \ alias_n \ \rrbracket(trans_A \llbracket \ alias_{n-1} \ \rrbracket(\dots \ trans_A \llbracket \ alias_1 \ \rrbracket(\sigma)))
 trans_A: Alias \rightarrow \Sigma \rightarrow
```

```
trans_A \llbracket id \rrbracket (\sigma) =
     LET id = \text{tensorflow THEN } \sigma[\text{"tensor\_flow"} \mapsto id]
     LET id = \text{keras} THEN \sigma[\text{"keras"} \mapsto id]
     LET id = os THEN \sigma["os" \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
     LET id_1 = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id_2]
     LET id_1 = tensorflow.keras THEN \sigma["keras" \mapsto id_2]
     LET id_1 = \text{os} THEN \sigma[\text{"os"} \mapsto id_2]
     ELSE \sigma
trans_A \llbracket id_1 . id_2 (.id_3)^* \text{ (as } id_2)? \rrbracket (\sigma) = \sigma
 trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow (WithItem list \times \Sigma)
trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
     LET with_item<sub>1</sub>', \sigma_1 = trans_W \llbracket with_item_1 \rrbracket (\sigma) IN
     LET with_item<sub>2</sub>', \sigma_2 = trans_W \llbracket with_item_2 \rrbracket (\sigma_1) IN
     . . .
     LET with\_item_n', \sigma_n = trans_W \llbracket with\_item_n \rrbracket (\sigma_{n-1}) IN
     (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
 trans_W : WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
trans_W \llbracket expr \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma), \sigma)
trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (smodenv) =
     IF \sigma("tensor_flow") = id_1 AND expr_1 = id_1.GradientTape() AND expr_2 = id_2 THEN
          (expr_1 \text{ as } expr_2, \sigma[\text{"gradient\_tape"} \mapsto id_2])
     ELSE (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
               : MatchCase \rightarrow \Sigma \rightarrow MatchCase
trans_C \llbracket \text{ case } pattern \text{ (if } expr)? : stmt^* \rrbracket (\sigma) =
     case trans_P \llbracket pattern \rrbracket (\sigma) (if trans_E \llbracket expr \rrbracket (\sigma))? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma)._1
 trans_P: Pattern \rightarrow \Sigma \rightarrow Pattern
trans_P \llbracket expr \rrbracket (\sigma) = trans_E \llbracket expr \rrbracket (\sigma)
trans_P \llbracket constant \rrbracket (\sigma) = constant
trans_P \llbracket [pattern^*] \rrbracket (\sigma) = \llbracket trans_P \llbracket pattern \rrbracket (\sigma)^* \rrbracket
trans_P \llbracket *(id)? \rrbracket (\sigma) = *(id)?
```

```
trans_{P} \llbracket \{(expr : pattern)^* \ id?\} \ \llbracket (\sigma) = \{(expr : trans_{P} \llbracket pattern \rrbracket (\sigma))^* \ id?\} 
trans_{P} \llbracket \ expr \ (pattern_{1}^{*} \ (id = pattern_{2})^{*}) \ \rrbracket (\sigma) = expr \ (trans_{P} \llbracket pattern_{1} \rrbracket (\sigma)^{*} \ (id = trans_{P} \llbracket pattern_{2} \rrbracket (\sigma))^{*}) 
trans_{P} \llbracket \ (pattern \ as)? \ id \ \rrbracket (\sigma) = (trans_{P} \llbracket \ pattern \ \rrbracket (\sigma) \ as)? \ id 
trans_{P} \llbracket \ pattern_{1} \ \lVert \ pattern_{2} \ \rrbracket (\sigma) = trans_{P} \llbracket \ pattern_{1} \ \rrbracket (\sigma) \ \lVert \ trans_{P} \llbracket \ pattern_{2} \ \rrbracket (\sigma) 
trans_{P} \llbracket \ - \ \rrbracket (\sigma) = -
```

3 Identifying training loop

3.1 Restrictions

- 1. Training loop must be defined in only one file.
- 2. Training loop type is either distributed gradient tape or distributed optimizer.
- 3. Each model must have only one type of training loop.
- 4. Function must not be assigned to the variables or passed as an argument.
- 5. Training loop must not be defined conditionally.

3.2 Rules

3.2.1 Summary

```
Summary ::=
                   ModuleSummary id \sigma_{\top} tl (ModuleSummary)
                    FuncSummary tl
                                                    (FuncSummary)
                                                    (CLASSSUMMARY)
                    ClassSummary arg
                    {\tt ValueSummary}\ s
                                                    (ValueSummary)
              ::= Model \mid \bot
                                                    (ARG)
arg
tl
                    GradTape \mid Optimizer \mid \bot \quad (TrainingLoop)
                   \sigma \cup \top
              ::=
\sigma \in \Sigma = Id \stackrel{\text{fin}}{\rightarrow} Summary
                                 Environment storing mappings from ids to summaries
```

3.2.2 Training Loop

 $summary_{\overline{S}}$

Stmt list

tl)

 $(\Sigma \times$

 $\Sigma \rightarrow$

```
summary_{\overline{S}} \llbracket stmt_1 \quad stmt_2 \dots stmt_n \  \rrbracket(\sigma) = \mathbf{LET} \ \sigma_1, tl_1 = summary_{\overline{S}} \llbracket stmt_1 \  \rrbracket(\sigma) \  \mathbf{IN}
                                                                     LET \sigma_2, tl_2 = summary_{\overline{S}} [\![ stmt_2 ]\!] (\sigma_1) IN
                                                                    LET \sigma_n, tl_n = summary_{\overline{S}} [\![ stmt_n ]\!] (\sigma_{n-1}) IN
                                                                     (\sigma_n, tl_1 \sqcup tl_2 \sqcup \ldots tl_n)
   summary_S: Stmt \rightarrow \Sigma \rightarrow (\Sigma \times )
                                                                  tl)
 summary_S[(@expr_1)^*] def id (args) (-> expr_2)? : (#type:s)? stmt^*[(\sigma) =
      LET \sigma', tl = summary_{\overline{S}} [stmt^*] IN
      (\sigma[id \mapsto \texttt{FuncSummary}\ tl], \perp)
 summary_S \llbracket (@expr_1)^*  async def id (args) (-> expr_2)? : (\#type:s)? stmt^* \rrbracket (\sigma) =
      LET \sigma', tl = summary_{\overline{S}} [stmt^*] IN
      (\sigma[id \mapsto \text{FuncSummary } tl], \perp)
 summary_S[(@expr)^* \text{ class } id (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) : stmt^*](\sigma) =
      IF expr_{1i} = id_c.keras.Model WHEN 1 \le i \le n AND
           \sigma(id_c) = \text{ModuleSummary Id}("tensorflow") [] \perp \textbf{THEN} (\sigma[id \mapsto \text{ClassSummary } Model], \bot)
      ELIF expr_{2i} = id_c.keras.Model WHEN 1 \le i \le k AND
           \sigma(id_c) = \text{ModuleSummary Id}("tensorflow") \quad [] \perp \textbf{THEN} \quad (\sigma[id \mapsto \text{ClassSummary } Model], \perp)
      ELSE (\sigma[id \mapsto \text{ClassSummary } \bot], \bot)
A strict form of assignment statements
 summary_S \llbracket id_r = id_c \text{ () (#type:}s)? \rrbracket (\sigma) =
      IF \sigma(id_c) = \text{ClassSummary } Model \text{ THEN } (\sigma[id_r \mapsto \text{ValueSummary "model_instance"}], \bot)
      ELSE (\sigma, \perp)
 summary_S \llbracket \text{ (#type:}s)? \text{ for } expr_1 \text{ in } expr_2 : stmt_1^* \text{ (else : } stmt_2^*)? \rrbracket (\sigma) =
      LET __, tl = summary_{\overline{S}}[\![ stmt_1^* ]\!](\sigma) IN
      (\sigma, tl)
 summary_S \llbracket \text{ (#type:} s)? \text{ async for } expr_1 \text{ in } expr_2 : stmt_1^* \text{ (else : } stmt_2^*)? \rrbracket (\sigma) =
      LET __, tl = summary_{\overline{S}}[stmt_1^*](\sigma) IN
      (\sigma, tl)
 summary_S \llbracket while (expr) : stmt_1^* (else : stmt_2^*)? \rrbracket(\sigma) =
      LET __, tl = summary_{\overline{S}} [stmt_1^*](\sigma) IN
      (\sigma, tl)
 summary_S \llbracket \text{ (#type:}s)? \text{ with } with\_item^* : stmt^* \rrbracket (\sigma) =
      LET __, tl = summary_{\overline{S}}[\![ stmt^* ]\!](\sigma) IN
      (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
 summary_{S}[ (\#type:s)?  async with with\_item^* : stmt^* ][(\sigma) =
      LET __, tl = summary_{\overline{S}}[\![ stmt^* ]\!](\sigma) IN
      (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
```

```
summary_S[ try : stmt_1^* exc_handler* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
       (\sigma, summary_{\overline{S}}[\![stmt_1^*]\!](\sigma))
 summary_S[\![\!] import \ alias^* ]\!](\sigma) = (summary_A[\![\!]\!] alias^* ]\!](\sigma), \perp)
 summary_S[\![\!] from 0 id^* import alias^* \![\!](\sigma) =
       \mathbf{LET} \ \ \sigma' \ \ = \ summary_{\overline{A}} \llbracket \ alias^* \ \rrbracket (\sigma) \quad \mathbf{IN}
      LET [id_2 \mapsto \texttt{ModuleSummary} \ id_2 \ \sigma_2 \ \bot, \ id_2 \mapsto \texttt{ModuleSummary} \ id_2 \ \sigma_2 \ \bot,
            ... id_n \mapsto \texttt{ModuleSummary} \ id_n \ \sigma_n \ \bot] = \sigma' \setminus \sigma \ \textbf{IN}
      \sigma \ ++ \ [id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot, \quad id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot,
            ... id_n \mapsto \text{ModuleSummary} (id^* + id_n) \sigma_n \perp
 summary_S \llbracket expr \rrbracket(\sigma) = (\sigma, summary_E \llbracket expr \rrbracket(\sigma))
 summary_S[\![stmt]\!](\sigma) = (\sigma, \bot)
  \overline{summary_{\overline{A}}} : Alias list \rightarrow \Sigma \rightarrow \Sigma
 summary_{\overline{A}} \llbracket \ alias_1 \ ... \ alias_{n-1} \ alias_n \ \rrbracket (\sigma) =
       summary_A \llbracket alias_n \rrbracket (summary_A \llbracket alias_{n-1} \rrbracket (... summary_A \llbracket alias_1 \rrbracket (\sigma) ...))
 LET \sigma_n = [id_n \mapsto \text{ModuleSummary } id_n \top \bot]
      LET \sigma_{n-1} = [id_{n-1} \mapsto ModuleSummary id_{n-1} \sigma_n \perp]
      LET \sigma_2 = [id_2 \mapsto ModuleSummary id_2 \sigma_3 \perp]
      LET \sigma_1 = [id_1 \mapsto ModuleSummary id_1 \sigma_2 \perp]
       \sigma ++ \sigma_1
  summary_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow tl
 summary_{\overline{W}}[with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ ](\sigma) =
       summary_{W} \llbracket \ with\_item_1 \ \rrbracket (\sigma) \ \sqcup \ summary_{W} \llbracket \ with\_item_2 \ \rrbracket (\sigma) \ \sqcup \ \ldots \quad summary_{W} \llbracket \ with\_item_n \ \rrbracket (\sigma)
   summary_W: WithItem \rightarrow \Sigma \rightarrow tl
 summary_W \llbracket expr_1 \text{ as } expr_2? \rrbracket (\sigma) = summary_E \llbracket expr_1 \rrbracket (\sigma)
  summary_E : Expr \rightarrow \Sigma
                                                                tl
A strict form of call expression
```

```
summary_E \llbracket \ expr_1 \ (expr_{11} \ ... \ expr_{1n} \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k}) \ \rrbracket (\sigma) = \\ \textbf{IF} \ \sigma (id_r) \ = \ \texttt{ValueSummary "model_instance" AND} \\ expr_1 \ = \ id_r . \texttt{fit THEN } Optimizer \\ \textbf{ELIF} \ \sigma (id_r) \ = \ \texttt{ModuleSummary } Id("tensorflow") \ \sigma' \ tl \ \textbf{AND} \\ expr_1 \ = \ id_r . \texttt{GradientTape } \ \textbf{THEN } GradTape \\ \textbf{ELIF} \ \sigma (id_r) \ = \ \texttt{FuncSummary } tl \ \textbf{AND} \\ expr_1 \ = \ idr \ \ \textbf{THEN } tl \\ \textbf{ELSE } \ \bot \\ summary_E \llbracket \ expr \ \rrbracket (\sigma) = \bot
```