# Code Transformation for Distributed Python ML Code

## 1 Python Abstract Syntax

```
stmt^* type\_ignore
                                                                                 (ModuleDef)
module
         ::=
              (@expr)^* def id (args) (-> expr)? : (#type:s)? stmt^*
                                                                                 (FunDef)
stmt
              (@expr)^* async def id (args) (\rightarrow expr)? : (\#type:s)? stmt^*
                                                                                 (AsyncFunDef)
              (@expr)^* class id (expr^* keyword^*) : stmt^*
                                                                                 (ClassDef)
             return expr?
                                                                                 (Return)
             delete expr^*
                                                                                 (Delete)
             expr^* = expr (\#type:s)?
                                                                                 (Assign)
              expr \ binop = \ expr
                                                                                 (Augassign)
             expr : expr (= expr)?
                                                                                 (AnnAssign)
              (#type:s)? for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (FORLOOP)
              (#type:s)? async for expr in expr : stmt^* (else : stmt^*)?
                                                                                 (AsyncForLoop)
             while (expr) : stmt^* (else : stmt^*)?
                                                                                 (WHILELOOP)
              if (expr) : stmt^* (else : stmt^*)?
                                                                                 (IF)
              (#type:s)? with with\_item^* : stmt^*
                                                                                 (WITH)
             (#type:s)? async with with_{-}item^* : stmt^*
                                                                                 (AsyncWith)
             match expr : match\_case^*
                                                                                 (Match)
             raise expr? (from expr)?
                                                                                 (Raise)
             try : stmt^* exc\_handler^* (else : stmt^*)? (finally : stmt^*)?
                                                                                 (TRY)
              assert expr expr?
                                                                                 (Assert)
              import alias^*
                                                                                 (Import)
             from i\ id? import alias^*
                                                                                 (IMPORTFROM)
              global id^*
                                                                                 (GLOBAL)
             nonlocal id^*
                                                                                 (NonLocal)
                                                                                 (EXPRSTMT)
              expr
             pass
                                                                                 (Pass)
                                                                                 (Break)
             break
                                                                                 (CONTINUE)
              continue
```

```
(BOOLOP)
                     expr boolop expr
expr
                ::=
                              expr
                                                                                         (NAMEDEXPR)
                     expr :=
                     expr binop expr
                                                                                         (BINARYOP)
                                                                                         (UNARYOP)
                     unop expr
                     lambda args : expr
                                                                                         (LAMBDA)
                                                                                         (IFEXPR)
                     expr if expr else expr
                     \{(expr : expr)^* (**expr)^*\}
                                                                                         (DICTIONARY)
                     \{expr^*\}
                                                                                         (Set)
                      [expr^*]
                                                                                         (List)
                      (expr^*)
                                                                                         (Tuple)
                     \{expr: expr comprehension^*\}
                                                                                         (DICTIONARY COMP)
                      \{expr \ comprehension^*\}
                                                                                         (SetComp)
                      [expr comprehension^*]
                                                                                         (LISTCOMP)
                      (expr \ comprehension^*)
                                                                                         (GENERATORCOMP)
                     await expr
                                                                                         (AWAIT)
                     yield expr?
                                                                                         (Yield)
                                                                                         (YIELDFROM)
                     yield from expr
                     expr (compop \ expr)^*
                                                                                         (COMPOP)
                     expr (expr^* keyword^*)
                                                                                         (Call)
                     \{expr (!i)? (:expr)?\}
                                                                                         (FORMATTED VALUE
                     expr^*
                                                                                         (JoinedStr)
                     constant
                                                                                         (Constant)
                     expr.id
                                                                                         (Attribute)
                     expr[expr]
                                                                                         (Subscript)
                     *expr
                                                                                         (Starred)
                     **expr
                                                                                         (DoubleStarred)
                                                                                         (NAME)
                     expr? (:expr)? (:expr)?
                                                                                         (SLICE)
                     and | or
                                                                                         (BOOLOPERATOR)
boolop
                ::=
binop
                     + | - | * | @ | / | ** | << | >> | | | ^ | & | // | %
                                                                                         (BINOPERATOR)
                ::=
unop
                ::=
                     \sim | not | + | -
                                                                                         (Unoperator)
                     == | != | < | <= | > | >= | is | is not | in | not in
compop
                ::=
                                                                                         (COMPOPERATOR)
comprehension
                     for expr in expr (if expr)*
                                                                                         (Comprehension)
                ::=
                     async for expr in expr (if expr)*
                                                                                         (ASYNCCOMPREHEN
                     except expr? (as id)? : stmt*
exc\_handler
                                                                                         (EXCHANDLER)
                ::=
args
                     (arg (= expr)?)^*, (arg (= expr)?)^*, arg?, (arg (= expr)?)^*, arg?
                                                                                         (Arguments)
                ::=
arg
                ::=
                     id expr? s?
                                                                                         (Argument)
keyword
                     id? = expr
                                                                                         (Keyword)
                ::=
                     id (.id)^* (as id)?
alias
                                                                                         (ALIAS)
                ::=
with\_item
                     expr (as expr)?
                                                                                         (WITHITEM)
                ::=
```

```
case pattern (if expr)? : stmt^*
                                                       (MATCHCASE)
match\_case
             ::=
pattern
             ::=
                  expr
                                                       (MATCHVALUE)
                  constant
                                                       (MATCHSINGLETON)
                                                       (MATCHSEQUENCE)
                  [pattern*]
                  *(id)?
                                                       (MATCHSTAR)
                  \{(expr: pattern)^* id?\}
                                                       (MATCHMAPPING)
                  expr (pattern^* (id = pattern)*)
                                                       (MATCHCLASS)
                  (pattern as)? id
                                                       (MatchAs)
                  pattern | pattern
                                                       (MATCHOR)
                                                       (MATCHWILDCARD)
                                                       (NoneLiteral)
constant
             ::=
                  None
                                                       (IntLiteral)
                  i
                                                       (FLOATLITERAL)
                  c
                                                       (ComplexLiteral)
                                                       (STRINGLITERAL)
                                                       (BOOLEANLITERAL)
                  (constant^*)
                                                       (TupleLiteral)
                                                       (Ellipsis)
                  i^*
                                                       (TypeIgnore)
type\_ignore
             ::=
                  Id
id
              \in
              \in
                  Str
s
                  {True, False}
              \in
i
              \in
                  \mathbb{Z}
f
              \in \mathbb{R}
                  \mathbb{C}
c
              \in
```

Note: there may be more constant terms such as an immutable container containing only constant elements. Please update the constant rule if you know such terms.

## 2 Transformation Rule for TensorFlow ML Training Code

#### 2.1 Restrictions

- 1. All import statements must be placed at the top of a module.
- 2. The tensorflow module must be assigned to a variable only using an import statement.
- 3. Members of the tensorflow module must not be aliased.
- 4. print function call expressions must not introduce side-effects.
- 5. A dataset and an optimizer object must only be created once via an assignment statement with a function call expression and must not be aliased.
- 6. Variables storing a dataset or a optimizer object must not be reassigned to store another value that is not a dataset or an optimizer object.
- 7. A dataset and an optimizer object must not be created conditionally.
- 8. optimizer.apply\_gradients function call expressions must be expression statements or a direct RHS of an assignment statement.
- 9. Global variables storing an optimizer object and referred in functions must be defined before the functions' definitions and must not be changed after their initializations.
- 10. A checkpoint object must only be created once via an assignment statement with a function call expression and must not be aliased.

## 2.2 Rules

### 2.2.1 Types and Auxiliary Functions

```
\tau ::=
        Module
                         (Modules)
        Stmt
                         (STATEMENTS)
        Expr
                         (Expressions)
        Comprehension
                         (Comprehensions)
        ExcHandler
                         (EXCEPTION HANDLERS)
        Alias
                         (ALIASES)
        With Item
                         (WITHITEMS)
        Pattern
                         (Patterns)
        Id
                         (IDENTIFIERS)
        Str
                         (STRINGS)
        \tau list
                         (List of elements typed \tau)
```

 $\sigma \in \Sigma = Str^{\text{fin}} Id$  Environment storing mappings from strings to identifiers

```
._1 : \tau \times \tau \to \tau Get the first element of the given pair
```

 $au : au o au ext{ list } o au ext{ list } ext{ Append an element to a list (right-associative)}$ 

<:  $Expr \times Expr \rightarrow \mathbb{B}$  Whether classes specified by the expressions are subclasses

## 2.3 Rule: TensorFlow 2.x Keras API Pattern

### 2.3.1 Transformation Rules

```
trans_M: Module \rightarrow Module
 trans_M \llbracket stmt^* \quad type\_ignore \rrbracket = trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\_1 \quad type\_ignore
  trans_{\overline{S}}: Stmt list \rightarrow \Sigma \rightarrow (Stmt list \times \Sigma)
 trans_{\overline{S}}[\![\![stmt_1 \quad stmt_2 \dots stmt_n \ ]\!](\sigma) = \mathbf{LET} \quad stmt_1^{*\prime}, \sigma_1 = trans_S[\![\![stmt_1 \ ]\!](\sigma) \mathbf{IN}
                                                       LET stmt_2^{*\prime}, \sigma_2 = trans_S[stmt_2](\sigma_1) IN
                                                       LET stmt_n^{*\prime}, \sigma_n = trans_S[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                       (stmt_1^{*\prime} \otimes stmt_2^{*\prime} \otimes ... \otimes stmt_n^{*\prime}, \sigma_n)
  trans_S: Stmt \rightarrow \Sigma \rightarrow (Stmt \ \textbf{list} \times \Sigma)
 trans_S[(@expr_1)^* \text{ def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } stmt^*](\sigma) =
     ([(@expr_1)^* def id (args) (-> expr_2)? : (\#type:s)? trans_{\overline{s}}[[stmt^*]](\sigma)._1], \sigma)
 trans_S \llbracket (@expr_1)^*  async def id (args) (-> expr_2)? : (#type:s)? <math>stmt^* \llbracket (\sigma) =
     ([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[[stmt^*]](\sigma).\_1], \sigma)
 trans_S[(@expr_1)^* \ class \ id \ (expr_2^* \ keyword^*) : stmt^*](\sigma) =
     ([(@expr_1)^* \text{ class } id \text{ } (expr_2^* \text{ } keyword^*) \text{ } : \text{ } trans_{\overline{S}}[[stmt^*]](\sigma).\_1], \sigma) =
 trans_S[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_E[\![ expr \ ]\!](\sigma))?], \sigma)
 trans_S[\![ delete \ expr^* \ ]\!](\sigma) = ([delete \ expr^*], \sigma)
A strict form of assignment statements
 {f IF}\ expr_1<: {f tensorflow.keras.optimizers.schedules.PiecewiseConstantDecay}\ {f THEN}
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
             \sigma["lr_scheduler" \mapsto id_r])
     ELIF expr_1 <: tensorflow.keras.experimental.PiecewiseConstantDecay THEN
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
             \sigma[\text{"lr\_scheduler"} \mapsto id_r])
     ELIF expr_1 <: tensorflow.keras.optimizers.schedules.LearningRateSchedule THEN
         IF id_i = initial_learning_rate WHEN 1 \le i \le k THEN
             ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
                  ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler"\mapsto id_r])
         ELSE
              ([id_r = expr_1 \ (expr_{11} * hvd.size() \ ... \ expr_{1n} \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                  \sigma["lr_scheduler" \mapsto id_r])
     ELIF expr_1 <: tensorflow.compat.v1.train.exponential_decay THEN
         IF id_i = initial_learning_rate WHEN 1 \le i \le k THEN
```

```
([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
           ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["lr_scheduler" \mapsto id_r])
   ELSE
       ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
           \sigma["lr_scheduler" \mapsto id_r])
{f IF} expr_1<: tensorflow.keras.optimizers.Optimizer {f THEN}
   ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
       \sigma["optimizer" \mapsto id_r])
IF \sigma("tensor_flow") = id_t AND expr_1 = id_t.data.Dataset.expr_3 THEN
   ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
       \sigma["dataset"\mapsto id_r])
ELIF \sigma ("tensor_flow") = id_t AND expr_1 = id_t.train.Checkpoint THEN
   ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
       \sigma["checkpoint"\mapsto id_r])
ELIF \sigma(\text{"tensor_flow"}) = id_t \text{ AND } expr_1 = id_t.\text{optimizers.Adam THEN}
   IF id_i = learning_rate WHEN 1 \le i \le k THEN
       ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size())
           ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["optimizer" \mapsto id_r])
   ELSE
       ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
           \sigma["optimizer" \mapsto id_r])
ELIF \sigma("optimizers") = id_t AND expr_1 = id_t.Adam THEN
   IF id_i = learning_rate WHEN 1 \le i \le k THEN
       ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
           ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["optimizer" \mapsto id_r])
   ELSE
       ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
           \sigma["optimizer"\mapsto id_r])
ELIF \sigma("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
   IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
       LET id_z = \text{NewID}() IN
       ([id_z = expr_{2i},
       id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = id_z \dots (id_k = )? expr_{2k}) (\#type:s)?,
       global hvd_broadcast_done,
       if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in id_z], root\_rank=0),
           hvd.broadcast_variables(id_t.variables(), root_rank=0),
           hvd_broadcast_done = True ]], \sigma)
   ELSE
       LET id_z = \text{NewID}() IN
       ([id_z = expr_{11},
       id_r = expr_1 \ (id_z \ expr_{12} \ \dots \ expr_{1n} \ \ (id_1 = )? \ expr_{21} \ \dots \ (id_k = )? \ expr_{2k}) \ (\#type:s)?,
       global hvd_broadcast_done,
       if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in <math>id_z], root_rank=0),
           hvd.broadcast_variables(id_t.variables(), root_rank=0),
```

```
hvd\_broadcast\_done = True ]], \sigma)
      ELIF \sigma ("checkpoint") = id_t AND expr_1 = id_t.save THEN
          ([if hvd.rank() == 0: [id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k}) (#type:s)?]],
      ELIF \sigma(\text{``keras''}) = id_k \text{ AND } expr_1 = id_k.\text{models.Sequential THEN}
          ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k})], \sigma["model"\mapsto id_r])
     ELIF \sigma("keras") = id_t AND expr_1 = id_t.optimizers.Adam THEN
          IF id_i = learning_rate WHEN 1 \le i \le k THEN
              ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
          ... (id_k = )? expr_{2k}) (#type:s)?
              id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r]
          ELSE
              ([id_r = expr_1 (expr_{11} * hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (#type:s)?
              id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{``optimizer''} \mapsto id_r]
      ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
              \sigma)
 trans_{S} \llbracket expr_{0} = expr_{1} \text{ (#type:}s)? \rrbracket (\sigma) =
      IF \sigma(\text{``os''}) = id_{os} AND expr_0 = id_{os}.\text{environ [`CUDA_VISIBLE_DEVICES']}
      THEN ([], \sigma)
A general form of assignment statements except for the strict form
 trans_S[\![expr_1^*]\!] = expr_2 (#type:s)? [\![\sigma]\!] = ([expr_1^*]\!] = trans_E[\![expr_2]\!] = (\sigma) (#type:s)?], \sigma)
 trans_S \llbracket expr_1 \ binop = expr_2 \ \rrbracket(\sigma) = ([expr_1 \ binop = trans_E \llbracket \ expr_2 \ \rrbracket(\sigma)], \ \sigma)
 trans_S[\![expr_1:expr_2:expr_3]\!](\sigma) = ([expr_1:expr_2:expr_2:expr_3]\!](\sigma))?], \sigma)
      IF expr_1 = id_1 AND \sigma(\text{"tensor\_flow"}) = id_2
      AND expr_3 = id_2.data.Dataset.expr_4 (expr_5^* keyword^*) THEN
          ([expr_1 : expr_2 = expr_3 (\#type:s)?], \sigma["dataset" \mapsto id_1])
      ELSE ([expr_1 : expr_2 (= trans_E [ expr_3 ] (\sigma))?], \sigma)
 trans_S[ (#type:s)? for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
      ([(#type:s)? for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
          trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
 trans_S[ (#type:s)? async for expr_1 in expr_2 : stmt_1^* (else : stmt_2^*)? ](\sigma) =
      ([(#type:s)? async for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
          trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
 trans_{S} \llbracket \text{ while } (expr) : stmt_{1}^{*} \text{ (else : } stmt_{2}^{*})? \rrbracket (\sigma) =
      (\llbracket \text{while } (trans_E \llbracket \ expr \ \rrbracket(\sigma)) : trans_{\overline{S}} \llbracket \ stmt_1^* \ \rrbracket(\sigma).\_1 \ (\text{else } : trans_{\overline{S}} \llbracket \ stmt_2^* \ \rrbracket(\sigma).\_1)? \rrbracket, \ \sigma)
 trans_{S}[\![ if (expr) : stmt^{*} (else : stmt^{*})? ]\![(\sigma) =
      ([\text{if } (trans_E \| expr \| (\sigma)) : trans_{\overline{S}} \| stmt^* \| (\sigma)...1 \text{ (else } : trans_{\overline{S}} \| stmt^* \| (\sigma)...1)?], \sigma)
```

```
trans_S[ (\#type:s)? \text{ with } with\_item^* : stmt^* ][(\sigma) =
    LET with\_item^{*\prime}, \sigma_1 = trans_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}}[stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
        ([(\#type:s)? with with\_item^{*\prime} : stmt^{*\prime},
        id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![ (#type:s)? async with with\_item^* : stmt^*[\!](\sigma) =
    LET with_item*', \sigma_1 = trans_{\overline{W}} \llbracket with_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}}[stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
        ([(\#type:s)? async with with\_item^{*\prime} : stmt^{*\prime},
        id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? async with with_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
    ([match trans_E[\![expr]\!](\sigma) : (trans_C[\![match\_case]\!](\sigma))^*], \sigma)
trans_S[ raise expr_1? (from expr_2)? [(\sigma) = ([raise expr_1? (from <math>expr_2)?], \sigma)
trans_S \llbracket try : stmt_1^* = exc\_handler^* \text{ (else } : stmt_2^*)? \text{ (finally } : stmt_3^*)? \rrbracket (\sigma) =
    ([try : trans_{\overline{S}} [stmt_1^*] (\sigma)._1 (trans_H [exc\_handler] (\sigma))^*
    (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)._1)? (finally : trans_{\overline{S}}[\![stmt_3^*]\!](\sigma)._1)?], \sigma)
trans_S[\![ assert \ expr_1 \ expr_2? \ ]\!](\sigma) = ([assert \ trans_E[\![ \ expr_1 \ ]\!](\sigma) \ expr_2?], \sigma)
trans_S import alias^* (\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
        ([import alias*,
        import horovod.tensorflow as hvd,
        hvd_broadcast_done = False,
        hvd.init(),
        gpus = id.config.experimental.list_physical_devices('GPU'),
        for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
        if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
```

```
trans_S import alias^* (\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
       ([import alias*,
       import horovod.tensorflow as hvd,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
 trans_{S}[\![from\ i\ id?\ import\ alias^*]\!](\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [alias^*](\sigma) IN
    IF id = \text{tensorflow AND } \sigma_1 \setminus \sigma = [\text{"keras"} \mapsto id] THEN
       ([from i id? import alias^*,
       import horovod.tensorflow.keras as hvd,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([from i id? import alias^*], \sigma_1)
 trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
 trans_S[\![ nonlocal id^* ]\!](\sigma) = ([nonlocal id^*], \sigma)
A strict form of expr statements
 trans_S[\![expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k})]\!](\sigma) =
    IF \sigma("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
        IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
           LET id_z = \text{NewID}() IN
           ([id_z = expr_{2i},
           expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = id_z ... (id_k = )? expr_{2k}),
           global hvd_broadcast_done,
           if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
               hvd.broadcast_variables(id_t.variables(), root_rank=0),
               hvd\_broadcast\_done = True ]], \sigma)
        ELSE
           LET id_z = \text{NewID}() IN
           ([id_z = expr_{11},
           expr_1 (id_z expr_{12} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}),
           global hvd_broadcast_done,
           if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
               hvd.broadcast_variables(id_t.variables(), root_rank=0),
```

```
hvd\_broadcast\_done = True ]], \sigma)
ELIF expr_1 = print OR expr_1 = expr. write OR expr_1 = expr. summary OR
   expr_1 = expr.save_weights OR expr_1 = expr.load_weights THEN
       ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
ELIF \sigma("checkpoint") = id_t AND expr_1 = id_t.save THEN
   ([if hvd.rank() == 0: [expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k})]], \sigma)
ELIF \sigma(\text{``model''}) = id_t \text{ AND } expr_1 = id_t.\text{fit THEN}
   IF id_i = verbose WHEN 1 \le i \le k THEN
       IF id_j = callbacks WHEN 1 \le j \le k THEN
          ([callback = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)]
          if hvd.rank() == 0: callbacks.append(expr_{2i})
          expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = 1 if hvd.rank() == 0 else 0
          ... id_j = \text{callbacks ... } (id_k = )? \ expr_{2k}), \sigma)
       ELSE
          ([expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ...
              id_i = 1 if hvd.rank() == 0 else 0 ... (id_k = )? expr_{2k}
              callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)])], \sigma)
   ELSE
       IF id_j = callbacks WHEN 1 \le j \le k THEN
          ([callback = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)]
          if hvd.rank() == 0: callbacks.append(expr_{2j})
          expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_j = callbacks ... (id_k = )? expr_{2k}
              verbose = 1 if hvd.rank() == 0 else 0), \sigma)
       ELSE
          ([expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
              verbose = 1 if hvd.rank() == 0 else 0
              callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(0)])], \sigma)
ELIF \sigma(\text{``model''}) = id_t \text{ AND } expr_1 = id_t.\text{compile THEN}
   IF id_i = optimizer AND expr_{2i} = "adam" WHEN 1 \le i \le k THEN
       (id_z = tf.optimizers.Adam(learning.rate=0.001 * hvd.size())
       id_z = hvd.DistributedOptimizer(id_z)
       expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = id_z ... (id_k = )? expr_{2k})], \sigma)
   ELIF expr_{11} = "adam" THEN
       (id_z = tf.optimizers.Adam(learning_rate=0.001 * hvd.size())
       id_z = hvd.DistributedOptimizer(id_z)
       expr_1 (id_z ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}), \sigma)
   ELSE
       [trans_E[\![expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})]\![\sigma], \sigma]
ELIF expr_1 = model.summary THEN
   ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
ELSE
   [trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) \mid, \sigma)
```

A general form of expr statements except for the strict form

 $trans_{S}[\![expr]\!](\sigma) = ([trans_{E}[\![expr]\!](\sigma)], \sigma)$ 

```
trans_S[\![ pass ]\!](\sigma) = ([pass], \sigma)
trans_S break (\sigma) = ([break], \sigma)
trans_S[\![ continue ]\!](\sigma) = ([continue], \sigma)
 trans_E : Expr \rightarrow \Sigma \rightarrow Expr
trans_{E}[\![expr_{1} \quad boolop \quad expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \quad boolop \quad trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E}[\![expr_{1} := expr_{2}]\!](\sigma) = expr_{1} := trans_{E}[\![expr_{2}]\!](\sigma)
trans_{E}[\![expr_{1} \quad binop \quad expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \quad binop \quad trans_{E}[\![expr_{2} \ ]\!](\sigma)
trans_{E} \llbracket unop \ expr \ \rrbracket(\sigma) = unop \ trans_{E} \llbracket \ expr \ \rrbracket(\sigma)
trans_{E}[\![ ] ] lambda args: expr[\![ ] ](\sigma) = lambda <math>args: trans_{E}[\![ ] ] expr[\![ ] ](\sigma)
trans_{E}[\![ expr_{1} ]\!] if expr_{2}  else expr_{3}[\!] (\sigma) =
     trans_{E} \llbracket \ expr_{1} \ \rrbracket(\sigma) if trans_{E} \llbracket \ expr_{2} \ \rrbracket(\sigma) else trans_{E} \llbracket \ expr_{3} \ \rrbracket(\sigma)
trans_{E}[\![ expr_{1} ]\!] if expr_{2}  else expr_{3}[\!] (\sigma) =
     trans_{E}[\![expr_{1}]\!](\sigma) if trans_{E}[\![expr_{2}]\!](\sigma) else trans_{E}[\![expr_{3}]\!](\sigma)
trans_{E}[\![\{(expr_{1}: expr_{2})^{*} \ (**expr_{3})^{*}\}\ ]\!](\sigma) = \{(expr_{1}: trans_{E}[\![expr_{2}]\!](\sigma))^{*} \ (**expr_{3})^{*}\}\}
trans_E[\![\{expr^*\}\ ]\!](\sigma) = \{(trans_E[\![expr]\!](\sigma))^*\}
trans_E[\![expr^*]\!](\sigma) = [(trans_E[\![expr]\!](\sigma))^*]
trans_E[\![ (expr^*) \ ]\!](\sigma) = ((trans_E[\![ expr ]\!](\sigma))^*)
trans_{E}[\![\{expr_1: expr_2 \ comprehension^*\}]\!](\sigma) = \{expr_1: trans_{E}[\![\ expr_2]\!](\sigma) \ (trans_{O}[\![comprehension]\!](\sigma))^*\}
trans_{E}[\![\{expr \ comprehension^*\}]\!](\sigma) = \{trans_{E}[\![\ expr \ ]\!](\sigma) \ (trans_{O}[\![comprehension]\!](\sigma))^*\}
trans_E[\![expr\ comprehension^*]\!](\sigma) = [trans_E[\![expr\ ]\!](\sigma)\ (trans_O[\![comprehension]\!](\sigma))^*]
```

```
trans_{E} \llbracket (expr \ comprehension^*) \ \rrbracket (\sigma) = (trans_{E} \llbracket \ expr \ \rrbracket (\sigma) \ (trans_{O} \llbracket comprehension \rrbracket (\sigma))^*)
trans_{E}[\![ await \ expr \ ]\!](\sigma) = await \ trans_{E}[\![ \ expr \ ]\!](\sigma)
trans_{E}[\![\!] yield expr? [\![\!](\sigma) = yield (trans_{E}[\![\!] expr [\!]\!](\sigma))?
trans_{E}[\![\  \, \text{yield from } expr\ ]\!](\sigma) = \text{yield from } trans_{E}[\![\  \, expr\ ]\!](\sigma)
trans_{\mathbb{E}} \llbracket expr_1 \ (compop \ expr_2)^* \ \rrbracket(\sigma) = trans_{\mathbb{E}} \llbracket expr_1 \ \rrbracket(\sigma) \ (compop \ trans_{\mathbb{E}} \llbracket expr_2 \rrbracket(\sigma))^*
trans_E \llbracket expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \rrbracket (\sigma) =
     IF \sigma("dataset") = id_t AND expr_1 = id_t.take THEN
           IF id_i = \text{count} WHEN 1 \le i \le k THEN
                 expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} // hvd.size() ... (id_k = )? expr_{2k})
           ELSE
                 expr_1 (expr_{11} // hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
      ELSE
           trans_{E} \llbracket expr_{1} \rrbracket (\sigma) \ (trans_{E} \llbracket expr_{11} \rrbracket (\sigma) \ ... \ trans_{E} \llbracket expr_{1n} \rrbracket (\sigma)
                 (id_1 = )? trans_E \llbracket expr_{21} \rrbracket (\sigma) \dots (id_k = )? trans_E \llbracket expr_{2k} \rrbracket (\sigma))
trans_{E} [ \{expr_{1} \ (!i)? \ (:expr_{2})?\} ] [\sigma] = \{expr_{1} \ (!i)? \ (:expr_{2})?\} ]
trans_{E} \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_{E} \llbracket expr.id \rrbracket (\sigma) = (trans_{E} \llbracket expr \rrbracket (\sigma)).id
trans_{E}[\![expr_{1}[expr_{2}]]\!](\sigma) = trans_{E}[\![expr_{1}]\!](\sigma)[trans_{E}[\![expr_{2}]]\!](\sigma)]
trans_E[\![ *expr ]\!](\sigma) = *expr
trans_E[\![ **expr ]\!](\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_E \llbracket expr_1? (:expr_2)? (:expr_3)? \rrbracket(\sigma) = trans_E \llbracket expr_1 \rrbracket(\sigma)? (:trans_E \llbracket expr_2 \rrbracket(\sigma))? (:trans_E \llbracket expr_3 \rrbracket(\sigma))?
```

Comprehension

 $Comprehension \rightarrow$ 

 $trans_{O}$ 

```
trans_O \llbracket for expr_1 in expr_2 (if expr_3 \rrbracket^* \rrbracket (\sigma) = for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) (if trans_E \llbracket expr_3 \rrbracket (\sigma) )^*
               : ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\_1
 trans_{\overline{A}}: Alias list \rightarrow \Sigma \rightarrow \Sigma
trans_{\overline{A}} \llbracket \ alias_1 \ \dots \ alias_{n-1} \ alias_n \ \rrbracket (\sigma) = trans_A \llbracket \ alias_n \ \rrbracket (trans_A \llbracket \ alias_{n-1} \ \rrbracket (\dots \ trans_A \llbracket \ alias_1 \ \rrbracket (\sigma)))
 trans_A: Alias \rightarrow \Sigma \rightarrow
trans_A \llbracket id \rrbracket (\sigma) =
     LET id = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id]
     LET id = \text{keras} THEN \sigma[\text{"keras"} \mapsto id]
     LET id = os THEN \sigma["os" \mapsto id]
     LET id = \text{optimizers} THEN \sigma[\text{"optimizers"} \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
     LET id_1 = \text{tensorflow THEN } \sigma[\text{"tensor_flow"} \mapsto id_2]
     LET id_1 = tensorflow.keras THEN \sigma["keras" \mapsto id_2]
     LET id_1 = \text{os} THEN \sigma[\text{"os"} \mapsto id_2]
     LET id = \text{optimizers} THEN \sigma[\text{"optimizers"} \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 . id_2 (.id_3)^* \text{ (as } id_2)? \rrbracket (\sigma) = \sigma
 trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow (WithItem list \times \Sigma)
trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
     LET with_item<sub>1</sub>', \sigma_1 = trans_W \llbracket with_item_1 \rrbracket (\sigma) IN
     LET with_item<sub>2</sub>', \sigma_2 = trans_W \llbracket with_item_2 \rrbracket (\sigma_1) IN
     LET with\_item_n', \sigma_n = trans_W \llbracket with\_item_n \rrbracket (\sigma_{n-1}) IN
     (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
               : WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
 trans_W
trans_W \llbracket expr \rrbracket(\sigma) = (trans_E \llbracket expr \rrbracket(\sigma), \sigma)
trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (smodenv) =
     IF \sigma("tensor_flow") = id_1 AND expr_1 = id_1.GradientTape() AND expr_2 = id_2 THEN
          (expr_1 \text{ as } expr_2, \sigma[\text{"gradient\_tape"} \mapsto id_2])
     ELSE (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
 trans_C: MatchCase \rightarrow \Sigma \rightarrow MatchCase
```

```
trans_{C} \llbracket \text{ case } pattern \text{ (if } expr)? : stmt^* \rrbracket (\sigma) = \\ \text{ case } trans_{P} \llbracket pattern \rrbracket (\sigma) \text{ (if } trans_{E} \llbracket expr \rrbracket (\sigma))? : } trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\mathbf{1}
trans_{P} : Pattern \to \Sigma \to Pattern
trans_{P} \llbracket expr \rrbracket (\sigma) = trans_{E} \llbracket expr \rrbracket (\sigma)
trans_{P} \llbracket constant \rrbracket (\sigma) = constant
trans_{P} \llbracket pattern^* \rrbracket \rrbracket (\sigma) = \llbracket trans_{P} \llbracket pattern \rrbracket (\sigma)^* \rrbracket
trans_{P} \llbracket *(id)? \rrbracket (\sigma) = *(id)?
trans_{P} \llbracket *(id)? \rrbracket (\sigma) = *(id)?
trans_{P} \llbracket \{(expr : pattern)^* id?\} \rrbracket (\sigma) = \{(expr : trans_{P} \llbracket pattern \rrbracket (\sigma))^* id?\}
trans_{P} \llbracket expr \ (pattern_{1}^{*} \ (id = pattern_{2})^{*}) \ \rrbracket (\sigma) = expr \ (trans_{P} \llbracket pattern_{1} \rrbracket (\sigma)^{*} \ (id = trans_{P} \llbracket pattern_{2} \rrbracket (\sigma))^{*})
trans_{P} \llbracket (pattern \ as)? \ id \ \rrbracket (\sigma) = (trans_{P} \llbracket pattern \ \rrbracket (\sigma) \ as)? \ id
trans_{P} \llbracket pattern_{1} \ | \ pattern_{2} \ \rrbracket (\sigma) = trans_{P} \llbracket pattern_{1} \ \rrbracket (\sigma) \ | \ trans_{P} \llbracket pattern_{2} \ \rrbracket (\sigma)
trans_{P} \llbracket -  \rrbracket (\sigma) = -
```

## 2.4 Rule: TensorFlow 2.x GradientTape API Pattern

### 2.4.1 Transformation Rules

 $trans_M$ :  $Module \rightarrow Module$ 

```
trans_{M} \llbracket stmt^{*} \quad type\_ignore \rrbracket = trans_{\overline{S}} \llbracket stmt^{*} \rrbracket (\sigma).\_1 \quad type\_ignore
trans_{\overline{S}} : Stmt \quad list \rightarrow \Sigma \rightarrow (Stmt \quad list \times \Sigma)
trans_{\overline{S}} \llbracket stmt_{1} \quad stmt_{2} \dots stmt_{n} \rrbracket (\sigma) = \mathbf{LET} \quad stmt_{1}^{*'}, \sigma_{1} = trans_{S} \llbracket stmt_{1} \rrbracket (\sigma) \quad \mathbf{IN}
\mathbf{LET} \quad stmt_{2}^{*'}, \sigma_{2} = trans_{S} \llbracket stmt_{2} \rrbracket (\sigma_{1}) \quad \mathbf{IN}
\dots
\mathbf{LET} \quad stmt_{n}^{*'}, \sigma_{n} = trans_{S} \llbracket stmt_{n} \rrbracket (\sigma_{n-1}) \quad \mathbf{IN}
(stmt_{1}^{*'} @ stmt_{2}^{*'} @ \dots @ stmt_{n}^{*'}, \sigma_{n})
```

```
trans_S[ (@expr_1)^* \text{ async def } id (args) (-> expr_2)? : (\#type:s)? stmt^* ](\sigma) =
     ([(@expr_1)^* \text{ async def } id \text{ } (args) \text{ } (-> expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } trans_{\overline{S}}[stmt^*](\sigma)._1], \sigma)
 trans_{S}[(@expr_{1})^{*} class id (expr_{2}^{*} keyword^{*}) : stmt^{*}](\sigma) =
     ([(@expr_1)^* \text{ class } id \text{ } (expr_2^* \text{ } keyword^*) \text{ } : \text{ } trans_{\overline{S}}[[stmt^*]](\sigma)._1], \sigma) =
 trans_{S}[\![ return \ expr? \ ]\!](\sigma) = ([return \ (trans_{E}[\![ expr \ ]\!](\sigma))?], \sigma)
 trans_S[\![ delete \ expr^* \ ]\!](\sigma) = ([delete \ expr^*], \sigma)
A strict form of assignment statements
 trans_S \llbracket id_r = expr_1 \text{ ($expr_{11} \dots expr_{1n} \text{ ($id_1 = $)$? $expr_{21} \dots ($id_k = $)$? $expr_{2k}$) (#type:s)? } \rrbracket (\sigma) = rans_S \llbracket id_r = expr_1 \text{ ($expr_{11} \dots expr_{1n} \text{ ($id_1 = $)$? $expr_{21} \dots ($id_k = $)$? $expr_{2k}$)} \right]
     {f IF} expr_1<: tensorflow.keras.optimizers.schedules.LearningRateSchedule {f THEN}
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma[\text{"lr\_scheduler"} \mapsto id_r])
     IF expr_1 <: tensorflow.keras.optimizers.Optimizer THEN
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma["optimizer" \mapsto id_r])
     IF \sigma("tensor_flow") = id_t AND expr_1 = id_t.data.Dataset.expr_3 THEN
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma["dataset"\mapsto id_r])
     ELIF \sigma(\text{"tensor\_flow"}) = id_t \text{ AND } expr_1 = id_t.\text{train.Checkpoint THEN}
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?],
              \sigma["checkpoint"\mapsto id_r])
     ELIF \sigma(\text{"tensor_flow"}) = id_t \text{ AND } expr_1 = id_t.\text{optimizers.Adam THEN}
         IF id_i = learning_rate WHEN 1 \le i \le k THEN
              ([id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = expr_{2i} * hvd.size())
                  ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["optimizer" \mapsto id_r])
         ELSE
              ([id_r = expr_1 \ (expr_{11} * hvd.size() \ ... \ expr_{1n} \ (id_1 = )? \ expr_{21} \ ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                  \sigma["optimizer"\mapsto id_r])
     ELIF \sigma ("optimizers") = id_t AND expr_1 = id_t. Adam THEN
         IF id_i = learning_rate WHEN 1 \le i \le k THEN
              ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
                  ... (id_k = )? expr_{2k}) (#type:s)?], \sigma["optimizer" \mapsto id_r])
         ELSE
              ([id_r = expr_1 \ (expr_{11} * hvd.size() ... \ expr_{1n} \ (id_1 = )? \ expr_{21} ... \ (id_k = )? \ expr_{2k}) \ (\#type:s)?],
                  \sigma["optimizer" \mapsto id_r])
     ELIF \sigma ("optimizer") = id_t AND expr_1 = id_t.apply_gradients THEN
         IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
              LET id_z = \text{NewID}() IN
              ([id_z = expr_{2i},
              id_r = expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = id_z \dots (id_k = )? expr_{2k}) (#type:s)?,
              global hvd_broadcast_done,
```

```
if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
                 hvd.broadcast_variables(id_t.variables(), root_rank=0),
                 hvd\_broadcast\_done = True ]], \sigma)
         ELSE
             LET id_z = \text{NewID}() IN
             ([id_z = expr_{11},
             id_r = expr_1 \ (id_z \ expr_{12} \ \dots \ expr_{1n} \ \ (id_1 = )? \ expr_{21} \ \dots \ (id_k = )? \ expr_{2k}) \ (\#type:s)?,
             global hvd_broadcast_done,
             if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in <math>id_z], root\_rank=0),
                 hvd.broadcast_variables(id_t.variables(), root_rank=0),
                 hvd\_broadcast\_done = True ]], \sigma)
     ELIF \sigma("checkpoint") = id_t AND expr_1 = id_t.save THEN
         ([if hvd.rank() == 0: [id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 =)? expr_{21} ... (id_k =)? expr_{2k}) (#type:s)?]],
     ELIF \sigma(\text{``keras''}) = id_k \text{ AND } expr_1 = id_k.\text{models.Sequential } \text{THEN}
         ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_2 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma["model"\mapsto id_r])
     ELIF \sigma(\text{``keras''}) = id_t \text{ AND } expr_1 = id_t.\text{optimizers.Adam THEN}
         IF id_i = learning_rate WHEN 1 \le i \le k THEN
             ([id_r = expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} * hvd.size()
         ... (id_k = )? expr_{2k}) (#type:s)?
             id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{"optimizer"} \mapsto id_r])
         ELSE
             ([id_r = expr_1 (expr_{11} * hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}) (\#type:s)?
             id_r = \text{hvd.DistributedOptimizer}(id_r), \sigma[\text{``optimizer''} \mapsto id_r]
     ELSE ([id_r = trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_2 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma) (\#type:s)?],
             \sigma)
 trans_S[\![expr_0 = expr_1 (\#type:s)?]\!](\sigma) =
     IF \sigma(\text{``os''}) = id_{os} AND expr_0 = id_{os}.\text{environ [`CUDA_VISIBLE_DEVICES']}
     THEN ([], \sigma)
A general form of assignment statements except for the strict form
 trans_S[\![expr_1^* = expr_2 \text{ (#type:}s)?]\!](\sigma) = ([expr_1^* = trans_E[\![expr_2]\!](\sigma) \text{ (#type:}s)?], \sigma)
 trans_S[\![expr_1\ binop = expr_2\ ]\!](\sigma) = ([expr_1\ binop = trans_E[\![expr_2\ ]\!](\sigma)], \sigma)
 trans_S \llbracket expr_1 : expr_2 (= expr_3)? \rrbracket (\sigma) = ([expr_1 : expr_2 (= trans_E \llbracket expr_3 \rrbracket (\sigma))?], \sigma)
     IF expr_1 = id_1 AND \sigma(\text{"tensor\_flow"}) = id_2
     AND expr_3 = id_2.data.Dataset.expr_4 (expr_5^* keyword^*) THEN
         ([expr_1: expr_2 = expr_3 (\#type:s)?], \sigma["dataset" \mapsto id_1])
     ELSE ([expr_1 : expr_2 (= trans_E [expr_3 ](\sigma))?], \sigma)
 trans_S[\![ (\#type:s)? for \ expr_1 \ in \ expr_2 \ : \ stmt_1^* \ (else : \ stmt_2^*)? ]\!](\sigma) =
     ([(#type:s)? for expr_1 in trans_E \llbracket \ expr_2 \ \rrbracket(\sigma) :
         trans_{\overline{S}} \llbracket \ stmt_1^* \ \rrbracket (\sigma).\_1 \ \ (\texttt{else} \ : \ trans_{\overline{S}} \llbracket \ stmt_2^* \ \rrbracket (\sigma).\_1)? \rrbracket, \ \sigma)
```

```
trans_S \llbracket \text{ (#type:} s)? \text{ async for } expr_1 \text{ in } expr_2 : stmt_1^* \text{ (else : } stmt_2^*)? \rrbracket (\sigma) =
    ([(#type:s)? async for expr_1 in trans_E \llbracket expr_2 \rrbracket (\sigma) :
         trans_{\overline{S}}[\![stmt_1^*]\!](\sigma).\_1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma).\_1)?], \sigma)
trans_{S}[ while (expr) : stmt_{1}^{*} (else : stmt_{2}^{*})? [(\sigma) =
    ([while (trans_{\overline{S}}[\![expr]\!](\sigma)) : trans_{\overline{S}}[\![stmt_1^*]\!](\sigma)._1 (else : trans_{\overline{S}}[\![stmt_2^*]\!](\sigma)._1)?], \sigma)
trans_{S}[\![ if (expr) : stmt^* (else : stmt^*)? [\![ (\sigma) =
    ([\text{if }(trans_E[\![expr]\!](\sigma)) : trans_{\overline{S}}[\![stmt^*]\!](\sigma).\_1 \ (\text{else }: trans_{\overline{S}}[\![stmt^*]\!](\sigma).\_1)?], \sigma)
trans_{S}[ (\#type:s)? \text{ with } with\_item^* : stmt^* ] (\sigma) =
    LET with_item*', \sigma_1 = trans_{\overline{W}} \llbracket with_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}} [stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
         ([(\#type:s)? with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? with with\_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![ (\#type:s)?  async with with\_item^* : stmt^* ]\!](\sigma) =
    LET with\_item^{*\prime}, \sigma_1 = trans_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) IN
    LET stmt^{*\prime}, \sigma_2 = trans_{\overline{S}}[stmt^*](\sigma_1) IN
    IF \sigma_1 \setminus \sigma = ["gradient\_tape" \mapsto id] THEN
         ([(#type:s)? async with with\_item^{*\prime} : stmt^{*\prime},
         id = hvd.DistributedGradientTape(id), \sigma_2
    ELSE ([(#type:s)? async with with_item^{*\prime} : stmt^{*\prime}], \sigma_2)
trans_{S}[\![match\ expr\ :\ match\_case^*\ ]\!](\sigma) =
    ([match trans_E[\![expr]\!](\sigma) : (trans_C[\![match\_case]\!](\sigma))^*], \sigma)
trans_S[ raise expr_1? (from expr_2)? [(\sigma) = ([raise expr_1? (from <math>expr_2)?], \sigma)
trans_S[[ try : stmt_1^* | exc\_handler^* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
    ([try : trans_{\overline{S}}[stmt_1^*]](\sigma)._1 (trans_H[exc\_handler](\sigma))^*
    (else : trans_{\overline{S}} [stmt_2^*](\sigma).1)? (finally : trans_{\overline{S}} [stmt_3^*](\sigma).1)?], \sigma)
trans_{S} assert expr_{1} expr_{2}? \|(\sigma) = ([assert \ trans_{E} \| \ expr_{1} \ \|(\sigma) - expr_{2}?], \sigma)
```

```
trans_S import alias^* (\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
       ([import alias*,
       import horovod.tensorflow as hvd,
       hvd_broadcast_done = False,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
 trans_S[\![\!] import \ alias^* ]\![\![\!](\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
    IF \sigma_1 \setminus \sigma = [\text{"tensor\_flow"} \mapsto id] THEN
       ([import alias*,
       import horovod.tensorflow as hvd,
       hvd.init(),
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([import alias^*], \sigma_1)
 trans_{S}[\![from \ i \ id? \ import \ alias^*]\!](\sigma) =
    LET \sigma_1 = trans_{\overline{A}} [\![ alias^* ]\!] (\sigma) IN
    IF id = \text{tensorflow AND } \sigma_1 \setminus \sigma = [\text{"keras"} \mapsto id] THEN
       ([from i id? import alias^*,
       import horovod.tensorflow.keras as hvd,
       hvd.init().
       gpus = id.config.experimental.list_physical_devices('GPU'),
       for gpu in gpus: id.config.experimental.set_memory_growth(gpu, True),
       if gpus: id.config.experimental.set_visible_devices(gpus[hvd.local_rank()], 'GPU')], \sigma_1)
    ELSE ([from i id? import alias^*], \sigma_1)
 trans_S[\![global\ id^*]\!](\sigma) = ([global\ id^*], \sigma)
 trans_S[\![ nonlocal id^* ]\!](\sigma) = ([nonlocal id^*], \sigma)
A strict form of expr statements
 trans_S[\![expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k})]\!](\sigma) =
     IF \sigma(\text{"optimizer"}) = id_t AND expr_1 = id_t.apply_gradients THEN
        IF id_i = grads\_and\_vars WHEN 1 \le i \le k THEN
            LET id_z = \text{NewID}() IN
            ([id_z = expr_{2i},
```

```
expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots id_i = id_z \dots (id_k = )? expr_{2k}),
      global hvd_broadcast_done,
      if not hvd_broadcast_done: [hvd.broadcast\_variables([x[1] for x in id_z], root\_rank=0),
          hvd.broadcast_variables(id_t.variables(), root_rank=0),
         hvd\_broadcast\_done = True ]], \sigma)
   ELSE
      LET id_z = NewID() IN
      ([id_z = expr_{11},
      expr_1 (id_z expr_{12} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}),
      global hvd_broadcast_done,
      if not hvd_broadcast_done: [hvd.broadcast_variables([x[1] for x in id_z], root_rank=0),
         hvd.broadcast_variables(id_t.variables(), root_rank=0),
         hvd\_broadcast\_done = True ]], \sigma)
ELIF expr_1 = print OR expr_1 = expr.write OR expr_1 = expr.summary OR
   expr_1 = expr.save_weights OR expr_1 = expr.load_weights THEN
      ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
ELIF \sigma("checkpoint") = id_t AND expr_1 = id_t.save THEN
   ([if hvd.rank() == 0: [expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})]], \sigma)
ELIF \sigma(\text{``model''}) = id_t \text{ AND } expr_1 = id_t.\text{fit THEN}
   IF id_i = verbose WHEN 1 \le i \le k THEN
      IF id_i = callbacks WHEN 1 \le j \le k THEN
          ([callback = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)]
          if hvd.rank() == 0: callbacks.append(expr_{2j})
          expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = 1 if hvd.rank() == 0 else 0
          ... id_i = \text{callbacks} ... (id_k = )? expr_{2k}), \sigma
      ELSE
          ([expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots
             id_i = 1 if hvd.rank() == 0 else 0 ... (id_k = )? expr_{2k}
             callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)])], \sigma)
   ELSE
      IF id_i = callbacks WHEN 1 \le j \le k THEN
          ([callback = [hvd.callbacks.BroadcastGlobalVariablesCallback(root_rank=0)]
          if hvd.rank() == 0: callbacks.append(expr_{2j})
          expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_j = callbacks ... (id_k = )? expr_{2k}
             verbose = 1 if hvd.rank() == 0 else 0), \sigma)
      ELSE
          ([expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
             verbose = 1 if hvd.rank() == 0 else 0
             callbacks = [hvd.callbacks.BroadcastGlobalVariablesCallback(0)])], \sigma)
ELIF \sigma(\text{``model''}) = id_t \text{ AND } expr_1 = id_t.\text{compile THEN}
   IF id_i = optimizer AND expr_{2i} = "adam" WHEN 1 \le i \le k THEN
      (id_z = tf.optimizers.Adam(learning_rate=0.001 * hvd.size())
      id_z = hvd.DistributedOptimizer(id_z)
      expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = id_z ... (id_k = )? expr_{2k})], \sigma)
```

```
ELIF expr_{11} = "adam" THEN
                ([id_z = tf.optimizers.Adam(learning_rate=0.001 * hvd.size()))
                id_z = hvd.DistributedOptimizer(id_z)
                expr_1 (id_z ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k}), \sigma)
           ELSE
                [trans_{E}[\![ expr_{1} \ (expr_{11} \ ... \ expr_{1n} \ (id_{1} = )? \ expr_{21} \ ... \ (id_{k} = )? \ expr_{2k}) \ ]\!](\sigma)], \ \sigma)
      ELIF expr_1 = model.summary THEN
           ([if hvd.rank() == 0: expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})], \sigma)
      ELSE
           [trans_E \parallel expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \parallel (\sigma)], \sigma)
A general form of expr statements except for the strict form
 trans_S \llbracket expr \rrbracket (\sigma) = ([trans_E \llbracket expr \rrbracket (\sigma)], \sigma)
 trans_S[\![ pass ]\!](\sigma) = ([pass], \sigma)
 trans_S break (\sigma) = ([break], \sigma)
 trans_S[\![ continue ]\!](\sigma) = ([continue], \sigma)
  trans_E : Expr \rightarrow \Sigma \rightarrow Expr
 trans_{E} \llbracket expr_{1} := expr_{2} \rrbracket (\sigma) = expr_{1} := trans_{E} \llbracket expr_{2} \rrbracket (\sigma)
 trans_{E}[\![expr_{1} \quad binop \quad expr_{2} \ ]\!](\sigma) = trans_{E}[\![expr_{1} \ ]\!](\sigma) \quad binop \quad trans_{E}[\![expr_{2} \ ]\!](\sigma)
 trans_{E}[\![unop\ expr\ ]\!](\sigma) = unop\ trans_{E}[\![expr\ ]\!](\sigma)
 trans_{E}[\![ ] ] lambda args: expr[\![ ] ](\sigma) = lambda <math>args: trans_{E}[\![ ] ] expr[\![ ] ](\sigma)
 trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
      trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
 trans_{E} \llbracket expr_{1} \text{ if } expr_{2} \text{ else } expr_{3} \rrbracket (\sigma) =
      trans_{E} \llbracket expr_{1} \rrbracket (\sigma) if trans_{E} \llbracket expr_{2} \rrbracket (\sigma) else trans_{E} \llbracket expr_{3} \rrbracket (\sigma)
 trans_{E}[\{(expr_{1}: expr_{2})^{*} \ (**expr_{3})^{*}\}] (\sigma) = \{(expr_{1}: trans_{E}[[expr_{2}]](\sigma))^{*} \ (**expr_{3})^{*}\}]
 trans_E[\![\{expr^*\}]\!](\sigma) = \{(trans_E[\![expr]\!](\sigma))^*\}
```

```
trans_E \llbracket [expr^*] \rrbracket (\sigma) = \llbracket (trans_E \llbracket expr \rrbracket (\sigma))^* \rrbracket
trans_E \llbracket (expr^*) \rrbracket (\sigma) = ((trans_E \llbracket expr \rrbracket (\sigma))^*)
trans_E[\![\{expr_1: expr_2 : comprehension^*\}]\!](\sigma) = \{expr_1: trans_E[\![\ expr_2\ ]\!](\sigma) : (trans_O[\![\ comprehension]\!](\sigma))^*\}
trans_E[\![\{expr\ comprehension^*\}\]](\sigma) = \{trans_E[\![\ expr\]](\sigma)\ (trans_O[\![\ comprehension]\!](\sigma))^*\}
trans_E[\![expr\ comprehension^*]\!](\sigma) = [trans_E[\![expr\ ]\!](\sigma)\ (trans_O[\![comprehension]\!](\sigma))^*]
trans_{E} \llbracket (expr \ comprehension^*) \ \rrbracket (\sigma) = (trans_{E} \llbracket \ expr \ \rrbracket (\sigma) \ (trans_{O} \llbracket comprehension \rrbracket (\sigma))^*)
trans_{E}[\![ await \ expr \ ]\!](\sigma) = await \ trans_{E}[\![ \ expr \ ]\!](\sigma)
trans_E yield expr? \ \|(\sigma) = \text{yield } (trans_E \ expr \ \|(\sigma))?
trans_{E}[\![\!] yield from expr[\![\!](\sigma) = yield from trans_{E}[\![\!]\!] expr[\![\!](\sigma)
trans_{E}[\![expr_{1}\ (compop\ expr_{2})^{*}\ ]\!](\sigma) = trans_{E}[\![expr_{1}\ ]\!](\sigma)\ (compop\ trans_{E}[\![expr_{2}\ ]\!](\sigma))^{*}
trans_{E}[\![expr_{1} (expr_{11} ... expr_{1n} (id_{1} = )? expr_{21} ... (id_{k} = )? expr_{2k})]\!](\sigma) =
     IF \sigma(\text{``dataset"}) = id_t \text{ AND } expr_1 = id_t.\text{take THEN}
           IF id_i = \text{count} WHEN 1 \le i \le k THEN
                expr_1 (expr_{11} ... expr_{1n} (id_1 = )? expr_{21} ... id_i = expr_{2i} // hvd.size() ... (id_k = )? expr_{2k})
           ELSE
                expr_1 (expr_{11} // hvd.size() ... expr_{1n} (id_1 = )? expr_{21} ... (id_k = )? expr_{2k})
     ELSE
           trans_{E} \llbracket expr_{1} \rrbracket (\sigma) \ (trans_{E} \llbracket expr_{11} \rrbracket (\sigma) \ ... \ trans_{E} \llbracket expr_{1n} \rrbracket (\sigma)
                (id_1 = )? \ trans_E \llbracket \ expr_{21} \ \rrbracket (\sigma) \ ... \ (id_k = )? \ trans_E \llbracket \ expr_{2k} \ \rrbracket (\sigma))
trans_{E}[\![\{expr_{1} \quad (!i)? \quad (:expr_{2})?\}]\!](\sigma) = \{expr_{1} \quad (!i)? \quad (:expr_{2})?\}
trans_E \llbracket expr^* \rrbracket (\sigma) = expr^*
trans_E \llbracket constant \rrbracket (\sigma) = constant
trans_E \llbracket expr.id \rrbracket (\sigma) = (trans_E \llbracket expr \rrbracket (\sigma)).id
trans_{E}[\![expr_{1}[expr_{2}]]\!](\sigma) = trans_{E}[\![expr_{1}]\!](\sigma)[trans_{E}[\![expr_{2}]]\!](\sigma)]
```

```
trans_E \llbracket *expr \rrbracket (\sigma) = *expr
trans_E \llbracket **expr \rrbracket (\sigma) = **expr
trans_E \llbracket id \rrbracket (\sigma) = id
trans_{E} \llbracket expr_{1}? (:expr_{2})? (:expr_{3})? \rrbracket(\sigma) = trans_{E} \llbracket expr_{1} \rrbracket(\sigma)? (:trans_{E} \llbracket expr_{2} \rrbracket(\sigma))? (:trans_{E} \llbracket expr_{3} \rrbracket(\sigma))?
 trans_O: Comprehension \rightarrow \Sigma \rightarrow Comprehension
trans_O \llbracket for expr_1 in expr_2 (if expr_3)* \rrbracket(\sigma) = for expr_1 in trans_E \llbracket expr_2 \rrbracket(\sigma) (if trans_E \llbracket expr_3 \rrbracket(\sigma))*
 trans_H: ExcHandler \rightarrow \Sigma \rightarrow ExcHandler
trans_H \llbracket \text{ except } expr? \text{ (as } id)? : stmt^* \rrbracket (\sigma) = \text{except } expr? \text{ (as } id)? : trans_{\overline{S}} \llbracket stmt^* \rrbracket (\sigma).\_1
 trans_{\overline{A}}: Alias list \rightarrow \Sigma \rightarrow \Sigma
trans_{\overline{A}} \llbracket \ alias_1 \ \dots \ alias_{n-1} \ alias_n \ \rrbracket (\sigma) = trans_A \llbracket \ alias_n \ \rrbracket (trans_A \llbracket \ alias_{n-1} \ \rrbracket (\dots \ trans_A \llbracket \ alias_1 \ \rrbracket (\sigma)))
                                                     \sum
 trans_A: Alias \rightarrow
                                        \Sigma \rightarrow
trans_A \llbracket id \rrbracket (\sigma) =
     LET id = \text{tensorflow THEN } \sigma[\text{"tensor\_flow"} \mapsto id]
     LET id = \text{keras THEN } \sigma[\text{"keras"} \mapsto id]
     LET id = os THEN \sigma["os" \mapsto id]
     LET id = \text{optimizers} THEN \sigma[\text{"optimizers"} \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 \text{ as } id_2 \rrbracket (\sigma) =
     LET id_1 = \text{tensorflow THEN } \sigma[\text{"tensor\_flow"} \mapsto id_2]
     LET id_1 = tensorflow.keras THEN \sigma["keras" \mapsto id_2]
     LET id_1 = os THEN \sigma["os" \mapsto id_2]
     LET id = \text{optimizers} THEN \sigma[\text{"optimizers"} \mapsto id]
     ELSE \sigma
trans_A \llbracket id_1 . id_2 (.id_3)^* \text{ (as } id_2)? \rrbracket (\sigma) = \sigma
 trans_{\overline{W}}: WithItem list \rightarrow \Sigma \rightarrow (WithItem list \times \Sigma)
trans_{\overline{W}} \llbracket with\_item_1 \ with\_item_2 \ ... \ with\_item_n \ \rrbracket(\sigma) =
     LET with\_item_1', \sigma_1 = trans_W \llbracket with\_item_1 \rrbracket (\sigma) IN
     LET with\_item_2', \sigma_2 = trans_W \llbracket with\_item_2 \rrbracket (\sigma_1) IN
     LET with\_item_n', \sigma_n = trans_W[with\_item_n](\sigma_{n-1}) IN
     (with\_item_1' :: with\_item_2' :: ... :: [with\_item_n'], \sigma_n)
```

```
trans_W: WithItem \rightarrow \Sigma \rightarrow (WithItem \times \Sigma)
trans_W \llbracket expr \rrbracket(\sigma) = (trans_E \llbracket expr \rrbracket(\sigma), \sigma)
trans_W \llbracket expr_1 \text{ as } expr_2 \rrbracket (smodenv) =
     IF \sigma("tensor_flow") = id_1 AND expr_1 = id_1.GradientTape() AND expr_2 = id_2 THEN
           (expr_1 \text{ as } expr_2, \sigma[\text{"gradient\_tape"} \mapsto id_2])
     ELSE (trans_E \llbracket expr_1 \rrbracket (\sigma) \text{ as } expr_2, \sigma)
                       MatchCase \rightarrow \Sigma \rightarrow MatchCase
 trans_C
trans_{C} \llbracket \text{ case } pattern \text{ (if } expr)? : stmt^* \rrbracket (\sigma) =
      case trans_{P}[\![pattern\ ]\!](\sigma) (if trans_{E}[\![expr\ ]\!](\sigma))? : trans_{\overline{S}}[\![stmt^*\ ]\!](\sigma)._1
 \overline{trans_P} : Pattern \rightarrow \Sigma \rightarrow Pattern
trans_{P}[\![ expr \ ]\!](\sigma) = trans_{E}[\![ expr \ ]\!](\sigma)
trans_P \llbracket constant \rrbracket (\sigma) = constant
trans_P[\![pattern^*]\!](\sigma) = [trans_P[\![pattern]\!](\sigma)^*]
trans_P \llbracket *(id)? \rrbracket (\sigma) = *(id)?
trans_P \llbracket \{(expr : pattern)^* \ id?\} \rrbracket (\sigma) = \{(expr : trans_P \llbracket pattern \rrbracket (\sigma))^* \ id?\} 
trans_P \llbracket expr \ (pattern_1^* \ (id = pattern_2)^*) \ \rrbracket (\sigma) = expr \ (trans_P \llbracket pattern_1 \rrbracket (\sigma)^* \ (id = trans_P \llbracket pattern_2 \rrbracket (\sigma))^*)
trans_P \llbracket (pattern \ as)? \ id \ \rrbracket(\sigma) = (trans_P \llbracket pattern \ \rrbracket(\sigma) \ as)? \ id
trans_P \llbracket pattern_1 \mid pattern_2 \rrbracket(\sigma) = trans_P \llbracket pattern_1 \rrbracket(\sigma) \mid trans_P \llbracket pattern_2 \rrbracket(\sigma)
trans_P \llbracket \ \_ \ \rrbracket(\sigma) = \_
```

## 3 Identifying training loop

## 3.1 Restrictions

- 1. Training loop must be defined in only one file.
- 2. Training loop type is either distributed gradient tape or distributed optimizer.
- 3. Each model must have only one type of training loop.
- 4. Function must not be assigned to the variables or passed as an argument.

5. Training loop must not be defined conditionally.

#### 3.2 Rules

### 3.2.1 Summary

```
Summary ::=
                   ModuleSummary id \sigma_{\top} tl (ModuleSummary)
                   FuncSummary tl
                                                  (FuncSummary)
                   ClassSummary arg
                                                  (CLASSSUMMARY)
                   {\tt ValueSummary}\ s
                                                  (ValueSummary)
             ::= Model \mid \bot
                                                  (ARG)
arg
tl
                   GradTape \mid Optimizer \mid \bot \quad (TrainingLoop)
                   \sigma \cup \top
\sigma_{\top}
             ::=
```

 $\sigma \in \Sigma = Id \stackrel{\text{fin}}{\to} Summary$  Environment storing mappings from ids to summaries

### 3.2.2 Training Loop

```
: Module \rightarrow \Sigma \rightarrow
                                                         Module Summary
 summary_M
summary_M \llbracket id \ stmt^* \ type\_ignore \rrbracket =
     LET \sigma, tl = summary_{\overline{S}}[stmt^*](\sigma) IN
     ModuleSummary id \sigma tl
 summary_{\overline{S}} : Stmt list
                                          \rightarrow \Sigma \rightarrow (\Sigma \times tl)
summary_{\overline{S}}[\![\![ stmt_1 \quad stmt_2 \dots stmt_n \ ]\!](\sigma) = \mathbf{LET} \quad \sigma_1, tl_1 = summary_S[\![\![ stmt_1 \ ]\!](\sigma) \quad \mathbf{IN}
                                                                   LET \sigma_2, tl_2 = summary_{\overline{S}}[\![stmt_2]\!](\sigma_1) IN
                                                                   LET \sigma_n, tl_n = summary_{\overline{S}}[\![ stmt_n ]\!](\sigma_{n-1}) IN
                                                                   (\sigma_n, tl_1 \sqcup tl_2 \sqcup \ldots tl_n)
 summary_S: Stmt \rightarrow \Sigma \rightarrow (\Sigma \times tl)
summary_S \llbracket (@expr_1)^* \text{ def } id \text{ } (args) \text{ } (-\text{>} expr_2)? \text{ } : \text{ } (\#type:s)? \text{ } stmt^* \rrbracket (\sigma) =
     LET \sigma', tl = summary_{\overline{S}} [stmt^*] IN
     (\sigma[id \mapsto \texttt{FuncSummary}\ tl], \perp)
summary_S \llbracket (@expr_1)^*  async def id (args) (-> expr_2)? : (\#type:s)? stmt^* \rrbracket (\sigma) =
     LET \sigma', tl = summary_{\overline{S}} [stmt^*] IN
     (\sigma[id \mapsto \texttt{FuncSummary}\ tl], \perp)
summary_S[(@expr)^* \text{ class } id \ (expr_{11} \dots expr_{1n} \ (id_1 = )? \ expr_{21} \dots (id_k = )? \ expr_{2k}) : stmt^*](\sigma) =
     IF expr_{1i} = id_c.keras.Model WHEN 1 \le i \le n AND
         \sigma(id_c) = \text{ModuleSummary Id}("tensorflow") [] \perp \textbf{THEN} (\sigma[id \mapsto \texttt{ClassSummary } Model], \bot)
    ELIF expr_{2i} = id_c.keras.Model WHEN 1 \le i \le k AND
         \sigma(id_c) = \text{ModuleSummary Id}(\text{"tensorflow"}) \quad [] \perp \text{THEN} \quad (\sigma[id \mapsto \text{ClassSummary } Model], \perp)
     ELSE (\sigma[id \mapsto \text{ClassSummary } \bot], \bot)
```

```
summary_S \llbracket id_r = id_c \text{ () (\#type:}s)? \rrbracket (\sigma) =
     IF \sigma(id_c) = \text{ClassSummary } Model \text{ THEN } (\sigma[id_r \mapsto \text{ValueSummary "model_instance"}], \bot)
     ELSE (\sigma, \perp)
LET _-, tl = summary_{\overline{S}} [\![ stmt_1^* ]\!](\sigma) IN
     (\sigma, tl)
summary_S[\![ (\#type:s)?  async for expr_1 in expr_2: stmt_1^* (else: stmt_2^*)? ]\![ (\sigma) =
     LET __, tl = summary_{\overline{S}} [\![ stmt_1^* ]\!](\sigma) IN
     (\sigma, tl)
summary_S[\![ while (expr) : stmt_1^* (else : stmt_2^*)? ]\![(\sigma) =
     LET __, tl = summary_{\overline{S}} [stmt_1^*](\sigma) IN
     (\sigma, tl)
summary_S \llbracket \text{ (#type:}s)? \text{ with } with\_item^* : stmt^* \rrbracket (\sigma) =
     LET _-, tl = summary_{\overline{S}} [stmt^*](\sigma) IN
     (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
summary_{S}[ (\#type:s)?  async with with\_item^* : stmt^* ][(\sigma) =
     LET _, tl = summary_{\overline{S}}[stmt^*](\sigma) IN
     (\sigma, summary_{\overline{W}} \llbracket with\_item^* \rrbracket (\sigma) \sqcup tl)
summary_S[ try : stmt_1^* exc_handler* (else : stmt_2^*)? (finally : stmt_3^*)? ](\sigma) =
     (\sigma, summary_{\overline{S}} \llbracket stmt_1^* \rrbracket (\sigma))
summary_S[\![\!] import \ alias^* ]\!](\sigma) = (summary_A[\![\!]\!] alias^* ]\!](\sigma), \perp)
summary_S \llbracket \text{ from } 0 \quad id^* \quad \text{import } alias^* \, \rrbracket(\sigma) =
     LET \sigma' = summary_{\overline{A}} [\![ alias^* ]\!](\sigma) IN
     LET [id_2 \mapsto \texttt{ModuleSummary} \ id_2 \ \sigma_2 \ \bot, \ id_2 \mapsto \texttt{ModuleSummary} \ id_2 \ \sigma_2 \ \bot,
          ... id_n \mapsto \text{ModuleSummary } id_n \sigma_n \perp] = \sigma' \setminus \sigma \text{ IN}
     \sigma ++ [id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot, \ id_2 \mapsto \texttt{ModuleSummary} \ (id^*+id_2) \ \sigma_2 \ \bot,
          ... id_n \mapsto \text{ModuleSummary } (id^* + id_n) \ \sigma_n \ \bot]
summary_S \llbracket expr \rrbracket (\sigma) = (\sigma, summary_E \llbracket expr \rrbracket (\sigma))
summary_S \llbracket stmt \rrbracket (\sigma) = (\sigma, \bot)
 summary_{\overline{A}}: Alias list \rightarrow \Sigma \rightarrow \Sigma
summary_{\overline{A}} \llbracket \ alias_1 \ ... \ alias_{n-1} \ alias_n \ \rrbracket (\sigma) =
     summary_A \llbracket alias_n \rrbracket (summary_A \llbracket alias_{n-1} \rrbracket (... \ summary_A \llbracket alias_1 \rrbracket (\sigma) \ ...))
```

A strict form of assignment statements

```
trans_A : Alias \rightarrow \Sigma \rightarrow \Sigma
 trans_A \llbracket id_1 id_2 \dots id_n \rrbracket (\sigma) =
      LET \sigma_n = [id_n \mapsto \texttt{ModuleSummary} \ id_n \ \top \ \bot]
      \mathbf{LET} \ \sigma_{n-1} = [id_{n-1} \mapsto \mathtt{ModuleSummary} \ id_{n-1} \ \sigma_n \ \bot]
      LET \sigma_2 = [id_2 \mapsto \texttt{ModuleSummary} \ id_2 \quad \sigma_3 \quad \bot]
      \mathbf{LET} \ \sigma_1 = [id_1 \mapsto \mathtt{ModuleSummary} \ id_1 \ \sigma_2 \ \bot]
      \sigma ++ \sigma_1
  summary_{\overline{W}} : WithItem\ \mathbf{list} \rightarrow \Sigma \rightarrow tl
 summary_{\overline{W}}[\![with\_item_1\ with\_item_2\ ...\ with\_item_n\ ]\!](\sigma) =
      summary_W \llbracket with\_item_1 \rrbracket (\sigma) \sqcup summary_W \llbracket with\_item_2 \rrbracket (\sigma) \sqcup \dots \quad summary_W \llbracket with\_item_n \rrbracket (\sigma) 
  summary_W : WithItem \rightarrow \Sigma \rightarrow tl
 summary_W \llbracket expr_1 \text{ as } expr_2? \rrbracket (\sigma) = summary_E \llbracket expr_1 \rrbracket (\sigma)
  summary_E : Expr \rightarrow \Sigma
A strict form of call expression
 summary_E \llbracket expr_1 (expr_{11} \dots expr_{1n} (id_1 = )? expr_{21} \dots (id_k = )? expr_{2k}) \rrbracket (\sigma) =
      IF \sigma(id_r) = ValueSummary "model_instance" AND
           expr_1 = id_r.fit THEN Optimizer
      ELIF \sigma(id_r) = ModuleSummary Id("tensorflow") \sigma' tl AND
           expr_1 = id_r.GradientTape THEN GradTape
      \mathbf{ELIF} \sigma(id_r) = FuncSummary tl \mathbf{AND}
           expr_1 = idr THEN tl
      ELSE \perp
 summary_E \llbracket expr \rrbracket (\sigma) = \bot
```