Problem 4

We have multiple robots that can generate point clouds such as those coming from a RealSense camera. In many cases we want to use the robots to detect objects in its environment. We provide three data files:

- (a) Empty2.asc which containts a data for an empty table
- (b) TableWithObjects2.asc contains point cloud for a cluttered table
- (c) hallway1b.asc contains data from a hallway

Each file has the point cloud file in a format with each line contains xi yi zi. You can use np.loadtxt to load a pointcloud into a numpy array.

Problem 4: Part 1

Provide a method to estimate the plane parameter for the table. Test it both with the empty and cluttered table. Describe how you filter out the data from the objects. You have to be able to estimate the table parameters in the presence of clutter.

Solution:

The general equation of a plane can be written as follows:

$$a(x - x_0) + b(y - y_0) + c(z - z_0) = 0$$

$$ax + by + cz = ax_0 + by_0 + cz_0; d = ax_0 + by_0 + cz_0$$

$$ax + by + cz = d$$

where,

n is the normal vector of the plane, < a, b, c >.

The plane equation can also be re-written in this form:

$$ax + by - d = -cz$$

$$-\frac{a}{c}x - \frac{b}{c}y + \frac{d}{c} = z$$

$$Ax + By + C = z$$

The re-written normal vector of the plane, n became $\langle A, B, -1 \rangle$.

The distance between a point and the plane, d can be calculated as shown below:

$$v = \begin{bmatrix} x_i - \bar{x} & y_i - \bar{y} & z_i - \bar{z} \end{bmatrix}$$

$$\hat{n} = \frac{1}{||n||} \begin{bmatrix} A \\ B \\ -1 \end{bmatrix}$$

$$d = |v \cdot \hat{n}|$$

where,

 \hat{n} is the normalized normal vector of the plane

 \bar{x} is the average of the x-coordinate

 \bar{y} is the average of the y-coordinate

 \bar{z} is the average of the z-coordinate

||n|| is the norm of the normalized normal vector of the plane

The least square plane fitting is a common method to estimate plane parameters with a given point cloud, even when the data are a little noisy. However, if the point cloud consists of many outliers, the least square fitting method might not be sufficiently robust to estimate plane parameters, and outliers will lower the quality of the plane fitting process. Hence, to improve the quality and robustness of the plane fitting process, the random sample consensus (RANSAC) plane fitting method is used to estimate the dominant plane parameters of the empty table, and the table with objects even though there are outliers in the point cloud.

Since the RANSAC method is considered as a heuristics algorithm, the RANSAC algorithm will iterate several thousands of times to perform least square plane fitting with a set of randomly selected 3 points from the point cloud data. If the distance between a point and the fitted plane, d, is less than or equal to the acceptable distance between a point and the fitted plane, $d_{threshold}$, then the point is an inliers; otherwise, the point is an outlier. Besides that, the RANSAC algorithm will also count the number inliers; if the current number of inliers is larger than the previous iteration, the algorithm will store the best set of inliers and store the outliers separately. Lastly, the RANSAC algorithm will output the normalized normal vector of the fitted plane, normalized coefficient C, the average of the points, and the distance between a point and the plane for every points, inliers, and outliers. Hence, the RANSAC algorithm successfully filter out the outliers from the point cloud.

```
In [63]: import matplotlib
         import numpy as np
         import matplotlib.pyplot as plt
         import mpl_toolkits.mplot3d
         from mpl_toolkits.mplot3d import Axes3D
         import random
         %matplotlib notebook
         ### Problem 4 Part 1: Use Random Sample Consensus (RANSAC) Algorithm for Plane Detection in
                               the Empty and Clutter Table Point Cloud Data
         # Load Empty Table and Table with Objects files
         empty_Table_pts = np.loadtxt("Empty2.asc")
         table_with_Obj_pts = np.loadtxt("TableWithObjects2.asc")
         # Store Empty Table x, y, z coordinates
         #empty_Table_x = empty_Table_pts[:,0]
         #empty_Table_y = empty_Table_pts[:,1]
         #empty_Table_z = empty_Table_pts[:,2]
         # Store Table with Objects x, y, z coordinates
         #table_with_Obj_x = table_with_Obj_pts[:,0]
         #table_with_Obj_y = table_with_Obj_pts[:,1]
         #table_with_Obj_z = table_with_Obj_pts[:,2]
         ### User-defined Plane Fitting with Least Square Method Function
         ## Input : 3D-points (m x 3)
         ## Outputs: normal_vec_normalized - normalized normal vector of the fitted plane (1 x 3)
         ##
                     coeff C normalized - Coefficient C from the equation Ax + By + C = z
         ##
                     mean point
                                           - Average of the points (1 x 3)
         ##
                     dist pt2pl
                                           - Distance between a point and the plane (m x 1)
         def LSQ_plane_fitting(points_3D):
             Pseudocode:
                 1.) Construct Matrix A, [x_i, y_i, 1] (m x 3)
                 2.) Construct Z Vector, [z_i] (m x 1)
                 3.) Call numpy built-in linear regression to find the coefficients A, B, and C
                     from the plane equation, Ax + By + C = z
                 4.) Nomalize the plane equation
                 5.) Determine distance between a point and the fitted plane for every points, dist pt2pl
                 6.) Output normalized normal vector, normalized coefficient C, average point, dist pt2pl
             # Determine total number of points
             tot num pts = points 3D.shape[0]
             # Determine the number of dimensions
             num dims = points 3D.shape[1]
             \# Ax = b \Rightarrow An = Z
             # Initialize matrix A, [x_i, y_i, 1]
             A = np.ones((tot_num_pts, num_dims))
             A[:, 0] = points_3D[:, 0] # Pass x-coordinates to matrix A
             A[:, 1] = points_3D[:, 1] # Pass y-coordinates to matrix A
             # Initialize Z column vector [z_i]
             Z = np.zeros((tot_num_pts, 1))
             Z[:, 0] = points 3D[:, 2]
             # Perform Least Square plane fitting
             coeffs, _, _, _ = np.linalg.lstsq(A, Z, rcond = None)
             # Normal Vector of the Plane [A, B, -1]
             normal\_vec = (coeffs[0][0], coeffs[1][0], -1)
             # Coefficient C
             coeff C = coeffs[2][0]
             # Normalized the plane equation
             normal_norm = np.linalg.norm(normal_vec) # Norm of the normal vector
             normal_vec_normalized = normal_vec / normal_norm
             # Normalized the Coefficient C
             coeff_C_normalized = coeff_C / normal_norm
             # Determine the mean point from the plane
             mean point = np.mean(points 3D, axis=0)
```

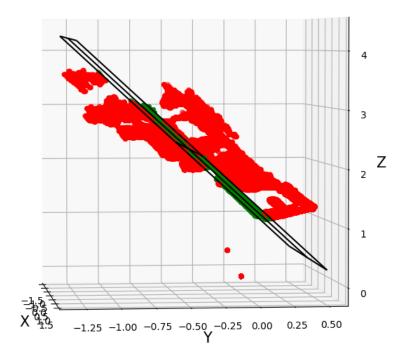
```
# Calculate the distance between a point and the fitted plane for every points
   dist_pt2pl = abs(np.dot(points_3D-mean_point, normal_vec_normalized))
   return normal vec normalized, coeff_C_normalized, mean_point, dist_pt2pl
### LSQ_plane_fitting() function print test
#normal_vec_normalized, coeff_C_normalized, mean_point, dist = LSQ_plane_fitting(empty_Table_pts)
#print(normal_vec_normalized, coeff_C_normalized, mean_point, dist)
### User-defined Random Sample Consensus (RANSAC) Function
## Input : 3D-points (m x 3)
##
           Maximum Iterations
##
           Maximum Threshold for the Distance between a point and the plane
## Outputs: RanSaC_normal_vec_normalized - RanSaC normalized normal vector of the fitted plane (1 x 3)
          RanSaC\_coeff\_C\_normalized - RanSaC\_coefficient\ C from the equation Ax + By + C = z
                                       - RanSaC Average of the points (1 x 3)
##
           RanSaC_mean_point
           RanSaC_dist_pt2pl
##
                                        - RanSaC Distance between a point and the plane (m x 1)
##
           inlier pts
                                        - Points that are inliers
##
           outlier_pts
                                        - Points that are outliers
def RanSaC algorithm(points 3D, max iterations, dist pt2pl threshold):
    Pseudocode:
        1.) Initialize the maximum number of inliers and best inliers set
        2.) Start the iteration till it reaches maximum iterations with for loop
            a.) Pick 3 random points
            b.) Perform least square plane fitting with those random n points
           c.) Check the distance threshold for every points
            d.) Determine total number of points that are within the distance threshold
            e.) Store the total number inliers and the best set of inliers if it is more than the previous one
        3.) Perform another least square plane fitting with best set of inliers
        4.) Outputs the Output normalized normal vector, normalized coefficient C, average point, dist_pt2pl f
rom the
           best set of inlier
   # Initialize the maximum number of inliers
   max num Inliers = None
    # Initialize the best set of inliers
   best set Inliers = None
    # Initialize the set of outlier
   set_Outliers = None
    # Start the iteration to perform RanSaC to discard outliers
   for iteration in range(0, max_iterations):
        # Pick 3 Random Points from the set of the points 3D
        rand_points = points_3D[random.sample(range(0,points_3D.shape[0]), 3),:]
        # Perform least square plane fitting with those randomly selected points.
       normal_vec_normalized, coeff_C_normalized, mean_point, _ = LSQ_plane_fitting(rand_points)
        # Determine the distance between a point and the plane.
       dist_pt2pl = abs(np.dot(points_3D - mean_point, normal_vec_normalized))
        # Store the inlier index that are equal or below the distance threshold
        inliers_index = np.where(dist_pt2pl <= dist_pt2pl_threshold)</pre>
        # Store the outlier index
        outliers index = np.where(dist pt2pl > dist pt2pl threshold)
        # Count the Total number of inliers
        num Inliers = inliers index[0].shape[0]
        # If the score is better than the previous iteration
        if (max num Inliers is None) or (num Inliers > max num Inliers):
            # Store the index of the inliers
           best_set_Inliers = inliers_index
            # Store the index of the outliers
            set_Outliers = outliers_index
            # Store the new maximum number of inliers
           max_num_Inliers = num_Inliers
    # Store outliers
   outlier_pts = points_3D[set_Outliers[0], :]
```

```
# Store only points that are inliers
      inlier_pts = points_3D[best_set_Inliers[0], :]
      # Perform another least square plane fitting with those inlier points.
      RanSaC_normal_vec_normalized, RanSaC_coeff_C_normalized, RanSaC_mean_point, RanSaC_dist_pt2pl = LSQ_plane_
fitting(inlier pts)
      return RanSaC_normal_vec_normalized, RanSaC_coeff_C_normalized, RanSaC_mean_point, RanSaC_dist_pt2pl, inli
er pts, outlier pts
### User-defined display of the plane plot function
## Input : Inliers
##
                   Outliers
##
                    3D-points (m \times 3)
                   Normal Vector
##
                   Average point
##
                    Graph title in string
## Outputs: None
def display_plane_plot(inlier_pts, outlier_pts, points_3D, normal_vec, mean_point, graph_title):
      # Initialize figure object and set figure size
      CSE_276C_fig = plt.figure(figsize=(7,7))
       # Initialize axes object
      CSE_276C_ax1 = Axes3D(CSE_276C_fig)
      # Plot scatter points
       # Inliers are green
      CSE 276C ax1.scatter(inlier pts[:,0], inlier pts[:, 1], inlier pts[:, 2], c = 'green', label = "Inliers")
      # Outliers are red
      CSE_276C_ax1.scatter(outlier_pts[:,0], outlier_pts[:, 1], outlier_pts[:, 2], c = 'red', label = "Outliers"
      plt.legend(loc="upper right") # Legend location
      # Plot the fitted plane
      X_coord = np.linspace(min(points_3D[:,0]), max(points_3D[:,0]),3) # Determine the x-axis limit
      Y_coord = np.linspace(min(points_3D[:,1]), max(points_3D[:,1]),3) # Determine the y-axis limit
      x_coord, y_coord = np.meshgrid(X_coord, Y_coord)
      z_coord = -(normal_vec[0] / normal_vec[2]) * x_coord - (normal_vec[1]/normal_vec[2]) * y_coord + (np.dot(n
ormal_vec, mean_point)/normal_vec[2])
      CSE_276C_ax1.plot_wireframe(x_coord,y_coord,z_coord,color='k')
      # Label Axis
      CSE_276C_ax1.set_xlabel("X", fontsize = 15)
      CSE_276C_ax1.set_ylabel("Y", fontsize = 15)
      CSE_276C_ax1.set_zlabel("Z", fontsize = 15)
      # Plot title
      plt.title(graph_title, fontsize = 18, fontweight = "bold")
      # Show Plot
      plt.show()
       # Change View of the Plot
      #CSE_276C_ax1.view_init(0, 0)
       """# Initialize axes object
      CSE 276C ax2 = CSE 276C fig.add subplot(222, projection='3d')
      # Plot scatter points
      # Inliers are green
      CSE_276C_ax2.scatter(inlier_pts[:,0], inlier_pts[:, 1], inlier_pts[:, 2], c = 'green')
      CSE_276C_ax2.scatter(outlier_pts[:,0], outlier_pts[:, 1], outlier_pts[:, 2], c = 'red')
      # Plot the fitted plane
      x_coord, y_coord = np.meshgrid(X_coord, Y_coord)
        z\_coord = -(normal\_vec[0] \ / \ normal\_vec[2]) \ * \ x\_coord - (normal\_vec[1] \ / \ normal\_vec[2]) \ * \ y\_coord + (np.dot(normal\_vec[2]) \ * \ y\_coord + (np.dot(normal\_ve
ormal vec, mean point)/normal vec[2])
      CSE_276C_ax2.plot_wireframe(x_coord,y_coord,z_coord,color='k')
      # Label Axis
      CSE_276C_ax2.set_xlabel("X", fontsize = 8)
      CSE 276C ax2.set ylabel("Y", fontsize = 8)
      CSE_276C_ax2.set_zlabel("Z", fontsize = 8)
      # Plot title
      plt.title(graph_title, fontsize = 10, fontweight = "bold")
       CSE 276C ax2.view init(0, 0)""
# Plane Fitting for the Empty Table with RanSaC
```

```
RanSaC_normal_vec_normalized, RanSaC_coeff_C_normalized, RanSaC_mean_point, RanSaC_dist_pt2pl, inlier_pts, out
lier_pts = RanSaC_algorithm(empty_Table_pts, 2000, 0.05)
 # Plane Fitting for the Table with Objects with RanSaC
RanSaC_normal_vec_normalized2, RanSaC_coeff_C_normalized2, RanSaC_mean_point2, RanSaC_dist_pt2pl2, inlier pts2
 , outlier_pts2 = RanSaC_algorithm(table_with_Obj_pts, 5000, 0.05)
# Display Plane Fitting Plot for the Empty Table
display_plane_plot(inlier_pts, outlier_pts, empty_Table_pts, RanSaC_normal_vec_normalized, RanSaC_mean_point,
 "Empty Table")
 # Show the plane equation for the Empty Table
print("The equation of the empty table fitted plane:")
 print("%f x + %f y + %f z + %f = 0" % (RanSaC_normal_vec_normalized[0], RanSaC_normal_vec_normalized[1], RanSaC_normal_vec_normalized[1], RanSaC_normal_vec_normalized[1], RanSaC_normal_vec_normalized[1], RanSaC_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal_vec_normal
C_normal_vec_normalized[2], RanSaC_coeff_C_normalized))
print("The average distance between an inlier and the fitted plane = %f" % (np.mean(RanSaC_dist_pt2pl)))
# Display Plane Fitting Plot for Table with Objects
display_plane_plot(inlier_pts2, outlier_pts2, table_with_Obj_pts, RanSaC_normal_vec_normalized2, RanSaC_mean_p
oint2, "Table with Objects")
 # Show the plane equation for Table with Objects
print("The equation of the table with objects fitted plane:")
print("%f x + %f y + %f z + %f = 0" % (RanSaC_normal_vec_normalized2[0], RanSaC_normal_vec_normalized2[1], Ran
SaC_normal_vec_normalized2[2], RanSaC_coeff_C_normalized2))
print("The average distance between an inlier and the fitted plane = %f" % (np.mean(RanSaC_dist_pt2pl2)))
### Plot samples by Professor Christensen and Dr. Wong
#fig = plt.figure()
#ax = fig.add_subplot(111, projection='3d')
#ax.plot_trisurf(empty_Table[:,0], empty_Table[:,1], empty_Table[:,2], color='white', edgecolors='grey', alpha
#ax.scatter(empty_Table[:,0], empty_Table[:,1], empty_Table[:,2], c='red')
```

Empty Table

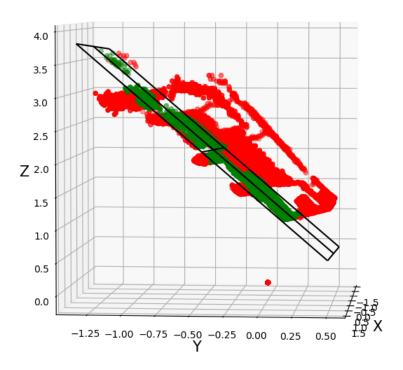




The equation of the empty table fitted plane: $-0.011647 \times + -0.906377 \text{ y} + -0.422310 \text{ z} + 0.593806 = 0$ The average distance between an inlier and the fitted plane = 0.010851

Table with Objects



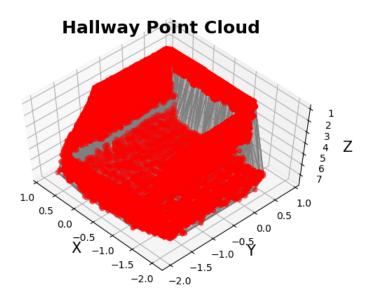


The equation of the table with objects fitted plane: 0.027658 x + -0.870000 y + -0.492276 z + 0.670482 = 0The average distance between an inlier and the fitted plane = 0.018778

After the empty table point cloud file, "Empty2.asc" was loaded, the empty table point cloud was input to RANSAC algorithm with a maximum iteration of 2000 and $d_{dest} = 0.05$. The "Empty Table" figure above shows that the equation of the empty table fitted plane is

-0.011647x - 0.906377y - 0.422310z + 0.593806 = 0. The average distance between an inlier of the empty table and the plane is 0.010851, which is below the set d_{dest} . Then, the table with objects point cloud, "TableWithObjects2.asc" was also loaded, the table with objects point cloud was input to the RANSAC algorithm with a maximum iteration of 5000 and $d_{dest} = 0.05$. The RANSAC algorithm ran 3000 more iteration with table with objects point cloud because there are more outlier to filter out to determine the best fitted plane. The "Table with Objects" figure above shows that the equation of the table with objects fitted plane is 0.027658x - 0.870000y - 0.492276z + 0.670482 = 0. The average distance between an inlier of the table with objects and the plane is 0.018778, which is below the set d_{dest} .

```
In [15]: import matplotlib
          import numpy as np
          import matplotlib.pyplot as plt
          import mpl_toolkits.mplot3d
          from mpl_toolkits.mplot3d import Axes3D
          import random
          %matplotlib notebook
          # Load Hallway files
          hallway = np.loadtxt("hallway1b.asc")
          ### Points Cloud Plot
          fig = plt.figure()
          ax = fig.add_subplot(111, projection='3d')
          ax.plot_trisurf(hallway[:,0], hallway[:,1], hallway[:,2], color='white', edgecolors='grey', alpha=0.5)
          ax.scatter(hallway[:,0], hallway[:,1], hallway[:,2], c='red')
          # Label Axis
          ax.set_xlabel("X", fontsize = 15)
ax.set_ylabel("Y", fontsize = 15)
ax.set_zlabel("Z", fontsize = 15)
          plt.title("Hallway Point Cloud", fontsize = 18, fontweight = "bold")
          plt.show()
```



Problem 4: Part 2

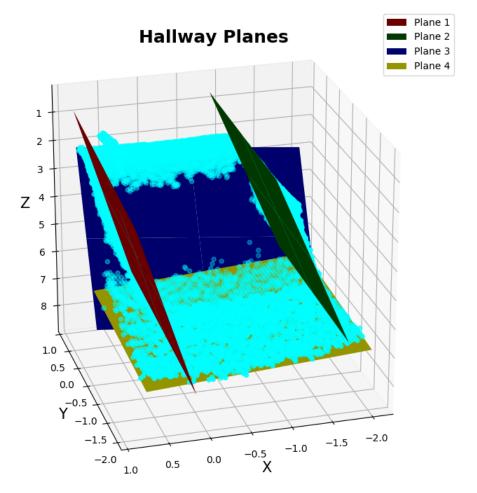
Describe and show how the method can be generalized to extract all the dominant planes in a relatively empty hallway.

Solution:

In order to detect multiple planes in the hallway, a user-defined function, "dominant_planes_Hunter()" was created. The dominant_planesHunter() user-defined function will run the RANSAC algorithm with the hallway 3D point cloud and store the first plane parameters including the normal vector, coefficient C, mean point, etc. Then, the outliers will be stored, and re-run the RANSAC algorithm with the outliers to exclude the previous inliers. The process will be repeated another 3 times to find all the remaining dominant plane in the hallway. The RANSAC algorithm maximum iterations was set to be 10000, and the distance threshold, \$d{thres}\$, to be 0.2. The planes in the hallway was plotted as shown in the figure below:

```
In [55]: import matplotlib
         import numpy as np
         import matplotlib.pyplot as plt
         import mpl_toolkits.mplot3d
         from mpl_toolkits.mplot3d import Axes3D
         import random
         %matplotlib notebook
         # Load Hallway files
         hallway pts = np.loadtxt("hallway1b.asc")
         ### User-defined dominant planes finder and plotter function
         ## Input : 3D-points (m x 3)
         ##
                    Maximum iterations for each plane (array form)
         ##
                    Maximum distance threshold for each plane (array form)
         ##
                    Number of Expected Planes
         ## Outputs: All the normal vectors in a list form
         ##
                    All coefficient Cs in a list form
         ##
                     All the mean points in a list form
         ##
                    All the inlier points in a list form
         ##
                    All the outlier points in a list form
         def dominant_planes_Hunter(points3D, max_iterations, dist_pt2pl_thres, num_dom_pln):
             # Initialize figure object and set figure size
             CSE_276C_fig = plt.figure(figsize=(7,7))
             # Initialize axes object
             CSE_276C_ax = Axes3D(CSE_276C_fig)
             # Plot Point Cloud Hallway
             CSE_276C_ax.scatter(hallway_pts[:,0], hallway_pts[:,1], hallway_pts[:,2], c='cyan')
             # Label Axis
             CSE_276C_ax.set_xlabel("X", fontsize = 15)
             CSE_276C_ax.set_ylabel("Y", fontsize = 15)
CSE_276C_ax.set_zlabel("Z", fontsize = 15)
             # Plot title
             plt.title("Hallway Planes", fontsize = 18, fontweight = "bold")
             # Set plot colors
             colors = ['r', 'g', 'b', 'y', 'm', 'k']
             # Labels
             labels = ["Plane 1", "Plane 2", "Plane 3", "Plane 4", "Plane 5", "Plane 6"]
             # Create empty lists that store all the normal vectors, coefficent Cs, mean points, inliers, and outliers
             # for every dominant plane
             normal vec ALL = []
             coeff_C_ALL = []
             mean point ALL = []
             inlier_pts_ALL = []
             outlier_pts_ALL = []
             # Initialize New Set of Point
             new set pts = hallway pts
             for plane_ID in range(0, num_dom_pln):
                 # Run RanSaC Plane Fitting
                 normal_vec, coeff_C, mean_point, _, inlier_pts, outlier_pts = RanSaC_algorithm(new_set_pts, max_iterat
         ions[plane_ID], dist_pt2pl_thres[plane_ID])
                 # Plot Plane
                 X_coord = np.linspace(min(inlier_pts[:,0]),max(inlier_pts[:,0]),3) # Determine the x-axis limit
                 Y_coord = np.linspace(min(inlier_pts[:,1]), max(inlier_pts[:,1]), 3) # Determine the y-axis limit
                 x_coord, y_coord = np.meshgrid(X_coord, Y_coord)
                 ot(normal vec, mean point)/normal vec[2])
                 #CSE_276C_ax.plot_wireframe(x_coord,y_coord,z_coord,color='k')
                 #CSE_276C_ax.plot_wireframe(x_coord,y_coord,z_coord,color=colors[plane_ID])
                 pln = CSE 276C ax.plot surface(x coord, y coord, z coord, color=colors[plane ID], label = labels[plane ID
         ])
                 pln._facecolors2d = pln._facecolors3d
                 pln._edgecolors2d = pln._edgecolors3d
                 CSE_276C_ax.legend()
                 # Store Plane Information to the lists
                 normal_vec_ALL.append(normal_vec)
                 coeff C ALL.append(coeff C)
                 mean_point_ALL.append(mean_point)
```

```
inlier_pts_ALL.append(inlier_pts)
        outlier_pts_ALL.append(outlier_pts)
        # Store the remaining points to the new_set_pts
        new_set_pts = outlier_pts
    # Show plot
    plt.show()
    return normal_vec_ALL, coeff_C_ALL, mean_point_ALL, inlier_pts_ALL, outlier_pts_ALL
# Set parameters
max_iterations =[10000, 10000, 10000, 10000]
dist_pt2pl_thres =[0.2, 0.2, 0.2, 0.2]
num\_dom\_pln = 4
# Let's hunt down the planes in the hallway!
normal_vec_ALL, coeff_C_ALL, mean_point_ALL, inlier_pts_ALL, outlier_pts_ALL = dominant_planes_Hunter(hallway_
pts, max_iterations, dist_pt2pl_thres, num_dom_pln)
\ensuremath{\textit{\###}} Plot samples by Professor Christensen and Dr. Wong
#fig = plt.figure()
#ax = fig.add_subplot(111, projection='3d')
#ax.plot_trisurf(hallway[:,0], hallway[:,1], hallway[:,2], color='white', edgecolors='grey', alpha=0.5)
#ax.scatter(hallway[:,0], hallway[:,1], hallway[:,2], c='red')
#plt.show()
```



```
In [58]: # Show the 1st plane equation from the hallway
        print("The equation of 1st fitted plane from the hallway:")
        print("%f x + %f y + %f z + %f = 0" % (normal_vec_ALL[0][0], normal_vec_ALL[0][1], normal_vec_ALL[0][2], coeff
        _C_ALL[0]))
        # Show the 2nd plane equation from the hallway
       print("\nThe equation of 2nd fitted plane from the hallway:")
       print("%f x + %f y + %f z + %f = 0" % (normal_vec_ALL[1][0], normal_vec_ALL[1][1], normal_vec_ALL[1][2], coeff
        _C_ALL[1]))
        # Show the 3rd plane equation from the hallway
        print("\nThe equation of 3rd fitted plane from the hallway:")
        _C_ALL[2]))
        # Show the 4th plane equation from the hallway
       print("\nThe equation of 4th fitted plane from the hallway:")
       C ALL[3]))
       The equation of 1st fitted plane from the hallway:
       -0.975413 \times + -0.145478 \times + -0.165546 \times + 1.098832 = 0
       The equation of 2nd fitted plane from the hallway:
       -0.987955 x + -0.009184 y + -0.154469 z + -0.748513 = 0
       The equation of 3rd fitted plane from the hallway:
       -0.047033 \times + -0.985149 \text{ y} + -0.165134 \text{ z} + 1.250932 = 0
       The equation of 4th fitted plane from the hallway:
```

The equations of each plane in the hallway are presented above. The RANSAC algorithm was run at a higher iterations and d_{dest} , which are 10000 and 0.2 for every plane in the hallway because the point cloud data in the hallway was not that clean and a little scatter. Hence, the implemented "dominant_planes_Hunter()" user-defined function that also uses the RANSAC algorithm succesfully extracted all the dominant plane from the relatively empty hallway.

 $0.172249 \times + -0.133171 y + -0.976010 z + 6.806987 = 0$