Seawatch

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Data Clean

Overview

VISIT

POP80

HHMEDI

POVPR

PERCAPI

LST

CPI

5.0

1.0

161799.0 161111.0

300.9

47646.0

17850.0

26.1

4.0 0.67

64.5 -0.85

25.7 2.00

0.38

3.60

1.03

1.30

1.0

37538.0

12662.0

```
# remove environment
rm(list=ls())
# data import
seawatch.ori<-read_excel("~/MSBA notes/Business Stats/Seawatch C w blanks-1.xlsx")
# we delete CNVHRS, Notes, City and Zip code.
seawatch<-seawatch.ori[,3:20]
seawatch<-seawatch[,-2]
# overview
describe(seawatch)
##
           vars
                   n
                         mean
                                      sd
                                          median
                                                  trimmed
                                                                mad
                                                                         min
## GROSS
                      3441.30
                                4056.82
                                          2419.5
                                                  2755.20
                                                            2227.61
                                                                        43.0
               1 394
## MOY
               2 396
                          6.62
                                   2.45
                                             7.0
                                                     6.66
                                                               1.48
                                                                         1.0
                                   0.99
## YR
               3 396
                        81.79
                                            82.0
                                                     81.86
                                                                        80.0
                                                               1.48
## MON
               4 396
                        28.13
                                  11.72
                                            31.0
                                                     28.85
                                                              17.79
                                                                         3.0
## VISIT
               5 396
                         2.00
                                   0.97
                                             2.0
                                                     1.90
                                                               1.48
                                                                         1.0
## LST
               6 396
                          0.41
                                   0.49
                                             0.0
                                                     0.38
                                                               0.00
                                                                         0.0
                                  16.85
## CPI
               7 396
                       282.14
                                           290.6
                                                   284.31
                                                              13.34
                                                                       236.4
## POP80
               8 387 19179.16 22616.29 13212.0 14863.73 11421.95
                                                                       688.0
## HHMEDI
                                6654.16 21304.0 21984.26
                                                            6862.96 10108.0
               9
                 387 22643.48
## PERCAPI
             10 387
                      8706.69
                                2236.39
                                          8060.0
                                                  8429.94
                                                            1885.87
                                                                      5188.0
## POVPR
                                   3.96
                                                     5.68
              11 387
                          6.20
                                             5.1
                                                               2.67
                                                                         0.4
## MFGPR
             12 371
                        23.89
                                   9.65
                                            22.3
                                                     23.41
                                                               8.60
                                                                         3.0
## COLLPR
             13 371
                        28.72
                                  13.20
                                            25.9
                                                     27.55
                                                              14.97
                                                                         8.2
## MAGE
             14 387
                        32.23
                                   3.06
                                            32.1
                                                     32.07
                                                               2.67
                                                                        21.7
## CART
             15 380
                      3784.08
                                5064.56
                                          2171.5
                                                  2628.76
                                                            1965.19
                                                                        97.0
## REAG
             16 380
                      3881.71
                                3430.15
                                          3067.0
                                                  3359.21
                                                            2604.93
                                                                        84.0
##
  ANDR
              17 380
                      1528.81
                                1463.64
                                          1105.0
                                                  1262.62
                                                             919.21
                                                                        63.0
##
                        range
                                skew kurtosis
                 max
                                                     se
## GROSS
                      38213.0
                               4.12
                                         25.26
                                                204.38
             38256.0
## MOY
                          11.0 -0.24
                12.0
                                          0.52
                                                  0.12
## YR.
                83.0
                          3.0 -0.28
                                         -1.03
                                                  0.05
## MON
                44.0
                         41.0 -0.27
                                         -1.06
                                                  0.59
```

16.78 1149.65

0.05

0.02

0.85

338.25

113.68

0.20

-0.27

-1.86

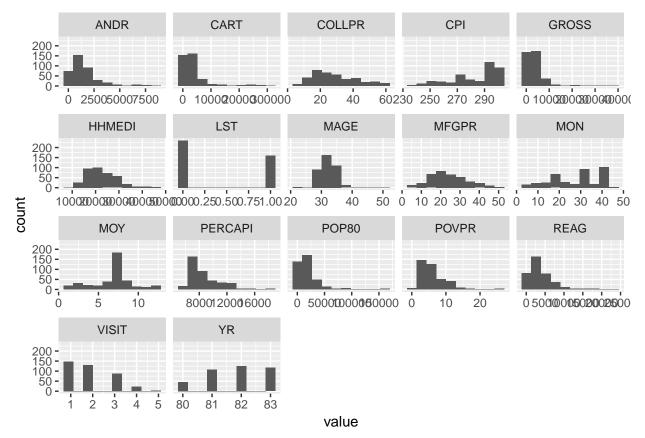
-0.38

1.39

1.94

6.23

```
## MFGPR
               48.4
                         45.4 0.41
                                       -0.16
                                                 0.50
               61.7
                                                 0.69
## COLLPR
                         53.5
                              0.65
                                       -0.47
               50.2
                         28.5
                               1.33
                                        7.57
                                                 0.16
## MAGE
## CART
            31225.0
                     31128.0
                               3.13
                                        10.62
                                               259.81
## REAG
            23339.0
                     23255.0
                               2.17
                                        7.07
                                               175.96
## ANDR
             8586.0
                       8523.0
                              2.28
                                        6.40
                                                75.08
ggplot(gather(seawatch), aes(value)) +
    geom histogram(bins = 10) +
    facet_wrap(~key, scales = 'free_x')
```



```
## Note that VISIT and LST are categorical variables
## Convert numberic variables to Categorical
seawatch$VISIT<-as.factor(seawatch$VISIT)
seawatch$LST<-as.factor(seawatch$LST)</pre>
```

Missing Values

```
# number of NA's
nrow(seawatch)-nrow(na.omit(seawatch))

## [1] 34

## Since there are only 34 rows containing na's we can simply delete it
seawatch<-na.omit(seawatch)</pre>
```

Other strange observation

CART, REAG, and ANDR

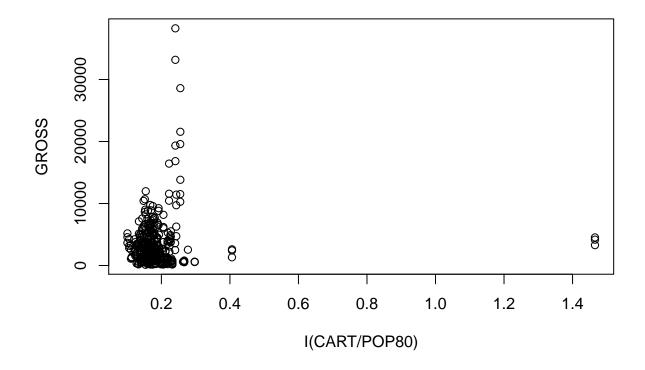
3 16301

4638

1572 23888

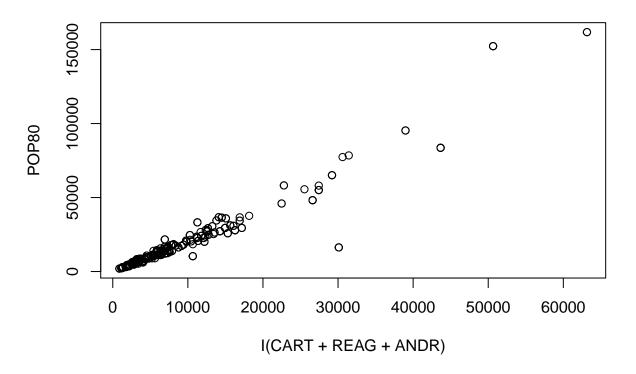
• For some observations, the number of votes is bigger than total population. Due to the high correlation (0.9533607) between POP80 and the sum of those there vote numbers, we can build a model to predict the right population.

```
# scatter plot
plot(GROSS~I(CART/POP80),data = seawatch)
```



```
summary(seawatch$CART)
##
     Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                              Max.
##
              1148
                      2254
                              3955
                                      4215
                                             31225
  • Note that some observations have CART/POP80 > 1, indicating CART larger than total population.
# observations that CART or REAG or ANDR is larger than total population
ex.obs<-seawatch$CART>seawatch$POP80 | seawatch$REAG>seawatch$POP80 | seawatch$POP80
seawatch[ex.obs,c("POP80",'REAG','ANDR','CART')]
## # A tibble: 3 x 4
##
     POP80 REAG ANDR CART
##
     <dbl> <dbl> <dbl> <dbl> <
## 1 16301
            4638
                  1572 23888
## 2 16301
            4638
                  1572 23888
```

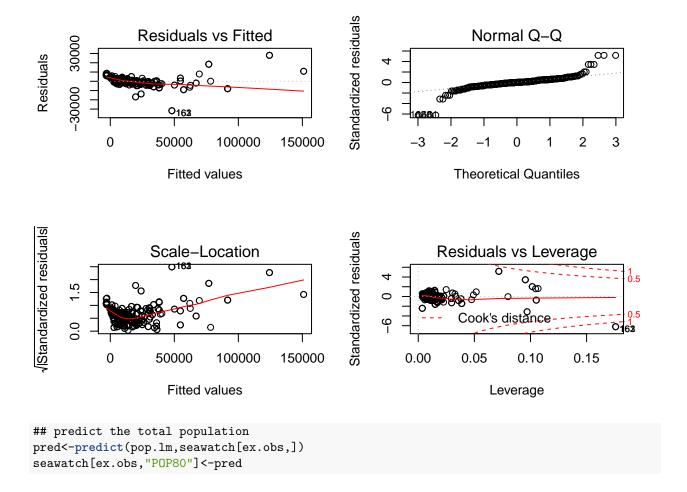
```
# correlation
cor(seawatch$POP80,I(seawatch$CART+seawatch$REAG+seawatch$ANDR))
## [1] 0.9533607
# plot pop80 and sum of those 3 vote numbers
plot(POP80~I(CART+REAG+ANDR),data = seawatch)
```



```
# original sd
sd(seawatch[-ex.obs,]$POP80)
## [1] 23057.15
# predictive model
## full model
pop.lm<-lm(POP80~.+I(CART+REAG+ANDR),data = seawatch[-ex.obs,])</pre>
## Predictors selection
step(pop.lm,direction = "backward",trace = 0)
##
## Call:
## lm(formula = POP80 ~ GROSS + MOY + CPI + HHMEDI + POVPR + MFGPR +
       MAGE + CART + REAG + ANDR, data = seawatch[-ex.obs, ])
##
##
## Coefficients:
## (Intercept)
                      GROSS
                                      MOY
                                                    CPI
                                                              HHMEDI
##
    -1.515e+04
                 -8.491e-01
                               -1.790e+02
                                              5.996e+01
                                                           1.132e-01
         POVPR
##
                      MFGPR
                                     MAGE
                                                   CART
                                                                REAG
```

```
##
    7.209e+02
                 1.418e+02
                             -4.204e+02
                                          1.183e+00
                                                        2.222e+00
##
         ANDR.
##
    7.499e+00
## update model
pop.lm<-lm(formula = POP80 ~ GROSS + MOY + CPI + HHMEDI + POVPR + MFGPR +
   MAGE + CART + REAG + ANDR,data = seawatch[-ex.obs,])
## check multicolinearity
vif(pop.lm)
##
      GROSS
                  MOY
                            CPI
                                   HHMEDI
                                              POVPR.
                                                        MFGPR.
                                                                   MAGE
##
  4.153757 1.049295 1.275316 2.534493 2.855746 1.470281 1.322949
       CART
                 REAG
                           ANDR
## 5.099883 15.065419 29.754043
## drop ANDR
pop.lm<-update(pop.lm,.~.-ANDR)
vif(pop.lm)
     GROSS
                YOM
                         CPI
                               HHMEDI
                                         POVPR
                                                  MFGPR
                                                            MAGE
                                                                     CART
## 1.729190 1.048175 1.144997 2.474438 2.671959 1.445496 1.307185 4.138947
##
      R.F.A.G
## 3.836808
## summary and plot of the model
summary(pop.lm)
##
## Call:
## lm(formula = POP80 ~ GROSS + MOY + CPI + HHMEDI + POVPR + MFGPR +
      MAGE + CART + REAG, data = seawatch[-ex.obs, ])
##
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
## -32491 -1937
                   114
                         2064 27325
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 855.88035 7263.72590 0.118 0.90627
## GROSS
                -0.09501
                            0.09354 -1.016 0.31047
## MOY
              -206.87222 125.20657 -1.652 0.09938 .
## CPI
                16.50456
                          18.91713
                                     0.872 0.38355
## HHMEDI
                 0.03962
                            0.06937
                                      0.571 0.56829
## POVPR
               938.76317 122.01284
                                      7.694 1.46e-13 ***
## MFGPR
                                      2.945 0.00344 **
               108.83178
                          36.95402
## MAGE
              -502.76916 110.16717 -4.564 6.96e-06 ***
## CART
                            0.11747 13.347 < 2e-16 ***
                 1.56789
## REAG
                            0.16951 24.753 < 2e-16 ***
                 4.19580
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5626 on 351 degrees of freedom
## Multiple R-squared: 0.942, Adjusted R-squared: 0.9405
## F-statistic: 632.9 on 9 and 351 DF, p-value: < 2.2e-16
```

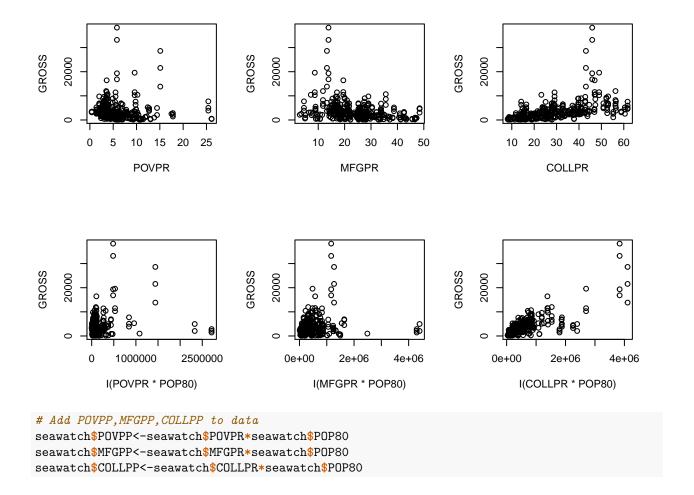
```
## drop GROSS, MOY, CPI and HHMEDI
pop.lm<-update(pop.lm,.~.-GROSS-MOY-CPI-HHMEDI)</pre>
summary(pop.lm)
##
## Call:
## lm(formula = POP80 ~ POVPR + MFGPR + MAGE + CART + REAG, data = seawatch[-ex.obs,
##
      ])
##
## Residuals:
     Min
            1Q Median
                         3Q
                               Max
## -31778 -2049 114 2375 28029
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5141.8484 4034.3412 1.275 0.2033
                       84.1918 10.858 < 2e-16 ***
## POVPR
             914.1322
## MFGPR
              115.1605
                         33.6754
                                 3.420 0.0007 ***
## MAGE
             -508.0712 107.4020 -4.731 3.24e-06 ***
## CART
               ## REAG
                          0.1648 25.096 < 2e-16 ***
                4.1345
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5632 on 355 degrees of freedom
## Multiple R-squared: 0.9412, Adjusted R-squared: 0.9403
## F-statistic: 1136 on 5 and 355 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
plot(pop.lm)
```



POVPR, COLLPR and MFGPR

• Due to the increasing variance, instead of percentage, we transform those varibles to exact number by mutiplying total population. As a result, the linear correlations is more obvious.

```
#Compare variance before and after transformation
par(mfrow=c(2,3))
plot(GROSS~POVPR,data = seawatch)
plot(GROSS~MFGPR,data = seawatch)
plot(GROSS~COLLPR,data = seawatch)
plot(GROSS~I(POVPR*POP80),data = seawatch)
plot(GROSS~I(MFGPR*POP80),data = seawatch)
plot(GROSS~I(COLLPR*POP80),data = seawatch)
```



Modeling

Training and Testing subsets split

```
set.seed(1024)
train.num<-sample(1:dim(seawatch)[1],round(nrow(seawatch)*0.75))
seawatch.train<-seawatch[train.num,]
seawatch.test<-seawatch[-train.num,]</pre>
```

Predictors Selections

```
# full model
full.lm<-lm(data = seawatch.train,GROSS~.)
# predictors selection
step(full.lm,direction = "backward",trace = 0)</pre>
```

##

```
## Call:
## lm(formula = GROSS ~ MOY + YR + VISIT + LST + HHMEDI + CART +
      REAG + ANDR + POVPP + COLLPP, data = seawatch.train)
##
## Coefficients:
## (Intercept)
                        YOM
                                      YR
                                               VISIT2
                                                            VISIT3
  -5.801e+04
                  9.315e+01
                               6.935e+02
                                           -1.625e+02
                                                         4.430e+02
##
       VISIT4
                    VISIT5
                                    LST1
                                               HHMEDI
                                                              CART
##
     2.590e+03
                  1.700e+04
                              -7.933e+02
                                            6.632e-02
                                                        -3.096e-01
##
                                   POVPP
          REAG
                       ANDR
                                               COLLPP
## -4.408e-01
                  2.561e+00
                              -1.915e-03
                                            3.714e-03
# update model
fit.lm<-lm(formula = GROSS ~ MOY + YR + VISIT + LST + HHMEDI + CART +
    REAG + ANDR + POVPP + COLLPP, data = seawatch.train)
# check multicolinearity
vif(fit.lm)
##
              GVIF Df GVIF<sup>(1/(2*Df))</sup>
## MOY
           1.182588 1
                              1.087469
## YR
           3.647111 1
                              1.909741
## VISIT
           3.691875 4
                              1.177351
## LST
           2.093257 1
                              1.446809
## HHMEDI 2.119586 1
                              1.455880
## CART
        11.627003 1
                              3.409839
        19.918715 1
## REAG
                              4.463039
## ANDR 41.908423 1
                              6.473672
## POVPP
          4.223934 1
                              2.055221
## COLLPP 18.224195 1
                              4.268981
# drop ANDR
fit.lm<-update(fit.lm,.~.-ANDR)</pre>
vif(fit.lm)
              GVIF Df GVIF<sup>(1/(2*Df))</sup>
##
## MOY
          1.169804 1
                            1.081575
## YR
          3.386926 1
                             1.840360
## VISIT 3.483543 4
                            1.168833
## LST
          2.057111 1
                            1.434263
## HHMEDI 1.656580 1
                            1.287082
## CART 9.243068 1
                             3.040241
## REAG
        3.974517 1
                             1.993619
## POVPP 3.560529 1
                             1.886937
## COLLPP 5.917441 1
                             2.432579
# drop CART
fit.lm<-update(fit.lm,.~.-CART)</pre>
vif(fit.lm)
              GVIF Df GVIF^(1/(2*Df))
##
## MOY
          1.169804 1
                            1.081575
## YR
          3.268160 1
                             1.807805
## VISIT 3.211092 4
                             1.156995
          2.048469 1
## LST
                             1.431247
## HHMEDI 1.651053 1
                             1.284933
## REAG
        3.521195 1
                            1.876485
```

```
## POVPP 2.650217 1
                          1.627949
## COLLPP 2.842762 1
                            1.686049
# summary
summary(fit.lm)
##
## Call:
## lm(formula = GROSS ~ MOY + YR + VISIT + LST + HHMEDI + REAG +
      POVPP + COLLPP, data = seawatch.train)
##
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -8740.9 -747.8 -177.7
                            700.2 10321.6
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -9.377e+03 1.717e+04 -0.546 0.58539
               6.628e+01 5.079e+01
                                      1.305 0.19304
## YR
               1.128e+02 2.081e+02
                                     0.542 0.58823
## VISIT2
              3.916e+02 3.193e+02
                                    1.227 0.22106
## VISIT3
              1.459e+03 4.404e+02
                                     3.313 0.00105 **
## VISIT4
              4.772e+03 6.767e+02
                                     7.052 1.59e-11 ***
## VISIT5
              2.079e+04 2.163e+03 9.611 < 2e-16 ***
## LST1
              -7.261e+02 3.343e+02 -2.172 0.03074 *
## HHMEDI
              1.641e-02 2.220e-02
                                     0.739 0.46042
## REAG
              7.518e-02 6.352e-02
                                     1.184 0.23763
## POVPP
              -2.824e-03 5.347e-04 -5.282 2.70e-07 ***
## COLLPP
              4.558e-03 2.829e-04 16.114 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1898 on 260 degrees of freedom
## Multiple R-squared: 0.8164, Adjusted R-squared: 0.8086
## F-statistic: 105.1 on 11 and 260 DF, p-value: < 2.2e-16
# drop YR, POVPR, PERCAPI
fit.lm<-update(fit.lm,.~.-YR-MOY-HHMEDI-REAG)</pre>
summary(fit.lm)
##
## lm(formula = GROSS ~ VISIT + LST + POVPP + COLLPP, data = seawatch.train)
##
## Residuals:
##
               1Q Median
      Min
                               3Q
                                      Max
## -8804.8 -785.8 -157.8
                            762.9 10598.9
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 7.253e+02 2.156e+02 3.364 0.000882 ***
               5.104e+02 2.767e+02
## VISIT2
                                     1.845 0.066217 .
## VISIT3
               1.644e+03 3.577e+02
                                     4.597 6.64e-06 ***
## VISIT4
               4.929e+03 5.648e+02 8.726 3.03e-16 ***
              2.128e+04 2.068e+03 10.292 < 2e-16 ***
## VISIT5
              -6.765e+02 2.774e+02 -2.439 0.015398 *
## LST1
```

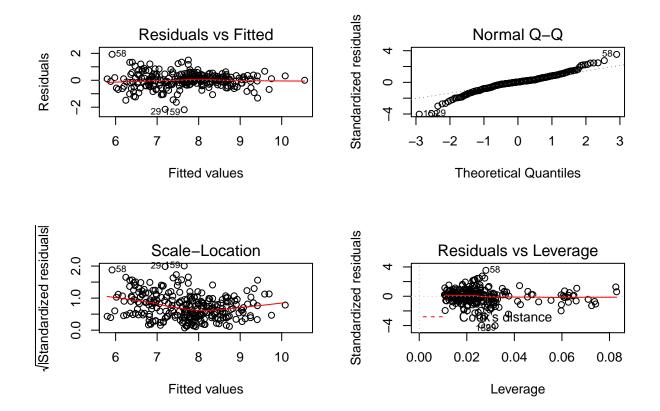
```
-2.618e-03 4.053e-04 -6.460 5.01e-10 ***
## POVPP
## COLLPP
                  4.740e-03
                               2.299e-04
                                            20.617 < 2e-16 ***
##
                      0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 1896 on 264 degrees of freedom
## Multiple R-squared: 0.8141, Adjusted R-squared: 0.8091
## F-statistic: 165.1 on 7 and 264 DF, p-value: < 2.2e-16
# residual analysis
par(mfrow=c(2,2))
plot(fit.lm)
## Warning: not plotting observations with leverage one:
##
     152
## Warning: not plotting observations with leverage one:
                                                    Standardized residuals
                 Residuals vs Fitted
                                                                         Normal Q-Q
     10000
                          1450
2470
                                                          9
Residuals
                                                          \alpha
     -10000
           0
                 10000
                          20000
                                   30000
                                                                                            2
                                                                                                 3
                      Fitted values
                                                                      Theoretical Quantiles
(Standardized residuals)
                                                    Standardized residuals
                   Scale-Location
                                                                   Residuals vs Leverage
                     O<sup>182</sup> 2470
                                                                                                   0.5
      1.5
                                                                           k's distance
     0.0
                                  30000
           0
                 10000
                          20000
                                                              0.00
                                                                    0.05
                                                                           0.10 0.15
                                                                                        0.20 0.25
                      Fitted values
                                                                            Leverage
```

• There exists clear non-constant variance. Also predictors are not normally distributed. As a result, we use the power transformation to modify the model.

Power Transformation model

```
powerTransform(cbind(seawatch.train$GROSS,seawatch$POVPR,seawatch$COLLPP)~1)
```

```
## Warning in cbind(seawatch.train$GROSS, seawatch$POVPR, seawatch$COLLPP):
## number of rows of result is not a multiple of vector length (arg 1)
## Estimated transformation parameters
           Y1
## 0.12458545 0.10717096 -0.05498497
# Thus, we build another model by taking natural log on both sides
new.fit.lm<-lm(formula = log(GROSS) ~ VISIT + LST + log(POVPP) + log(COLLPP), data = seawatch.train)</pre>
summary(new.fit.lm)
##
## Call:
## lm(formula = log(GROSS) ~ VISIT + LST + log(POVPP) + log(COLLPP),
##
       data = seawatch.train)
##
## Residuals:
##
       Min
                 1Q Median
                                   30
## -2.18775 -0.22711 0.02269 0.27381 1.92732
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -0.93422
                          0.47035 -1.986 0.04804 *
## VISIT2
               0.17483
                          0.08055
                                    2.170 0.03087 *
## VISIT3
               0.51467
                          0.10682
                                   4.818 2.45e-06 ***
## VISIT4
               0.84580
                          0.16582
                                   5.101 6.47e-07 ***
                                    2.754 0.00629 **
## VISIT5
               1.57043
                          0.57016
                          0.08260 -3.114 0.00205 **
## LST1
              -0.25719
## log(POVPP) -0.27453
                          0.03869 -7.097 1.18e-11 ***
## log(COLLPP) 0.90809
                          0.04800 18.919 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5531 on 264 degrees of freedom
## Multiple R-squared: 0.7195, Adjusted R-squared: 0.7121
## F-statistic: 96.76 on 7 and 264 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
plot(new.fit.lm)
## Warning: not plotting observations with leverage one:
## Warning: not plotting observations with leverage one:
##
     152
```



• Note that the variance of error is more constant and the predictors are distributed better than the original linear model

Model based on correlation

```
model2<- lm(GROSS ~ VISIT + POP80 + PERCAPI + MFGPR + REAG + POVPP + COLLPP, data = seawatch.train)
summary(model2)
##
## Call:
##
  lm(formula = GROSS ~ VISIT + POP80 + PERCAPI + MFGPR + REAG +
##
       POVPP + COLLPP, data = seawatch.train)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
##
   -5930.0
           -750.4
                    -166.7
                              698.2 10360.4
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
                                       -0.224 0.822673
## (Intercept) -1.502e+02
                           6.698e+02
## VISIT2
                3.314e+02
                            2.591e+02
                                        1.279 0.202013
                            2.996e+02
                                        3.795 0.000184 ***
## VISIT3
                1.137e+03
## VISIT4
                3.919e+03
                            5.029e+02
                                        7.792 1.57e-13 ***
                                       10.092 < 2e-16 ***
## VISIT5
                1.936e+04
                            1.918e+03
## POP80
               -2.365e-01 3.756e-02
                                       -6.296 1.29e-09 ***
```

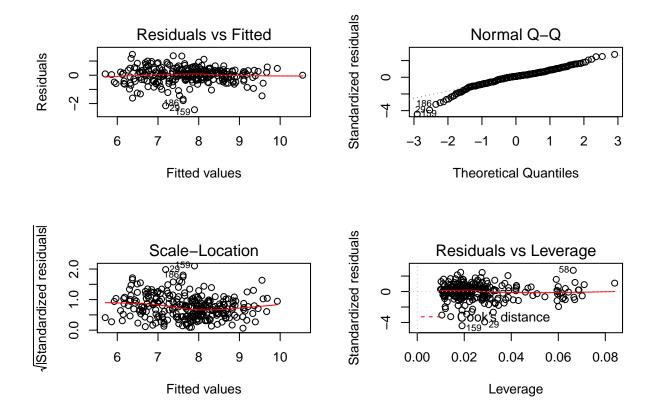
```
## PERCAPI
                  8.191e-03 6.120e-02
                                             0.134 0.893638
## MFGPR
                  2.078e+01
                               1.296e+01
                                             1.603 0.110085
## REAG
                  7.606e-01
                               1.248e-01
                                             6.094 3.94e-09 ***
## POVPP
                  4.770e-03
                               1.284e-03
                                             3.714 0.000249 ***
##
   COLLPP
                  6.293e-03
                               3.888e-04
                                            16.186 < 2e-16 ***
##
                      0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 1784 on 261 degrees of freedom
## Multiple R-squared: 0.8372, Adjusted R-squared: 0.831
## F-statistic: 134.3 on 10 and 261 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
plot(model2)
## Warning: not plotting observations with leverage one:
## Warning: not plotting observations with leverage one:
##
     152
                                                     Standardized residuals
                                                                         Normal Q-Q
                 Residuals vs Fitted
     10000
                          1450
2470
                                                                                            <sub>24</sub>7450
Residuals
                                                          4
     -5000
                                                          0
           0
                                   30000
                 10000
                          20000
                                                                                0
                                                                                            2
                                                                                                  3
                      Fitted values
                                                                       Theoretical Quantiles
/Standardized residuals
                                                     Standardized residuals
                   Scale-Location
                                                                    Residuals vs Leverage
                          2470<sup>50</sup>
                                                                                              2470
                                                          9
                                                                                                    1
0.5
      1.5
                                                          \alpha
                            0
     0.0
           0
                                                              0.00
                                                                                       0.20
                 10000
                          20000
                                  30000
                                                                          0.10
                      Fitted values
                                                                            Leverage
```

#multicolinearity check vif(model2)

```
## GVIF Df GVIF^(1/(2*Df))
## VISIT 1.343200 4 1.037570
## POP80 65.917474 1 8.118958
## PERCAPI 1.590806 1 1.261272
```

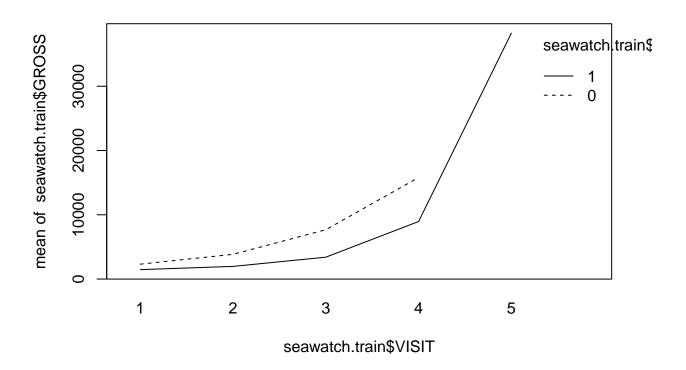
```
## MFGPR
           1.324058 1
                               1.150677
## REAG
          15.398087 1
                               3.924040
## POVPP
          17.316278 1
                               4.161283
## COLLPP
           6.080990 1
                               2.465966
model2<-update(model2,.~.-POP80)</pre>
vif(model2)
              GVIF Df GVIF<sup>(1/(2*Df))</sup>
## VISIT
          1.322948 4
                             1.035602
## PERCAPI 1.510947 1
                              1.229206
## MFGPR
          1.184886
                              1.088525
## REAG
          3.239980 1
                              1.799994
## POVPP
          2.450437 1
                              1.565387
## COLLPP 3.022401 1
                              1.738505
#powertransformation
powerTransform(cbind(seawatch.train$GROSS,seawatch.train$PERCAPI,seawatch.train$MFGPR,seawatch.train$RE
## Estimated transformation parameters
##
                         Y2
                                      Y3
                                                   Y4
                                                                 Y5
   0.143119027 -1.417761071 0.645988351 0.205752122 0.058852475
##
##
## 0.002208676
#model2
model2<-lm(log(GROSS) ~ VISIT + 1/PERCAPI + sqrt(MFGPR) + log(REAG) + log(POVPP) + log(COLLPP), data = s
summary(model2)
##
## Call:
## lm(formula = log(GROSS) ~ VISIT + 1/PERCAPI + sqrt(MFGPR) + log(REAG) +
       log(POVPP) + log(COLLPP), data = seawatch.train)
##
##
## Residuals:
       Min
                 1Q
                      Median
                                    3Q
                                            Max
## -2.41640 -0.29439 0.05938 0.29932 1.46012
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
                          0.60186 -1.110 0.268140
## (Intercept) -0.66788
## VISIT2
               0.15328
                          0.08056
                                   1.903 0.058152 .
## VISIT3
               0.36345
                        0.09370
                                   3.879 0.000133 ***
## VISIT4
               0.62299
                          0.15366
                                   4.054 6.63e-05 ***
## VISIT5
               1.24336
                          0.56763
                                   2.190 0.029372 *
## sqrt(MFGPR) -0.09132
                          0.03720 -2.455 0.014732 *
## log(REAG)
              -0.03229
                          0.10592 -0.305 0.760711
## log(POVPP) -0.28518
                          0.04374
                                   -6.520 3.58e-10 ***
## log(COLLPP) 0.94737
                          0.08122 11.664 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.5564 on 263 degrees of freedom
## Multiple R-squared: 0.7172, Adjusted R-squared: 0.7086
## F-statistic: 83.36 on 8 and 263 DF, p-value: < 2.2e-16
```

```
model2<-update(model2,.~.-log(REAG))</pre>
summary(model2)
##
## Call:
## lm(formula = log(GROSS) ~ VISIT + sqrt(MFGPR) + log(POVPP) +
##
      log(COLLPP), data = seawatch.train)
##
## Residuals:
##
       Min
                1Q
                    Median
## -2.43230 -0.29927 0.05704 0.31874 1.47228
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
##
## VISIT2
             0.15500
                        0.08022 1.932 0.054418 .
## VISIT3
              0.36555
                       0.09329
                                 3.918 0.000114 ***
## VISIT4
              0.62705
                      0.15282
                                 4.103 5.43e-05 ***
## VISIT5
              1.24861 0.56640
                                 2.204 0.028353 *
## sqrt(MFGPR) -0.09498
                        0.03515 -2.702 0.007342 **
## log(POVPP) -0.29182
                        0.03787 -7.707 2.62e-13 ***
## log(COLLPP) 0.92717
                         0.04687 19.781 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5555 on 264 degrees of freedom
## Multiple R-squared: 0.7171, Adjusted R-squared: 0.7096
## F-statistic: 95.58 on 7 and 264 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
plot(model2)
## Warning: not plotting observations with leverage one:
##
    152
## Warning: not plotting observations with leverage one:
##
    152
```



model with interaction

Interaction plot
interaction.plot(seawatch.train\$VISIT,seawatch.train\$LST,seawatch.train\$GROSS)



```
interaction.lm<-lm(data = seawatch.train, GROSS~MOY + YR + VISIT + LST + HHMEDI + CART + REAG + ANDR +
# Power transformation
powerTransform(cbind(seawatch.train$GROSS,seawatch.train$MOY,seawatch.train$HHMEDI,seawatch.train$CART,
## Estimated transformation parameters
##
            Y1
                                    Y3
                                                Y4
   ##
            Y6
  0.113241384 0.053069424 -0.016952640
interaction.lm<-lm(data = seawatch.train,log(GROSS)~MOY + YR + VISIT + LST + log(HHMEDI) + log(CART) +
#predictors selection
step(interaction.lm,trace = 0)
##
## Call:
## lm(formula = log(GROSS) ~ VISIT + LST + log(CART) + log(REAG) +
      log(ANDR) + log(POVPP) + log(COLLPP) + VISIT:log(REAG) +
      VISIT:log(COLLPP) + LST:log(YR) + LST:log(CART) + LST:log(REAG) +
##
      LST:log(COLLPP), data = seawatch.train)
##
##
## Coefficients:
```

VISIT3

0.3570

LST1

VISIT2

-0.3555

VISIT5

##

##

##

(Intercept)

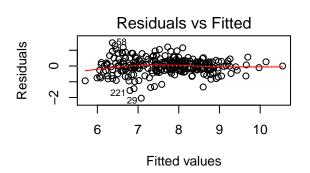
10.8365

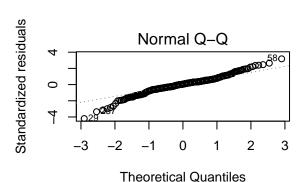
VISIT4

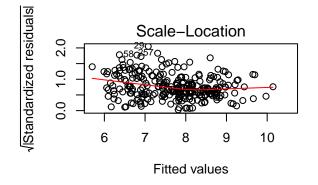
```
##
              -1.7746
                                   1.3286
                                                      -61.6314
##
            log(CART)
                                log(REAG)
                                                     log(ANDR)
              -0.3339
                                  -0.3450
                                                        0.8543
##
##
           log(POVPP)
                              log(COLLPP)
                                              VISIT2:log(REAG)
##
              -0.2195
                                   0.7354
                                                        0.4256
##
     VISIT3:log(REAG)
                         VISIT4:log(REAG)
                                              VISIT5:log(REAG)
##
               0.8192
                                   0.9483
##
  VISIT2:log(COLLPP) VISIT3:log(COLLPP)
                                           VISIT4:log(COLLPP)
##
              -0.2261
                                  -0.5094
                                                       -0.4251
##
  VISIT5:log(COLLPP)
                             LST0:log(YR)
                                                  LST1:log(YR)
##
                                  -2.4555
                                                       11.1822
                   NA
##
       LST1:log(CART)
                           LST1:log(REAG)
                                              LST1:log(COLLPP)
              -0.2702
                                  -0.6843
                                                        0.6999
interaction.lm<-lm(formula = log(GROSS) ~ VISIT + LST + log(CART) + log(REAG) +
    log(ANDR) + log(POVPP) + log(COLLPP) + VISIT:log(REAG) +
    VISIT:log(COLLPP) + LST:log(YR) + LST:log(CART) + LST:log(REAG) +
   LST:log(COLLPP), data = seawatch.train)
# Delete ANDR and CART due to high colinear
vif(lm(formula = log(GROSS) ~ VISIT + LST + log(CART) + log(REAG) +
    log(ANDR) + log(POVPP) + log(COLLPP),data=seawatch.train))
##
                    GVIF Df GVIF^(1/(2*Df))
## VISIT
                1.753425 4
                                   1.072719
## LST
                1.516618 1
                                   1.231511
## log(CART)
               10.643074 1
                                   3.262372
## log(REAG)
                                   3.862428
               14.918347 1
## log(ANDR)
               28.902853
                                   5.376137
## log(POVPP)
                4.827899 1
                                   2.197248
## log(COLLPP) 10.529501 1
                                   3.244919
interaction.lm<-update(interaction.lm,.~.-log(ANDR)-log(CART)-log(REAG))
vif(lm(formula = log(GROSS) ~ VISIT + LST + log(POVPP) + log(COLLPP),data=seawatch.train))
                   GVIF Df GVIF^(1/(2*Df))
##
## VISIT
               1.662805 4
                                  1.065627
## LST
               1.473458 1
                                  1.213861
## log(POVPP) 1.739047
                                  1.318729
## log(COLLPP) 1.977095
                                  1.406092
# Summary
summary(interaction.lm)
##
## Call:
## lm(formula = log(GROSS) ~ VISIT + LST + log(POVPP) + log(COLLPP) +
       VISIT:log(REAG) + VISIT:log(COLLPP) + LST:log(YR) + LST:log(CART) +
##
##
       LST:log(REAG) + LST:log(COLLPP), data = seawatch.train)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                             Max
## -1.99511 -0.22558 0.02319 0.22924 1.48289
## Coefficients: (2 not defined because of singularities)
                        Estimate Std. Error t value Pr(>|t|)
                       24.272905 24.787894 0.979 0.328412
## (Intercept)
```

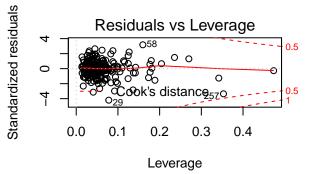
```
## VISIT2
                       -0.486731
                                   1.038692 -0.469 0.639763
                                              0.001 0.999080
## VISIT3
                        0.001534 1.329173
## VISIT4
                       -1.975110
                                   2.484788 -0.795 0.427434
## VISIT5
                        2.259105
                                   1.608448
                                              1.405 0.161399
## LST1
                      -62.300339 34.844070 -1.788 0.074986
## log(POVPP)
                                  0.055334 -2.116 0.035335 *
                       -0.117084
## log(COLLPP)
                        0.998388
                                  0.127257
                                              7.845 1.24e-13 ***
## VISIT1:log(REAG)
                        0.070206
                                   0.152628
                                              0.460 0.645927
## VISIT2:log(REAG)
                        0.472828
                                   0.170658
                                              2.771 0.006013 **
## VISIT3:log(REAG)
                        0.900123
                                   0.255660
                                              3.521 0.000511 ***
## VISIT4:log(REAG)
                        0.833409
                                   0.414798
                                              2.009 0.045587 *
## VISIT5:log(REAG)
                              NA
                                         NA
                                                 NA
                                                          NΑ
                                            -1.219 0.223902
## VISIT2:log(COLLPP)
                       -0.199478
                                  0.163610
                       -0.484505
                                   0.214585
## VISIT3:log(COLLPP)
                                            -2.258 0.024813 *
## VISIT4:log(COLLPP)
                       -0.281602
                                   0.345664
                                            -0.815 0.416033
## VISIT5:log(COLLPP)
                                                 NA
                              NA
                                         NΑ
                       -5.944179
                                   5.564870
                                            -1.068 0.286474
## LSTO:log(YR)
## LST1:log(YR)
                        7.959812
                                   6.399207
                                              1.244 0.214706
## LSTO:log(CART)
                       -0.323994
                                   0.120376 -2.692 0.007591 **
## LST1:log(CART)
                       -0.621472
                                   0.144371
                                             -4.305 2.40e-05 ***
## LST1:log(REAG)
                       -0.593899
                                   0.245864 -2.416 0.016426 *
## LST1:log(COLLPP)
                        0.622829
                                   0.165288
                                              3.768 0.000205 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.5047 on 251 degrees of freedom
## Multiple R-squared: 0.7779, Adjusted R-squared: 0.7602
## F-statistic: 43.97 on 20 and 251 DF, p-value: < 2.2e-16
# drop VISIT and log(POVPP)
interaction.lm<-update(interaction.lm,.~.-VISIT-log(POVPP))
summary(interaction.lm)
##
## Call:
  lm(formula = log(GROSS) ~ LST + log(COLLPP) + VISIT:log(REAG) +
       VISIT:log(COLLPP) + LST:log(YR) + LST:log(CART) + LST:log(REAG) +
##
##
       LST:log(COLLPP), data = seawatch.train)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -2.04089 -0.23343 0.02387 0.25991 1.47342
##
## Coefficients: (1 not defined because of singularities)
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       30.00053
                                  24.24917
                                             1.237 0.217159
## LST1
                      -63.22464
                                  34.57876
                                           -1.828 0.068654
## log(COLLPP)
                                   0.10903
                                             9.688 < 2e-16 ***
                        1.05626
## VISIT1:log(REAG)
                        0.04575
                                   0.14842
                                             0.308 0.758149
## VISIT2:log(REAG)
                        0.47390
                                   0.16882
                                            2.807 0.005386 **
## VISIT3:log(REAG)
                        0.84991
                                   0.25125
                                             3.383 0.000831 ***
## VISIT4:log(REAG)
                        0.90017
                                   0.40937
                                             2.199 0.028781 *
## VISIT5:log(REAG)
                        0.20828
                                   0.15853
                                             1.314 0.190075
## log(COLLPP):VISIT2 -0.25185
                                   0.11199 -2.249 0.025372 *
## log(COLLPP):VISIT3 -0.46487
                                   0.15620 -2.976 0.003200 **
```

```
## log(COLLPP):VISIT4 -0.47961
                                   0.25227
                                            -1.901 0.058406 .
## log(COLLPP):VISIT5
                             NA
                                        NA
                                                 NA
                                                          NΑ
## LSTO:log(YR)
                       -7.42012
                                   5.43890
                                             -1.364 0.173686
## LST1:log(YR)
                        6.67108
                                   6.38468
                                             1.045 0.297078
## LSTO:log(CART)
                       -0.46420
                                   0.09990
                                             -4.647 5.41e-06 ***
## LST1:log(CART)
                       -0.75559
                                   0.12527
                                             -6.032 5.67e-09 ***
## LST1:log(REAG)
                       -0.59373
                                   0.24244
                                             -2.449 0.015002 *
## LST1:log(COLLPP)
                        0.62645
                                   0.15968
                                             3.923 0.000112 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5058 on 255 degrees of freedom
## Multiple R-squared: 0.7734, Adjusted R-squared: 0.7592
## F-statistic: 54.39 on 16 and 255 DF, p-value: < 2.2e-16
par(mfrow=c(2,2))
plot(interaction.lm)
## Warning: not plotting observations with leverage one:
     152
##
## Warning: not plotting observations with leverage one:
```









Cross Validation

```
#MSE function
MSE<-function(pred,actual){</pre>
  return(mean((pred-actual)^2))
#predictions based on each model
pred.test<-predict(update(new.fit.lm,.~+VISIT:LST),newdata = seawatch.test)</pre>
## Warning in predict.lm(update(new.fit.lm, . ~ +VISIT:LST), newdata =
## seawatch.test): prediction from a rank-deficient fit may be misleading
pred.fit<-predict(fit.lm,newdata = seawatch.test)</pre>
pred.fit.new<-predict(new.fit.lm,newdata = seawatch.test)</pre>
pred.model2<-predict(model2,newdata = seawatch.test)</pre>
pred.interaction<-predict(interaction.lm,newdata = seawatch.test)</pre>
## Warning in predict.lm(interaction.lm, newdata = seawatch.test): prediction
## from a rank-deficient fit may be misleading
#MSE table
data.frame(
 Model=c("fit.lm","fit.powertrans","model2","interaction model","predict test"),
 MSE=c(MSE(pred.fit,seawatch.test$GROSS),MSE(exp(pred.fit.new),seawatch.test$GROSS),MSE(exp(pred.model
##
                 Model
                             MSE
## 1
                fit.lm 8248999
        fit.powertrans 5771242
## 2
                model2 5959332
## 3
```

• The model with lowest MSE so far is the log-transformation model.

4 interaction model 13573104

predict test 25648547

5