

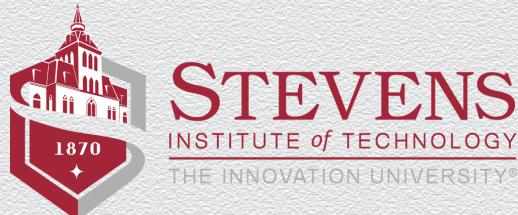
# CS306: Introduction to IT Security

## Fall 2018

### Lecture 9: Cloud & Network Security

Instructor: **Nikos Triandopoulos**

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# CS306: Tentative Syllabus

Week	Date	Topics	Reading	Assignment
1	Aug 28	Introduction	Ch. 1	-
2	Sep 4	Symmetric encryption	Ch. 2 & 12	Lab 1
3	Sep 11	Symmetric encryption II	Ch. 2 & 12	Lab 2, HW 1
4	Sep 18	Message authentication	Ch. 2 & 12	Lab 3, HW 1
5	Sep 25	Hash functions	Ch. 2 & 12	Lab 4
6	Oct 2	Public-key cryptography	Ch. 2 & 12	Lab 5
-	Oct 9	No class (Monday schedule)		Help session
7	Oct 16	Midterm (closed books)	All materials covered	No labs

# CS306: Tentative Syllabus (continued)

Week	Date	Topics	Reading	Assignment
8	Oct 23	User authentication	Ch. 2	No labs
9	Oct 30	Access Control	Ch. 2	Lab 6
10	Nov 6	Cloud & Network security	Ch. 6, 8	Lab 7, HW2, HW3
11	Nov 13	Web, Software & Database		
12	Nov 20	Privacy		
13	Nov 27	Economics		
14	Dec 4	Legal & ethical issues		
15	Dec 11 (or later)	Final (closed books)	All materials covered*	

## **Number-theoretic facts**

# Public-key encryption algorithms

Typically

- ◆ Based on **number theory & modular arithmetic**
- ◆ Security relies on some **hardness assumption**
  - ◆ a mathematical computational problem that is assumed to be hard to solve

We will learn about two such

- ◆ RSA
  - ◆ based on the hardness of factoring large numbers
- ◆ El Gamal
  - ◆ based on the hardness of solving discrete logarithm
  - ◆ using the same idea as Diffie-Hellman key agreement

# Multiplicative inverses

The residues modulo a positive integer  $n$  comprise set  $Z_n = \{0, 1, 2, \dots, n - 1\}$

- ◆ let  $x$  and  $y$  be two elements in  $Z_n$  such that  $x y \bmod n = 1$ 
  - ◆ we say:  $y$  is the multiplicative inverse of  $x$  in  $Z_n$
  - ◆ we write:  $y = x^{-1}$
- ◆ example:
  - ◆ multiplicative inverses of the residues modulo 11

$x$	0	1	2	3	4	5	6	7	8	9	10
$x^{-1}$		1	6	4	3	9	2	8	7	5	10

# Multiplicative inverses (cont'ed)

## Fact

An element  $x$  in  $\mathbb{Z}_n$  has a multiplicative inverse iff  $x$  and  $n$  are **relatively prime**

- ◆ e.g., the only elements of  $\mathbb{Z}_{10}$  having a multiplicative inverse are 1, 3, 7, 9

$x$	0	1	2	3	4	5	6	7	8	9
$x^{-1}$		1		7				3		9

## Corollary

If  $p$  is prime, every nonzero residue in  $\mathbb{Z}_p$  has a multiplicative inverse

## Fact

If they exist, inverses are computed by the **Extended Euclidean Algorithm**

# Multiplicative group $Z_n^*$

Defined as the subset of  $Z_n$  containing all integers that are relative prime to n

- ◆ closed under multiplication, every element has an inverse

Two cases

- ◆ if n is a **prime** number, then all non-zero elements in  $Z_n$  have an inverse
  - ◆  $Z_7^* = \{1, 2, 3, 4, 5, 6\}$ ,  $n = 7$
  - ◆  $2 \cdot 4 = 1 \pmod{7}$ ,  $3 \cdot 5 = 1 \pmod{7}$ ,  $6 \cdot 6 = 1 \pmod{7}$ ,  $1 \cdot 1 = 1 \pmod{7}$
- ◆ if n is **not prime**, not all integers in  $Z_n$  have an inverse
  - ◆  $Z_{10}^* = \{1, 3, 7, 9\}$ ,  $n = 10$
  - ◆  $3 \cdot 7 = 1 \pmod{10}$ ,  $9 \cdot 9 = 1 \pmod{10}$ ,  $1 \cdot 1 = 1 \pmod{10}$

# Order of a multiplicative group

The order of a group is its cardinality of group (i.e., number of its elements)

- ◆ the totient function  $\phi(n)$  denotes the order of  $Z_n^*$ , i.e.,  $\phi(n) = |Z_n^*|$
- ◆ **if  $n = p$  is prime**, then the order of  $Z_p^* = \{1, 2, \dots, p-1\}$  is  $p-1$ , i.e.,  $\phi(n) = p-1$ 
  - ◆ e.g.,  $Z_7^* = \{1, 2, 3, 4, 5, 6\}$ ,  $n = 7$ ,  $\phi(7) = 6$
- ◆ **if  $n$  is not prime**,  $\phi(n) = n(1-1/p_1)(1-1/p_2)\dots(1-1/p_k)$ , where  $n = p^{e_1} p^{e_2} \dots p^{e_k}$ 
  - ◆ e.g.,  $Z_{10}^* = \{1, 3, 7, 9\}$ ,  $n = 10$ ,  $\phi(10) = 4$
- ◆ if  $n = p q$ , where  $p$  and  $q$  are distinct primes, then  $\phi(n) = (p-1)(q-1)$ 
  - ◆ difficult problem: Given  $n = pq$ , where  $p, q$  are primes, find  $p$  and  $q$  or  $\phi(n)$

# Fermat's Little Theorem (case 1)

## Theorem

- If  $p$  is a prime, then for each nonzero  $x$  in  $\mathbb{Z}_p$ , we have  $x^{p-1} \bmod p = 1$
- ◆ example ( $p = 5$ ):

$$1^4 \bmod 5 = 1$$

$$2^4 \bmod 5 = 16 \bmod 5 = 1$$

$$3^4 \bmod 5 = 81 \bmod 5 = 1$$

$$4^4 \bmod 5 = 256 \bmod 5 = 1$$

## Corollary

- If  $p$  is a prime, then the multiplicative inverse of each nonzero residue  $x$  in  $\mathbb{Z}_p$  is  $x^{p-2} \bmod p$

- ◆ proof:

$$x(x^{p-2} \bmod p) \bmod p = xx^{p-2} \bmod p = x^{p-1} \bmod p = 1$$

# Euler's Theorem (case 2)

## Theorem

For each element  $x$  in  $\mathbb{Z}_n^*$ , we have  $x^{\phi(n)} \bmod n = 1$

- ◆ example ( $n = 10$ )
  - ◆  $\mathbb{Z}_{10}^* = \{1, 3, 7, 9\}$ ,  $n = 10$ ,  $\phi(10) = 4$
  - ◆  $3^{\phi(10)} \bmod 10 = 3^4 \bmod 10 = 81 \bmod 10 = 1$
  - ◆  $7^{\phi(10)} \bmod 10 = 7^4 \bmod 10 = 2401 \bmod 10 = 1$
  - ◆  $9^{\phi(10)} \bmod 10 = 9^4 \bmod 10 = 6561 \bmod 10 = 1$

# Computing in the exponent

For the multiplicative group  $Z_n^*$ , we can reduce the exponent modulo  $\phi(n)$

$$x^y \bmod n = x^{k\phi(n) + r} \bmod n = (x^{\phi(n)})^k x^r \bmod n = x^{y \bmod \phi(n)} \bmod n$$

- ◆ **example**

- ◆  $Z_{10}^* = \{1, 3, 7, 9\}$ ,  $n = 10$ ,  $\phi(10) = 4$
- ◆  $3^{1590} \bmod 10 = 3^{1590 \bmod 4} \bmod 10 = 3^2 \bmod 10 = 9$
- ◆ how about  $2^8 \bmod 10$ ?

Corollary: For  $Z_p^*$ , we can reduce the exponent modulo  $p-1$

- ◆ **example**

- ◆  $Z_p^* = \{1, 2, \dots, p-1\}$ ,  $p = 19$ ,  $\phi(19) = 18$
- ◆  $15^{39} \bmod 19 = 15^{39 \bmod 18} \bmod 19 = 15^3 \bmod 19 = 12$

# Euclid's GCD algorithm

Computes the greater common divisor by repeatedly applying the formula

$$\gcd(a, b) = \gcd(b, a \bmod b)$$

- ◆ example
  - ◆  $\gcd(412, 260) = 4$

**Algorithm** *EuclidGCD(a, b)*

**Input** integers *a* and *b*

**Output**  $\gcd(a, b)$

**if** *b* = 0

**return** *a*

**else**

**return** *EuclidGCD(b, a mod b)*

a	412	260	152	108	44	20	4
b	260	152	108	44	20	4	0

# \*Proof of correctness

We need to prove that  $\text{GCD}(a, b) = \text{GCD}(b, a \bmod b)$

- ◆ facts
  - ◆ every divisor of  $a$  and  $b$  is a divisor of  $b$  and  $(a \bmod b)$ 
    - ◆ because  $(a \bmod b)$  can be written as the sum of  $a$  and a multiple of  $b$ , i.e.,  $a \bmod b = a + kb$ , for some integer  $k$
    - ◆ similarly, every divisor of  $b$  and  $(a \bmod b)$  is a divisor of  $a$  and  $b$ 
      - ◆ because  $a$  can be written as the sum of  $(a \bmod b)$  and a multiple of  $b$ , i.e.,  $a = kb + (a \bmod b)$ , for some integer  $k$
  - ◆ therefore the set of all divisors of  $a$  and  $b$  is **the same** with the set of all divisors of  $b$  and  $(a \bmod b)$ , thus the greatest should also be the same

# Extended Euclidean algorithm

## Theorem

If, given positive integers  $a$  and  $b$ ,  
 $d$  is the smallest positive integer  
s.t.  $d = ia + jb$ , for some integers  
 $i$  and  $j$ , then  $d = \gcd(a, b)$

- ◆ example
  - ◆  $a = 21, b = 15$
  - ◆  $d = 3, i = 3, j = -4$
  - ◆  $3 = 3 \cdot 21 + (-4) \cdot 15 = 63 - 60 = 3$

**Algorithm** *Extended-Euclid(a, b)*

**Input** integers  $a$  and  $b$

**Output**  $\gcd(a, b)$ ,  $i$  and  $j$

s.t.  $ia+jb = \gcd(a,b)$

**if**  $b = 0$

**return**  $(a, 1, 0)$

$(d', x', y') = \text{Extended-Euclid}(b, a \bmod b)$

$(d, x, y) = (d', y', x' - [a/b]y')$

**return**  $(d, x, y)$

# Computing multiplicative inverses

Goal: Compute the multiplicative inverse of  $a$  in  $\mathbb{Z}_b$

Fact

- ◆ given two numbers  $a$  and  $b$ , there exist integers  $x, y$  s.t.  $\textcolor{red}{x} a + \textcolor{red}{y} b = \gcd(a, b)$
- ◆ can be computed efficiently by the extended Euclidean algorithm

Therefore

- ◆ the multiplicative inverse of  $a$  in  $\mathbb{Z}_b$  exists if and only if  $\gcd(a, b) = 1$ 
  - ◆ if the extended Euclidean algorithm computes  $x$  and  $y$  s.t.  $\textcolor{red}{x} a + \textcolor{red}{y} b = 1$  then the multiplicative inverse of  $a$  in  $\mathbb{Z}_b$  is  $\textcolor{red}{x}$

# The RSA algorithm

# The RSA algorithm (for encryption)

## General case

Setup (run by a given user)

- ◆  $n = p \cdot q$ , with  $p$  and  $q$  primes
- ◆  $e$  relatively prime to  $\phi(n) = (p - 1)(q - 1)$
- ◆  $d$  inverse of  $e$  in  $Z_{\phi(n)}$

Keys

- ◆ public key is  $K_{PK} = (n, e)$
- ◆ private key is  $K_{SK} = d$

Encryption

- ◆  $C = M^e \text{ mod } n$  for plaintext  $M$  in  $Z_n$

Decryption

- ◆  $M = C^d \text{ mod } n$

## Example

Setup

- ◆  $p = 7, q = 17, n = 7 \cdot 17 = 119$
- ◆  $e = 5, \phi(n) = 6 \cdot 16 = 96$
- ◆  $d = 77$

Keys

- ◆ public key is  $(119, 5)$
- ◆ private key is  $77$

Encryption

- ◆  $C = 19^5 \text{ mod } 119 = 66$  for  $M = 19$  in  $Z_{119}$

Decryption

- ◆  $M = 66^{77} \text{ mod } 119 = 19$

# Another complete example

- ◆ Setup
  - ◆  $p = 5, q = 11, n = 5 \cdot 11 = 55$
  - ◆  $\phi(n) = 4 \cdot 10 = 40$
  - ◆  $e = 3, d = 27 \quad (3 \cdot 27 = 81 = 2 \cdot 40 + 1)$
- ◆ Encryption
  - ◆  $C = M^3 \bmod 55$  for  $M$  in  $\mathbb{Z}_{55}$
- ◆ Decryption
  - ◆  $M = C^{27} \bmod 55$

$M$	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
$C$	1	8	27	9	15	51	13	17	14	10	11	23	52	49	20	26	18	2
$M$	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
$C$	39	25	21	33	12	19	5	31	48	7	24	50	36	43	22	34	30	16
$M$	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
$C$	53	37	29	35	6	3	32	44	45	41	38	42	4	40	46	28	47	54

# \*Correctness of RSA

## Given

## Setup

- ◆  $n = p \cdot q$ , with  $p$  and  $q$  primes
- ◆  $e$  relatively prime to  $\phi(n) = (p - 1)(q - 1)$
- ◆  $d$  inverse of  $e$  in  $Z_{\phi(n)}$  **(1)**

## Encryption

- ◆  $C = M^e \text{ mod } n$  for plaintext  $M$  in  $Z_n$

## Decryption

- ◆  $M = C^d \text{ mod } n$

## Fermat's Little Theorem **(2)**

- ◆ for prime  $p$ , non-zero  $x$ :  $x^{p-1} \text{ mod } p = 1$

## Analysis

Need to show

- ◆  $M^{ed} = M \text{ mod } p \cdot q$
  - ◆ Use **(1)** and apply **(2)** for prime  $p$
  - ◆  $M^{ed} = M^{ed-1}M = (M^{p-1})^{h(q-1)}M$
  - ◆  $M^{ed} = 1^{h(q-1)}M \text{ mod } p = M \text{ mod } p$
- Similarly (w.r.t. prime  $q$ )
- ◆  $M^{ed} = M \text{ mod } q$
- Thus, since  $p, q$  are co-primes
- ◆  $M^{ed} = M \text{ mod } p \cdot q$

# A useful symmetry

## [1] RSA setting

- ◆ modulo  $n = p \cdot q$ ,  $p$  &  $q$  are **primes**, public & private keys  $(e, d)$ :  $d \cdot e = 1 \pmod{(p-1)(q-1)}$

## [2] RSA operations involve **exponentiations**, thus they are **interchangeable**

- ◆  $C = M^e \pmod{n}$  (encryption of plaintext  $M$  in  $Z_n$ )
- ◆  $M = C^d \pmod{n}$  (decryption of ciphertext  $C$  in  $Z_n$ )

Indeed, their order of execution does not matter:  $(M^e)^d = (M^d)^e \pmod{n}$

## [3] RSA operations involve exponents that “cancel out”, thus they are **complementary**

- ◆  $x^{(p-1)(q-1)} \pmod{n} = 1$  (Euler's Theorem)

Indeed, they invert each other:  $(M^e)^d = (M^d)^e = M^{ed} = M^{k(p-1)(q-1)+1} \pmod{n}$

$$= (M^{(p-1)(q-1)})^k \cdot M = 1^k \cdot M = M \pmod{n}$$

# Signing with RSA

RSA functions are complementary & interchangeable w.r.t. order of execution

- ◆ core property:  $M^{ed} = M \text{ mod } p \cdot q$  for any message  $M$  in  $Z_n$

RSA cryptosystem lends itself to a signature scheme

- ◆ ‘reverse’ use of keys is possible :  $(M^d)^e = M \text{ mod } p \cdot q$
- ◆ signing algorithm  $\text{Sign}(M,d,n)$ :  $\sigma = M^d \text{ mod } n$  for message  $M$  in  $Z_n$
- ◆ verifying algorithm  $\text{Vrfy}(\sigma,M,e,n)$ : return  $M == \sigma^e \text{ mod } n$

# The RSA algorithm (for signing)

## General case

Setup (run by a given user)

- ◆  $n = p \cdot q$ , with  $p$  and  $q$  primes
- ◆  $e$  relatively prime to  $\phi(n) = (p - 1)(q - 1)$
- ◆  $d$  inverse of  $e$  in  $Z_{\phi(n)}$

Keys (same as in encryption)

- ◆ public key is  $K_{PK} = (n, e)$
- ◆ private key is  $K_{SK} = d$

Sign

- ◆  $\sigma = M^d \text{ mod } n$  for message  $M$  in  $Z_n$

Verify

- ◆ Check if  $M = \sigma^e \text{ mod } n$

## Example

Setup

- ◆  $p = 7, q = 17, n = 7 \cdot 17 = 119$
- ◆  $e = 5, \phi(n) = 6 \cdot 16 = 96$
- ◆  $d = 77$

Keys

- ◆ public key is  $(119, 5)$
- ◆ private key is  $77$

Signing

- ◆  $\sigma = 66^{77} \text{ mod } 119 = 19$  for  $M = 66$  in  $Z_{119}$

Verification

- ◆ Check if  $M = 19^5 \text{ mod } 119 = 66$

# Digital signatures & hashing

Very often digital signatures are used with hash functions

- ◆ the hash of a message is signed, instead of the message itself

## **Signing message M**

- ◆ let  $h$  be a cryptographic hash function, assume RSA setting  $(n, d, e)$
- ◆ compute signature  $\sigma$  on message  $M$  as:  $\sigma = h(M)^d \text{ mod } n$
- ◆ send  $\sigma, M$

## **Verifying signature $\sigma$**

- ◆ use public key  $(e, n)$  to compute (candidate) hash value  $H = \sigma^e \text{ mod } n$
- ◆ if  $H = h(M)$  output ACCEPT, else output REJECT

# Security of RSA

Based on difficulty of **factoring** large numbers (into large primes), i.e.,  $n = p \cdot q$  into  $p, q$

- ◆ note that for RSA to be secure, both  $p$  and  $q$  must be large primes
- ◆ widely believed to hold true
  - ◆ since 1978, subject of extensive cryptanalysis without any serious flaws found
  - ◆ best known algorithm takes exponential time in security parameter (key length  $|n|$ )
- ◆ how can you break RSA if you can factor?

Current practice is using 2,048-bit long RSA keys (617 decimal digits)

- ◆ estimated computing/memory resources needed to factor an RSA number within one year

Length (bits)	PCs	Memory
430	1	128MB
760	215,000	4GB
1,020	$342 \times 10^6$	170GB
1,620	$1.6 \times 10^{15}$	120TB

# RSA challenges

Challenges for breaking the RSA cryptosystem of various key lengths (i.e.,  $|n|$ )

- ◆ known in the form RSA-`key bit length' expressed in bits or decimal digits
- ◆ provide empirical evidence/confidence on strength of specific RSA instantiations

## Known attacks

- ◆ RSA-155 (**512-bit**) factored in **4 mo.** using 35.7 CPU-years or 8000 Mips-years (**1999**) and 292 machines
  - ◆ 160 175-400MHz SGI/Sun, 8 250MHz SGI/Origin, 120 300-450MHz Pent. II, 4 500MHz Digital/Compaq
- ◆ RSA-**640** factored in **5 mo.** using 30 2.2GHz CPU-years (**2005**)
- ◆ RSA-**220** (**729-bit**) factored in **5 mo.** using 30 2.2GHz CPU-years (**2005**)
- ◆ RSA-**232** (**768-bit**) factored in **2 years** using **parallel** computers 2K CPU-years (1-core 2.2GHz AMD Opteron) (**2009**)

## Most interesting challenges

- ◆ prizes for factoring RSA-**1024**, RSA-**2048** is \$100K, \$200K – estimated at 800K, 20B Mips-centuries

# Deriving an RSA key pair

- ◆ public key is pair of integers  $(e, n)$ , secret key is  $(d, n)$  or  $d$
- ◆ the value of  $n$  should be quite large, a product of two large primes,  $p$  and  $q$
- ◆ often  $p, q$  are nearly 100 digits each, so  $n \approx 200$  decimal digits ( $\sim 512$  bits)
  - ◆ but 2048-bit keys are becoming a standard requirement nowadays
- ◆ the larger the value of  $n$  the harder to factor to infer  $p$  and  $q$ 
  - ◆ but also the slower to process messages
- ◆ a relatively large integer  $e$  is chosen
  - ◆ e.g., by choosing  $e$  as a prime that is larger than both  $(p - 1)$  and  $(q - 1)$
  - ◆ why?
- ◆  $d$  is chosen s.t.  $e \cdot d = 1 \pmod{(p - 1)(q - 1)}$ 
  - ◆ how?

# Discussion on RSA

- ◆ Assume  $p = 5, q = 11, n = 5 \cdot 11 = 55, \phi(n) = 40, e = 3, d = 27$ 
  - ◆ why encrypting small messages, e.g.,  $M = 2, 3, 4$  is tricky?
  - ◆ recall that the ciphertext is  $C = M^3 \bmod 55$  for  $M$  in  $\mathbb{Z}_{55}$

$M$	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
$C$	1	8	27	9	15	51	13	17	14	10	11	23	52	49	20	26	18	2
$M$	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
$C$	39	25	21	33	12	19	5	31	48	7	24	50	36	43	22	34	30	16
$M$	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
$C$	53	37	29	35	6	3	32	44	45	41	38	42	4	40	46	28	47	54

# Discussion on RSA

- ◆ Assume  $p = 5, q = 11, n = 5 \cdot 11 = 55, \phi(n) = 40, e = 3, d = 27$ 
  - ◆ why encrypting small messages, e.g.,  $M = 2, 3, 4$  is tricky?
  - ◆ recall that the ciphertext is  $C = M^3 \text{ mod } 55$  for  $M$  in  $\mathbb{Z}_{55}$
- ◆ Assume  $n = 20434394384355534343545428943483434356091 = p \cdot q$ 
  - ◆ can  $e$  be the number 4343253453434536?
- ◆ Are there problems with applying RSA in practice?
  - ◆ what other algorithms are required to be available to the user?
- ◆ Are there problems with respect to RSA security?
  - ◆ does it satisfy CPA security?

# Algorithmic issues

The implementation of the RSA cryptosystem requires various algorithms

- ◆ Main issues
  - ◆ representation of integers of arbitrarily large size; and
  - ◆ arithmetic operations on them, namely computing modular powers
- ◆ Required algorithms (at setup)
  - ◆ generation of **random numbers** of a given number of bits (to compute candidates **p, q**)
  - ◆ **primality testing** (to check that candidates **p, q** are prime)
  - ◆ computation of the **GCD** (to verify that **e** and  $\phi(n)$  are relatively prime)
  - ◆ computation of the **multiplicative inverse** (to compute **d** from **e**)

# Modular powers

## Repeated squaring algorithm

- ◆ speeds up computation of  $a^p \bmod n$
- ◆ write the exponent  $p$  in binary
  - ◆  $p = p_{b-1} p_{b-2} \dots p_1 p_0$
- ◆ start with  $Q_1 = a^{p_{b-1}} \bmod n$
- ◆ repeatedly compute  
 $Q_i = ((Q_{i-1})^2 \bmod n)a^{p_{b-i}} \bmod n$
- ◆ obtain  $Q_b = a^p \bmod n$

In total  $\mathbf{O}(\log p)$  arithmetic operations

## Example

- ◆  $3^{18} \bmod 19$  ( $18 = 10010$ )
- ◆  $Q_1 = 3^1 \bmod 19 = 3$
- ◆  $Q_2 = (3^2 \bmod 19)3^0 \bmod 19 = 9$
- ◆  $Q_3 = (9^2 \bmod 19)3^0 \bmod 19 = 81 \bmod 19 = 5$
- ◆  $Q_4 = (5^2 \bmod 19)3^1 \bmod 19 = (25 \bmod 19)3 \bmod 19 = 18 \bmod 19 = 18$
- ◆  $Q_5 = (18^2 \bmod 19)3^0 \bmod 19 = (324 \bmod 19) \bmod 19 = 17 \cdot 19 + 1 \bmod 19 = 1$

# Pseudo-primality testing

Testing whether a number is prime (**primality testing**) is a difficult problem

An integer  $n \geq 2$  is said to be a base- $x$  **pseudo-prime** if

- ◆  $x^{n-1} \bmod n = 1$  (Fermat's little theorem)
- ◆ Composite base- $x$  pseudo-primes are rare
  - ◆ a random 100-bit integer is a composite base-2 pseudo-prime with probability less than  $10^{-13}$
  - ◆ the smallest composite base-2 pseudo-prime is 341
- ◆ Base- $x$  pseudo-primality testing for an integer  $n$ 
  - ◆ check whether  $x^{n-1} \bmod n = 1$
  - ◆ can be performed efficiently with the repeated squaring algorithm

# Security properties

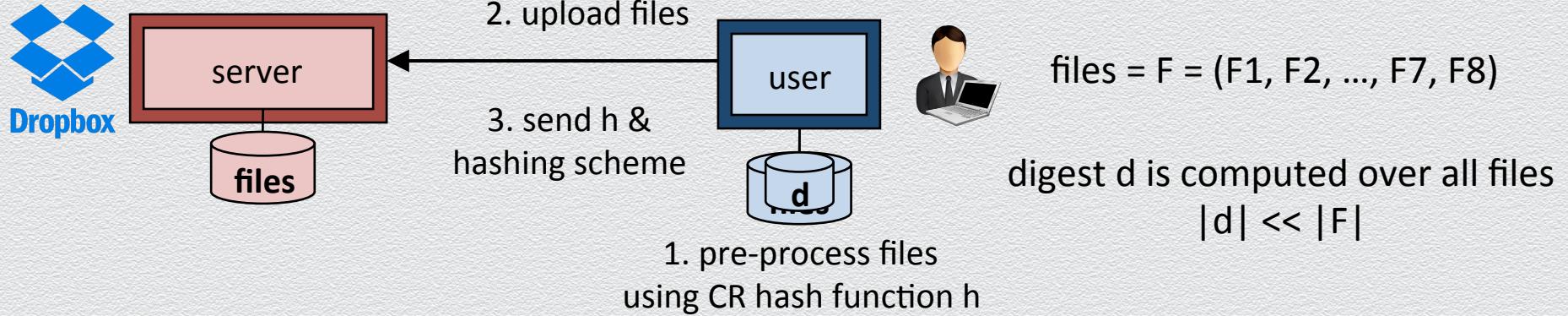
- ◆ Plain RSA is deterministic
  - ◆ why is this a problem?
- ◆ Plain RSA is also homomorphic
  - ◆ what does this mean?
  - ◆ multiply ciphertexts to get ciphertext of multiplication!
  - ◆  $[(m_1)^e \text{ mod } N][(m_2)^e \text{ mod } N] = (m_1 m_2)^e \text{ mod } N$
  - ◆ however, not additively homomorphic

# Real-world usage of RSA

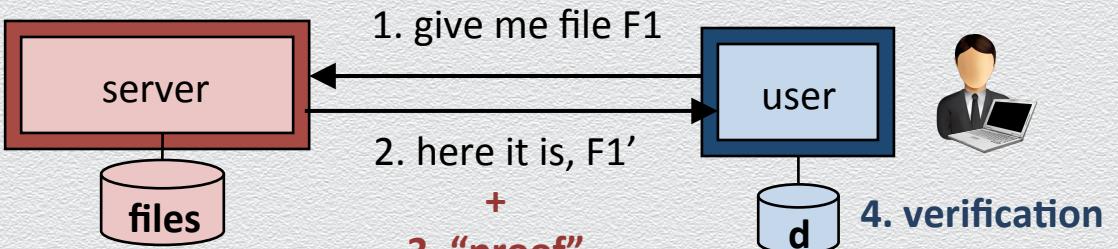
- ◆ Randomized RSA
  - ◆ to encrypt message  $M$  under an RSA public key  $(e, n)$ , generate a new random session AES key  $K$ , compute the ciphertext as  $[K^e \bmod n, \text{AES}_K(M)]$
  - ◆ prevents an adversary distinguishing two encryptions of the same  $M$  since  $K$  is chosen at random every time encryption takes place
- ◆ Optimal Asymmetric Encryption Padding (OAEP)
  - ◆ roughly, to encrypt  $M$ , choose random  $r$ , encode  $M$  as  $M' = [X = M \oplus H_1(r), Y = r \oplus H_2(X)]$  where  $H_1$  and  $H_2$  are cryptographic hash functions, then encrypt it as  $(M')^e \bmod n$

# **Database-as-a-service authentication model**

# Securing your cloud storage optimally – setup



# Securing your cloud storage optimally – data authentication



$F = (F_1, F_2, \dots, F_7, F_8)$  (or helper information)

user has

- ◆ authentic digest  $d$  (locally stored)
- ◆ file  $F_1'$  (to be checked)
- ◆ **proof** (to help checking integrity)

verification involves

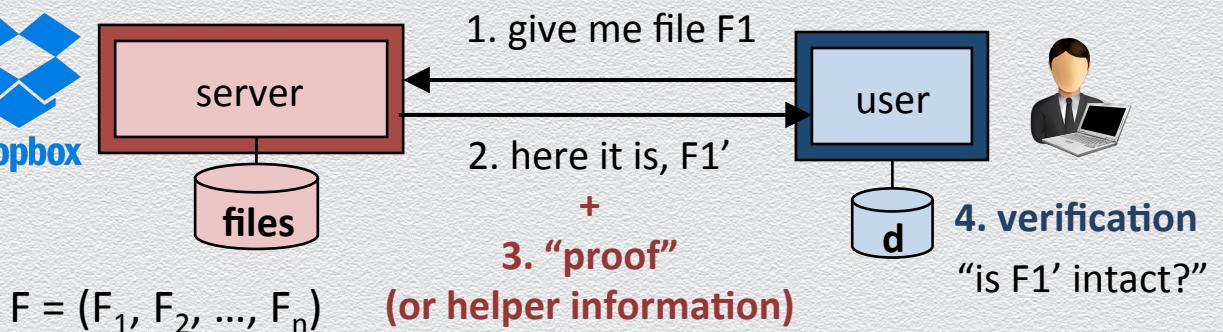
- ◆ combine file  $F_1'$  with the proof to re-compute candidate digest  $d'$
- ◆ check if  $d' = d$
- ◆ if yes, then  $F_1$  is intact; otherwise tampering is detected!

## goals

security: Step 4 is reliable test  
efficiency:

- ◆  $d$  is as small as possible
- ◆ proof is as small as possible
- ◆ verification is as fast as possible

# Hashing the files: Individually or as a whole?



let  $h_i = h(F_i)$ ,  $1 \leq i \leq n$

$$d = (h_1, h_2, \dots, h_n)$$

Vs.

$$d = h(h_1 || h_2 || \dots || h_n)$$

Vs.

$$d = h(F_1 || F_2 || \dots || F_n)$$

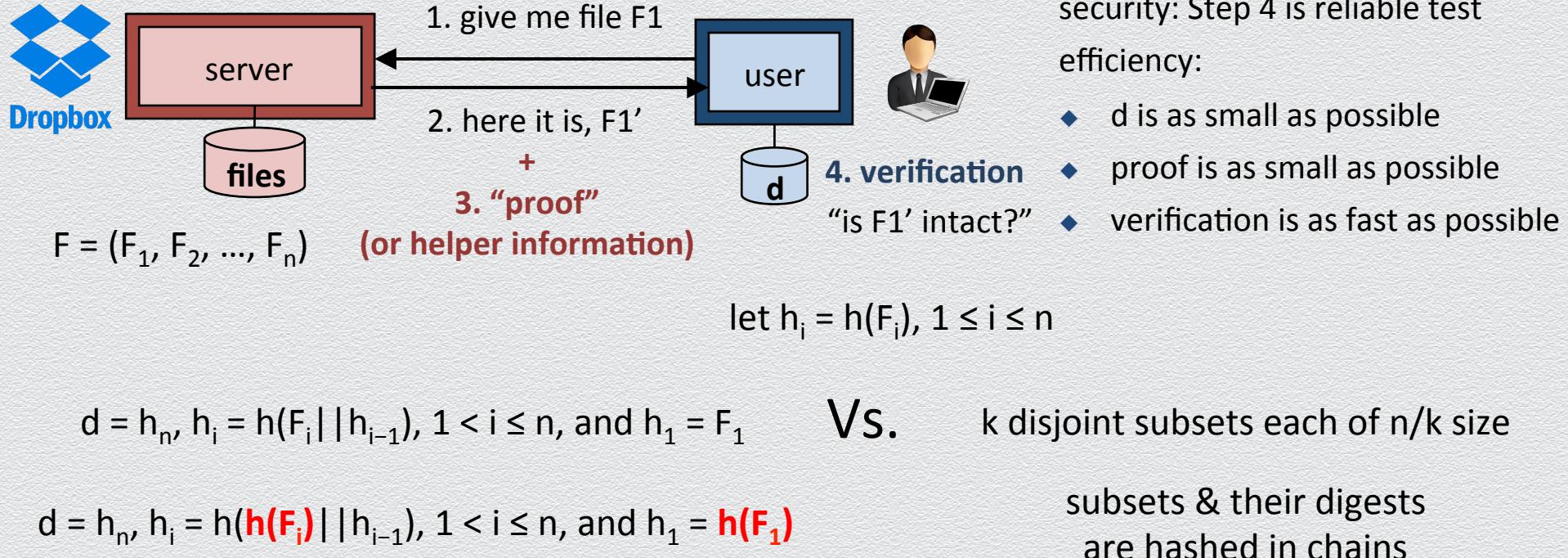
## goals

security: Step 4 is reliable test

efficiency:

- ◆  $d$  is as small as possible
- ◆ proof is as small as possible
- ◆ verification is as fast as possible

# Hashing the files: In a chain or in a partition?

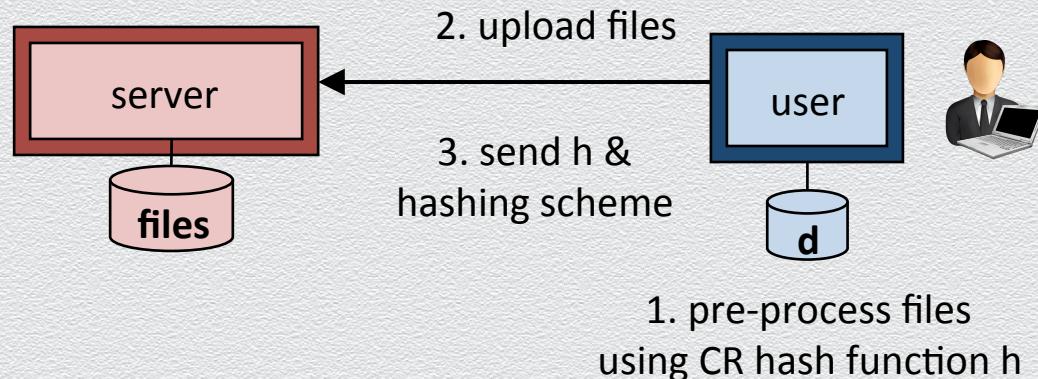


# Towards an optimal hashing scheme

## Lessons learned

- ◆ files should better be individually hashed as  $h_i = h(F_i)$ ,  $1 \leq i \leq n$ , over which the final digest should be computed
- ◆ for  $k > 2$ :
  - ◆ hashing  $k$  files in a hash chain is preferable to hashing files as a whole
  - ◆ hash chains over  $k$  objects (hash values/files) result in **unbalanced** verification costs
    - ◆ e.g., proof size/verification time are sensitive to a file's position in the hash chain
- ◆ hashing file subsets individually across a balanced partition of the files:
  - ◆ offers trade-offs between space and verification costs
  - ◆ allows for hierarchical hashing schemes

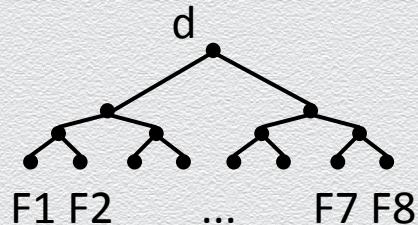
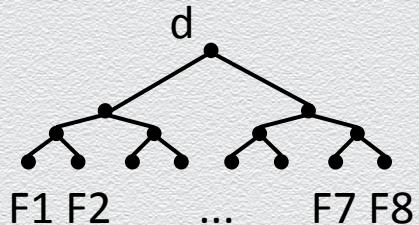
# Hashing via the Merkle tree



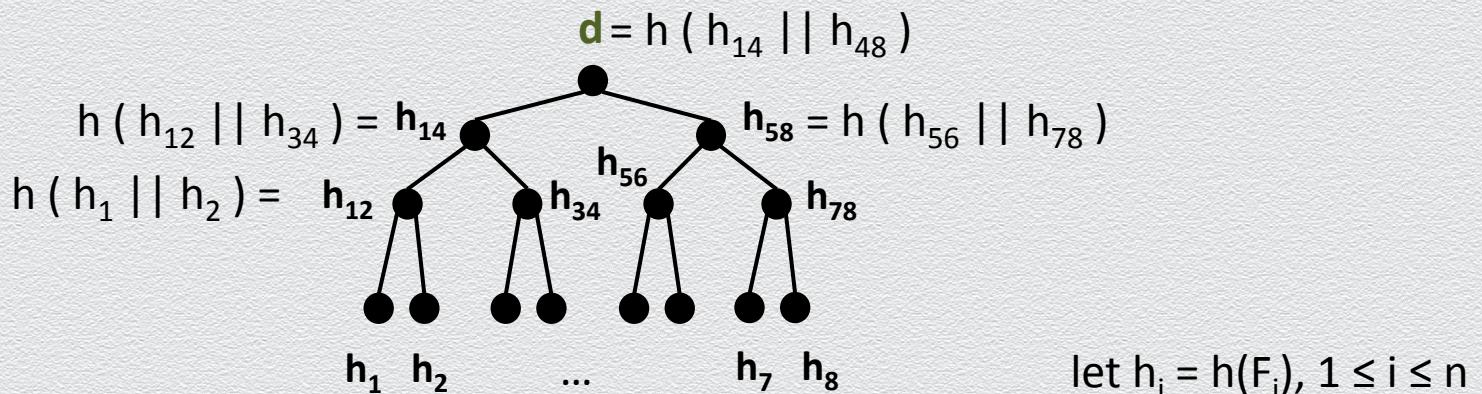
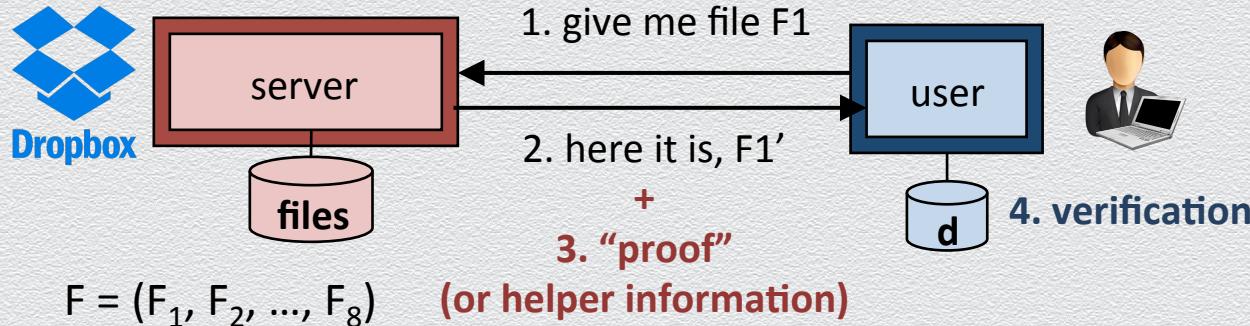
files =  $F = (F_1, F_2, \dots, F_7, F_8)$

digest  $d$  is computed over all files  
 $|d| \ll |F|$

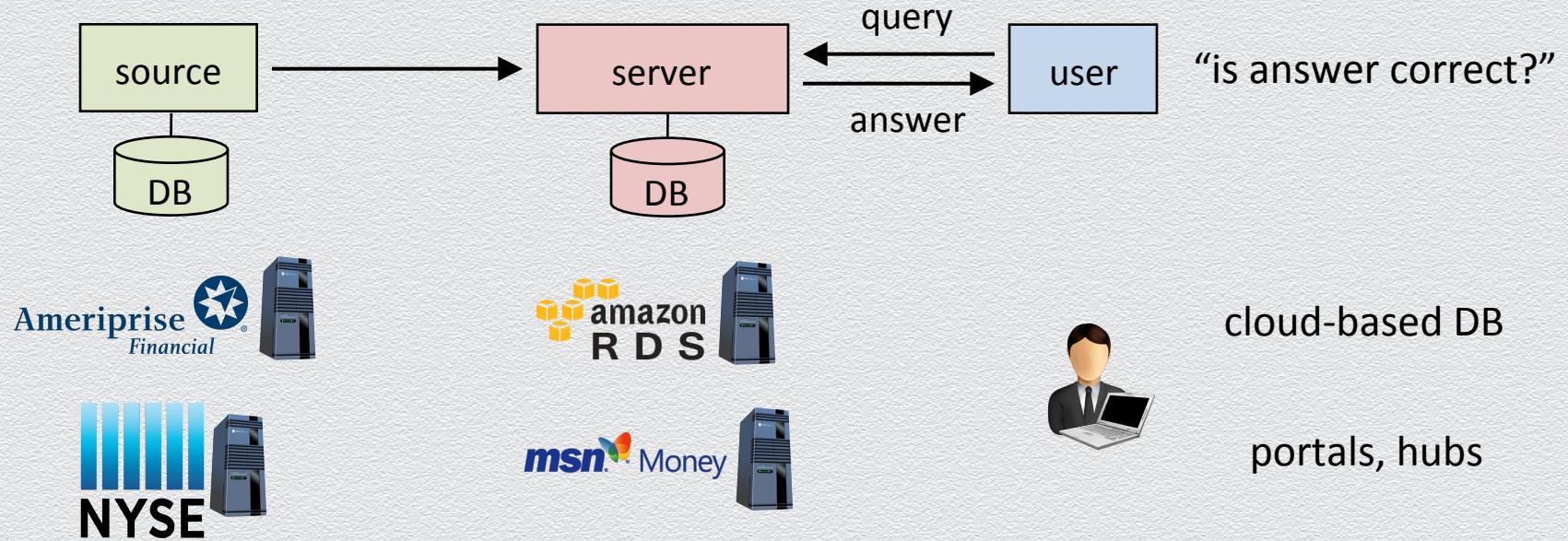
$h$ : collision resistant iterative  
hash function (e.g., SHA-2)



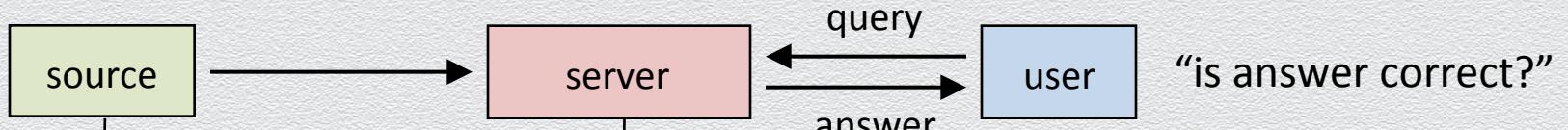
# The Merkle tree



# Generalization: DB-as-a-service authentication model

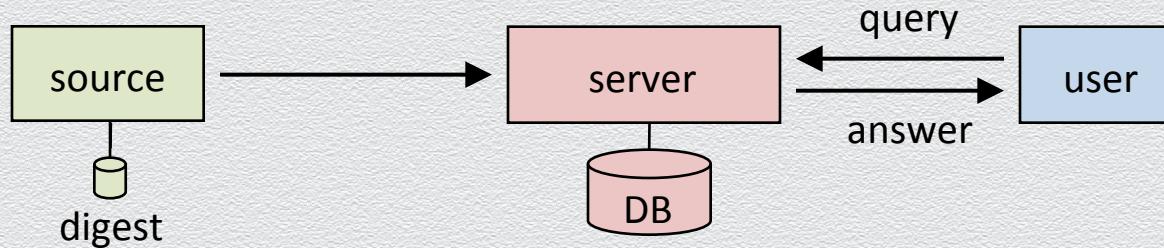


# Generalization: DB-as-a-service authentication model



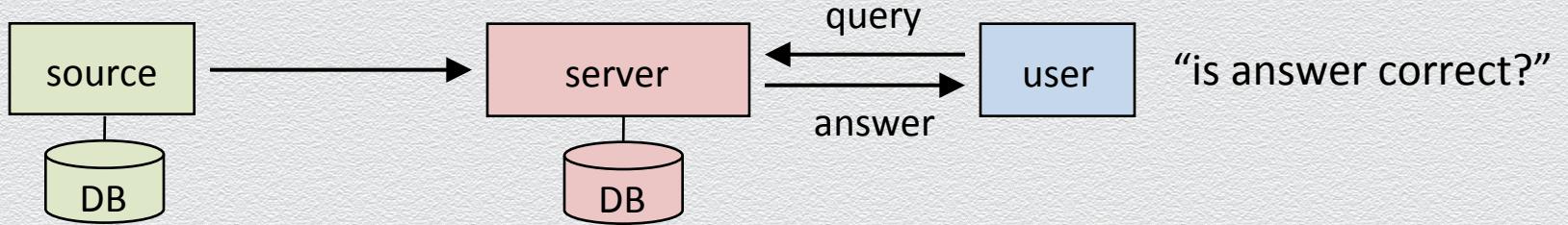
Internet protocols  
(DNS, OCSP)

# Generalization: DB-as-a-service authentication model



file hosting

# DB-as-a-service authentication model

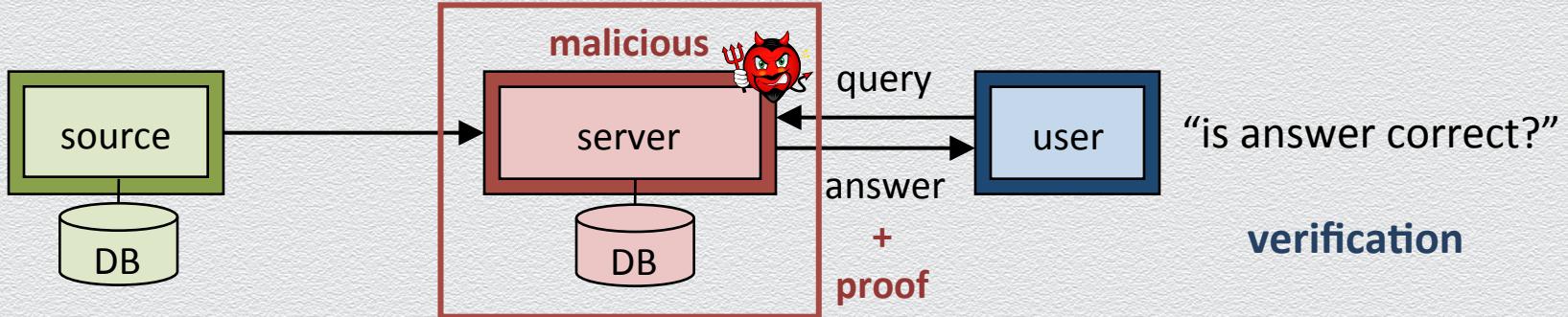


**Integrity checks** offer authenticated queries



guarantees correct answer, as if coming directly from the source!

# DB-as-a-service authentication model



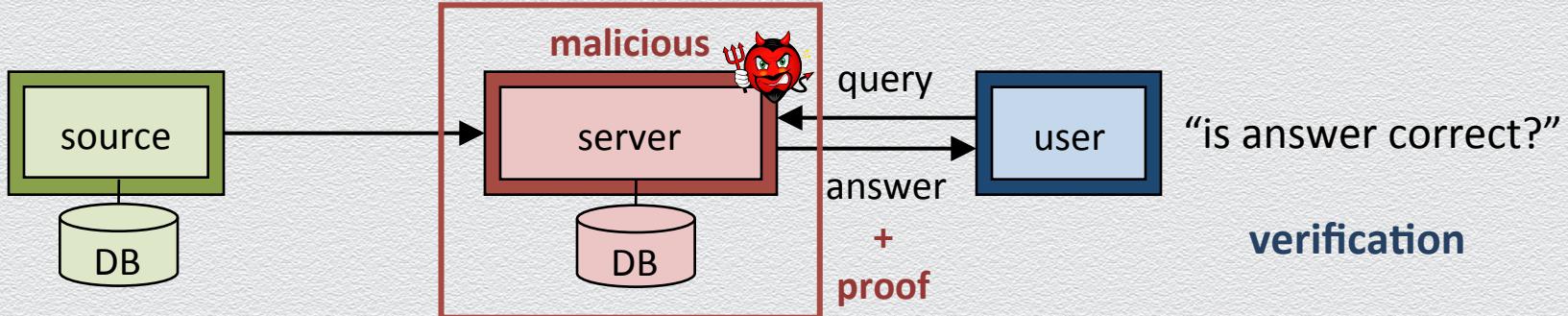
**Integrity checks** offer authenticated queries

- ◆ crypto-based: harden data/computations to provide verifiable answers
- ◆ reliable: allow no false positives or negatives



crypto does its work!

# DB-as-a-service authentication model



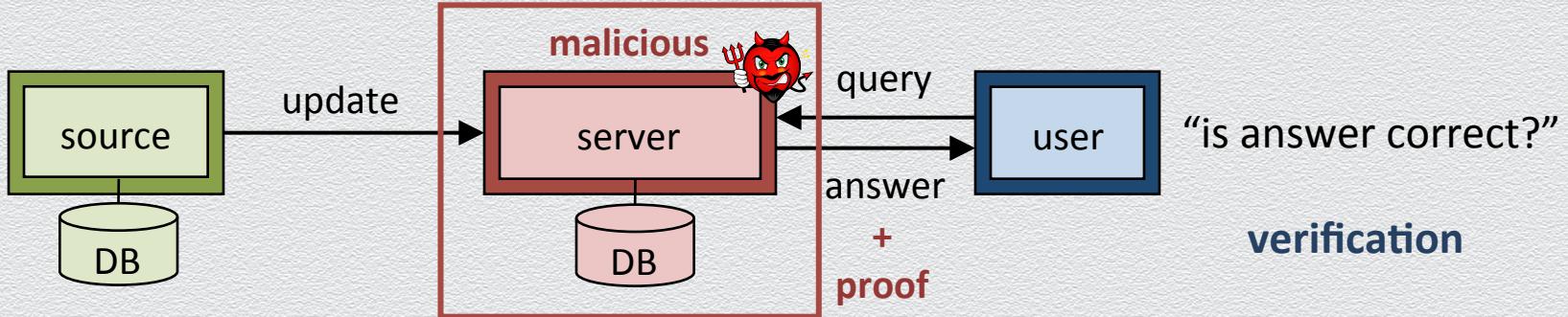
**Integrity checks** offer authenticated queries

- ◆ crypto-based: harden data/computations to provide verifiable answers
- ◆ reliable: allow no false positives or negatives
- ◆ utility-preserving: practical & easy to adopt
  - ◆ fast times for query, verification
  - ◆ near total storage, low bandwidth usage for proof



minimize all overheads

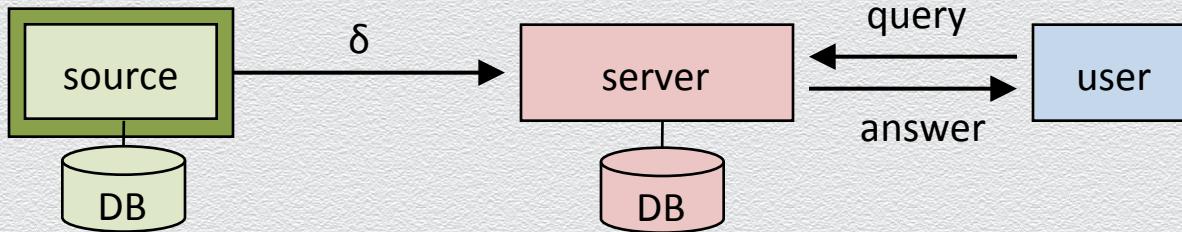
# DB-as-a-service authentication model



**Integrity checks** offer authenticated queries

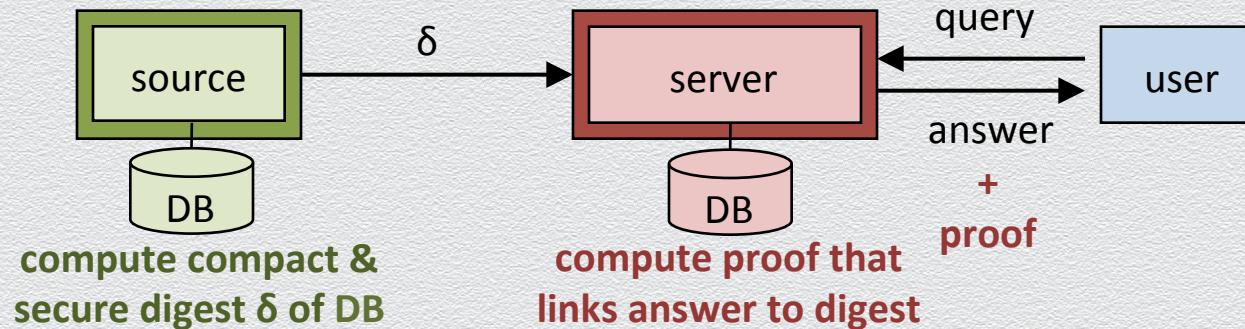
- ◆ crypto-based: harden data/computations to provide verifiable answers
- ◆ reliable: allow no false positives or negatives
- ◆ utility-preserving: practical & easy to adopt
  - ◆ fast times for query, verification, update
  - ◆ near total storage, low bandwidth usage for proof, update

# Intro to authenticated querying (AQ101)



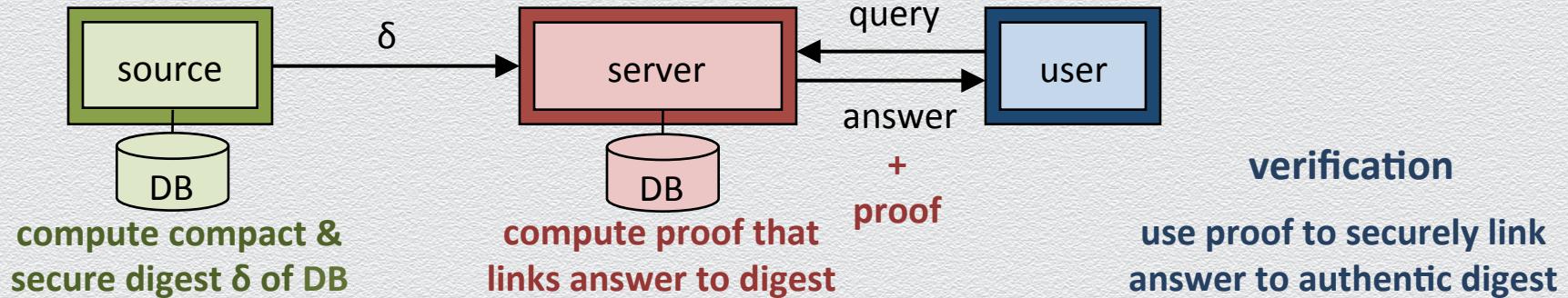
**compute compact &  
secure digest  $\delta$  of DB**

# Intro to authenticated querying (AQ101)



# Intro to authenticated querying (AQ101)

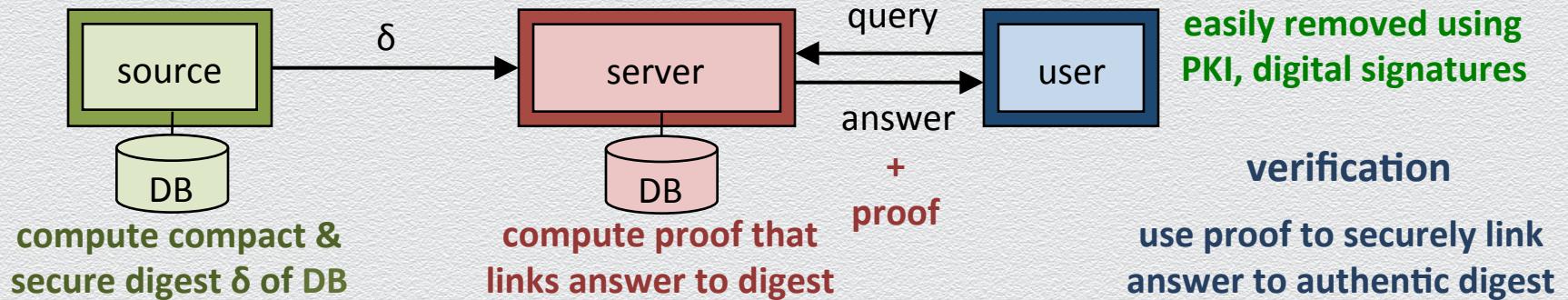
Assumption: user possesses authentic  $\delta$



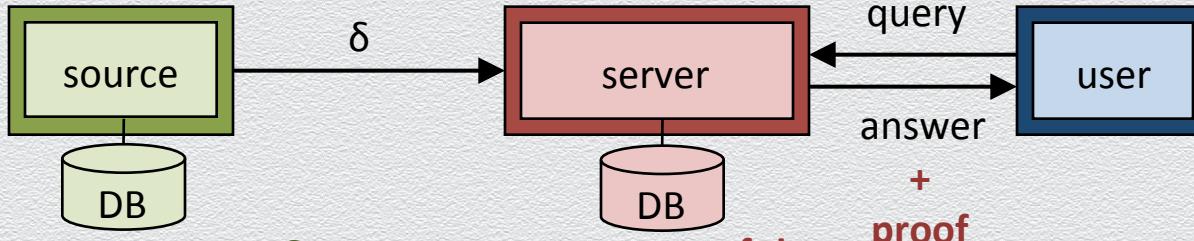
verification

use proof to securely link answer to authentic digest

# Intro to authenticated querying (AQ101)



# Intro to authenticated querying (AQ101)



compute compact &  
secure digest  $\delta$  of DB

compute proof that  
links answer to digest

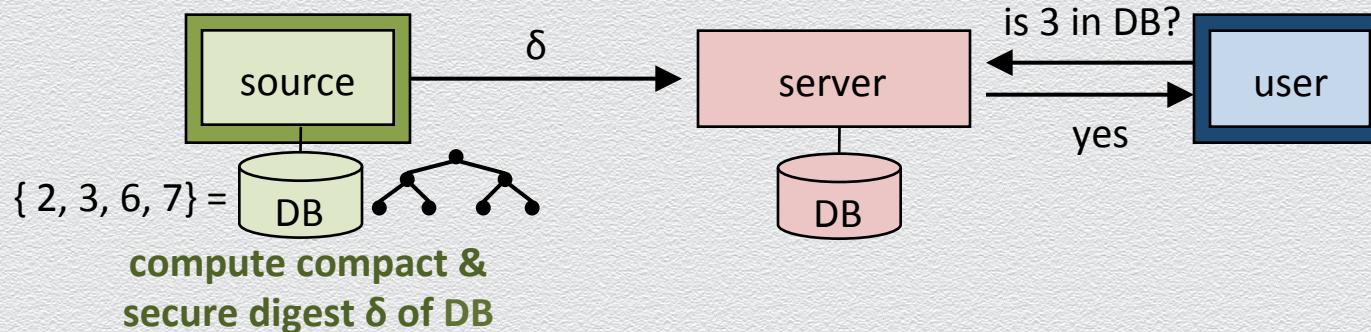
query  
answer  
+  
proof

(given  $\delta$ )  
**verification**

use proof to securely link  
answer to authentic digest

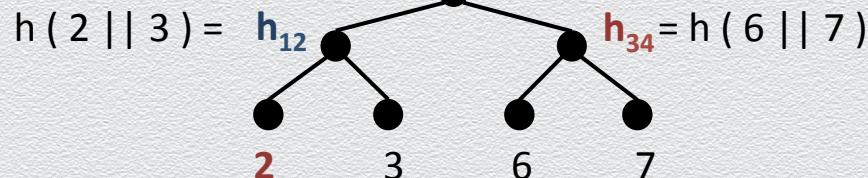
Using digital signatures to provide authentic digest  $\delta$

# Example: Set membership – digest computation

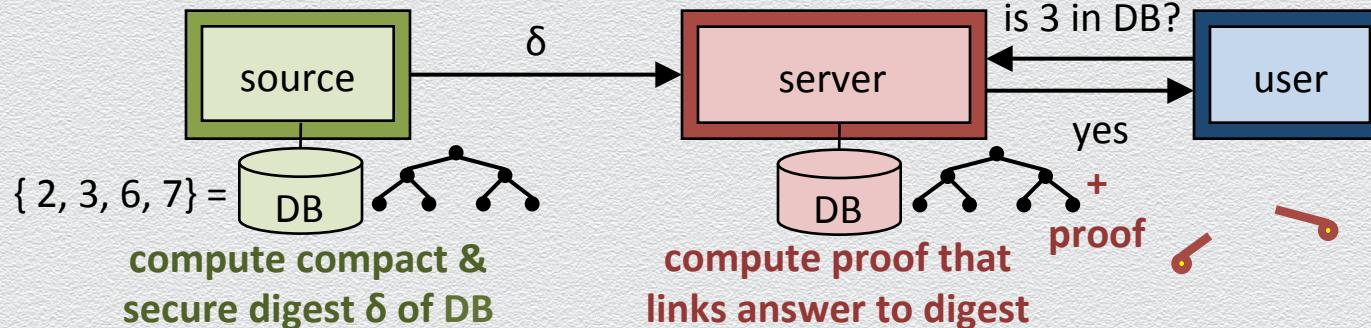


**Merkle tree hash**     $\delta = h( h_{12} || h_{34} )$

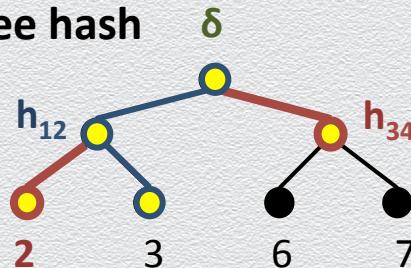
$h$ : collision resistant iterative hash function (e.g., SHA-2)



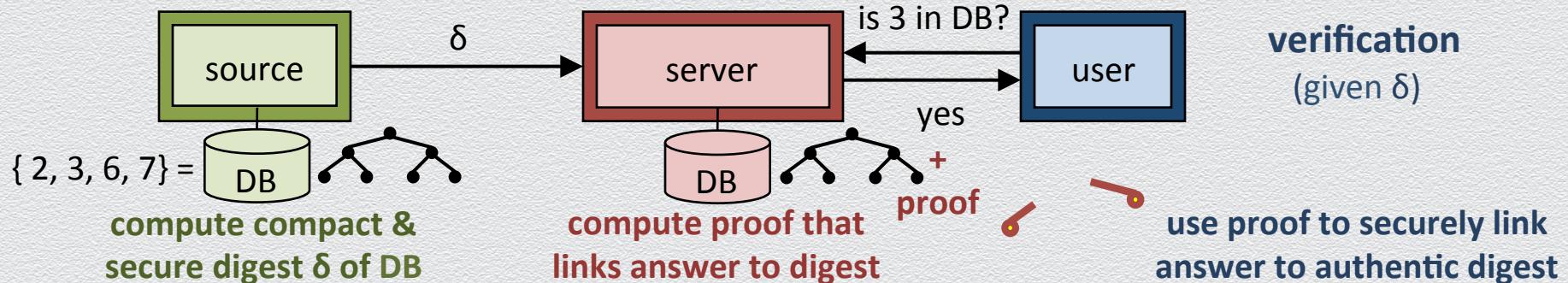
# Example: Set membership – proof computation



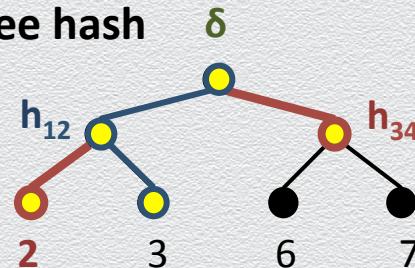
Merkle tree hash



# Example: Set membership – proof verification



Merkle tree hash



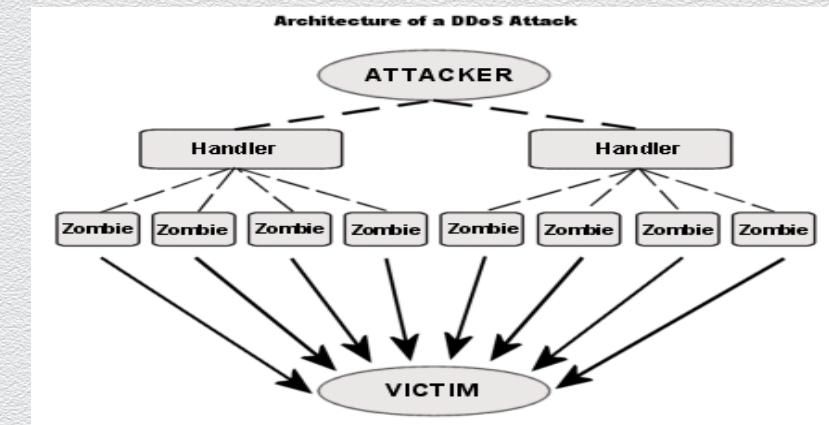
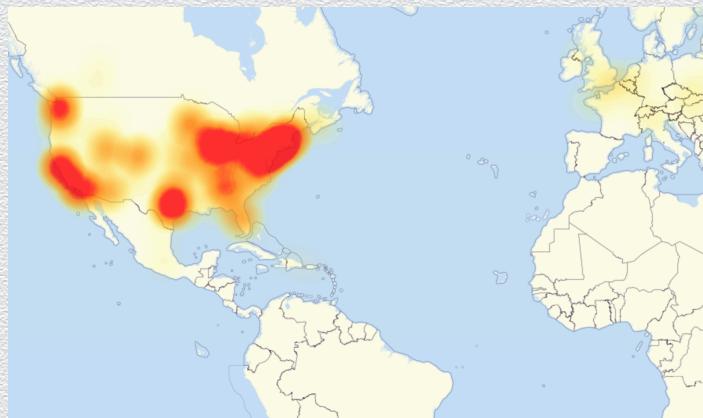
i.e.:  
recompute  $h_{12}$   
recompute  $\delta$   
compare against given  $\delta$

# **Dyn DDoS attack**

# It's unfair! – I had no class but couldn't watch my Netflix series!

On October 21, 2016, a large-scale cyber was launched

- ◆ it affected globally the entire Internet but particularly hit U.S. east coast
- ◆ during most of the day, no one could access a long list of major Internet platforms and services, e.g., Netflix, CNN, Airbnb, PayPal, Zillow, ...
- ◆ this was a **Distributed Denial-of-Service (DDoS)** attack



# DoS: A threat (mainly) against availability

Which main security property does a Denial-of-Service (DoS) attack attempt to defeat?

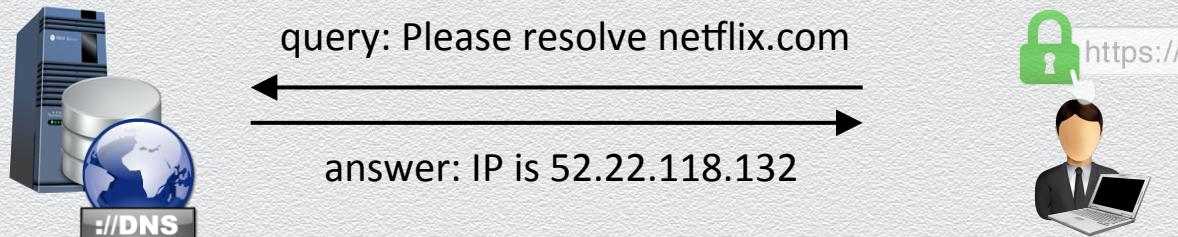
- ◆ availability; a user is denied access to authorized services or data
  - ◆ availability is concerned with preserving authorized access to assets
  - ◆ a DoS attack aims against this property; its name itself implies its main goal
- ◆ integrity & confidentiality; services or data are modified or accessed by an unauthorized user
  - ◆ elements of a DoS attack may include breaching the integrity or confidentiality of a system
  - ◆ but the end goal is disruption of a service or data flow; not the manipulation, fabrication or interception of data and services

# DNS security

# The Domain Name Service (DNS) protocol

Resolving domain names to IP addresses

- ◆ when you type a URL in your Web browser, its IP address must be found
  - ◆ e.g., domain name “netflix.com” has IP address “52.22.118.132”
  - ◆ larger websites have multiple IP responses for redundancy to distributing load
- ◆ at the heart of Internet addressing is a protocol called DNS
  - ◆ a database translating Internet names to addresses

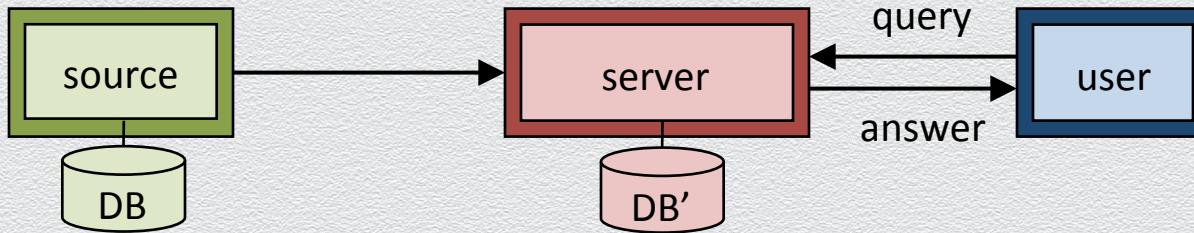


# DNS name resolution is a critical asset – a target itself!

What main security properties must be preserved in such an important service?

- ◆ all properties in CIA triad are relevant!
- ◆ resolving domain names to IP addresses is a service that
  - ◆ must critically be available during all times – availability
    - ◆ or else your browser does not know how to connect to Netflix...
  - ◆ must critically be trustworthy – integrity
    - ◆ or else connections to malicious sites may occur (e.g., DNS-spoofing attacks)
  - ◆ must also protect database entries that are not queried – confidentiality
    - ◆ or else an attacker may find out about the structure of a target organization (e.g., zone-enumeration attacks)

# DNS as a (distributed) database-as-a-service



**DNS entries:**

<netflix.com, 52.22.118.132>



"primary"  
name server

**subset of cached queried entries**

(or information of other resolvers)



"secondary"  
name server

please resolve netflix.com

IP is 52.22.118.132

(or “aWa2j3netflix.com  
is a non-existent domain”)



# Recursive name resolution: hierarchical search

Search is performed recursively and hierarchically across different type of DNS resolvers

- ◆ application-level (e.g., Web browser), OS-level (e.g., stub resolver): locally managed
- ◆ recursive DNS servers: query other resolvers and cache recent results

**DNS entries:**  
<netflix.com, 52.22.118.132>



**subset of cached queried entries**  
(or information of other resolvers)



**locally cached IP addresses**  
(at Web browser and OS)



netflix.com

52.22.118.132  
(or “non-existent”)

65

# Recursive name resolution: hierarchical search

Search is performed recursively and hierarchically across different type of DNS resolvers

- ◆ application-level (e.g., Web browser), OS-level (e.g., stub resolver): locally managed
- ◆ recursive DNS servers: query other resolvers and cache recent results
- ◆ root name servers: refer to appropriate TLD (top-level domain) server
- ◆ TLD servers: control TLD zones such as .com, .org, .net, etc.

**DNS entries:**  
<netflix.com, 52.22.118.132>



**subset of cached queried entries**  
(or information of other resolvers)



...



secondary      (or “non-existent”)

netflix.com

52.22.118.132

**locally cached IP addresses**  
(at Web browser and OS)



# Recursive name resolution: flexibility

Infrastructure allows for different configurations

- ◆ authoritative-only servers: answer queries on zones they are responsible for
  - ◆ fast resolution, no forwarding, no cache
- ◆ caching / forwarding DNS servers: answer queries on any public domain name
  - ◆ recursive search / request forwarding, caching for speed, first-hop resolvers
- ◆ master / slaves DNS servers: authoritative servers replicating DNS data of their domains
- ◆ public / private DNS servers: control access to protected resources within an organization



# Recursive name resolution: benefits

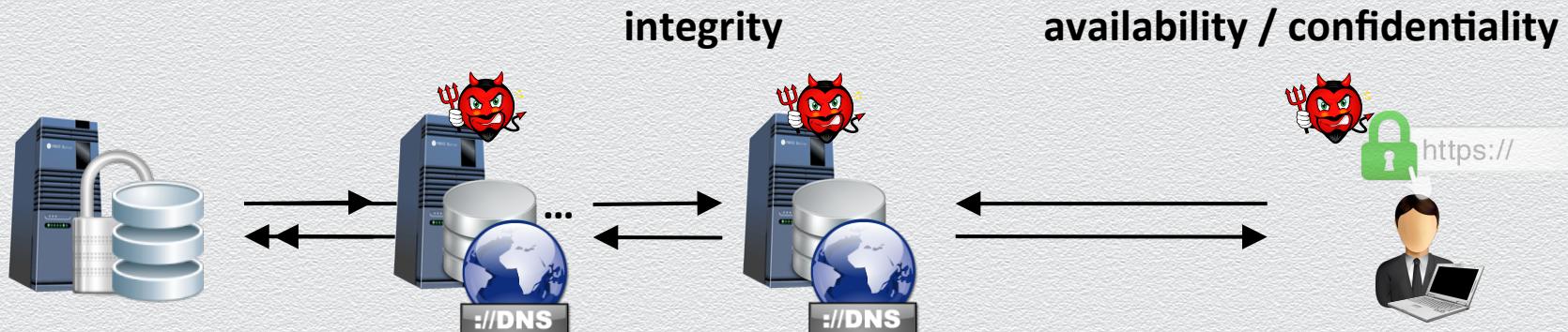
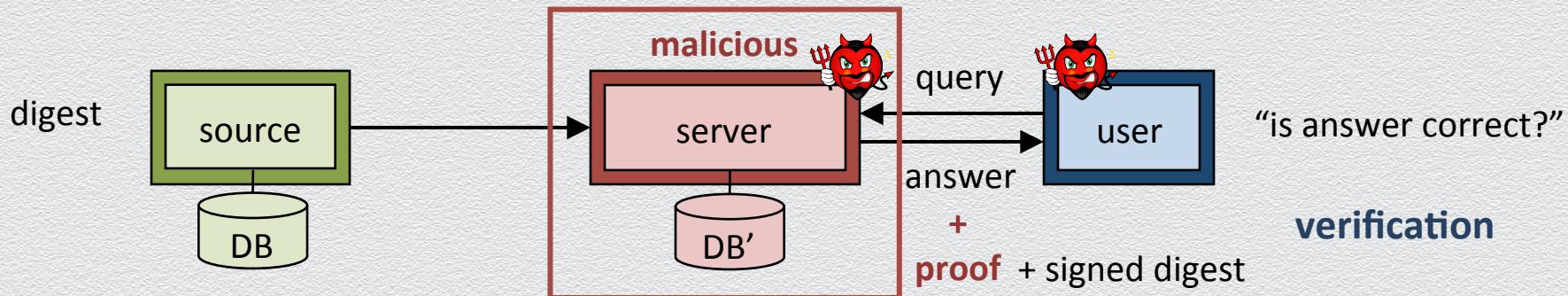
Why DNS uses non-authoritative name servers (that is, recursive resolution)?

- ◆ for more scalability & locality
  - ◆ high query loads can saturate the response capacity of primary servers
  - ◆ secondary do not have to store large volumes of DNS entries
  - ◆ cached recently queried domain names speed up searches due to locality of queries
- ◆ for added security / locality / scalability alone – not quite
  - ◆ e.g., non-authoritative name servers are untrusted and thus possibly compromised



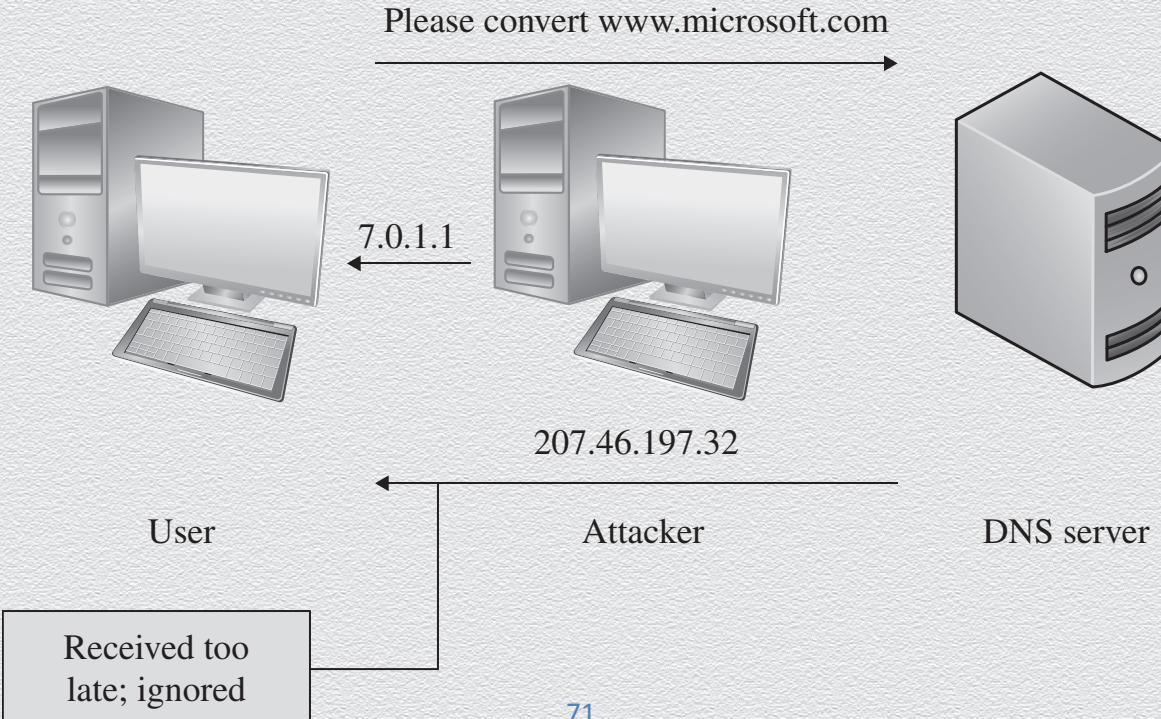
# **DNSSEC & NSEC3**

# A critical asset prone to attacks



# DNS spoofing (or cache poisoning)

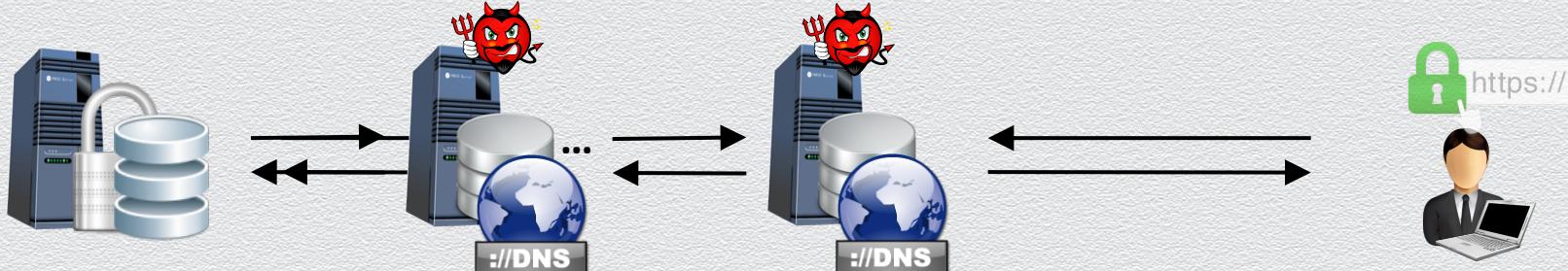
The attacker acts as the DNS server in order to redirect the user to malicious sites



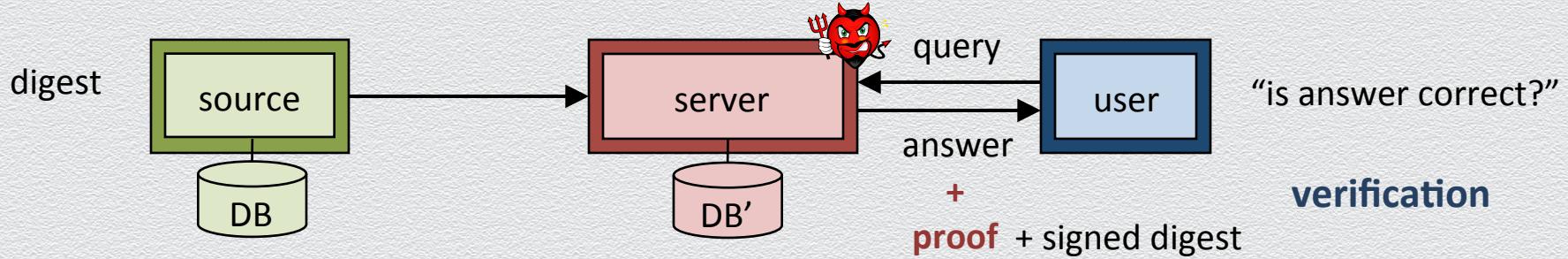
# DNSSEC (& NSEC)

Security extension of DNS protocol to protect integrity of DNS data

- ◆ correct resolution, origin authentication, authenticated denial of existence
- ◆ specifications made by Internet Engineering Task Force (IETF) via RFCs
  - ◆ an RFC (request for comments) is a suggested solution under peer review
- ◆ challenges: backward-compatible, simplicity, confidentiality, who signs
  - ◆ NSEC (next secure record): extension that provides proofs of denial of existence



# DNSSEC & NSEC: core idea

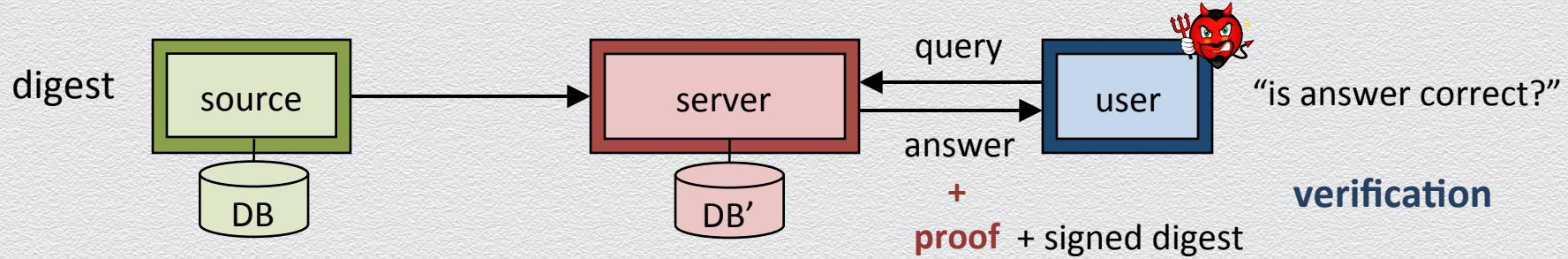


**DNSSEC protocol:** each DNS entry is pre-signed by primary name server

**NSEC protocol:**

- domain names are lexicographically ordered and then each pair of neighboring existing domain names is pre-signed by the primary name server
- non-existing names, e.g., aWa2j3netflix.com are proved by providing this pair “containing” missed query name, e.g., <awa.com, awb.com>

# From NSEC to NSEC3



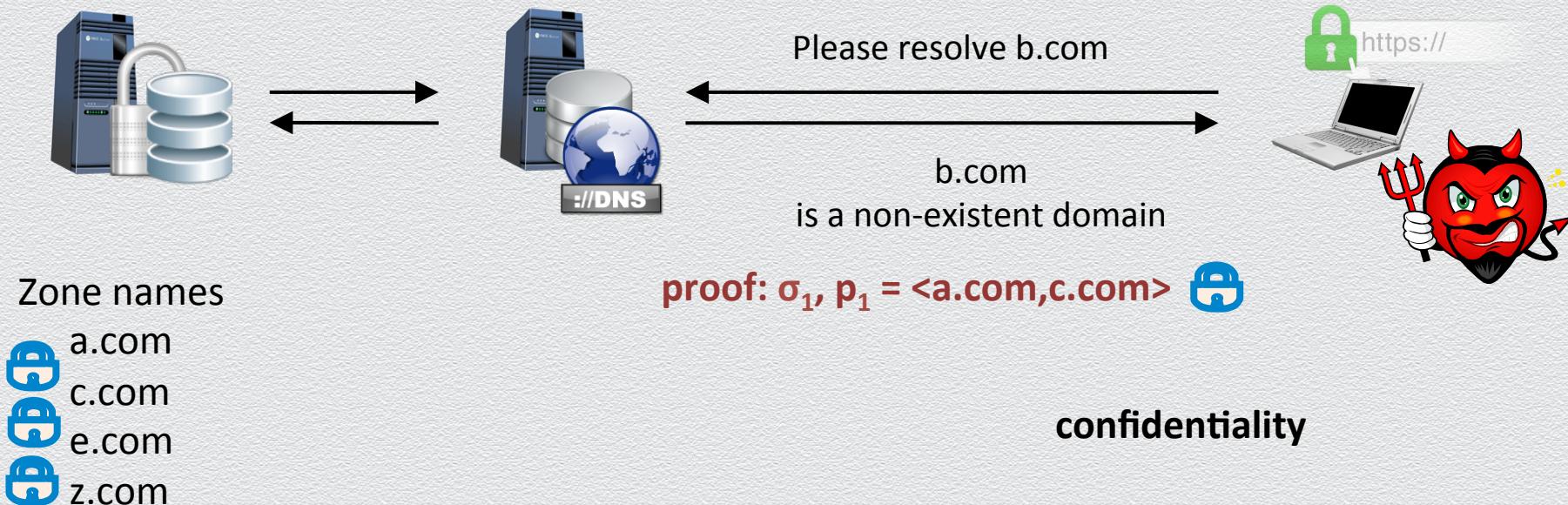
Vulnerability in NSEC protocol

**confidentiality**

- ◆ proofs of non-existing names reveal information about domain names
- ◆ an attacker can simply as a “querier” learn information about the network structure of a target organization!

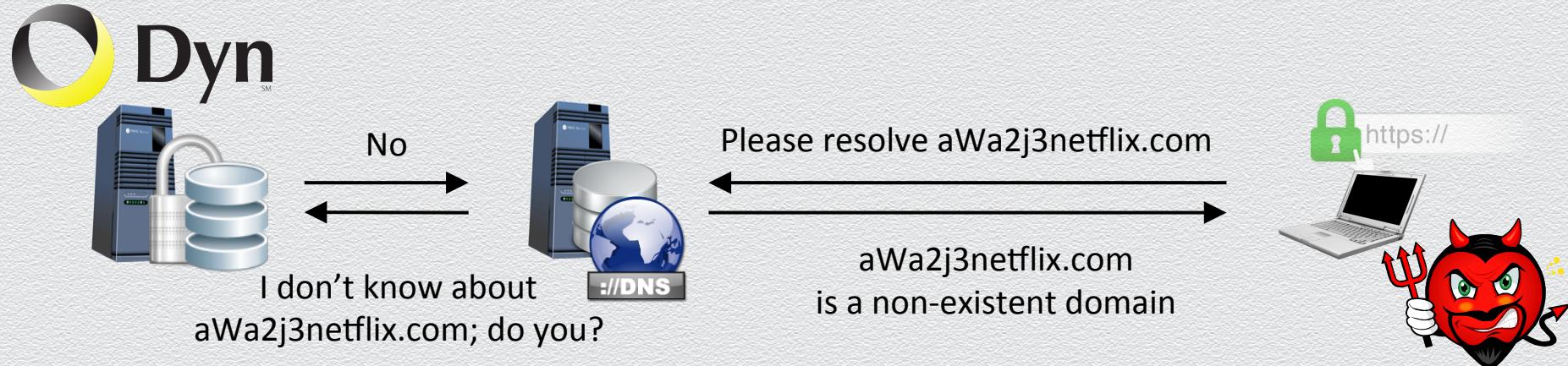
# DNS zone enumeration attack

The attacker acts as the user in order to learn the domain names of an entire zone



# **DDoS attacks**

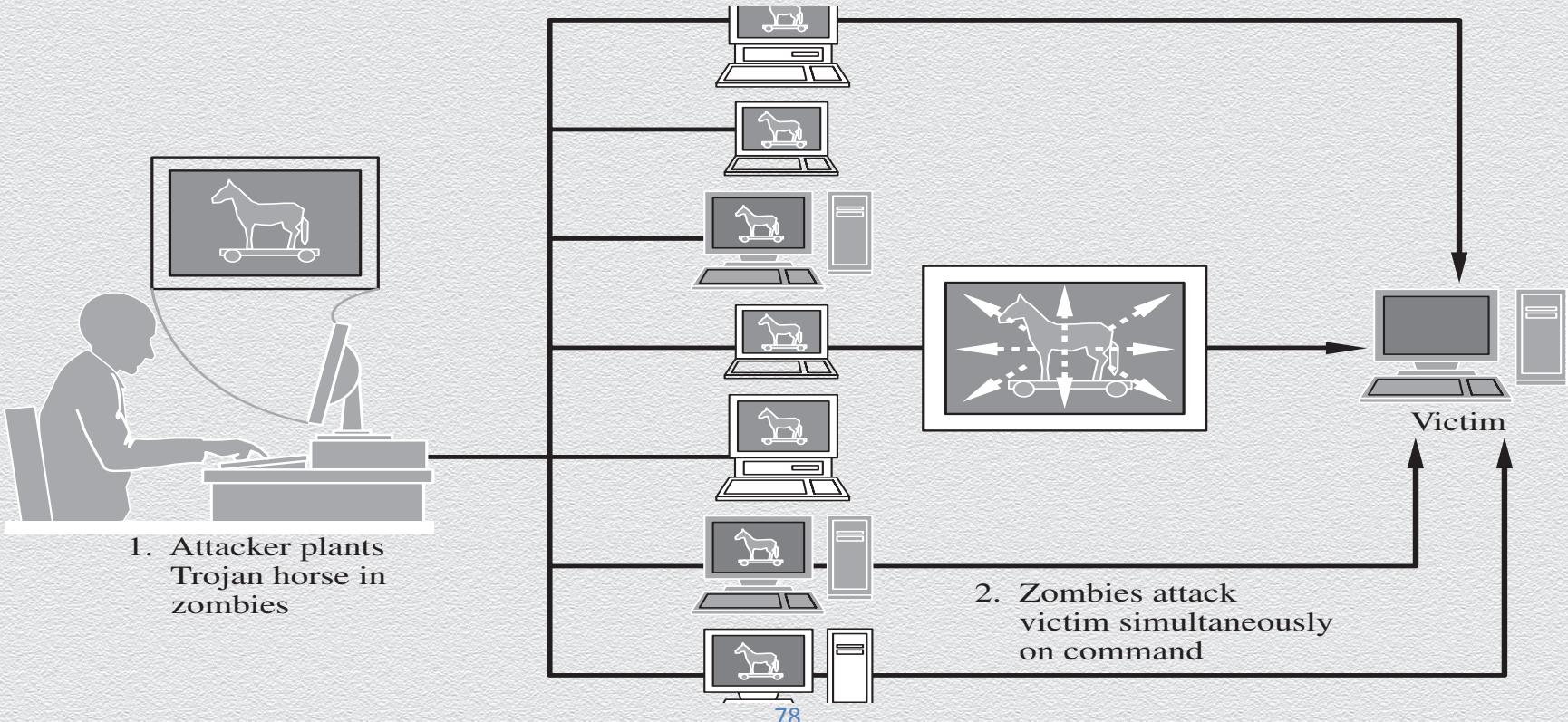
# Core idea of attack: Saturate Dyn's primary servers



## Attack:

- from a compromised machine ask for domain names that do not exist
- query is forwarded to fewer primary Dyn servers, i.e., defeating benefits of distribution
- ask **A LOT** of such queries to bring down the Dyn DNS service!

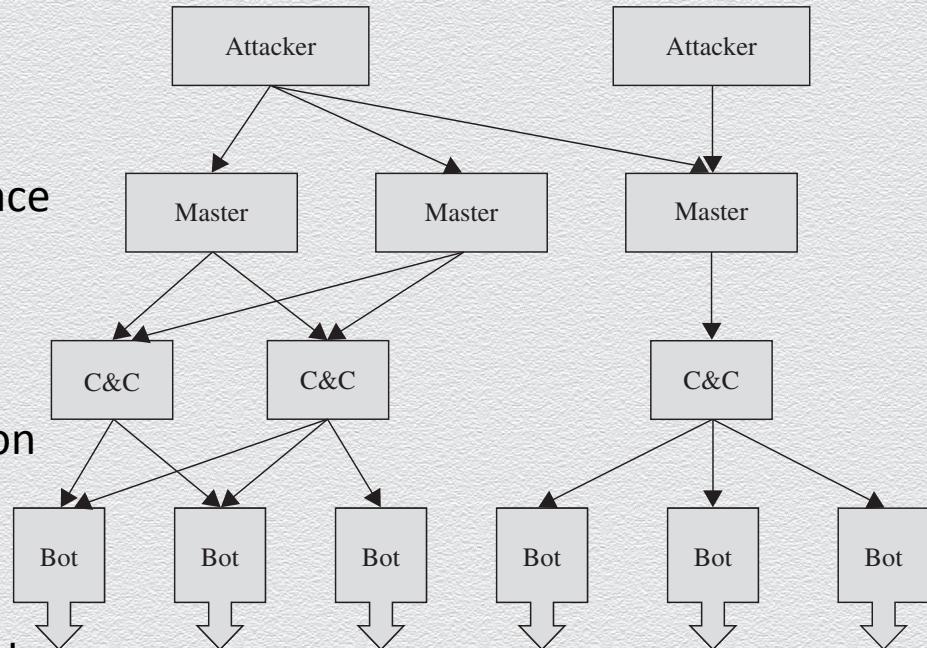
# Distributed Denial of Service (DDoS)



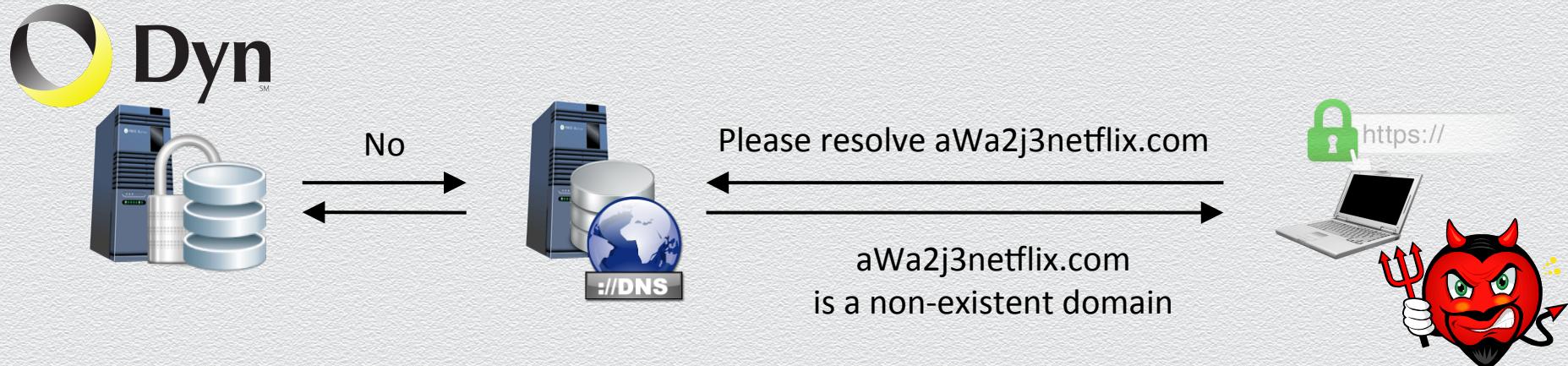
# Botnets

Networks of machines running malicious code under remote control

- ◆ massive: scale to million of bots
  - ◆ comprise main tool for DDoS attacks
- ◆ stealth: remain undetected & difficult to trace
  - ◆ do little harm to the host machines
    - ◆ users won't likely remove malware
  - ◆ multiple-level attacker Vs. bots separation
- ◆ resilient: have redundant components
  - ◆ even if one master or C&C node is taken down, connectivity is maintained

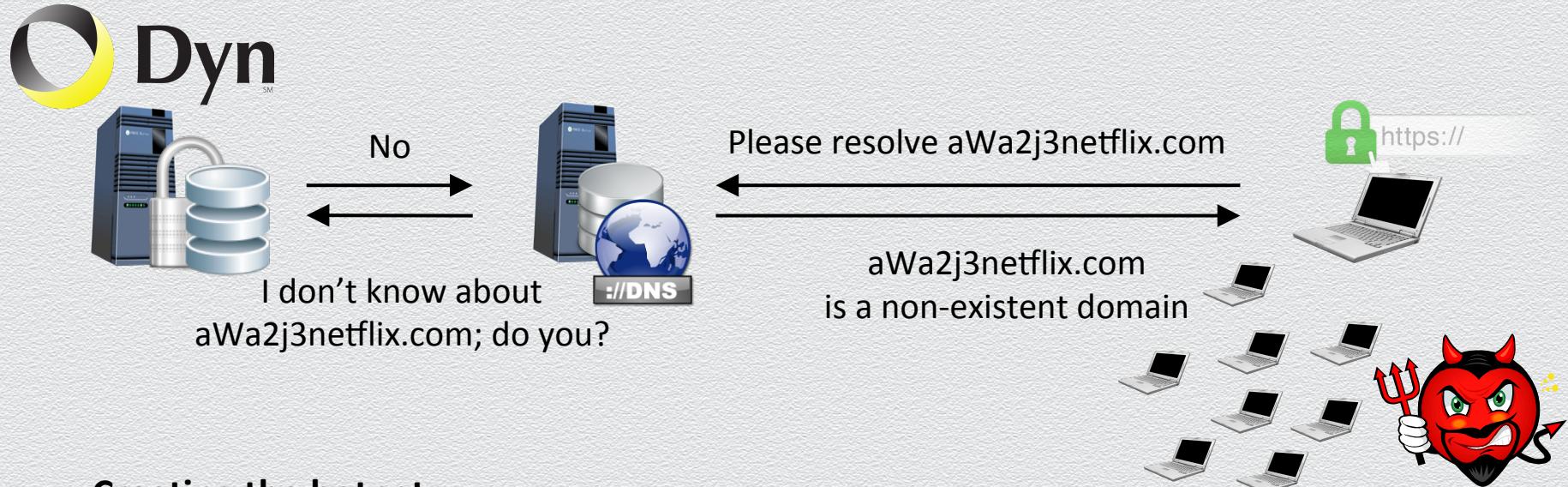


# Why botnets are often behind DoS attacks?



- ◆ to avoid effective countermeasures and increase "attack" traffic
  - ◆ if the high-volume "attack" traffic comes from few devices, they can be filtered out by blocking their connections to the Dyn servers
  - ◆ by employing a large botnet of millions of devices the attacker inflicts a larger, more devastating "attack" traffic against the victim Dyn servers

# Recruiting an army: Internet of Things (IoT)



## Creating the botnet:

- compromise easy targets: IoT “thin” devices, e.g., printers, cameras, home routers, ...
- how? find a vulnerability on these devices...
  - all such devices used an OS with a static, hard-wired, thus known, admin password...!

# The Internet of Things (IoT)

Refers to Internet-connected everyday devices

- ◆ comprise a world of so-called smart devices
- ◆ examples:
  - ◆ smart appliances, such as refrigerators and dishwashers
  - ◆ smart home, such as thermostats and alarm systems
  - ◆ smart health, such as fitness monitors and insulin pumps
  - ◆ smart transportation, such as driverless cars
  - ◆ smart entertainment, such as video recorders
- ◆ potential downsides
  - ◆ loss of privacy
  - ◆ loss of control of data
  - ◆ potential for subversion
  - ◆ mistaken identification
  - ◆ uncontrolled access

# Smartphones

The control hub of the IoT – important target for malware

- ◆ 2013: 143,211 distinct new forms of malware against mobile devices
- ◆ 98% targeted Android devices, far in excess of its market share
  - ◆ Android: open approach
    - ◆ unlike its competitors, does not limit the software users are allowed to install
    - ◆ thus, an easier target
  - ◆ Apple: locked-down approach
    - ◆ in contrast, only allows apps from its app store to be installed on its smartphones
    - ◆ all apps go through an approval process, which includes some security review
    - ◆ once approved, apps are signed, using a certificate approach

# More generally on DoS attacks

DoS attacks are attempts to defeat a system's availability

- ◆ volumetric attacks (e.g., flooding)
  - ◆ potential weaknesses in the capacity of a computer network
- ◆ application-based attacks (e.g., routing malfunction, blocked access)
  - ◆ exhaust the resources of an application that services a particular network
- ◆ disabled communications (e.g., access failure)
  - ◆ physically disable a communication link or disrupt a single-point of failure
- ◆ hardware or software failure (e.g., access failure)
  - ◆ failures on machines or programs (without fault-tolerance provisions)

} insufficient capacity,  
overloading

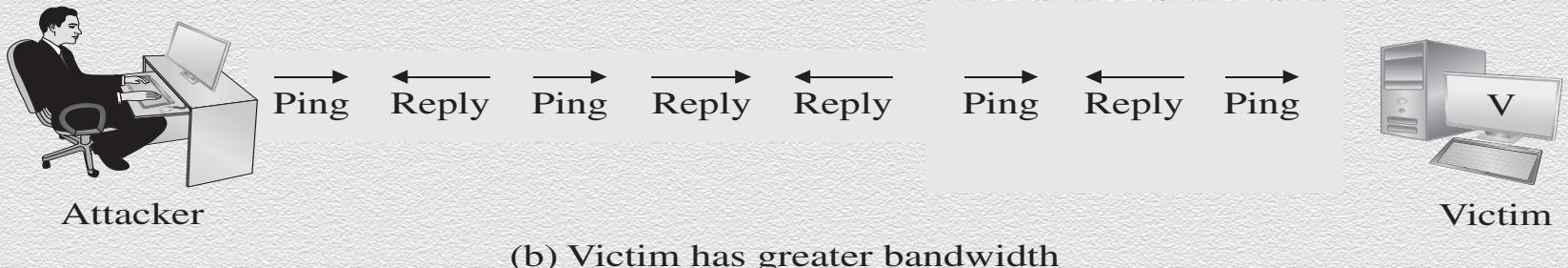
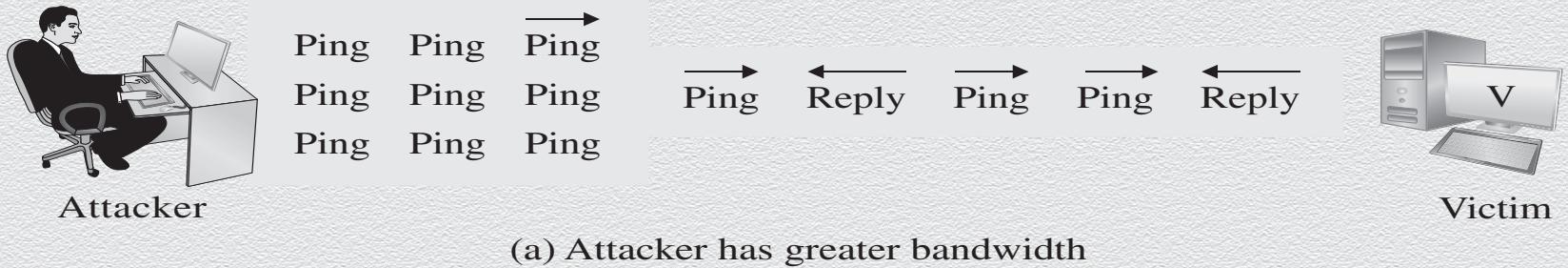
} blocked  
access

} unresponsive  
asset

# Examples

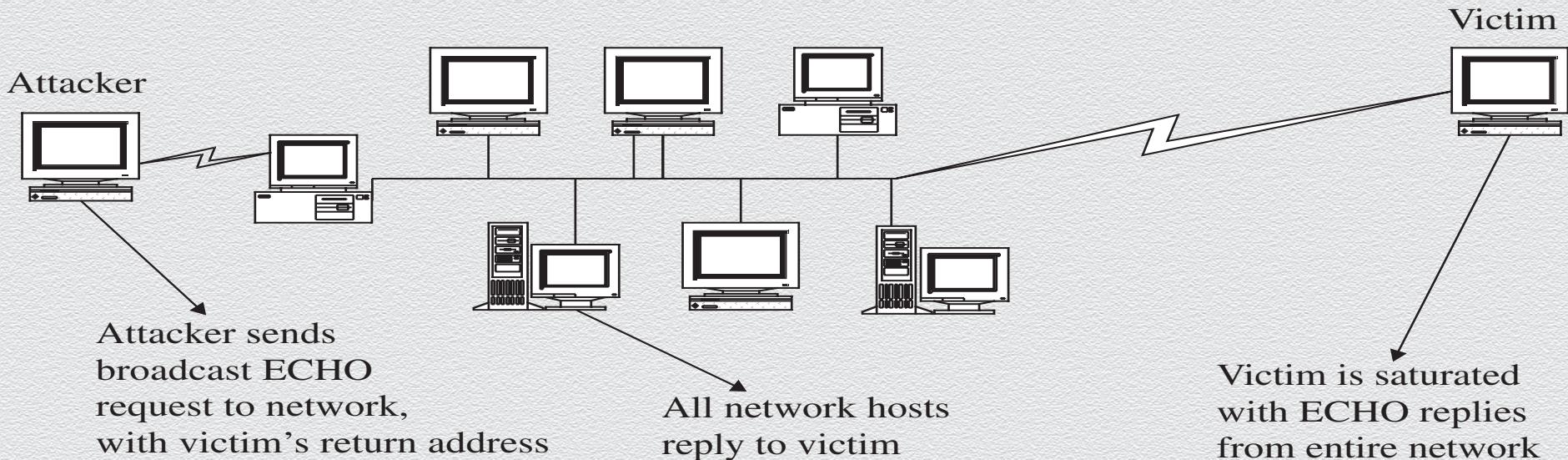
- ◆ Benign errors
  - ◆ Beth Israel Hospital system downtime, in 2002, due to mishandling of switches
- ◆ Malicious code
  - ◆ use vulnerabilities in communication protocols
  - ◆ e.g., cause uncontrolled congestion in TCP communications (Vs. UDP)
  - ◆ e.g., exploit/misuse Internet Control Message Protocols (ICMP)
    - ◆ ping (destination is reachable and functional)
    - ◆ echo (the connection between two machines is reliable)
    - ◆ destination unreachable (destination address cannot be accessed)
    - ◆ source quench (destination is saturated and source should suspend transmissions)

# Ping flood (or pink of death)



# Smurf Attack

Unwitting victims become accomplices



# Echo-Chargen



Victim A

Chargen packet with echo bit on →

← Echoing what you just sent me



Victim B

Chargen another packet with echo bit on →

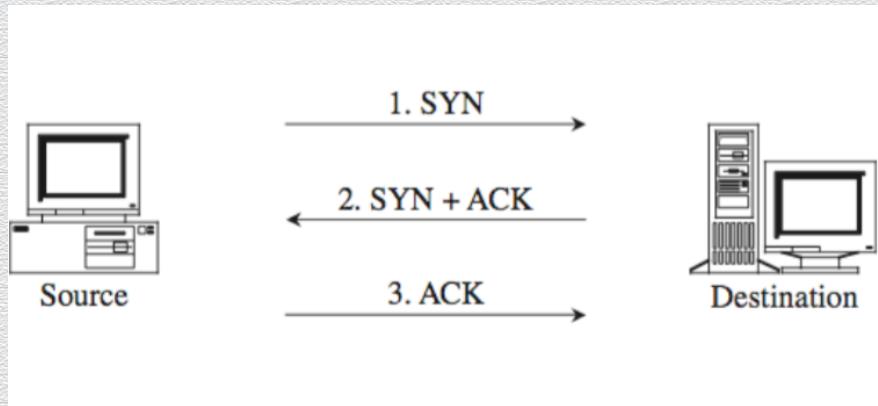
← Echoing that again

Chargen another packet with echo bit on →

# SYN flood

Three-way handshake used in TCP to establish a new session

- ◆ source & destination exchange control messages to complete session creation
- ◆ destination keeps track of incomplete session-creation protocols (SYN-RECV cache)
- ◆ attacker spoofs return address of many SYN handshake messages sent to victim
- ◆ victim's cache is filled (after ~20) pending incomplete sessions and delays are created

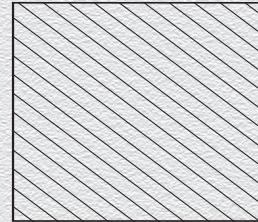


# Teardrop Attack

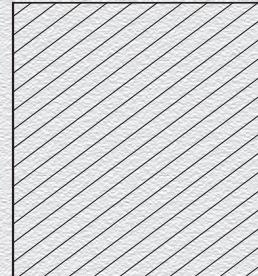
IP datagrams allow to carry variable-length data

- ◆ each datagram specifies the length of its data payload and its offset (start-end)
- ◆ the attacker can spoof these metadata so that recipient's state remains inconsistent
- ◆ sent packets cannot possibly be reassembled, as they conflict instructions
- ◆ in extreme cases, this can cause the entire OS to lock up

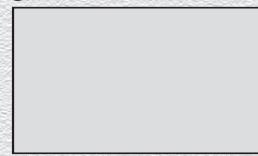
Fragment start = 10 len = 50



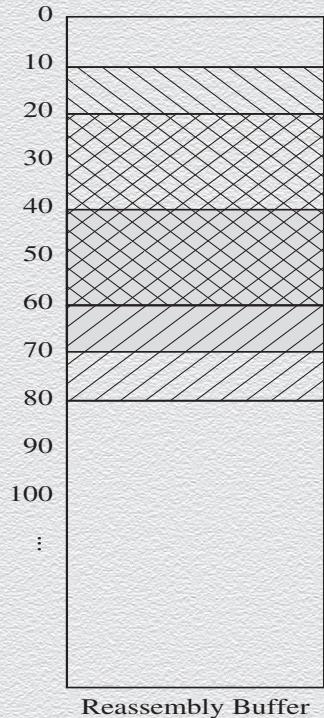
Fragment start = 20 len = 60



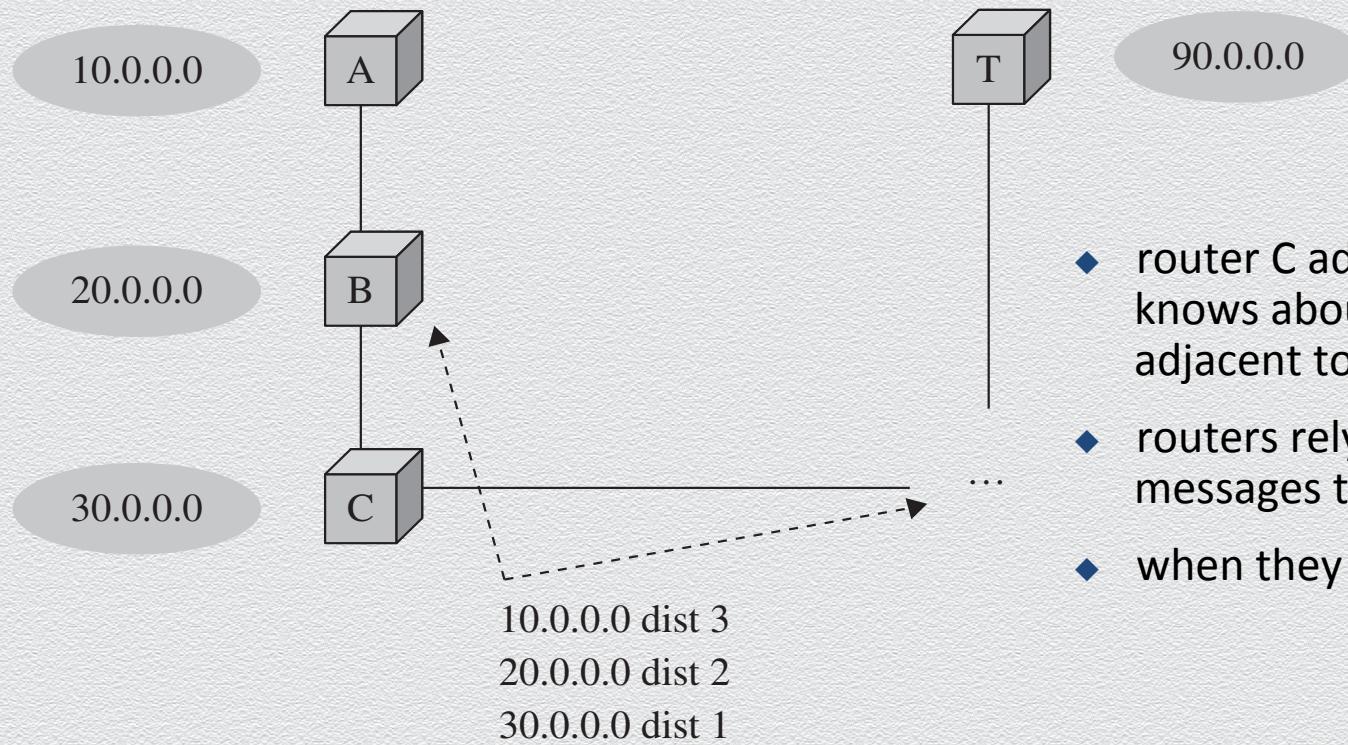
Fragment start = 40 len = 30



Packet Fragments



# Rerouting routing



- ◆ router C advertises the routes it knows about to the routers adjacent to it
- ◆ routers rely on these advertising messages to be accurate
- ◆ when they aren't, DoS can ensue

# TCP/IP headers

- ◆ headers of IP datagram and TCP packet
- ◆ IP: right
- ◆ TCP: below

bytes	0	1	2	3
0	Flags		Length	
4	Identification		Flags	Fragment Offset
8	Time to Live	Protocol	Header Checksum	
12	Source IP Address			
16	Destination IP Address			
20	IP Options		Padding	
24+	Data ...			

bytes	0	1	2	3
0	Sender Port		Receiver Port	
4	Sequence Number			
8	Acknowledgment Number			
12	Data Offset, Reserved, Flags		Window	
16	Checksum		Urgency	
20	IP Options		Padding	
24+	Data ...			

# Session hijacking

- ◆ an attacker is able to synchronize with a receiver while breaking synchronization with the sender and resetting the sender's connection
- ◆ the attacker continues the TCP session while the sender thinks the connection just broke off

