

**CS 334 - Homework 2 (Regular Languages)** ←[0-indexed!]  
**Due 3/29/2016**

*Construction of Context-Free Languages*

1. Define a context-free grammar which accepts any valid mathematical expression over the alphabet  $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 8, +\}$ .
2. Define a context-free grammar which accepts any palindrome over the alphabet  $\{0, 1\}$ .

*Construction of Pushdown Automata*

1. Define a pushdown-automaton which accepts any string over the alphabet  $\{0, 1\}$  for which there are the same number of "0"s as "1"s.
2. Let  $w, z$  be strings over the alphabet  $\{0, 1, \$\}$ . Define a pushdown-automaton which accepts any string  $w\$z$ , where  $w^{-1}$  is a subsequence of  $z$ , and both  $w$  and  $z$  do not contain "\$".

Ex: "**110\$001001**"

Ex: "**0101\$01001110101**"

*Pumping Lemma*

1. Let  $\Sigma = \{0, 1\}$ . Prove that the set  $\{w^2 \mid w \in \Sigma^*\}$  is not context-free.
- 2.