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Use the Master Theorem to find the complexity of each recurrence relation listed below.

1.  $T(n) = T\left(\frac{n}{2}\right) + n^2$

Complexity:  $T(n) = \theta(n^2)$ 

2.  $T(n) = 4T\left(\frac{n}{2}\right) + n^2$

Complexity:  $T(n) = \theta(n^2 \log_2 n)$ 

3.  $T(n) = 3T\left(\frac{n}{3}\right) + \sqrt{n}$

Complexity:  $T(n) = \theta(n)$ 

For each function below, write the recurrence relation for its running time and then use the Master Theorem to find its complexity.

```

4. int f(int arr[], int n) {
    int sum = 0;

    for (int j = 0; j < n; ++j) {
        sum += arr[j];
    }

    return f(n / 2) + sum + f(n / 2);
}

```

Recurrence:  $T(n) = 2T(n/2) + n$ Complexity:  $T(n) = \theta(n \log_2 n)$ 

```

5. void g(int n, int arrA[], int arrB[]) {
    for (int i = 0; i < n; ++i) {
        for (int j = 0; j < n; ++j) {
            arrB[j] += arrA[i];
        }
    }

    g(n / 2);
}

```

Recurrence:  $T(n) = T(n/2) + n^2$ Complexity:  $T(n) = \theta(n^2)$